Illustrating Transparency: communicating the 3D shape of layered transparent surfaces via texture

by

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ABSTRACT

Victoria L. Interrante. Illustrating Transparency: communicating the 3D shape of layered transparent surfaces via texture.

(Under the direction of Drs. Henry Fuchs and Stephen Pizer)

There are many applications in which transparency can be a useful tool for displaying the outer surface of an object together with underlying structures. The driving application for this research is radiation therapy treatment planning, in which physicians need to understand the volume distribution of radiation dose in the context of patient anatomy.

To effectively display data containing multiple overlapping surfaces, the surfaces must be rendered in such a way that they can simultaneously be seen and also seen *through*. In computer-generated images, as in real life, however, it is often difficult to adequately perceive the three-dimensional shape of a plain transparent surface and to judge its relative depth distance from underlying opaque objects.

Inspired by the ability of gifted artists to define a figure with just a few strokes, I have explored methods for automatically generating a small, stable set of intuitively meaningful lines that intend to capture the essence of a surface's shape. This dissertation describes my investigations into the use of opaque texture lines as an artistic device for enhancing the communication of the shape and depth of an external transparent surface while only minimally occluding underlying structure.

I provide an overview of the role of 3D visualization in radiation treatment planning and a survey of shape and depth perception, focusing on aspects that may be most crucial for conveying shape and depth information in computer-generated images, and then motivate the use of two specific types of shape-conveying surface markings: valley/ridge lines, which may be useful for sketching the essential form of certain surfaces, and distributed short strokes, oriented in the direction of greatest normal curvature, which may meaningfully convey the local shape of general surface patches.

An experimental paradigm is proposed for objectively measuring observers' ability to simultaneously see and see through a transparent surface, and is used to demonstrate, in an experiment with five subjects, that consistent performance improvements can be achieved, on a task relevant to the needs of radiotherapy treatment planning and based on images generated from actual clinical data, when opaque texture lines are added to an otherwise plain transparent surface.

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Table of C	Contents
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Pa	age
List of Tables	viii
List of Figures	ix
Chapter One: Introduction	1
Chapter Two: Motivation and Background	5
2.1: Applications for transparent surface display.	5
2.2. The driving application: radiation therapy treatment planning	6
2.2.1: Overview of the goals and methods of radiation therapy treatment planning	6
2.2.2: 2D and " $2\frac{1}{2}$ D" display techniques for treatment planning data	10
2.2.3: Advantages of using 3D transparent surfaces for data display	12
2.2.4: The role of visualization in the context of other treatment planning needs	13
2.3: A characterization of transparent surface types	14
2.4: Photorealistic rendering of transparent surfaces: a brief history	14
2.5: Empirical evidence for the insufficiency of photorealism	16
2.6: The perception of transparency	17
2.7: Representations of transparency in art and illustration-basic techniques	22
References for chapter two	25
	20
Chapter Three: Perceiving and Representing Shape and Depth	31
3.1: Pictorial depth cues	31
3.1.1: Occlusion	31
3.1.2: Linear perspective	32
3.1.3: Kelative familiar size	33
3.1.4. Relative neight	34 25
3.1.6: Spatial fragmancy focus doubt of field	36
2.2. On large ter Gues to Death	27
3.2: Oculomotor Cues to Deptn	37
3.2.1: Accommodation	3/
5.2.2. Vergence	30
3.3: Shading	39
3.3.1: Depth from shadows	39
3.3.2. Shape from shading	40
3.4: Binocular disparity (stereo)	48
3.5: Depth from motion	50
3.5.1: Motion parallax	50
3.5.2: Kinetic depth effect	51
3.5.3: Optic flow	52
2.5.4: Active versus passive viewing	52
3.5.6. Elistor	52
2.6. The integration of donth gues	52
	55
3.7: Snape and depth from texture	55 E(
3.7.1. Texture properties characterizing a large planar surface receding in depth	00 61
3.7.3. Texture properties characterizing cylinders and ellipses of various eccentricities	61
3.7.4: Insights from computational models for extracting shape from texture	66

	3.7.5: Representing a curved surface with "contour" lines	67
Re	ferences for chapter three	71
Chapter	Four: Feature Line Textures	77
4.1	: Silhouette and contour curves	79
4.2	· Valley and ridge curves: an introduction	83
4.3	Perceptual motivation for highlighting valley lines	84
4.4	: The role of ridge lines	89
4.5	Parabolic curves: perceptually less-relevant shape feature lines	92
4.6	A proof-of-concept demonstration of the usefulness of explicitly marking ridge and valley lines on a transparent surface	93
4.7	Previous implementations of ridge-finding algorithms	94
4.8	 A straightforward ridge-finding algorithm	97 97 98 98
	4.8.4: Computing principal directions and principal curvatures	98
	4.8.5: Computing Gaussian and mean curvatures	99
	4.8.6: Determining whether a point lies on or near a ridge or valley line	99
4.9	: Improving the display of ridge and valley information	100
	4.9.2: Predicting the significance of a ridge or valley by the extent of its flanks	100
	4.9.3: The role of color	103
4.1	0: Empirical evidence of the benefits of opacifying ridge and valley lines	103
Ret	ferences for chapter four	107
Chapter	Five: Uniformly Distributed Surface Texture	111
Chapter 5.1	• Five: Uniformly Distributed Surface Texture	111
Chapter 5.1	 Five: Uniformly Distributed Surface Texture	111 111
Chapter 5.1 5.2	 Five: Uniformly Distributed Surface Texture Previous work in computer graphics using texture to represent or enhance transparent surfaces How artists represent form with line 	111 111 113
Chapter 5.1 5.2 5.3	 Five: Uniformly Distributed Surface Texture	111111113121
Chapter 5.1 5.2 5.3 5.4	 Five: Uniformly Distributed Surface Texture	111111113121123
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 127 129 120
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 129 130
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 130 130
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 129 130 130 131
Chapter 5.1 5.2 5.3 5.4 5.5	 Five: Uniformly Distributed Surface Texture Previous work in computer graphics using texture to represent or enhance transparent surfaces. How artists represent form with line Past work with principal direction texture, automatic pen-and-ink illustration techniques. Applying principal direction texture to transparent surfaces. Alternative texturing techniques. 5.5.1: Aligning texture elements with the direction of steepest gradient descent. 5.5.3: Empirical investigations. 5.5.3.1: Element orientation. 5.5.3.2: Spot textures. 5.5.3.4: Additional issues. 	 111 111 113 121 123 127 127 129 129 130 130 131 132
Chapter 5.1 5.2 5.3 5.4 5.5 8 8 8	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 129 130 131 132 134
Chapter 5.1 5.2 5.3 5.4 5.5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 129 130 130 131 132 134 137
Chapter 5.1 5.2 5.3 5.4 5.5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	 Five: Uniformly Distributed Surface Texture. Previous work in computer graphics using texture to represent or enhance transparent surfaces. How artists represent form with line. Past work with principal direction texture, automatic pen-and-ink illustration techniques. Applying principal direction texture to transparent surfaces. Alternative texturing techniques. 5.5.1: Aligning texture elements with the direction of steepest gradient descent. 5.5.3: Empirical investigations. 5.5.3.1: Element orientation 5.5.3.2: Spot textures. 5.5.3.3: Grid textures. 5.5.3.4: Additional issues. 	 111 111 113 121 123 127 127 129 130 131 132 134 137 137
Chapter 5.1 5.2 5.3 5.4 5.5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 127 129 129 130 130 131 132 134 137 138
Chapter 5.1 5.2 5.3 5.4 5.5 5.5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	 Five: Uniformly Distributed Surface Texture Previous work in computer graphics using texture to represent or enhance transparent surfaces. How artists represent form with line Past work with principal direction texture, automatic pen-and-ink illustration techniques. Applying principal direction texture to transparent surfaces. Alternative texturing techniques. 5.5.1: Aligning texture elements with the direction of steepest gradient descent. 5.5.2: Inspiration from flow visualization techniques. 5.5.3: Empirical investigations 5.5.3.1: Element orientation 5.5.3.2: Spot textures. 5.5.3.3: Grid textures. 5.5.3.4: Additional issues. ferences for chapter five Six: Experimental Validation. Observer experiments- when and why they are needed. Objectives of the study. Experimental design 	 111 111 113 121 123 127 129 129 130 131 132 134 137 138 138
Chapter 5.1 5.2 5.3 5.4 5.5 8 5.4 5.5 8 5.4 5.5 8 6.1 6.2 6.3	 Five: Uniformly Distributed Surface Texture Previous work in computer graphics using texture to represent or enhance transparent surfaces. How artists represent form with line. Past work with principal direction texture, automatic pen-and-ink illustration techniques. Applying principal direction texture to transparent surfaces. Alternative texturing techniques. 5.5.1: Aligning texture elements with the direction of steepest gradient descent. 5.5.2: Inspiration from flow visualization techniques. 5.5.3: Empirical investigations 5.5.3.2: Spot textures. 5.5.3.3: Grid textures. 5.5.3.4: Additional issues. ferences for chapter five Six: Experimental Validation. Observer experiments- when and why they are needed. Objectives of the study Experimental design 6.3.1: Task definition overview. 	 111 111 113 121 123 127 129 129 130 131 132 134 137 138 138 138 138 138 138
Chapter 5.1 5.2 5.3 5.4 5.5 5.4 5.5 8 5.4 5.5 8 6.2 6.1 6.2 6.3	 Five: Uniformly Distributed Surface Texture	 111 111 113 121 123 127 129 129 129 130 131 132 134 137 138 138 138 138 139 145

6.	3.2.2: Second phase	147
6.	3.2.3: Training phase	148
6.3.3:	Data preparation	149
6.4: Res	ults and evaluation	151
6.4.1:	Accuracy in localizing the closest points	152
6.4.2:	Accuracy in choosing in which of two datasets the outer and inner surfaces come	
	closest	158
6.4.3:	Confidence judgments	160
6.4.4:	Discussion	161
Reference	es for chapter six	163
Chapter Seve	n: Summary, Conclusions and Future Work	165
7.1: Sun	mary and conclusions	165
7.1.1:	Illustrating transparent surfaces	1/5
710		165
/.1.2:	Perceiving and representing shape and depth	165
7.1.2: 7.1.3:	Perceiving and representing shape and depth Valley and ridge lines	165 166 168
7.1.2: 7.1.3: 7.1.4:	Perceiving and representing shape and depth Valley and ridge lines Distributed surface texture	165 166 168 169
7.1.2: 7.1.3: 7.1.4: 7.2: Futt	Perceiving and representing shape and depth Valley and ridge lines Distributed surface texture Ire work	165 166 168 169 171
7.1.2: 7.1.3: 7.1.4: 7.2: Futu Appendix A:	Perceiving and representing shape and depth Valley and ridge lines Distributed surface texture Ire work Dbserver study written instructions	165 166 168 169 171 175
7.1.2: 7.1.3: 7.1.4: 7.2: Futu Appendix A: Appendix B:	Perceiving and representing shape and depth Valley and ridge lines Distributed surface texture ure work Observer study written instructions Dbserver study recorded responses	165 166 168 169 171 175 178

List of Tables

		Page
Table 6.1:	Shortest distance visible in the central view, in voxel units, between the outer and inner surfaces in each of the trial datasets	140
Table 6.2:	Proportion of the outer transparent surface covered by opaque or semi- opaque texture elements in the center view of each test dataset	144
Table 6.3a:	Average statistics for the test images with no texture applied to the outer transparent shell	152
Table 6.3b:	Average statistics for the test images with "grid line" texture applied to the outer transparent shell	153
Table 6.3c:	Average statistics for the test images with "principal direction" texture applied to the outer transparent shell	154

List of Figures

	Р	age
Figure 2.1	A selection of published images illustrating some of the applications that require or can benefit from the display of multiple superimposed surfaces	6
Figure 2.2	Two-dimensional display of the dose distribution over anatomy	10
Figure 2.3	"2 $\frac{1}{2}$ D" representation in which the dose distribution is displayed on orthogonal 2D slices through the anatomical volume	11
Figure 2.4	Three-dimensional display of radiation beam and anatomical surfaces	11
Figure 2.5	Multiple superimposed opaque surfaces	12
Figure 2.6	A series of photographs illustrating the three basic types of transparent surfaces encountered in everyday life	14
Figure 2.7	An illustration of the progression toward achieving photorealism in the modeling and illumination of transparent surfaces	15
Figure 2.8	Photographs illustrating the insufficiency of physically accurate rendering as a complete solution to the problem of representing transparent surfaces that can be adequately seen and also seen through	16
Figure 2.9	Photographs illustrating the difficulty of interpreting models constructed from layered transparent surfaces	17
Figure 2.10	An illustration of the global nature of transparency perception, based on the painting "Silver" by Albert Joseph Moore	18
Figure 2.11	Images demonstrating the effects of various figural conditions on the perception of transparency	19
Figure 2.12	A photograph of the marble sculpture "veiled nun" by Guiseppe Croff	20
Figure 2.13	An illustration of some of the luminance constraints affecting our perception of transparency	21
Figure 2.14	An illustration of some of the luminance and color contradictions that are tolerated in transparency perception	22
Figure 2.15a	Techniques for the representation of transparency in art and illustration	23
Figure 2.15b	Texturing techniques for the representation of transparency in illustration	23
Figure 3.1	An illustration, based on figures and discussion in [Nakayama et al. 1989], showing the effect of occlusion boundaries on the perception of relative depth and figural continuity	32
Figure 3.2	A photograph illustrating linear perspective (the apparent convergence, in the two-dimensional projection, of lines known to be parallel in the three dimensional scene)	32
Figure 3.3	A pair of photographs illustrating appropriate and inappropriate situations for using the "relative familiar size" cue to depth	33
Figure 3.4	A photocollage, modeled after an illustration by Lehmann [1966] (cited in [Metzger 1975]), that attempts to demonstrate the subordinate role of relative size in the judgment of relative depth	34

Figure 3.5	Experimental set-up constructed by Gibson [1950a] to demonstrate the tendency we have to perceive an object as resting on the ground plane over which it is superimposed in a projected view	35
Figure 3.6	A photograph illustrating the "aerial perspective" cue to depth	36
Figure 3.7	A photograph illustrating how an impression of distance can be intuitively understood from differences in relative focus, in an image with few complementary depth cues	37
Figure 3.8	An example of sample stimuli used by Yonas et al. [1978] to examine the influence of cast shadows on the perception of relative depth, height and size in pictorial representations	39
Figure 3.9	A photograph [Réunion des musées nationaux] of a leaf of a 6th century ivory diptych, in which variations in the extent of the relief are made apparent by the presence or absence of cast shadows	40
Figure 3.10	A photograph [Réunion des musées nationaux] of an 18th century stone relief [Clodion 1782] in which shading is the only available cue to shape	41
Figure 3.11	A diagram explaining why specular highlights are not, in general, perceived as lying on a curved surface but as floating in space either in front or in back of it	42
Figure 3.12	An illustration, from [Goral et al. 1984], of the radiosity algorithm they proposed for modeling the interaction of light between diffuse surfaces	43
Figure 3.13	A photograph illustrating the so-called "crater illusion", in which concavities are perceived as convexities when the image is rotated by 180°	44
Figure 3.14	A diagram, from [Koenderink 1990], representing the qualitative surface shape categorization defined by his shape index	45
Figure 3.15	Photographs of bronze sculptures in which surface shape is shown through contours and shading	46
Figure 3.16	A random dot stereogram	48
Figure 3.17	An sequence of frames illustrating the type of stimulus than can evoke a stereokinetic impression of depth	53
Figure 3.18	Stimuli used by Gibson [1950a] in experiments investigating the effects of texture gradients on the perception of surface slant	56
Figure 3.19	Stimuli used by Flock and Moscatelli [1964] to measure how various types of pattern regularity in surface texture influence the accuracy of slant judgments	57
Figure 3.20	Stimuli used by Attneave and Olson [1966] to demonstrate the effectiveness of linear convergence as a cue to the direction of recession of a planar surface	58
Figure 3.21	Stimuli used by Braunstein and Payne [1969] in experiments comparing the relative effects on slant judgments of "form ratio" (the relative ratio of vertical height to horizontal width) and "perspective projection" gradients	59
Figure 3.22a	Representation of some of the stimuli used by Cutting and Millard [1984] in experiments designed to reveal the relative contributions of perspective, density, and compression cues in evoking a subjective impression of a flat surface receding in depth	60

Figure 3.22b	Representation of some of the stimuli used by Cutting and Millard [1984] to examine the relative weights of perspective, density and compression cues in evoking a subjective impression of a smoothly curving, convex surface receding in depth	60
Figure 3.23	Stimuli, representing textured, elongated ellipsoids viewed end-on, used by Todd and Akerstrom [1987] in experiments designed to reveal the characteristics of texture important for communicating shape	62
Figure 3.24	A demonstration, by Todd and Akerstrom [1987], of the results obtained when this same isolated element texture is applied to a more complicated surface, contrasted with the results obtained when a "contour line" texture (after [Stevens 1981b]) is used	63
Figure 3.25	Stimuli used by Cumming et al. [1993] in experiments examining the characteristics of texture most important for communicating shape and depth in stereoscopically viewed images	65
Figure 3.26	An illustration of the type of texture anisotropy generated by surface slant	66
Figure 3.27	An illustration of the difference between homotropic and non-homotropic texture	67
Figure 3.28	A diagram representing how one might imagine that local surface shape could be inferred from the signs of the curvatures, in the projected image, of surface "contour" lines oriented in each of the principal directions	68
Figure 3.29	Images generated by Todd and Reichel [1990] to demonstrate the wide variety of conditions under which surface "contours" (texture lines) can, and cannot, convey a compelling impression of three-dimensional shape	69
Figure 3.30	Images generated by Reichel and Todd [1990] to demonstrate how occlusion contours can affect the global consistency of locally inferred relative depth order judgments	70
Figure 4.1	Examples of sample stimuli used by Biederman and Ju [1988] in experiments showing slightly lower error rates and faster reaction times for naming (or verifying the identity of) objects represented by line drawings as opposed to color photographs, for very brief, masked exposure durations	78
Figure 4.2	Examples of photographic vs. line drawing facial recognition task stimuli	78
Figure 4.3	Examples of silhouette and contour curves in the projection of a simple object	79
Figure 4.4	Enhanced images, generated by Saito and Takahashi [1990], in which various types of depth discontinuities, found using an edge operator on a two- dimensional depth map, are highlighted with black or white lines	80
Figure 4.5	Surface patches of different shapes and their associated contour lines	81
Figure 4.6	Some contour features. Left: T-junction in the contour of an opaque surface. Right: swallowtail in the contour of a transparent surface	82
Figure 4.7	A stereo pair of images in which the surface points mapping onto the contour in the perspective projection from each eye are highlighted	83
Figure 4.8	Lines of curvature and three ridges on an ellipsoid	84

Figure 4.9	Left: a summary of the frequency with which individual points along a contour were chosen as one of the 10 points best representing the shape. Right: a drawing of a sleeping cat, derived from 38 points of relatively sharper contour curvature and the straight line connections between them	85
Figure 4.10	A comparison of figures in which deleted sections of the contour are located a) at the most highly curved regions of a figure or b) midway along the straight lines between the most highly curved regions	85
Figure 4.11	Sample stimuli used by Kennedy and Domander [1985] to show that objects are more easily recognized in images in which the contour is represented by straight lines at the midpoints of flat areas than in images in which lines are drawn only at the corner regions	86
Figure 4.12	Sample stimuli used by Biederman and Blickle [Biederman 1985] in experiments measuring the effect of contour deletion on object recognition	87
Figure 4.13	A two-dimensional surface that appears to naturally partition along its valley lines	88
Figure 4.14	An image that illustrates the effect of selectively darkening surface cavities	89
Figure 4.15	An image in which ridge lines appear to correspond to perceptually relevant surface shape features	90
Figure 4.16	A skull surface partitioned into patches using ridge and geodesic curves	91
Figure 4.17	An extremal mesh partitioning of a skull surface defined from acquired volume data	91
Figure 4.18	A photograph of a statue of Apollo of Belvedere, upon which Felix Klein had the parabolic lines drawn	92
Figure 4.19	Images of facial surfaces in which the values of the Gaussian and mean curvatures are used for shape description	93
Figure 4.20	A photograph of a transparent plastic bear, with colored tape applied along the ridge and valley lines	94
Figure 4.21	Deriving a line drawing from a photograph	94
Figure 4.22	An image in which lines are used to mark intensity discontinuities unrelated to surface boundaries or surface shape	95
Figure 4.23	"Surface intersection" lines computed by Ponce and Brady [1985] from differential geometry measurements on range data acquired from a variety of objects	96
Figure 4.24	An image, by Subsol <i>et al.</i> [1994], that very nicely illustrates a set of ridge lines on an isointensity surface in acquired volume data, computed according to the approach of Monga <i>et al.</i> [1992]	96
Figure 4.25	A demonstration of the insufficiency of a uniform representation of ridge and valley line opacity	100
Figure 4.26	Improving the display of ridge and valley information	101
Figure 4.27	A diagram illustrating the concept of a "narrow" ridge feature	103
Figure 4.28	Radiation therapy treatment plan for cancer of the nasopharynx	104
Figure 4.29	Radiation therapy treatment plan for prostate cancer	105

Figure 5.1	Examples of the use of various different types of texture to enhance the visibility of a layered transparent surface	. 112
Figure 5.2	Connolly dot and line surfaces	. 112
Figure 5.3	Examples of common methods for representing transparent skin and/or dose surfaces using graphical primitives, a type of "see-through texture"	. 113
Figure 5.4	An illustration demonstrating the potential significance of stroke characteristics	. 114
Figure 5.5	An illustration of the biasing effects of various stroke textures	. 115
Figure 5.6	Different pen-and-ink techniques for representing the surfaces of a simple object	. 116
Figure 5.7	An illustration, after <u><i>Tupa-3</i> [</u> Vasarely 1974], showing how texture can be misused to distort the appearance of surface shape	. 117
Figure 5.8	An illustration of some alternative conventions for determining stroke direction — following the light or following the form	. 118
Figure 5.9	A representative sample of medical line illustrations	. 119
Figure 5.10	An illustration of Drake's system for representing shape with line	. 119
Figure 5.11	A demonstration of the different techniques required to represent transparent and opaque spheres with line texture	. 120
Figure 5.12	An illustration by Frobin and Hierholzer [1982] in which information about back shape is communicated by short strokes on a grid, oriented in each of the principal directions, with lengths proportional to the magnitudes of the principal curvatures	. 121
Figure 5.13	A computer-generated line drawing illustration by Saito and Takahashi [1990]	. 122
Figure 5.14	An automatically-defined pen-and-ink style illustration by Winkenbach and Salesin [1994]	. 123
Figure 5.15	A semi-automatically generated line drawing illustration by Salisbury et al. [1994] in which stroke direction is defined by the intensity gradients in a 2D image	. 123
Figure 5.16	Principal direction textures with constant element length	. 125
Figure 5.17	Left: texture element length is proportional to the magnitude of the normal curvature in the stroke direction. Right: element length is constant	. 126
Figure 5.18	Methods for the display of cartographic relief	. 127
Figure 5.19	Examples of a sparse, opaque surface texture in which element orientation is defined according to the direction of steepest gradient descent	. 128
Figure 5.20	An isointensity surface of radiation dose	. 129
Figure 5.21	Alternative methods for defining element orientation	. 130
Figure 5.22	Spot textures	. 131
Figure 5.23	"Solid grid" textures, marking the intersection of the surface with planes perpendicular to various axes of the volume	. 132

Figure 6.1a	Subgroup of stimuli with no texture applied to the outer surface	141
Figure 6.1b	Subgroup of stimuli with "solid grid" texture applied to the outer surface	142
Figure 6.1c	Subgroup of stimuli with "principal direction line segment" (or "oriented dash") texture applied to the outer surface	143
Figure 6.2a	The view to the right eye of the display screen at the beginning of the first trial	145
Figure 6.2b	A "stereo" view of the screen at the beginning of the first trial, showing how the left and right eye images were displayed on alternate scan lines	146
Figure 6.3	An illustration of the second phase of each "trial" — determining in which of the two displayed datasets the outer surface comes closer to the inner	147
Figure 6.4	An illustration of the display of "answers" during the training session	148
Figure 6.5a	Chart describing the accuracy with which the closest points between the layered surfaces were localized by all subjects (pooled data)	155
Figure 6.5b	Chart describing the accuracy with which the closest points between the layered surfaces were localized by subject LVI	155
Figure 6.5c	Chart describing the accuracy with which the closest points between the layered surfaces were localized by subject TEO	156
Figure 6.5d	Chart describing the accuracy with which the closest points between the layered surfaces were localized by subject TGC	156
Figure 6.5e	Chart describing the accuracy with which the closest points between the layered surfaces were localized by subject TJF	157
Figure 6.5f	Chart describing the accuracy with which the closest points between the layered surfaces were localized by subject VLI	157
Figure 6.6	One possible view of the number and distribution of correct distance choices made by each of the observers	159
Figure 6.7	Another possible view of the rate of correct distance choices, based on the shortest distance to the inner surface from the points on the outer surface previously marked by each observer as being closest	159
Figure 6.8	Average confidence indicated by each observer in their ability to correctly specify the points on the outer transparent surface where it approached the inner more closely, arranged according to the type of texture, if any, applied to the outer surface	160