# THE AUTOMATIC SENSING AND ANALYSIS OF THREE-DIMENSIONAL SURFACE POINTS FROM VISUAL SCENES

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# THE AUTOMATIC SENSING AND ANALYSIS

# OF THREE-DIMENSIONAL SURFACE POINTS FROM VISUAL SCENES

bу

Henry Fuchs

A dissertation submitted to the faculty of the University of Utah in partial fulfillment of the requirements for the degree of

Doctor of Philosophy

Department of Computer Science

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## UNIVERSITY OF UTAIL GRADUATE SCHOOL

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To the Graduate Council of the University of Utah:

I have read the thesis of <u>Henry Fuchs</u> in its final form and have found that (1) its format, citations, and bibliographic style are consistent and acceptable; (2) its illustrative materials including figures, tables, and charts are in place; and (3) the final manuscript is satisfactory to the Supervisory Committee and is ready for submission to the Graduate School.

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# TABLE OF CONTENTS

Acknowledgements	iv
Abstract	VII
Chapter 1 Introduction	1
1.1 Problem Statement	1
1.2 A Sampling of Previous Methods	2
1.2.1 Direct Manual Measurement	2
1.2.2 Mechanical Moving Devices	4
1.2.3 A Holographic Method	6
1.2.4 A Moire Method	8
1.2.5 Multiple 2-D Images	8
1.2.6 Controlled Illumination on Objects	14
Chapter 2 Design Philosophy	17
2.1 Hardware Design Considerations	19
2.2 Analysis System Considerations	20
Chapter 3 The Hardware Sensing System	21
Chapter 4 Data Acquisition, Analysis and Object Reconstruction	21
4.1 Basic Data Acquisition Programs	21
4.2 Analysis and Object Reconstruction Methodology	27
4.2.1 Sorting	28
4.2.2 Coherence	28

•

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4.2.3 Applicability to the Present Situation	28
4.3 Description of Analysis and Reconstruction Algorithm	30
4.3.1 Analysis on Each Cutting Plane	33
4.3.2 Inter-Plane Reconstruction	37
Chapter 5 Conclusions and Further Development	47
5.1 Conclusions	47
5.2 Further Development	49
5.2.1 Hardware Improvements	49
5.2.2 Improved Analysis and Reconstruction Methods	51
Appendices	53
A. Descriptive List of Major Software Modules	53
B. Data File Formats	55
C. Sample Program Execution with Commentary	66
References	84

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#### ABSTRACT

Described are the design and implementation of a new range-measuring sensing device and an associated software algorithm for constructing surface descriptions of arbitrary three-dimensional objects from single or multiple views.

The sensing device, which measures surface points from objects in its environment, a computer-controlled, random-access, triangulating rangefinder with a mirror-deflected laser beam and revolving disc detectors.

The algorithm developed processes these surface points and generates, in a deterministic fashion, complete surface descriptions of all encountered objects. In its processing, the algorithm also detects parts of objects for which there is insufficient data, and can supply the sensing device with the control parameters needed to successfully measure the uncharted regions.

The resulting object descriptions are suitable for use in a number of areas, such as computer graphics, where the process of constructing object definitions has heretofore been very tedious. Together with the sensing device, this approach to object description can be utilized in a variety of scene analysis and pattern recognition applications which involve interaction with "real world", three-dimensional objects.

#### CHAPTER 1

#### INTRODUCTION

### 1.1 Problem Statement

Researchers in seemingly-diverse areas are often concerned with the acquisition of object descriptions. In artificial intelligence, for instance, a large part of most scene analysis systems is devoted to generating a description of objects in the system's working environment, whether this be a table-top scene of toy blocks, a rocky Martian surface, or a work-station on an auto assembly line.

In computer graphics, much time is spent attempting to create accurate pictorial images of real and imaginary objects. While the descriptions of imaginary objects are often created with the aid of an associated computer-aided design system, the descriptions of real objects usually has to be generated by laborious, largely-manual measurement techniques.

The interest in object descriptions is not limited to computer users. A prosthesis manufacturer may want to match the new artificial leg with the user's natural one, but they may not have the facilities to take more than a few basic measurements.

Researchers in artificial intelligence (specifically robotics) have been among the ones most intensely involved in the development of systems for the automatic acquisition of object descriptions. Most of their systems, however, have relied on a picture-oriented sensor, usually a TV camera. This report hopes to demonstrate that a significantly different kind of sensor, a computer-controlled rangefinder, may also prove useful for

some of these tasks. The design and implementation of such a rangefinding system is described. To demonstrate the feasibility of this approach, a simple scene-analysis algorithm is implemented, which can generate, solely from the range data, descriptions of objects in the sensor's field of view. It is hoped that this research will stimulate other attempts at sensing systems more readily adaptable to the computer than the human-oriented TV camera.

#### 1.2 A Sampling of Previous Methods

## 1.2.1 Direct Manual Measurement

The most elementary method of digitizing objects is by direct, manual measurement. With the aid of yardsticks, plumb lines and calipers, a great many solid objects can be successfully measured, and the set of values later input to a computer system.

This idea of being able to specify an arbirarily complex three-dimensional object with a set of simple measurements is hardly a recent development. The Renaissance artist Leon Battista Alberti, in his book *Della Statua*, published in 1440, describes a method for the accurate measurement of the human form (Figure 1-1). He claimed that by using his method, different parts of the same statue could be constructed at separate places and would still be able to fit together [10].

Today's approach, still basically the same, is often to mark all points of interest --"key" points -- on the surface of the original object and then measure the distance of each of these points from a common reference position (Figure 1-2). The surface is then defined as a topological net over these key points. Of course, many tedious hours must be spent to carefully measure the position of each selected point on the original



Fig. 1-1: Alberti's "Definer" (from [10])



Fig. 1-2: Manual measurement today (from [18])



object. The results are, however, often surprisingly effective. Although this method is not practical for serious, large-scale digitizing, it should be noted that it has several advantages over the other more sophisticated methods. Obviously, it requires almost no equipment -- hence no cost, except of course for manual labor. The resulting descriptions also tend to be very compact, since the user naturally wants to minimize the number of points that he has to measure. Although the less compact descriptions resulting from the more sophisticated automatic methods can often be trimmed in size according to some algorithm, it turns out that the subjective criteria used by humans are usually more effective.

### 1.2.2 Mechanical Moving Devices

An obvious next step to the simple manual approach is to substitute some computer sensing device for the user's calipers and yardsticks. The human user still has to define the surface points and their interconnections, but now he can just move some pointer around the object and tell the computer when the "current" position is of interest.

One device of this type is the so-called three-dimensional "crane" (Figure 1-3). This is a mechanical arrangement of rods and gears which allows sliding movement in each of the three axial directions. Through the amount of turning of each of three gears, the computer can calculate the distance extended along each axis. The user simply positions the tip of the crane's arm to a point of interest and instructs the computer --through a foot switch in this case-- to note the current position. Although this method is much faster than the completely manual approach, it is still very time-consuming. More serious is the severe limitation to the range of object sizes which can be measured. Being a mechanical device, there are also considerations of Its bulkiness and the inertia and slippage of its moving parts.



Fig. 1-3: Direct measurement with a 3-D "crane" (from [18])



Fig. 1-4a: Detail of fishing-line digitizing unit (from [20])



Fig. 1-4b: Fishing line-connected 3-D digitizing handle ("wand") resting on tripod (from [20])

A large variety of devices of this same general type have been constructed. One such device has been in use at the University of Utah for a number of years [20]. It uses three separate spring-loaded fishing-reel/fishing-line units (Figure 1-4a). These three assemblies are placed around the top corners of the working volume and the ends of the three fishing lines are all connected to the tip of a pointing device (Figure 1-4b). From the amount of rotation on the shaft of each reel, the length of fishing line rolled out can be calculated. Assuming that the lines are unobstructed, the three-dimensional position of the pointer tip can be calculated from the three separate lengths of the fishing lines.

#### 1.2.3 A Holographic Method

Gara, Majkowski and Stapleton of General Motors Research Laboratories report the development of a novel new digitization technique [8]. Although their system does not have direct applicability to the interaction-oriented scene analysis applications, it may provide a solution to the off-line object-digitization problem.

Their method consists of first taking a controlled, high-quality holograph of the object of interest, then extracting surface measurements from the developed holograph with a special-purpose computer-controlled video viewing system. The surface measurements are calculated by moving the video detection sytem about the object's holographic real image. As seen in Figure 1-5, there is a large angular orientation between the face of the video detector and the object's surface image to allow both in and out of focus parts of the image to hit the video detector's surface. The intersection of the object's surface and the video detector's face is the locus of points on the detector face at which the image is in sharpest focus. Figure 1-6 shows a typical video image from the detector. (To aid in this focus-determination process, an optical



Fig. 1-5: Orientation of video detector to holographic real image



Fig. 1-6: Image from video detector showing in- and out-of-focus areas



Fig. 1-7: Signal from part of one scan line, showing a region of focus (all three figures from [8])



interference pattern was projected onto the object's surface when the holograph was taken.) Figure 1-7 shows the video signal from one. scan line, the point of optimum focus being at the peak of the signal's envelope. After the optimum-focus locations are determined in a single video image, the system incrementally moves the video detector in an attempt to track the object's surface contours. In this way, all visible surfaces of the object can eventually be measured.

## 1.2.4 A Moire Method

Speight, Miles and Moledina report the application of a Moire method (suggested by H. Takasaki [19]) to the 3-D measurement of slaughtered animal carcasses [17]. Figure 1-8 shows an overhead view of the geometric arrangement of camera, flash-gun light sources, sliding grid and the carcass of interest. The resulting photographic image contains contour lines each of which is of equal depth from the grating plane (Figure 1-9). Although the actual digitization in the reported system was largely a manual operation, there do not seem to be any theoretical obstacles to the automatic processing of these contour maps. The main limitation to applying this method to the more general object-description problem may lie in the method's difficulty in accurately capturing complex, detailed, rapidly-varying surface structures.

## 1.2.5 Multiple 2-D Images

Acquisition of three-dimensional information from multiple two-dimensional photographic images is not just a widely used digitization method, but is the basis for an entire technical field, stereo-photogrammetry -- most likely inspired by the human stereo vision system.


Fig. 1-8: Geometry for generating Moiré patterns (from [17])



Fig. 1-9: Moiré contour maps of 4 views of a lamb carcass (from [17])



The geometry is beautifully simple. If a picture of a three-dimensional environment is considered to be an image drawn on a window-pane in front of the viewer's eye, then a point on that picture must correspond to a spot in the environment somewhere along the line defined by the viewer's eye and the point on the image.

Given another eye-image pair at a different orientation to the object, and assuming the point of interest is in view in both images, the point's three-dimensional position is simply at the intersection of the two lines of sight (Figure 1-10).

A variety of methods are based on this simple idea. A common technique consists of marking the points of interest on the object itself, then taking pictures from at least two different viewpoints (Figure 1-11). If the camera/eye positions and orientations are not known, they can be calculated from the correspondence between the picture positions and the known 3-D positions of a number (at least 6) of "reference" points in the object's environment [14].

When marking the subject is not practical, other methods can be employed. The common practice is to take two pictures from locations only a small distance from each other -- similar to the two human-eye views. An operator then looks at these images through a suitably adjusted stereo viewer and perceives the three-dimensionality of the object. By moving a pointer in each view until they "merge" in the virtual three-dimensional environment, he performs the correspondence which previously consisted of manually marking the object. From the X,Y distances of the pointers in each image, the three-dimensional position of the perceived point can be calculated [10]

An obvious advantage of this viewing approach is that an indefinitely large number of points can be digitized, since with the marking method, only the actual points marked can be measured. But with a stereo viewer, the accuracy of the measurements depends not



Fig. 1-10: Triangulation from two images



Fig. 1-11: Actual digitization using two images with a data tablet (from [18])



only on the interocular distance, but also on the visual acuity -- and the patience ! -- of the operator.

Several attempts have been made to eliminate the need for the human operator to specify the corresponce for each point to be measured. Levine et. al. [12], expand on an earlier algorithm of Julesz[11] which is based on the observation that when two views of a scene are taken from nearby positions, relative to the objects, then the differences between corresponding parts of the two images is largely an X-axis offset, with the amount of offset related inversely to the distance of the object from the viewer (see Figure 1-12).

The technique then, is to digitize the two images and cross-correlate parts of corresponding scan lines. The X offset of the best fit can be used to calculate the three-dimensional position of the point defined by the center of the two matching scan-line segments.

Some initial success has been reported with this method. The obvious difficulty is that the viability of the offset-difference assumption (due to the depth-variation of the object surface) is often inversely related to the distance of the object from the viewing position; the assumption is reasonable for distant or flat regions where the view from both eyes is essentially the same, but it is often invalid for close-by objects, as with the face of a person, for whom one view may contain one side of the nose, and the other view may contain the other side. On the other extreme, if the image of the local surface is too similar in both images -- e.g. flat side of a building, a new sidewalk -- then there will also be difficulties due to a lack of characteristic features with which to achieve a high cross-correlation.

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Fig. 1-12: Cross-correlation of stereo images for depth determination



Fig. 1-13: Object reconstruction from projected silhouettes (from [4])



As part of a more extensive project on computer vision, Baumgart[3,4] demostrates a technique of reconstructing 3-D objects from their image silhouettes. The geometry is similar to the triangulation technique in Figure 1-10, except that in this case instead of line-of-sights being projected, the cone-shaped projections of a silhouette are mapped into the object space. The object by definition is constrained to lie entirely within each and every one of these projections. Baumgart describes it as being like "the old joke about carving a statue by cutting away everything that does not look like the subject." Figure 1-13 shows 3 silhouettes of a plastic horse and a view of the reconstructed object. It is of interest to note that the input views were all from the horse's left side, while the view of the reconstructed object is of the horse's right side. Due to the projective nature of this method, however, surfaces with full concavities cannot be adequately reconstructed.

### 1.2.6 Controlled Illumination on Objects

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Methods for extracting three-dimensional information from multiple two-dimensional projections are not limited to considerations of photographs only. If the geometry of Figure 1-10 is reconsidered, it can be observed that a pencil-beam of light can replace one of the two lines-ol-sights used in the triangulation process. In this way, one of the photographs could be eliminated; the beam of light would be seen -- if not obscured by some object -- as a bright reference point in the remaining photograph. This kind of a system yields itself naturally to automatic processing; the origin and orientation of the pencil-beam of light can be placed under computer control and the photograph can be input as a video picture. If the object under investigation can be examined at length, then an arbitrary number of points on its surface can be digitized (Figure 1-14).



Fig. 1-14: Digitization with one image and a pencil-beam of light

Fortunately, the geometry of such a system is over-solved, and thus can be simplified. Instead of two lines, a plane and a single line are sufficient to uniquely define a surface point (Figure 1-15). A number of investigators have used this kind of a system [1,2,5,13,16]; a plane of light, rather than a pencil-beam, is projected onto the object's surface. In this way, from a single video image, the system can extract not just one surface position, but rather a large number of points along the visible intersections between the plane of light and the object's surface.

The method developed for the present system is in some ways the inverse of the above "plane-cf-light and single video image" design. The system is described in Chapter 3.



Fig. 1-15: Digitization with one image and a plane-beam of light



# CHAPTER 2

### **DESIGN PHILOSOPHY**

It is important in design considerations to review not only what the present limited system may be able to do, but also to delineate the scope of capabilities desired for the eventual "ideal" system.

is the basic goal of this research? It is to design a system which can easily acquire three-dimensional data and use it to construct surface descriptions of arbitrary three-dimensional objects. The general idea is to build a system in which the hardware sensor(s) and the software analysis algorithms interact to produce a more capable system than would be possible without this interaction.

The desired system would have a sensor whose orientation to the object(s) could be altered to 'allow input data from various views of the object. This could be accomplished in a number of different ways. There could be several sensors mounted at strategic locations around the system's environment. There could be a system-controlled device -- an arm, a turntable -- which could move the object. The sensor itself could be movable -- on a track, on a computer-controlled arm, or mounted on a moving platform. Of course, the particular application would influence the configuration design. For example, the "moving platform" model would be the one most likely to be used for a robotics application.

The scenario would go something like this. The object to be scanned is placed in the system's environment. The sensor starts scanning the environment according to some initial control parameters -- scanning the entire environment at a cursory level of

detail, or perhaps scanning only until a close-by object is encountered. The analysis system -- let's call it Analyzer -- processes this initial scan data and begins to contruct its object descriptions. These not yet being complete, Analyzer calculates the control parameters the sensor needs to obtain the additional input data. The sensor again gathers some data, now according to the new specifications. Analyzer processes the new scan data and integrates it into its developing object-description structures. It again determines whether it needs additional input data. If it does, it again calculates the sensor control parameters. Again, the sensor is instructed to obtain more data, according to its new set of control specifications. This interaction between the sensing device and Analyzer continues until some "completeness" criterion in Analyzer is satisfied.

This approach has several advantages over a simpler method. First, only the data which is needed is actually acquired by the sensor. In this way, neither the sensor nor Analyzer is burdened with unnecessary data. The level of detail can now vary with the specific application. If the task is to give object descriptions to help navigate a robot through an obstacle-filled environment, then one or two requests to the sensor may be sufficient. If, on the other hand, the task is to digitize some arbitrary object for a computer graphics system, then Analyzer could successively direct the sensor to those regions of the object which have yet to be charted with adequate detail. The level of input detail could also be context-dependent. If the objective is to inspect an assemblage for missing bolts, then the level of detail could be modified as Analyzer directs the sensor towards the regions of interest -- after, of course, it has located these regions from earlier inputs.

18

### 2.1 Hardware Design Considerations

For an integrated system such as the one just described, the hardware system should be as flexible as possible. Desired was a sensor which could acquire three-dimensional surface data simply, and directly under computer control. An accurate time-of-flight rangefinder would have been ideal, but, alas, too expensive. This kind of system needs very high speed electronics which are capable of sensing the delay between the time a pulse of laser light is started and the time its reflection returns from the objects's surface. This may be as little as a few nano-seconds (billionths of a second !). Time-of-flight rangefinders have been used to measure distances from a few meters to thousands of kilometers.

For the present purposes, the most reasonable of the previous approaches seems to be the "single image and a plane of light" method shown in Figure 1-15. Even with this system, however, the degree of interaction between the data acquisition and the analysis system is limited by the actual ("wall-clock") time and the computer-processing time commitment for an entire video image. Even if only one or two 3-D points are needed, an entire video image has to be input. In order to extract 3-D information, these systems must process the large amount of data inherent to a TV image. Although they can extract many 3-D positions from each TV image, the rigid input pattern required to do this -- for example, having all points be co-planar -- may discourage experimentation with analyses utilizing more context-dependent patterns of inputs, for instance, those analyses for which the density of input data varies with the level of interest in the local surface region. A system with efficient, explicit, single-point measurement capability was judged more suitable for the present effort.

## 2.2 Analysis System Considerations

Continuing the flexible approach to system design, it was decided that although Analyzer may specify control parameters to the given input device, it should not depend on interaction only with a particular kind of input device. Thus, for instance, when Analyzer is connected to the proper input device, it can be constructing object descriptions of buildings, automobiles, or microscope specimens. Also, while it can always request more data for its description-building process, it should always be ready to quit -- i.e., the *form* of its object descriptions should be the same after the analysis of one scan input as after ten. (These descriptions structures may, of course, abound with "unknown" and "not sure" markers for much of the object's surface.) It is also unrealistic to suppose that after each request to the input device, Analyzer will get the exact data it requested. Due to obstacles in its way, or because of difficult surface characteristics, the device may not be able to obtain the desired data; so Analyzer should be able to integrate any new data which it gets.

The system should also be able to deal concurrently with more than one object in the scene, and of course, there should be as little restriction as possible about the kinds of objects which are acceptable; restrictions to planar-faced solids or simple geometric shapes would be regrettable. As with any system operating in the "real world", the analysis process should not fail simply because it gets some conflicts about its environment -- e.g. different measurement values for the same surface from different views. In short, a system was sought which would be simple, yet flexible and powerful enough to allow implementation of a variety of experiments.

#### CHAPTER 3

#### THE HARDWARE SENSING SYSTEM

The present sensor implementation is a simple, computer-controlled triangulating rangefinder consisting of a mirror-deflected laser beam and spinning-disc detectors. The spinning-disc detectors were previously developed by Robert Burton as part of a PhD dissertation [6]. A basic description of his system will aid in understanding the present implementation.

The objective of Burton's project was the rapid digitization of multiple three-dimensinal points of interest. The tip of a wand, the fingertips of a designer, the key body points of a dancer can all be defined by the physical placement of very small light bulbs -- actually Light-Emitting-Diodes (LED's) -- connected by thin wire to the computer. With the room darkened, the computer, in sequence, turns on each of the lights, at which time several widely-spaced detectors are asked to note the position of the (only!) spot of light. By triangulating the data from several detectors, the three-dimensional position of the small light can be determined. A naive approach would have been to use TV cameras as detectors and find in each of the images the position of the single spot of light. The actual implementation uses much simpler, more efficient detectors than TV cameras. Each detector consists of a rapidly spinning disc set between a wide-angle camera lens and a light-sensitive Photo-Multiplier (PM) tube (see Figure. 3-1). The disc has radial slits cut at regular intervals, which at the proper orientation allow the light passing through the lens to reach the PM tube. A reference PM tube and reference light unit is added to monitor the slits as they pass by. From this information, the exact position of a slit at any instant can be calculated. Now, since

the room is entirely dark except for the illumination of the one small LED of interest, the only instant at which the PM tube senses any light is when the tube, a slit in the disc, the lens and the LED are all lined up. Since the position of the slit at that instant can be calculated from the reference PM tube data, the (unknown) position of the LED must be somewhere on the plane defined by the positions of the slit, the lens, and PM tube (see Figures 3-1,2,3). Since more than one of these sensors around the room is expected to "see" the LED, its position is simply at the intersection of all these detector-defined planes.

To modify this system into a computer-controlled rangefinder, a computer-deflected laser beam was added to replace the LED's. The amount of laser light reflected from most light surfaces was found to be sufficient to be noticed by the PM tubes in the detectors. Now any surface point within the laser's (and the detectors') field of view can be measured simply by aiming the laser beam in that direction. The deflection of the beam is accomplished by reflecting the beam off two small front-surface mirrors which are connected to the shafts of galvanometers mounted perpendicular to each other (Figure 3-4). The control signals to drive the galvanometer electronics come directly from the computer's digital-to-analog converters.

Although there are eight detectors in the present system -- two at each corner of the room -- it is easy to show that only one detector is actually necessary to obtain 3-D surface positions. Since the laser deflection system is under computer control, and the physical position of this unit in the room can be determined, the definition of the laser-beam line can be calculated directly from the current X and Y deflections. Now, since each detector identifies a plane through the room in which the spot of light must lie, the spot has to be at the intersection of this plane and the laser-beam line. (Because the present implementation has the luxury of using eight detectors, knowledge



Fig. 3-1: A spinning disc detector and a spot of light



Fig. 3-2: Details of spinning disc detector



Fig. 3-3: Primary signals from the detector system

of the laser-beam of light in the environment is not used in the 3-D calculations.)

It is important to distinguish this kind of a digitizing system from the similar ones described in Chapter 1. First, in place of the spinning disc detectors, TV cameras could have been used, similar to the "single spot of light and the single image" method shown in Figure 1-14. The primary advantage of the present disc detectors over TV cameras is their speed and simplicity. A disc (with 32 radial slits) spinning at 3500 r.p.m. scans the environment approximately 1900 times each second, as compared with the approximately 30 frames each second acquired by the standard TV camera. Also, as can be seen from Figure 3-3, each scan directly produces a single number ("C") for processing, bypassing the need to handle the approximately 250,000 points in each video frame.

Comparisons to the slightly different method of the "single image and a plane of light" (Figure 1-15) are somewhat more involved. The digitization rate of this method is substantially improved by being able to process many points (all along the plane of light) from a single video image. The orientation of the plane of light, however, can only be changed between video frames, perhaps each 1/30 of a second; so the system is "committed" to an orientation for a large number of points. With the present random-access laser-beam system, this commitment is only for a single point; so the orientation of the beam can be changed "on the fly." This feature is especially important for those applications in which the digitization of the laser beam may be a function of the previously calculated 3-D positions.

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Fig. 3-4: The laser deflection system

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Fig. 3-4: The laser deflection system


#### CHAPTER 4

#### DATA ACQUISITION, ANALYSIS AND OBJECT RECONSTRUCTION

The implemented programs consist of an interlocking set of modules, from those which directly control the sensing system to those which analyze the data and generate the actual object descriptions.

### 4.1 Basic Data Acquisition Programs

Since the laser deflection system is completely under computer control, a set of programs specify control parameters to the hardware system. These parameters are calculated from higher-level specifications obtained from the human operator. The operator can specify the subregion in the laser deflection system's field of view which is to be scanned. He can also specify the number of positions in the horizontal and vertical directions for which measurements should be taken.

Due to the primitive nature of the present scanning system, a number of strategies have been implemented in hopes of improving the accuracy of the input measurements. A multiple number of measurements are usually taken at each deflection position of the laser. The resulting measurements are then used to calculate a single more reliable value. In addition, if the laser spot is not "seen" by enough of the sensors for a minimum number of these attempts, then no final value is recorded for that particular laser position. Another filter traps any value which falls outside of the specific "working volume" of the scene. (A more detailed explanation, along with actual Teletype listings of the programs in execution, is provided in Appendix C.)

#### 4.2 Analysis and Object Reconstruction Methodology

While a number of different uses can be found for this unusual sensing system, it was decided that the task of object reconstruction would be an appropriate first application. The term object reconstruction is used here to mean the generation of complete, closed surface topologies, defined by a connected set of polygonal tiles, which approximates the surface data acquired from one or more views of the objects in the environment. Although this task has many similarities to the much-researched scene analysis problem in artificial intelligence, the present implementation has a somewhat different orientation in that it makes almost no assumptions about the specific kinds of objects it expects to find. This feature can be viewed as an advantage in favor of generality, but of course it also prevents the system from making many inferences from partial data -- concerning, for example, the likely location and characteristics of obscured surfaces.

Early in the project a similarity was noticed between this object reconstruction task and the task of visible surface algorithms in computer graphics. Basically, the task of a visible surface algorithm is to construct a particular view of a scene from a description of the objects in the scene and the specifications of the particular view. The task of the present effort is, in a way the reverse of this, to construct object descriptions from one or more views of the objects. Central to both these tasks is the effective manipulation of three-dimensional data. In a recent analysis of visible surface algorithms [18], Sutherland, Sproull and Schumacker make a number of observations which may also be applicable to the present effort. They note two important elements common to most visible surface algorithms: sorting and coherence. .

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## 4.2.1 Sorting

To bring order to the three-dimensional data with which all these algorithms must deal, they must all sort the data in an effective manner. The order of the dimensions of the sort and the type of sort used strongly influences the flavor of the final algorithm. Some sort along the Z axis first, then along the Y, then X; others sort Y first, then Z then X. The authors found implementations of almost all the combinations and even speculated on the characteristics of the algorithms which would evolve from the combinations not yet investigated.

### 4.2.2 Coherence

The idea of coherence was judged to be significant in reducing the enormous amount of processing involved in tasks of this kind. The basic notion is that there is a significant amount of coherence -- similarity, connectedness -- between adjacent parts of most pictures. In a scan-line oriented algorithm, for instance, every scan line does not have to be independently generated. Rather, it can simply be thought of as a modified version of the previous scan line. Making this modification is almost always cheaper than generating the line "from scratch."

### 4.2.3 Applicability to the Present Situation

Both these observations seem applicable, in a somewhat altered fashion to be sure, to the object reconstruction problem. Certainly some reasonable sorting mechanism must be developed to control the otherwise unwieldy interaction between all the elements of the input data. If all the input data was sorted along one of the three axial components, say the Z-axis, then the elements around one particular region (Z = 30



inches, for example) could easily be extracted and analyzed. This analysis process could presumably answer the quesion, "what do the objects 'look like' at this level" -i.e. along the Z=30 plane. The process' answer could be a set of closed contours which would hopefully approximate the cross-sections of each object at this (Z=30) level.

The coherence idea suggests that this description may not greatly differ from the results of the analysis executed at a nearby plane -- at Z=29-inches, for example. If it is found that the objects have indeed not changed significantly, then there would be no further need for analysis anywhere between these two planes; the object descriptions throughout this region would be an interpolation between the already-detemined adjoining descriptions.

Basically then, the algorithm reconstructs the scene at a sequence of these parallel planes. The cross-sectional contours found in adjacent planes are connected and a surface of triangular polygons is defined between each pair of connected countours. The final description for each object is a collection of connected contours and a polygonal surface defined over them. (In the following section this entire process in described in greater detail.)

This basic approach was chosen because it very neatly reduces the dimensionality --- initially from three to two dimensions, and as will be seen later, eventually from two dimensions to one. Also, since no assumptions are made about the input data coming from a single view of the scene, the actual data can as easily come from one as from ten different views. Neither are assumptions made about the distances between the adjacent "cutting" planes on which the actual analysis takes place; so the distances can be varied, being made larger in those regions in which the analysis proces reveals little

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change in the scene, being made smaller when the analyses from initially-adjacent planes are sufficient dissimilar. Also, as may become more apparent later, this approach allows incremental, modular improvements at virtually any place along the entire data-acquisition - analysis - reconstruction process.

# 4.3 Description of Analysis and Reconstruction Algorithm

Initially the basic surface points measured by the sensing system are converted into a surface representation. It is here that the single assumption about the scene is made. It is assumed that between adjacent scan-point positions the surface of the objects in the scene can be approximated linearly. (Of course, in an improved implementation, the distance between individual scan-point positions could be varied dynamically, perhaps according to the variation in the local surface contour, making the above assumption even less risky.) This single assumption allows the definition of a grid of small triangular tiles over the entire scanned region -- with each small triangle in the grid being defined by two consecutive laser positions on a laser scan line and a single laser position on one of the two adjacent scan lines. [Compare Figure 4-3 with Figures 4-1 and 4-2.] Of course since some of the points may be missing or may have been discarded as "unreliable", there may be holes in this surface structure.

These small triangular tiles are used as the data for all further processing. They are treated individually, so that tiles in the subsequent analysis and reconstruction programs can come from different scans, made most likely from different orientations to the scene.

Next, the entire group of these tiles -- whatever their origin -- are ordered according to their highest Z value (vertical distance from the floor). The series of



Fig. 4-1: Original 3-D data points



Fig. 4-2: Path of laser





Fig. 4-3: Polygonal surface defined over data points





"cutting planes" parallel to the ground is now determined. These can be at arbitrary positions along the Z axis. (Actually there are already some provisions for varying the correspondence between the axes named in the input data and their assignment in the analysis system, e.g. the X Y Z input sequence can be treated as -X Z Y -- see Figure 4-5.)

#### 4.3.1 Analysis on Each Cutting Plane

The cross-sectional processing on each "cutting plane" is at the heart of the analysis system. Since the input surface tiles have been sorted by Z, determining which tiles intersect the plane is straightforward. The intersections between this plane and these appropriate tiles are now calculated. Reconstructing the object cross-sections ("sectionals") at this cutting plane is a matter of organizing the just-determined line-segments into a number of simple closed regions (Figure 4-6).

The major difficulty is that these line-segments don't usually connect directly into simple closed regions. There are invariably gaps and usually some conflicts. Conflicts occur when two or more line-segments intersect or lie so close to each other that they are thought to represent the same surface, just disagreeing about its exact location. (The accuracy of the original system was claimed by Burton to be around .7 cm. At present, the system -- at least when used with the laser deflection unit -- does not achieve the same level of accuracy.)

To facilitate the construction of these closed regions, sorting is again employed -all the line-segments are ordered with respect to their larger Y coordinate. Closed regions are built up by sequentially processing the elements of this list, asking at each one, "does this line-segment connect to an already-begun regional contour ?" If it does,



Fig. 4-5: Alternate orientations of cutting-analysis plane



Fig. 4-6: The line-segment intersections between cutting plane and data polygons (segments not necessarily connected)



It is connected to that contour; otherwise a new contour is begun, with this line-segment as Its only member (Figure 4-7).

It is at this point in the analysis that the processing is effectively reduced from two to one dimension; to determine the disposition of the current line-segment, the situation is analyzed only along the horizontal line touching the top edge of this line-segment.

It is also at this stage that conflicts in the input data due to overlapping line-segments are resolved. When such a conflict occurs, a pair of new segments is generated such that the contour's boundary is defined along the "inside" of the intersecting segments. [The "inside" of a line-segment is the side on which the object is presumed to lie. This information is derived from the associated input polygonal tile whose original definition -- from the order of its vertices in the scanning pattern -enables distinction between the side of the tile toward the laser and the side toward the inside of the object on whose surface the tile lies. ]

Of course, it is possible for a line-segment to connect two already-established contours, in which case the two are merged into a single, longer contour.

Since the list of input segments is ordered, each segment need be considered only once in this region-constructing process. After all the line-segments are processed, a series of (possibly, but most likely not closed) contours will have been formed.

These contours are combined into a set of closed contours ("sectionals") by adding some artificially-created line-segments. These added segments are marked "blank-unknown" so that a later process can guide the sensing mechanism specifically to these regions in order to make direct measurements of these uncharted areas.



Fig. 4-7: Sectional building -- two started contours (unprocessed line-segments are indicated by dotted lines)



Fig. 4-8: Possible choices for sectional completion



Fig. 4-9: Optimal completion path (minimum total length) chosen



Since there are many possible connection configurations, the one is chosed which contains the minimum total length of these added "blank-unknown" line-segments (see Figures 4-8 and 4-9).

## 4.3.2 Inter-Plane Reconstruction

After sectionals have been constructed on all cutting-analysis planes (Figure 4-10), the object-reconstruction program defines a "skin" of new polygons between sectionals on adjacent levels which are determined to be connected. The connectivity criterion used here is based on the overlap of sectional bodies in the XY plane -- i.e., whether or not there would be an overlap if the Z values were ignored. In general the connection pattern between sectionals can be more complex than just 1-to-1 (see Figure 4-11).

When a sectional does not connect to any sectional on an adjacent level, it is assumed that this part of the object being reconstructed has terminated here. A "cap" polygon is then generated which covers the entire sectional.

After this sequence of determining cutting planes and sectionals and "skins" is finished for all levels from the top of the scene to the floor, all the objects in the scene have been reconstructed -- as far as possible, that is, with the given input data.

It is important to distinguish these newly-defined polygons from the original polygonal tiles (as in Figure 4-3 and Figure 4-4). The original polygonal tiles coming from the basic laser scans are unordered, may come from several different scans, usually do not completely cover the surface of any one object (i.e., have "holes") and may have conflicts among themselves as to the exact location of some surface. These new polygons which are mapped over the closed cross-sectional contours completely define each object, in the sense that there are no gaps or "holes" in the surface and all

the conflicts have been resolved in the surface structure; so, for instance, the bottom of an object can be "filled in" (as in Figures 4-12, 4-13 and 4-14e) even though no original scan data tiles were actually defined there.

The various colors in the reconstructed objects (Figures 4-13 and 4-14e) indicate different kinds of surface regions: 1) blue indicates surfaces which were derived directly from scan data, 2) green indicates parts interpolated between known points, using the completing-sectionals criterion; 3) red indicates conflicting areas -- those for which the input data conflicted about the exact location of the surface. In a more sophisticated implementation, the location of these regions could help a higher-level controller determine the most advantageous orientation of the sensing system for subsequent scan attempts.

Figures 4-14a through 4-14e illustrate the sequence of steps involved in the data analysis and object-reconstruction processes. [The actual teletype listings of the programs' executions, with commentary, are in Appendix C.]

Figures 4-15 and 4-16 demonstrate the situation in which the sectionals of the same object at adjacent analysis levels are completely disjoint in the X-Y plane. In such a case the connection between these sectionals is not discovered; this has happened in Figure 4-16 with both arms and one of the legs. Presumably subsequent scan attemps of the same object would gather enough additional data about these troublesome regions to enable the appropriate connections to be made.

Figures 4-17 and 4-18 show, in two different forms, the unprocessed scan data from scenes with a small vacuum cleaner and a chair and a small box.



Fig. 4-10: Closed contours of object at various analysis levels



Fig. 4-11: Polygonal skin defined over the contours (different object than Fig. 4-10)





Fig. 4-12: Front and back views of reconstructed object (torso)







Fig. 4-13: Color-coded front and back views of torso (Blue regions were extracted from the original laser-scan data. Green regions were added by the analysis-reconstruction process.)





Fig. 4-14a: Perspective views of two separate laser scans of a simple cube (simulated data)



Fig. 4-14b: Line-segments at a Z-level (from the above scan data) illustrating instances of gap and overlap





Fig. 4-14c: Completed cross-sections of cube, with gaps and overlaps resolved



Fig. 4-14d: Perspective views of simulated cube, reconstructed at 2 and 3 levels




Fig. 4-14e: Color-coded views of reconstructed cube, with and without top (blue = original data; green = added regions; red = conflict-resolved regions)





Fig. 4-15: Completed sectionals at 12 levels



Fig. 4-16: Incomplete reconstruction from the above sectionals





Fig. 4-17: Scanned surface of a vacuum and hose



Fig. 4-18: Laser path of a scan of a chair and a box  $\left( \begin{array}{c} & & \\ & & \\ \end{array} \right)$ 



#### CHAPTER 5

## CONCLUSIONS AND POSSIBLE FUTURE DEVELOPMENTS

## 5.1 Conclusions

A combined hardware and software system has been described and demonstrated. It can measure surface contours of arbitrary three-dimensional objects and construct completed closed contour descriptions of all the objects seen from one or more views of the scene.

While many different methods for acquiring three-dimensional data have been developed, the present approach was chosen as one which would allow the most easily-controlled and most flexible interaction with the host computer. The simple, direct mode of sensor operation -- the digitization of a single arbitrary point in the system's field of view -- seems uniquely well-suited to the general point-by-point, context-dependent operation of the many pictorial pattern recognition techniques which seem extendable to the analysis of this kind of three-dimensional data.

Also, if the laser deflection unit and the spinning-disc detectors were mobile, the system could work in a wide range of environments; in order to acquire a description of a VW automobile for a computer animation system, for instance, one would no longer need to manually measure a model VW or the actual automobile; it would be reasonable to expect that one could simply take the system out to the parking lot ( perhaps only at night,however ) and have the system itself generate the description. If the system were mounted on a computer-controlled cart, it might even be able to move around the object,

digitizing only those parts which the analysis algorithm indicated still needed more data.

As a sensor for a robot, the system may enable more efficient processing of visual scenes. As previously mentioned, the robot's vision processing could become more context-dependent; if it just wanted to move through an area, it may only need to measure and analyze a relatively few points in its direct path. Only when it encountered an obstacle would it need to digitize the local region more densely, with the pattern of the points being digitized perhaps being guided by an object recognition system.

The uses for this kind of system are not limited to traditional computer science areas. In the field of medicine, the accurate measurement and analysis of the complex, irregular contours of the human body has the potential for making available entire new areas of observation to aid the physician in the diagnosis of human ailments. Changes in the shape, size and volume of various parts -- arms, breasts, legs -- may be too small to be noticed by the unaided eye, but may signal the start of significant physiological activity. Slowly-developing deformations in growing children may not be noticed until the disorder has progressed beyond the reach of certain therapies.

Essential to the success of this kind of application is not only a suitably accurate and practical input device, but also an effective analysis system which can transform the raw surface measurements into a form meaningful to the physician. The present software system may be applicable almost without modification to some of these tasks. In the human measurement studies discussed in [10], some of the forms of graphical output bear striking resemblance to the cross-sectional contours determined by the present analysis and object-reconstruction system.

48

The object descriptions produced by this kind of system can also be used to generate program specifications for numerically-controlled milling machines. A copy of an object can thus easily be produced without touching the original. This may be useful either when the original object is too delicate to disturb, or when it is finally to be made from a material which is unsuited for the design process. With this kind of system the designer can construct the object from the material of his choice -- clay, soft wood, plastic -- and still have the final object in the required medium, perhaps aluminum or steel.

## 5.2 Further Development

Before most of these applications can become a reality, many improvements need to made, both in the actual hardware sensing system and the analysis and reconstruction software.

## 5.2.1 Harware Improvements

The weakest parts of the present sensing system are the spinning-disc detectors mounted on the corners of the room. As mentioned before, these were developed as part of an earlier project [6]. While they are an interesting first attempt, they are next to inadequate by current standards. For starters, a room ringed by four 22-inch slotted metal discs, spinning at 3600 r.p.m., is not exactly an ideal working environment. The noise alone prevents all but emergency conversation. More seriously, the heat generated by the necessarily large electric motors is such that the system must be shut down for cooling after each 30 minutes of use. Moreover, the accuracy of the system is largely determined by parameters which are difficult to calibrate: the constantly-changing spinning rate, the slightly different slit positions, the different pulse

widths from the light-sensitive Photo-Multiplier tubes.

Another graduate student, Larry Evans, is presently developing alternative digitizing methods. A number of different approaches are being explored, all based on the idea of transforming the signals from several two-dimensional images of the scene into one-dimensional measurements. A key feature of the various methods, the complete absence of moving parts, is most encouraging. Interested readers are referred to Evans' research proposal and his forthcoming dissertation [7].

The other major part of the hardware system, the laser deflection mechanism, also has several serious limitations. Being a moving mechanical device, it encounters inevitable overshoot problems when attempting to move quickly from one position to another. The present electronics attempt to minimize this problem by gradually, rather than instantly, changing the galvanometer signals from an old to a new value. This solution, however, is a very rough one at best. A significant improvement would be a system whose galvanometers could provide continuous positional feedback, from which the electronics could determine a much more accurate control signal, enabling the system to respond much faster, and presumably with more accuracy. With the increased speed, more sophisticated sensing strategies -- such a real-time contour tracking -- could become practical.

Perhaps the major inherent problem with the present hardware model is the one of obstruction. Since it is a triangulating rangefinder, it needs an unobstructed line-of-sight from both the laser origin and at least one of the detectors in order to digitize a surface position. The more extreme the concavities on the object's surface, the more often this obstruction problem prevents the digitization of a particular position. One possible solution is to have a different kind of ranging system. One which seems a

reasonable candidate is a modulated laser time-of-flight rangefinder. While there is at least one such product on the market whose specifications are outstanding, with accuracy approaching one part in 10\*\*6, its price is unfortunately prohibitively expensive [9].

Simpler, less expensive systems can, however, be constructed, but they are presently limited to an accuracy of about one inch [15]. While this is not accurate enough for most digitizing purposes, it may still be appropriate for certain other applications like robotics. These would certainly overcome many of the limitations of triangulating rangefinders. There would no longer be a need for at least two separate positions from which to triangulate. Thus the operating environment could become less restrictive. It is reasonable to expect that the range of useful distances could also be enlarged -- for instance, real autos could perhaps be analyzed instead of just toy models. All these advantages may outway the accuracy limitations for certain applications.

Of course, for some applications it may be advantages to have either the object or the sensing device on a movable platform to allow controlled changes of orientation between the sensing device and the object(s) under consideration.

## 5.2.2 Improved Analysis and Reconstruction Methods

The range of possible improvements in the software is even larger than in the hardware sensing system. Due to the modular nature of the software implementation, improvements in virtually any area can be made without modifying any other section.

The basic digitization could be made significantly more accurate. In the present implementation, the basic three-dimensional coordinate determination from the sensor



input values does not take full advantage of the fact that the line of the laser light in the room is known. If the deflection system were to be calibrated with some precision, then the angular deflection parameters could be used in these calculations. A formulation of the problem optimized to the geometry of the system may also be helpful; for instance, a polar coordinate representation with origin at the laser deflection point may yield a simpler set of equations to be solved.

Since the laser deflection is directly under computer control, an obvious improvement would be to implement a dynamically-changing scan of the environment. This could be as simple as varying the distance between adjacent sample positions based on the local surface contour, or it could be as involved as placing the entire reconstruction and recognition process directly in control of the scan. In this way, the laser beam could only be moved to those parts of the scene which were of significant interest to the system.

Perhaps the most far-reaching modification would be to infuse the analysis and reconstruction process with some 'a priori' knowledge about the objects it is likely to encounter. Such knowledge could aid not only in guiding the scanning process, but also in helping to resolve difficulties in reconstructing parts of objects about which there is incomplete information.

52

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## APPENDIX A

## MAJOR SOFTWARE MODULES

NWRSL--(NeW Real-time digitization with Scanning Laser) -- or RSL -- controls the laser deflection system, acquires raw points from the Burton Box hardware and software, generates a ---.DAT file of all acceptable 3-D measurements in a laser scan.

- NPTDIS -- (New Point DISplay) -- displays (onto a Tektronix 4012 storage scope) the raw 3-D points from a (---.DAT) file from NWRSL. It can also filter out points which are grossly out of place, the filtering being based on a minimum distance criterion from adjacent sample points.
- NGENPO--(New GENerate POlygonal surface) -- reads in a points file (---.DAT) from NWRSL and generates a surface of triangular polygons over these points. These polygon definitions are output onto a ---.POL file. For diagnostic purposes, a number of other data files can also be generated. The most frequently used ones are

---.PTB, a two-dimensional grid of characters showing whether or not the data point at each position in the scan has been succesfully digitized,

---.MDR, the original data points and the just-defined polygonal surface, In the standard (MOTION-DATARD) graphics system format. This enables easy display of the original points and polygonal covering.

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- SCANA -- (SCan ANAlyzer) -- accepts one or more pairs of point (---.DAT) and polygon (---.POL) files from NWRSL and NGENPO; and generates a file of line-segments (---.SGM). These line-segments are the intersections of the polygons with chosen cutting/analysis planes.
- MAKSEC -- (MAKe Sectionals) -- generates a (---.SEC) file of sectionals (closed cross-sectional regions) from a line-segment file from SCANA.
- OBREC -- (OBject REConstruction) -- generates complete object descriptions from a cross-sectional file (---.SEC) of MAKSEC. These descriptions are in the format of the current general-purpose graphics software at U. of Utah (MOTION-DATARD).

# APPENDIX B

# DATA FILE FORMATS

# Original Point File Format

<dat file=""></dat>	::= <scan descriptor=""> <a data="" point="">*</a></scan>	[* = one or more instances]
<scan descriptor=""></scan>	::= <number a="" line<br="" of="" on="" positions="" scan=""><scan i.d.="" number=""></scan></number>	> <number lines="" of="" scan=""></number>
<a data="" point=""></a>	::= <point i.d.="" number=""> <x-value> <y-va< td=""><td>alue&gt; <z-value></z-value></td></y-va<></x-value></point>	alue> <z-value></z-value>

A Sample ---.DAT File

531			
1001001	+.1	0.01	+20
1001002	-10	0.02	+10
1001003	-28	0.03	0
1001004	-10	0.02	-10
1001005	+.1	0.01	-20
1002005	+.1	10.01	-20
1002004	-10	10.02	-10
1002003	-20	10.03	Ø
1002002	-10	10.02	+10
1002001	+.1	10.01	+20
1003001	+.1	20.01	+20
1003002	-10	20.02	+10
1003003	-20	20.03	0
1003004	-10	20.02	-10
1003005	+.1	20.01	-20



## **Polygon File Format**

<---.POL file>

:= <one text line> <a polygon definition>\*

<a polygon definition> ::= <point i.d. number>\*\*\* <carriage-return and line-feed> [ \*\*\* = 3 or more instances ]

A sample ---.POL file

# NXSTEPS=5 NYSTEPS=3 IDSCAN=1000000 1001001 1002001 1001002 1001002 1002001 1002002 1001002 1002002 1001003 1001003 1002002 1002003 1001003 1002003 1001004 1001004 1002003 1002004 1001004 1002004 1001005 1001005 1002004 1002005 1002001 1003001 1002002 1002002 1003001 1003002 1002002 1003002 1002003 1002003 1003002 1003003 1002003 1003003 1002004 1002004 1003003 1003004 1002004 1003084 1002005 1002005 1003004 1003005



## Point-Table Format

<ptb file=""></ptb>	<pre>::= <single line="" text=""></single></pre>
<one descriptor="" line="" scan=""></one>	::= <scan #="" line=""> = <one descriptor="" position="" scan="">*</one></scan>
<one descriptor="" position="" scan=""></one>	∷= <position data="" good="" has=""> ∷= <position data="" does="" good="" have="" not=""></position></position>
<position data="" good="" has=""></position>	::= X ::= -
<position data="" does="" good="" have="" not=""></position>	::= ,

A Sample ---.PTB File

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NXSTEPS=40 NYSTEPS=30 IDSCAN=2000000						
30=,X >	<pre>&lt;.xxx,x,., xxxx,,</pre>					
29=XX	<pre></pre>					
28=XX.X.X	<					
27=X >	XXXXXX.XXX					
26=X )	xxxxxxx.xxx					
25=X	(XXX XXX XXX X					
24- X						
27-,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,						
23=,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,						
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11=XX	******					
10=	×××××××××× ×××××					
9	******					
8- X XXXXXX XX	****					
7- XXX X	Υ					
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Z=	, XXXX, , , , , , , , , , , , , , , , ,					
1=						

57



# Segments File Format

<---.SGM file > ::= <one level's segments>\* END

<one level's segments> ::= LEVEL <Z-value> <a segment description>\*

<a segment description> ::= <X1 value> <Y1 value> <X2 value> <Y2 value>
<orientation> <a single polygon description>

A Sample ---.SGM File

LEVEL 2	20.000						
9.980	-10.020	.000	-20.000	1	1002003	1003002	1003003
.000	-20.000	030	-19.970	1	1002003	1003003	1002004
030	-19.970	-10.000	-10.000	1	1002004	1003003	1003004
-9.980	10.020	.000	20.000	1	2002003	2003002	2003003
.000	20.000	.030	19.970	1	2002003	2003003	2002004
.030	19.970	10.000	10.000	1	2002004	2003003	2003004
19.990	.090	10.000	-10.000	1	1002002	1003001	1003002
10.000	-10.000	9.980	-10.020	1	1002002	1003002	1002003
-10.000	-10.000	-18.020	-9.980	1	1002004	1003004	1002005
-10.020	-9.980	-20.000	.100	1	1002005	1003004	1003005
-19.990	489	-10.000	10.000	1	2002002	2003001	2003002
-10.000	10.000	-9.980	10.020	1	2002002	2003002	2002003
10.000	10.000	18.020	9.979	1	2002004	2003004	2002005
10.020	9.979	28.000	500	1	2002005	2003004	2003005
20.000	.100	19.990	.090	1	1002001	1003001	1002002
-20.000	500	-19.990	489	1	2002001	2003001	2002002
LEVEL	9.000						
8.979	-11.021	.909	-20.000	1	1001003	1002002	1002093
.000	-20.000	-1.029	-18.971	1	1001003	1002003	1001004
-1.029	-18.971	-10.020	-10.000	1	1001004	1002003	1002004
<b>-8.</b> 979	11.021	.080	20.000	1	2001003	2002002	2002003
.000	20.000	1.029	18.971	1	2001003	2002003	2001004
1.029	18.971	13.000	10.000	1	2001004	2002003	2002004
18.989	921	10.000	-10.000	1	1001002	1902001	1002002
10.000	-10.990	8.979	-11.821	1	1001002	1002002	1881883
-10.000	-10.000	-11.019	-8.971	1	1001004	1002004	1001005
-11.019	-8.971	-20.000	.100	1	1091005	1002004	1002005
-18.989	.562	-18.000	10.000	1	2001002	2002001	2002002
-10.000	10.080	-8.979	11.021	1	2001002	2002002	2001003

10.000	18.000	11.019	8.930	1	2001004	2002004	2001005
11.019	8.930	20.009	~.500	1	2001005	2002004	2002005
<b>20.</b> 988	.100	18.989	921	1	1301001	1002001	1001002
LEVEL	3.000						
<b>2.</b> 973	-17.027	.000	-20.009	1	1001003	1002002	1002003
.000	-20.000	-7.023	-12.977	1	1001003	1002003	1001004
<b>-7.</b> 023	-12.977	-10.000	-10.000	1	1001004	1002003	1002004
<b>-2.</b> 973	17.027	.000	20.000	1	2001003	2002002	2002003
.000	20.000	7.023	12.977	1	2001003	2002003	2001004
7.023	12.977	10.000	10.000	1	2001004	2002003	2002004
12.983	-6.987	10.000	-10.000	1	1001002	1882881	1002002
10.000	-10.000	2.973	-17.027	1	1001002	1002002	1001003
-10.000	-10.000	-17.013	-2.917	1	1001004	1002004	1001005
<b>-17.0</b> 13	-2.917	-20.000	.100	1	1001005	1002004	1002005
-12.983	6.868	-10.000	10.000	1	2001002	2002001	2002002
-10.000	10.000	-2.973	17.027	1	2001002	2002002	2001003
10.000	10.000	17.013	2.636	1	2001004	2002004	2001005
17.013	2.536	20.020	~.500	1	2001005	2002004	2002005
2 <b>0.</b> 000	.100	12.983	-6.987	1	1001001	1002001	1001002
END							

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# Sectionals File Format

<sec file=""></sec>	::= <one level's="" sectionals="">≠ END</one>
<one level's="" sectionals=""></one>	::= LEVEL <z-value> <a description="" sectional="">*</a></z-value>
<a description="" sectional=""></a>	::= SECTIONAL <line-segment description="">***</line-segment>
<li>e-segment description&gt;</li>	::= <x-value> <y-value> <type (from="" line-segment="" next)="" of="" point="" the="" this="" to=""></type></y-value></x-value>
<type line-segment="" of=""></type>	∷= <standard line-segment=""> ∷= CONFLICT ∷= BLANK</standard>
<standard line-segment=""></standard>	::= POLYGON <a description="" polygon="" single=""></a>
<a description="" polygon="" single=""></a>	::= <point i.d.="" number="">***</point>

A Sample ---.SEC file

LEVEL 20.000						
SECTIONAL						
.000	-20.000	POLYGON	1002003	1003003	1002004	
030	-19.978	POLYGON	1002004	1003003	1003004	
-10.000	-10.003	POLYGON	1002004	1003004	1002005	
-10.020	-9.980	CONFLICT				
-19.709	194	CONFLICT				
-10.000	10.000	POLYGON	2882882	2003002	2002003	
-9.980	10.020	POLYGON	2002003	2003002	2003003	
.000	20.000	POLYGON	2002003	2003003	2002004	
.030	19.970	POLYGON	2002004	2003003	2003004	
10.000	10.000	POLYGON	2002004	2003004	2002005	
10.020	9.979	CONFLICT				
<b>19.</b> 709	194	CONFLICT				
10.000	-10.000	POLYGON	1002002	1003002	1002003	
<b>9.</b> 980	-10.020	POLYGON	1002003	1003002	1003003	
LEVEL	9.000					
SECTIONAL	-					
-18.989	.562	POLYGON	2001002	2002001	2002002	
-10.000	10.000	POLYGON	2001002	2882882	2001003	

-8.979	11.021	POLYGON	2001003	2002002	2002003
.000	20.000	POLYGON	2001003	2002003	2001004
1.029	18.971	POLYGON	2001004	2002003	2002004
10.000	10.000	POLYGUN	2001004	2882884	2001005
11.019	8.930	CONFLICT			
<b>19.</b> 709	194	CONFLICT			
18.989	921	POLYSON	1001002	1002001	1002002
10.000	-10.000	POL YGON	1001002	1002002	1001003
8.979	-11.021	POLYGON	1001003	1002002	1002003
.000	-20.000	POLYGON	1001003	1002003	1001004
-1.029	-18.971	POLYGON	1001004	1002003	1002004
-10.000	-10.000	POLYGON	1031034	1002004	1001005
-11.019	-8.971	POLYGON	1001005	1002004	1002005
-20.000	.100	BLANK			
LEVEL	3.000				
SECTIONAL	-				
-12.983	6,868	POLYGON	2001802	2002001	2002002
-10.000	10.000	POLYGON	2001002	2002002	2001003
-2.973	17.027	POLYGON	2001003	2002002	2002003
.000	20.000	POLYGON	2001003	2002003	2001004
7.023	12.977	POLYGON	2001004	2002003	2002004
10.003	10.000	POLYGON	2001004	2002004	2001005
<b>17.</b> 013	2.636	CONFLICT			
19.709	194	CONFLICT			
12.983	-6.987	POLYGON	1001002	1002001	1002002
10.000	-10.000	POLYGON	1001002	1002002	1001003
2.973	-17.027	POLYGON	1001003	1002002	1002003
.000	-20.000	POLYGON	1001003	1002003	1001004
-7.023	-12,977	POLYGON	1001004	1002003	1002004
-10.000	-10.000	FOLYGON	1001004	1002004	1001005
-17.013	-2.917	POLYGON	1001005	1002004	1002005
-20.000	.100	BLANK			

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END

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## A Sample of a Reconstructed Object File

Since this file is in the format of the currently popular Utah graphics software (MOTION-DATARD), interested readers should refer to the internal Computer Science Dept. memos on the subject. Basically the file consists of 3-D point positions and polygons defined over the points. The specific structure of the file here is a sequence of blocks surrounded by "NAME=" and "END=" statements. The names used with these statements are L1, L2, L3, etc., indicating the Z-levels at which the reconstruction process was applied. Defined at each level in this file are the points that lie in that plane (notice that their Z values are identical) and the polygons which form the surface between connected sectionals on this level and sectionals on the preceeding level. ( "↑" in the polygon definition sections refer to points at the preceeding level.) "COLTAB" commands indicate changes in the coloring of the polygons being defined. Colors of the polygons indicate the nature of the local surface region -- being either a 1) standard-measured surface, or 2) one which was initially blank but was later "filled in", or 3) one whose exact position was in conflict.

SMOOTH=NO NAHE=L1 BODY=SCENE POINTS 1 1 0 0 2 0 1 0 3 0 0 1 4 0 0 0 5 .000 -20.000 -20.000

```
6 -.030 -19.970 -20.000
7 -10.000 -10.000 -20.000
8 -10.020 -9.980 -20.000
9 -19.709 -.194 -20.000
10 -10.000 10.000 -20.000
11 -9.980 10.020 -20.000
12
    .000 20.000 -20.000
13
    .030
         19.970 -20.000
14
    10.000 10.000 -20.000
15
    10.020 9.979 -20.000
16
    19.709 -.194 -20.000
17
    10.000 -10.000 -20.000
18
    9.980 -10.020 -20.000
POLYGONS
  18 5 6
1
           7
COLTAB 9
  7
        9 10
               11 12
                       13 14 15
                                    16
                                       17
                                            18
2
     8
AXIS 1
       243
AXIS 2
       341
AXIS 3
      142
END=L1
NAME=L2
POP=L1
BODY=SCENE
POINTS
1 -18.989 .562 -9.000
2 -10.000 10.000 -9.000
3 -8.979 11.021 -9.022
4
   .000 20.000 -9.000
5
  1.029 18.971 -9.000
6
  10.000
          10.000 -9.000
7
   11.019 8.930 -9.000
8
   19.709 -.194 -9.000
9
  18.989 -.921 -9.000
10
   10.000 -10.000 -9.000
11
    8.979 -11.021 -9.000
    .000 -20.000 -9.000
12
13 -1.029 -18.971 -9.000
14 -10.000 -10.000 -9.000
15 -11.019 -8.971 -9.000
16 -20.000
           .100 -9.000
POLYGONS
1 15
      8 16
2 16
      8 17
3 17
      8 9
4 17
      9 18
5 18
      9 19
6 19
      9 10
7 19
      10 110
COLTAB 6
8 110 10 11
```

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# APPENDIX C

### SAMPLE PROGRAM EXECUTIONS

Here is an actual Teletype listing of the software system in execution. This informal commentary is meant to serve as a substitute for those interested readers unable to see a live demonstration. It is assumed that the rest of the dissertation and the previous appendices have been read.

(The underlined parts are those typed in by the user.)

First, the raw 3-D data are acquired from a laser-scan of a scene of object(s) by executing NWRSL (or RSL) on the "Single-User" PDP-10, the computer which controls the laser deflection system and the spinning-disc detectors.



The default scan area covers a region of approximately +/-28 units by +/-30 units at a distance of 100 units from the laser.

Declining this setting, we are allowed to specify each of the limits of the scan, to visually check them, for possible adjustment, before specifying the next limit value.

The section									
	YMIN =? -10	At each position of the laser the 3-D position							
0	OK 7 (Y/N) N	of the surface spot is measured by the							
0	YMIN =? -23	sensors and calculated a multiple number of times (for increased reliability and accuracy).							
	OK ? CY/ND N	[ In this case, this number NSAMP is set							
0	YMIN =? -26	to 10.] If the measurement attempt is successful for less than a prescribed number							
e	OK 2 CY/ND Y	(in this case 7) of these attempts (it can fail if							
-	YMAX =7 Ø	less than 3 of the sensors "see" the spot or							
6	-	the calculated position varies too far from the							
Ĭ	OK 7 (Y/N) Y	previously calculated position) then no 3-0							
0	NXSIEPS, NYSIEPS=7 15 15	the laser beam. To further minimize the							
	NSAMP>=MINSAM>=NCUTOF=? 10 7	6							
0	SCAN ID. NM. =? 1								
0	NM. OF TOTAL SCANS=? 1								
	JANT OUTPUT OF RAW MEASUREMENTS ?								
0		OK ? (Y/N) N							
	TRAPSS CALLED. IT IS NOT HERE	AND NO LONGER NECESSARY							
0	NUMBER OF L.E.D.S: 2								
C. Martin	the second s								

effect of position values which stray too far from mean position, the final value is calculated from a subset of the values which lie closest to the initial mean value. (In this case, the 6 closest values are used in the final calculations, i.e. the 1 to 4 farthest ones are ignored.)

An identification number is used for each scan so that data from multiple scan of the same scene can be uniquely identified and thus used in the same reconstruction process.

The raw measurements (as discussed above) can be output for diagnostic purposes.

Setting the number of L.E.D.'s is a vestige of Burton's program. The only purpose it serves with the laser option is to automatically eliminate calculated positions which are more than a threshold (16 inches) away from the previous position calculated.



In addition to going onto the DECtape, the data can also be directed to another device; in this application, output to the Tektronic 611 storage scope is the most convenient, enabling easy monitoring of the scan's progress.

100							
	DATA TO TELETYPE, SCOPE, OR DI	SX (T, S, D): <u>S</u>					
0	SCALE: 19	(Scale factor for putting data points onto the					
0	SI NGLE OR QUADRANT: Q	scope.)					
	G07 Y						
G	ENDFILE AND CALL RELEAS ON 10 NM. OF BAD POSITIONS: 37						
0							
0	DTA# & FILE NAME: (DTA#<-R =>	NO-OUTPUT TESTING) <u>rc</u>					
and had to		Quadrant option puts the data onto the scope in three different axes $-XY$ YZ and ZX					

(The scan now takes place -- approx. 5-10 minutes.) The End-of-File written onto theDECtape file signals the completion of the scan.

The number of points rejected (as described above) out of the (40 x 40 =) 1600 total laser positions.

Another, new scan can now be specified.

Listed now are the original data files, as they would come from the digitizing software described more fully in (NWRSL). As Appendix B, these files start with a descriptor line, telling the number of samples on a scan line (5), the number of scan lines (3), and the scan identification number (1 or 2 here). Of course most actual scans contain several hundred points or more.

It should be noted that the data used here is simulated, generated to illustrate, with minimum distractions, much of the system's capabilities.

We first generate a skin of polygons (triangles, actually) over all adjacent points which are in the input file.

N -- We don't care to save (in some disk file) all those polygons which are no good -- those for which one or more defining points are missing. We know that all current points are good.

POINT-TABLE -- is a scan grid showing present/missing status of each point.

(Like some real-world creditors, this computer system mercilessly pesters over-extended clients.)

(Dashed lines indicate typing errors.)

TBOX1.MDR -- This will be a point and polygon file of the just-defined surface in the format of the currently standard graphics software at Utah (MOTION-DATARD).

WXSTEPS =5 NYSTEPS =3 IDRCAN=122220 -102 103 -100 100 -103 153 ENLEG FIALLS OF ADDRIAG ADDRAGE ANDA AVA ANDA ANDA SALA SAUS SE

ENTER BOTTOM OF OBJECT HEIGHT (FOR COLORING THE) 7:0 SMOOTH = NO NA ME-SCAN 

COP TBOX1 DAT: 4 (TO) TTY: [ OK ]

3.91 +29

0.73 1

1.12 -12

1.11 -21 12.11 -20

13.22 -13

10.72 +11

11.01 +21

29.21 +29

1.11 -22

3.12 -11

0.01 +20

19.92 +19

11.72 -17

21.12 -11

29.92 +19

NEW POLYGON FILE NAME: ?TROXI.POL

FUCHS IS 315 PAGES OVER ALLOCATION !!

WANT NO-GOOD POLYGONS " FILE?" WANT POINT-TABLE FILE? 1866 DSK PAGES LEFT!!

WANT MOTION-DATARD DUTPHT ?Y MOTION-DATARD FILE=73 VATA 181 ... PR

VANT FILL-BLANK-POINTS 2N

3,03 3 1.12 +11

11,13 0

531

1031931 +.1

101113 -21

1991004 -19

1031335 + .1

1992095 + .1 1912034 -11

1012013 -20

1012102 -11

1022001 + 1

1093301 +.1

2391372 +13

2001003 +20

293 394 +19

2001 105 -.5

2132124 +11

29 72 973 +27

2 132 322 +13

2 903 932 +13 2793233 +29 29.93 3

2703314 +11

PNGENPO

v

532 2 191 391 -.5

1993292 -19 29.92 +19

2492015 -.5 17.91 +29

202001 -.5 10.01 -20

2913991 - 5 29.01 -27

2733035 -.5 23.31 +23

WANT POLYBONS-ONLY FILE?Y

INPUT FILE: TBOX1.DAT

1443443 -21 27,13 4 1013314 -11 21,12 -11 1003105 +.1 21.01 -21 THAT S (TO) TIY: INC

1001032 -13

> All points NOT within this defined volume are assumed to be incorrect and are discarded.

YNOW INITIALIZED TO I PTID. NEX1=1001001 PTID. NEXT=1001000 PTID. N+0

2 EXIT. tC SCOP TRAMI .POL:2 (TA) TTY: [OK] 0 WXSTEPS =5 WYSTEPS =3 105CAN=100000 1001001 1002001 1001002 1001002 1002001 1002002 1031332 10323 2 1331333 1201233 1022372 1372373 1991333 1992933 1391334 a 1031094 1992913 1 192324 1431334 1332334 1331935 1331035 1332334 1932935 3 11201 11301 1012012 1312212 1003001 100302 1972 772 1313172 172993 **1**0 1032313 131312 1913913 1002003 1003003 1002014 1902094 1293293 1993994 1002004 1003014 1002005 1912035 1913014 1973015 SCOP TRAXI .MAR. 2 (IS) TTY. ( N ) 2 SM00TH = 10 VAME:SCAN B 0 DY = 50 E 1E 5 POINTS 1 3 3 1 913 2 3 7 1 3 1 1 4 ٨ 5 -31 -5 25 £ 45 -5 25 6 45 -5 7 -32 . . 8 -37 -5 -37 -37 5 -37 ٥ POLYGONS COLTA3 5 . 5 6 7 8 1 2 7 8 9 3 6 9 7 Ð AXIS 1 2 4 3 AXI3 2 3 4 1 AXI5 3 1 4 2 a END:SCAN NAME:SONI BODY =SCENE POP = SCANI POINTS .193 .012 22.221 1 -10.111 .002 10.000 .331 ..... 3 -23 434 .321 -14,414 . Δ .101 .211 -00.201 5 .1 44 19,010 -21,000 5 -19,333 10.05 a - 10.030 10.05 a - 10.030 7 0 8 -21.111 11.121 -13.338 21,433 0 .173 11 c .1 33 21.71 7 21.111 11 -17, 477 21 -21 12 13 c 14 -10,303 21.421 -11.131 .111 15 21,010 -20,000 POLYGONS C

1 17 2

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The rest of this program is diagnostic messages; a +0 ("CONTROL-0") disables this kind of output.

We now look at the polygon file just generated; it looks good -- just a list of Input data points which define each polygon.

The large point i.d. numbers make it particularly easy to integrate data from many different scans into the same analysis structure and still maintain unique point i.d.'s.

We now look at the standard graphics format file just generated. It contains, in addition to the data in the previous point and polygon files, a definition of orthonormal vectors for easy rotation manipulations when later viewing this object. This file also defines two additional polygons -- a "floor" and a "tab" on this floor -to aid visual orientation when displaying the object(s).

The point values here match those of the original input files, except this graphic system requires consecutive point i.d.'s, starting with 1.

- 2 **S** . 10 ų 3 2 0 3 4 3 9 8 5 3 8 4 6 4 8 7 c. 7 7 5 4 5 8 7 6 9 12 11 9 19 9 11 12 11 0 12 8 8 12 13 12 13 8 13 7 14 7 13 14 15 7 14 14 6 C 15 5 15 We generate the polygons file for the second END=5 0 VI original point file. (Exactly the same as for the END:DA TA С ONGENP ) first file.) INPUT FILE: TBOX2 .DAT c. WANT POLYGONS-ONLY FILE? 1837 DSK PAGES LEFT!! FICHS IS 317 PAGES OVER ALLOCATION!! NEW POLYGON FILE NAME= ?TBOX2 .POL WANT NO-GOOD POLYGONS " FILE?" WANT POINT-TABLE FILE?Y WANT MOTION-DATARD DUTPUT?Y WANT FILL-BLANK -POINTS 74 -130 103 -103 103 -103 103 EALES 71 ALLS 92 ADALAS ANTAKAAA' AALA'AAA' JALA'AAA 97 EALES 71 ALLS 92 ADALAS ADALAS ADALAS ENTER BOITOM OF DEJECT HEIGHT (FOR COLDEINS HEF) 250 S MODIH = 10 NAME=SCAN YNOW INITIALIZED TO 1 PTID, NEX+0 For experimentation, let's alter the value of one of the original points -- from -.5 to -87.5. EXIT. ŧC. SPORT TICE 4-750-74 15P ארבאל <u>דאר דואר דאר דואר</u> ארביר <u>ביר דורפ</u>קועון 2001031 -.5 3.31 -23 2001031 -<u><87</u>.5 3.01 -23 2311031 -97.5 3.31 -23 1 5/ 5 3 2 211 331 -37.5 a.n2 -1 1 2001032 +11 C 1,23 1 2171113 +27 5441449 +14 0'45 +14 We'll again execute NGENPO to get a polygon #OVERWRITE TROX2 .DAT .7 [ 4FW VERSION] FINI mapping for this altered data file. O SV 3 DK 6 C INPUT FILE: TBOX2 .DAT

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WHAT PETERS TOPS TA & OTTO JOUT, LANS WANT POLYGONS-ONLY FILE? С We'll now look at a "no good" polygons file 1799 DSK PAGES LEFTI! to check if the polygon depending on this FUCHS IS 320 PAGES OVER ALLOCATIONI! altered (and to be discarded) data point is ٤. NEW POLYGON FILE WAME=?TVNVROY2.Pol also discarded. VANT NO-3000 POLYGONS ( FILERY NEW (FAILED) POLYGONS ( FILE NAMF=2TADY2.432 e WANT POINT-TABLE FILE?Y 86 We'll also look at ---.PTB file and check for POINT-TABLE FILE= ?T3 OYE.PT3 the discarded position. WANT MOTION-DATARD OUTPUT?Y c. MOTION-DATARD FILE=?TROY2. TOP Hopefully by defining the acceptable volume, the previously altered point will be WANT FILL-BLAWK -POINTS 24 c judged unacceptable. NXSTEPS = 5 NYSTEPS = 3 INSCANE2 233333 24123 114113 0F 4084145 V0[04E: X414, X44X, X414, X44, 7414, 744 2= С. ENTER BOTTOM OF OBJECT HEIGHT (FOR COLORING VE F) 2-0 ٤ 5 M00TH = 10 NAME:SCAN YNOW INITIALIZED TO 1 PTID+0 ¢ As expected the discarded polygon DIT. definition appears in this "discarded" list †C ς 900P TBOX2 .NGP:1 (TA) TTY: [AK] (it's the only entry). 50-1441 5445431 5431445 900P THOX2 PI3:2 (TO) TTY: [ 14 ] Looking at the point-table file we see (by 1X5 TEPS = 5 NY ITEPS = 3 I DSCAN = 2 - 13--the X's) that most of the positions have 3=\*\*\*\*\* 2 = 7 \* \* \* \* valid entries. The only missing position I = , X X X X 7304 14 (markded by a ",") is the first sample in the first row of the scan -- the very point we severely altered. MUMMY MODE? (Y/1)1 ۲ 1=13141.041 POINT FILE SCANA - This will accept an arbitrary number of point and polygon files and DESCRIPTION: 5 3 1 ٢ TOTAL NA. PTS .= 15 generate the line-segment intersections WANT SORTED POINTS? (Y/N)N between positions of the cut-plane c POLYGON FILE 1=TB0X1 .P01. (analysis plane) and the data polygons. DESCRIPTION: WASTERSES WASTERSES IDSCAMELANA TYPE DISCARDED POLYGOUS ? (Y/W) MAX .GR OUND -LEVEL? ¢ 1745 DSK PASES LETTI! FICHS IS 324 PASES OVER ALLOCATION!! ۰. n TOTAL NM. POLYGONS: IS TOTAL NM. POLYGONS CONSIDERED: POINT FILE 2:TROY2.DAT c. 15 One diagnostic output is listed here -- the DESCRIPTI DES 5 3 9 original points (from all input files) sorted TOTAL NM. PTS .= 31 WANT SORTED POLNTS 2 (Y/N) by their i.d. numbers. ¢ . 11 7 D: 1971921 23.923 ٢ 134

England - England , 112 11 , 13 1 -ر (2): [001002 ( . 12 1 J C . 19 5) = 1 811 815 -21,111 .149 ¢ 13.313 -19.309 .933 -00 6) = 1992021 20.023 14.114 ۲ ٥ 7) = 1032932 10 020 ¢ 19.919 C 8) = 1002003 9)= 1192014 -12.011 -12.000 C 19.929 0 .199 10) = 1992995 -29 999 11) = 1993991 - 29 999 ٢ .101 ( 21.121 12) = 1 813112 10,001 -10,000 C ø 999 -29 99A C 13) = 1013013 29.030 14) = 1293214 -11.999 -19.399 ٢ 22.000 21.11 C ö . 71 7 ٢ 15 a 15 a 15 a C 6 C 19)= 2011974 10,002 10,000 29)= 2031035 23.343 -.510 ¢ .113 21) = 2732341 -24 444 -.591 14.414 ¢ c 22) = 2002002 -10.000 10.000 10,000 ¢ 393 19 999 23): 2302 13 12,039 11 . 22 . ¢ 24) = 2332374 13.303 L - .599 25) = 2022115 21.911 14,414 ٢ 26) = 2003001 -20,000 -.590 ¢ 27,713 -11,111 ٢ 27) = 2113112 10 000 Su de a .331 28) = 2103033 21.444 21.120 ¢ 29)= 2713114 11.341 11,000 - 599 20 21 9 ¢ 31): 2733475 21,114 POLYGON FILE 2 =TR 1X2 .P 11. ž DESCRIPTION: WATEPS :S WASTEPS : IDSCAN:200101 10 TYPE DISCARDED POLYBONS (Y /N) 1723 DSK PAGES LEFT!! FUCHS 15 324 PAGES OVER ALLOCATION !! Y ź MAX. GROUND-LEVEL ? . 915 1 TOTAL MM. POLYGONS = 31 TOTAL MM. POLYGONS CONSIDERED= 31 C POINT FILE 3 = TYPEOUT POINTS ? (Y/N)N C TYPEDIT POLYGONS ? (Y/N) 4 Ċ TYPEOUT HIGH & LOW 7 S ? (Y/N)N TYPEOUT SORTED ? S ? (Y/")Y c 10.030 23.131 12 1 20.030 13 2 Ç 29.939 3 12 424 14 Δ 29.139 17.131 27 5 23.131 13.220 29 С 19.321 20 6 29.931 20.721 10 7 19.129 11.120 8 29,220 1.1 С 20.120 9 14,414 15 12 21.121 11.111 15 11 21.121 C 25 12 21.121 25 13 54 454 54 454 10,919 31 31 1 4 C 15 29.910 10,010 0

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Another example of diagnostic output -the high and low Z values in each polygon -- sorted by the high Z value. (This is useful for determining which polygons intersect with a cutting-analysis plane at a given Z level.

- - - -16 27.010 17. 1722 DSK PAGES LEFT!! С FUCHS IS 324 PAGES OVER ALLOCATION!! 919 24 .434 17 12.933 Å 0 .121 18 19.334 5 .12 0 10.031 19 6 .130 2 a 19.131 19 .123 11.133 27 21 .727 22 10,330 21 .121 c 23 13.329 2 .32 7 10.72 2 24 3 7 25 10,123 313 .111 26 10,123 g .12 1 27 19.323 17 The program now requests a trial .22 23 11.321 18 This 10.22 -17 22 Z value for a cutting plane. 29 c 110 33 10,223 23 program is usually run on а 19,210 .310 31 1 Tektronix 4012 graphic terminal; SCOPEFACTORS: с. XL09: -27,777 so the intersection line-segments XHIGH: 21.011 at each Z level can be observed on YLOW: -57.503 YHIGH: 23.000 C the screen. XORIGIN: 512.313 YORIGIN: 531.030 list the C Here we just YC= 7.153 line-segments, in format X1, Y1 X2, YC= 7.153 Y2, DIRECTION (not important ZHIGH: 27.334 7LOW: C .71 # 7LEVEL = ?? \* here), and POLYGON I.D. TYPE ED355 AT 715VEL: 23.000 ? (Y/4) TYPE ED355 AT 716VEL: 23.000 ? (Y/4) Ċ .212 -22.013 ţ 10 - 737 -19 077 1 13 ς. • 434 -10 54 -14 444 -14 444 • 434 -10 544 -14 444 -14 444 1 14 -D 0 27 1 27 13 1 .013 23,113 19.27 22 .033 19.974 19.434 13.343 20 1 19 09 - 19 09 19 09 - 19 09 0 19 09 - 19 09 19 09 0 11 1 11 1 -10.051 -0.051 -11.11.11.11. -11.051 -0.051 -51.151 -11.11.11. -11.015 -12.111 -11.151 -0.521 1 15 -0.042 -23 -33 - 133 - 449 -13 -23 - 13 -33 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 13 -23 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 -34 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 13 - 0.75 14 - 0.75 14 - 0.75 14 - 0.75 14 - 0.75 14 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 15 - 0.75 1 15 25 1 -11,333 25 1 11,133 33 1 1.7.121 - 511 0.070 27.117 ¢, 1 31 201201 100 1000 1000 1000 -201210 -500 - 200 13744 2022 20125 2017 501 501 502 2020 000 20 000 .003 WANT SCHEILE? (Y/N)? Here we put these line-segments WANT YEW SOM FILEDY into the newly-created segments WANT TO CLOSE EXISTING FILE?N file ---.SGM. SCH FILE MANESTADYIS .304 1 NM.SEGHENTS = FINENED DUPONT THIS LEVEL . MANT TO CLOSE STUE HOUSE MULTI-LEVEL DISPLAYS (Y/1) 1 ZHIGH: 29,333 71,00: .dld 71,FVF1,= 20 TYPE EDGES AT ZLEVEL: 0.334 2 (Y/V) TYPE EDGES AT ZLEVEL: 0.331 2 (Y/V) ς.

DISPLAY EDGES ? (NOTE: "E" TO EXIT FROM DISPLAY) (Y/N) N WANT SGMFILE? (Y/N)Y WANT NEW SOM FILE?" FINISHED DUTPUT THIS LEVEL. WANT TO CLOSE FILE NON ?N MULTI-LEVEL DIRPLAY? (Y/N) N ZHIGH: 27.234 ZLOW: .010 ZLEVEL = ?3 TYPE EDORS AT FLEVEL: 3. """ ? (Y/V) TYPE EDGES AT ZLEVEL-3, 999 2 (4/1) 1 DISPLAY EDGES ? (NOTE: "F" TO EXIT DOM DISPLAY) (Y/") V 1 223 DBK PAGES LEFT!! FUCHS IS 324 PARES OVER ALLOCATIONIT After selecting several other MANT 334FILE? (Y/1)Y levels for the cutting-analysis plane, we close the ---.SGM VANT VEW SOM FILF?" file. TINTER DUTPHT THIS SEVEL. MANT TO CLOSE THE NOW?Y We next list the ---.SGM file MULTI-LEVEL DISPLAY? (Y/4) +C 2009 I30/12.46\*+1 (TO) TIY: [0(1 we've just created. It not only gives the definition of each LEVEL 1 1972 993 1 line-segment at each level, but .... -Su'uuu - it also preserves the definition .933 -29, 333 - 13 - 10 .070 1 1000003 1 1 1992 gas in of the polygon which generated 244 24 444 1 2002 003 2: this line-segment. Although .731 10 077 1 2322774 2 this information is not used in 19.901 1 1932 372 1r the present implementation, a 1 1972 972 16 more sophisticated one could 0.027 -17.727 12.232 -12.233 -13 -53 -6 -6 -53 -53 -33 --19 -335 -19 -333 -15 -55 --0.021 .133 1 1992 995 1 take of this advantage - 100 - 10 200 10 10 000 10 200 - 0 000 10 10 00 10 200 - 0 000 10 10 00 9 979 20 200 - 0 070 9 979 20 200 - 0 070 1 2002002 20 (line-segment -10.001 to original -11,000 1 2332 04 2" polygon) mapping to control the 1 \* . 117 1 200 205 20 explosive growth of the number 11.121 21.111 117 10.001 .303 1 1992 321 13 of new polygons generated in -23,711 1 2772741 23 the later object-reconstruction - 577 -10.00? - .199 LEVEL 9.100 .113 -21,113 1 Inglass in section. 8.070 -11.321 I lastas lastas laataav -1.20 -12.071 -11.333 -13.333 I laulaat laabaas laabaat -8.079 979 11 721 330 20 333 344 21 173 1 211 113 2002 112 2002013 1 120 19.971 وبالبدة فبدكسدة فبلالدية ا 1.729 18.971 14,333 10 335 -13 338 19.080 - .921 1 1441445 1445441 1445445 8.979 -11.721 13,000 -1-2,000 لافسافها وسوقهما وسوامها a -13,330 -13,333 -11,319 -8.971 1 1341344 1342034 1341045 -11.19 .199 -3.071 -21.001 1 1001002 1000000 1002005 -18.030 552 -19 999 19,300 1 Saulaus Sausual Sausau -10,232 10,020 ø -9.979 11.321 [ 200] 002 2000 002 200] 003 11,111 10 404 11 410 8 030 20 444 2.937 11.710 - 510 113 18.090 o 23,331 -.921 Judal ladat ladat LEVEL 3.213 2.973 -17.127 .141 -24.412 1 Taalaas Taasaas Taasaas 3 .011 -21,101 -7.123 -12.077 1 1331333 1332333 133134 ---- -----

-1.925 -12.977 -11.999 -10.999 2.978 17.927 - 999 20.899 -2.978 17.927 - 999 20.897 - 998 27.991 - 7.923 12.977 1 1441449 1445443 1445449 1 5441443 5445443 5441444 1 5441443 5445445 5445443 حت 7.923 12.977 12,977 11,999 1 299 994 2992973 2992994 12.023 12.077 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.000 10.0000 10.0000 10.000 10.000 10.000 10.000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0000 10.0 1 ladias lassal lassas د 1 1001002 1002002 1001003 1 1391994 1992994 1991995 . 4 1992935 . 5.850 -14.391 14.988 12.291 -2.973 17.927 14.911 17.913 2.635 2.535 23.339 -.599 -12.983 1 5001405 5005001 500506 -11.112 1 Suulaus Suusaus Suulaus 17.713 1 2001000 2002002 2001005 د - .577 1 234 945 2442 44 2442 445 29.993 .177 12.093 -6.987 1 1401441 1405441 1441445 F 17 د PHAK 3 EC We now call the program which SEGNENTS IN-FILE NAMESTBOX12 SOM organizes the simple line-segments into closed contours (sectionals) at SECTIONALS OUT-FILE NAMESTROXIS -SEC each Z level. (Much diagnostics WANT TO ALWAYS CALL CONNECTRY follow.) د ۲۰۵۵ کې د ۲۰۵۵ کې ۲۰۱۹ ۲۰ ۲۰ ۲۰۵۵ کې ۲۰۵۵ کې د ۲۰۵۵ کې د ۲۰۱۶ ۲۰ ۲۰۱۹ کې ۲۰۱۹ ۲۰ ۲۰ ۲۰۱۹ ۲۰ ۲۰۵۹ کې ۲۰۵۵ کې د ۲۰۵۵ کې د ۲۶۷۶ ۲۰ 71.EV= 1953= 1 MDIF: -2.003 ZLEV: 20.000 DIAG AT: SHIFP TRYINIFRGEDTION: INTERS 1 [V. 3.#1] \*\* MDIF = 5.464 MOTES - .343 401 F = MOT F = 1.952 \* 21 F = -1.995 .143 101 F= MOLF: -1 915 YOI F= -.373 Y715= -1.943 VEVAI2 = 17 NEW312 = -18 313EG= 5 More diagnostics (solely for the L00KI2 = 7 AISEG: R system designer's benefit) 12 7 JOK 15 = MALE: 1.999 1.952 \*DI 7 = ISES: 0 MDIF= 1.08" MOIFE 1.942 154412= -10 1EV312 = 27 4155G= 7 L014 12 = 8 11 BISE3: 1.00% 12 = 11 1.900 MOIF: MOL F : - . 981 - .101 MOLE: 1550= 11 MDI F= -.719 MOLE: -1.003 701 F = -2.003

-1 .9'19 1917 = MDIF= -1.990 • HDI F= -2.909 -1.979 MD1 7 = MDIF: 2.029 \* 01 F = .21 9 .191 :3 ICS 101 F = 2.909 101F= -2.030 101F= MOIF= -2.930 MOIF= -1.909 7LEV: 20,000 DIAG AT: SWAPPED ISES 15 [Y . # 1100 SEFORE CONNECTLENSTH: TIP TALL DIST .114 1 1 39.004 1 2 30:004 2 1 .115 2 2 WANT DIAD AT ENTER-CONNINGTLENGTH? 1 573 DEK PAGES LEFT!! 1 0 FICHS IS 325 PAGES OVER ALLOCATION!! 1 7 FINAL+MINTOTAL= .29 .11 4 1 1 .115 2 2 IATIP: 1 IATAI'.= 1 IATIP: 2 141145 2 1411412: 2 <20,0705 <.0705 <-1,0205 <-0,0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.0705 <.07 1350: 1 771 5= -2.994 The characters between "<" and ">" MOIF= -2 114 MOIF= 2 111 are the first tokens encountered in - .0 48 101 F = each input line -- printed out as the \* DI 7 = 1.952 program first reads them in. (It's an \*DIF= -1.935 easy way to follow the program's MDI 5= -1 975 \*71 F= progress.) We can see that the \*71.5= -.113 program reads segment descriptors MD1 F= -1.043 until it reaches a new "LEVEL" YD1F= -.438 13 EG= g MOL F= indicator. .038 MDIF= 1.943 15 JA 12 = -15 VEV312 = 17 э AISEG: 7 1,00K12 = 7 BISES= 0 د L 0 0K 12 = g \*DI 5= .038 - .990 MOLET 9 MDI F= 1.087 \*DIF= -1.943 M01 F= -1.987 2 MDIF: -. 223 101 F = -1.952 MOLE: -1.003 MOI F = -.019 - .ala MOI 5 = MDIF= n 48 .310 MOLE:

F

MDIF= 1,997 \*DIF= .948 71.FV= 9.000 DIAG AT: ENTER TRYINTERSECTION: INTSEG: 12 [Y. N.#]174 MOLE : 2.999 MOLF : 1.991 -1 .9 52 :101 F = ÷ MDIFE -2 .444 -. 31 3 CYDIF: 3570PE CONNECTLENSTH: TIP TALL DIST 1 1.112 1 VANT DIAG AT ENTER-CONNNECTLENSTH? 14 FINAL-MINTOTAL: 1.112 1.112 1 1 INTIP: 141411: 1 <2.973> <.979> <-7.923> <-9.973> <.979> <-7.923> <-9.973> <.979> <-7.923> <\*19.973> <.19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-19.973> <-\*\*> <17,313> <29,003> <F1D> 1320: 1 " " I F = 2 000 2 000 10[F= ייז די -2,391 - . 40 \* DT == Here the program has encountered the 401 F = 1.952 END of the input file. 101 5 = -1.045 . 449 101 F = -1.975 ייזרא 🖅 - .000 MOIF= TIF= -1.0.12 YOI 7: -.138 1353: 8 YOI FE .739 NDIF 1 943 12.17 15 = -15 129312 = 17 4155G= 7 7 1,008 12 = 3[SE3= 0 1,10K 12 = Q MDIF: -1.943 MJI = -1.097 \* 71 F = - .993 .338 \* DI F = - .190 MOI F = YOLF : 1.087 1.981 "DI F = For illustrative purposes, we allow -1 .9 52 " )I F = diagnostic output this time. 1015= -1.004 - . 1 1 \*7I -= -.114 .44 3.300 DIAG AT: ENTER TRYINTERS EDTION: INTS ES= 401 F = MDI F = 11 [Y.N.# 1Y 71 EV= DIAGNOGTIC FILE TO DEK OR TTY 7114 TLEV: 3.300 DIAG AT: SWIFE TRYINTERSECTION: INTSEG: 11 ""3 JOI 53 : 2 3 ODY TALL BODYTIP BODYACTIVES 1 3 3 1 3 ż 2 3 2 MMACTI VES = I YTAIL GOODTAIL XTIP GOODTIP TAILACTIVE TIPACTIVE NEXTACTIVE LAST \*\*^CTIVE --• -~ . . -

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i st
900P 130x125ECNONFNS .350:1 (Th) TTY: [ 04 ] LEVEL 24.043 **SECTIONAL** .340 -23.372 POLYGON 1302033 133303 1 We now see the results of the -. 131 -19.07 POLY 101 1112112 1013113 1 -13.734 -14.333 POLYSON 1002 104 1003004 1 sectional-building programs. The -19,929 -9.981 COVT\_ICT sectionals produced carry with -.194 COUTLICT -19.739 them the information about their -12.177 14 443 501 XOM 5445400 5442440 5 11.12" PALY 111 -9.097 5405443 5443445 5 history. They are either marked .111 20,300 2014311 Sudbaus Sousaus 1) with definions of the polygons .131 19.272 PALYSAN 2002414 200303 2 which generated them, 2) as 10,003 10,000 DULADA Sassary Sassary S 0.070 C117 ICT "filler" (figure) 12,222 polygons ----.104 0119 ICT 10.70 generated to fill in unconnected 1335042 103205 1042442 13.043 -13.050 507A204 13.043 -13.959 507A204 1345805 1562465 1 3) boundary regions, or as conflicts -- part of a boundary 9.933 LEVEL region which had at least two JECTI ONAL different line-segments trying to 1. "444 2 JE x JA Sugar Substant 5. 28 JE x 30 Sugar Substant 5. -12.020 -17,249 define it. 1 120000 ASK STORE IESTI 12.071 FI DALVEDA 2001 000 2002003 2002000 Each line contains an X,Y value 1.1.0.10 13 240 50 240 541 544 5445 5465 44 54 pair and the description of the 11.210 1.031 CANT ICT line segment between it and the -.101 2019 ICT 19.770 - 001 507x304 1431445 1436441 14 12.020 following point. la'sad "la'sas survey httth lawlast ladeus la This file represents a contour description of all the (1 here) -13 300 -10 033 511 x 5 1V janjaa jaabaa ja object(s) found in the scene. H3 IS 327 PAGES OVER ALLOCATION!! 1 33 3L 4 VK

SECTIONAL 0441446 5445441 5445445 -12.983 5.250 PALYCAY -17,133 14.454 5014304 5441433 5455445 546544 14.454 5014004 5641845 5445445 5441443 -2.975 123 12 077 POLYSON 2001 004 200 003 200 004 7.123 12.233 13.311 9357338 2 441 444 2 342 444 2 441 445 17.113 2.535 CONFLICT -.194 CONFLICT 10.710 12.993 -5.987 POLYGON Turidus Turisar Turisaus Tratado Trao ado Trada das 1 221 233 1 222 202 1 202 203 "W3 -50 444 50 4304 Taulars Ladoaus Laaluav -7.723 -12.977 PALYANY -12.710 PALYANY Toulauv Liobdas Laubauv ississ juspeak justes -17.313 -2.017 PUTAUN 1001005 1002004 1002005 .100 BLAW -21,100 540 213750

INPUT (SEC) FILE: TROX12.5FC

-21,110 1.2.V.51

DHTPHT (TATAP) TILE NAME: TROVIS. MOR -11-54158-06K 1111 3ADENTER -1 WANT PLASTER ?Y contour description.

We now run the object reconstruction program to fit a "skin" polygonal over this

.

<covel> #140, NUMETTAN, LCVELNTT1 <> BUILDUAL> <. "#"> MCPUYE(140, ILVELNT1 \*\* .#0998EPDREPTAG, YTEMPT-29, 9993RT4G, IPTt5 <Pt0</pre> EXIT. †C 1 (10) TP 12 . 409 :1 (10) TTY: [0K] 3 1 2 2 4 - 10 We now lock at the completed reconstruction VAME=L1 file. It's in the standard (MOTION-DATARD) 30 DY =50 E 1E POINTS graphics format (see Figures 4-14d and 1 1 7 7 4-14e). 2 7 1 0 3 9 9 1 4 . . . 5 ·uuu -5u auu -5u 'uuu 7 -12 -013 -10 -003 -20 -034 3 -13, -27 - -27, -13 11 -0.000 11.001 -54.444 10 -14.554 11.366 -54.644 2 -16.755 -164 -54.644 133 16 043 53 54 643 193 54 963 53 264 12 17 13,153 6 6 76 - 53,333 13,153 6 6 76 - 53,333 1 4 15 15 10'140 - '107 -54'ada Ta daa -Ta saa -Sa adb 17 14 0.044 -14.024 -24.044 71143145 1 15 5 -5 7 00LT43 9 7 9 0 10 11 12-13 14 15 14 17 18 AYIS 1 2 2 3 AX15 2 3 4 1 AYIS 3 1 4 2 ENDELL VAME=L2 > )P = [1 3 DY ERCENE 201 115 1 -13,939 .552 -9.000 -11.01 10.01 -1.01 10.01 -1.01 10.01 -1.01 0.0 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 -1.02 3 4 1.20 19.071 -9.999 5 12.330 5 11 111 -0 110 11 111 -0 110 11.110 ? Q 19.709 - 194 -9.000 12.020 - 021 -0.110 12.020 - 12.100 -0.130 2.020 -11.121 -0.013 • 12 11 12 -10.000 -10.000 -0.000 13 -1.020 -10.000 -0.000 14 -10.000 -10.000 -0.000 15 -11, 110 -2,971 -9, 140 15 -22,203 .117 -9.210 PALYGONS 1 +5 9 16 15 2 17 ø 9 3 17 4 17 99 0 5 18 9 19 19 5 19 9 7 19 10 11 3 COLTAS 6 8 110 10 11

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9 11 11 12 10 119 `i2 111 11 111 12 1.3 12 +11 13 +12 13 +12 13 С 14 14 +12 14 15 COLTAS 7 15 +12 15 С 16 16 +12 16 1 COLTAB 5 C 17 +12 1 2 18 +12 2 3 19 112 3 113 20 113 C 3 4 21 +13 4 +1 4 22 t1.4 4 5 23 114 5 6 C COLTAS 9 24 114 6 +15 25 +15 7 C 6 26 115 7 11 6 27 115 7 117 28 +17 0 7 8 29 117 8 118 39 +18 8 +5 С ΕN 1826 DSK PAGES LEFT!! FUCHS IS 329 PAGES OVER ALLOCATION !! D=12 - C š VAME=L3 10 POP = L2 BODY SCENE POINTS 1 -12.983 -12.983 5.968 -3.303 10 2 3 -2.973 17.727 -3.003 .433 20.463 -3.433 7.423 12.977 -3.244 4 0 5 10.330 10.023 -3.333 6 7 17.713 2.635 -3.333 19.719 - 194 -3.711  $\overline{}$ 8 12.983 -5.027 -3.304 14.443 -14.434 -3.444 2.973 -17.327 -3.434 404 -24.464 -3.444 9 12  $\sim$ 11 12 13 -7,723 -12,977 -3,999 14 -19,970 -10,999 -3,999 15 -17,913 -2,917 -3,999 16 -29,999 -109 -3,999 ~ ~ POLYSONS COLTAS 7 11 15 1 COLTAS 6 ~ 2 11 1 2 3 11 2 12 4 12 ž ~ Ś †2 3 **†**3 6 +3 3 4 7 4 14 +3 ~ 8 14 4 5 5 9 14 15 19 15 5 5 • 11 +5 6 +6 COLTAB 9 12 15 5 7 0 13 16 7 +7 - 7 ~ ~

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14 T/
15 T7
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COLTAB
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19 19
20 110
21 110
22 111
23 111
              10 110
              10 11
                11 +11
                11
                      12
                12 +12
24 112
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                      13
25 t12
26 t13
27 t13
                13 113
                13
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               14 +14
27 113 14 114

COLTAB 9

28 114 14 15

29 114 15 15

30 115 15 16

COLTAB 7

31 115 16 116
32 115 16 11
COLTAB 6
33 14 13 12
                             11 13
COLTAB 9

    34
    14
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    35
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    16
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    14

END=L3
END= DATA
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DAY WEDNESDAY, MAY 21, 1975 05:20:11-MDT 4



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