

# Example

```
int search(int a[], int &n, int x)
{    //a[] is an array of n elements
    for (int i=0; i<n; i++)
        if (a[i] == x) return i;
    return -1;
}
```

- Run-time behaviour:
  - Best case
  - average case
  - worst case

# Asymptotic notation

- $T_A(n) = c_1 \cdot n^2 + c_2 \cdot n$
- $T_B(n) = c_3 \cdot n$
- For large  $n$ , Alg B is superior to Alg A, regardless of the value of  $c_1, c_2, c_3$ .
- I.e.

$$\exists n_0 : \forall n \geq n_0 : T_A(n) \geq T_B(n)$$

# Asymptotic notation

- $T_C(n) = 4 \cdot n^2 + 10 \cdot n$
- $T_D(n) = 6 \cdot n^2$
- For large  $n$ , Alg C is superior to Alg D
- I.e.

$$\exists n_0 : \forall n \geq n_0 : T_D(n) \geq T_C(n)$$

- But...

$$\forall n : T_D(n) \leq [6/4] \cdot T_C(n)$$

- i.e., even for large  $n$ , Alg D is “worse” by *at most*

# Asymptotic notation

$$T_A(n) = c_1 \cdot n^2 + c_2 \cdot n$$

$$T_B(n) = c_3 \cdot n$$

$$T_C(n) = 4 \cdot n^2 + 10 \cdot n$$

$$T_D(n) = 6 \cdot n^2$$

- We consider Algorithm B to be *better than* Algorithms A, C and D.
- Formalized in “Big Oh” notation: