

Computing the slope of  $x^3$  via a limit

$$\lim_{h \rightarrow 0} \frac{(x+h)^3 - x^3}{h} = 3x^2$$

A famous limit of an indeterminate form 0/0

$$\lim_{x \rightarrow 0} \frac{\sin(x)}{x} = 1$$

A limit as  $x$  approaches infinity

$$\lim_{x \rightarrow \infty} x^{\frac{1}{x}} = 1$$

A limit involving extra variables

$$\lim_{x \rightarrow 0} \frac{a^x - b^x}{x} = \ln(a) - \ln(b)$$

The limit of  $1/x$  as  $x$  approaches 0 from the left

$$\lim_{x \rightarrow 0} \frac{1}{x} = -\infty$$

A limit for which L'Hopital's rule would be slow

$$\lim_{x \rightarrow 0} \frac{(\sin(x))^{249} (\ln(1-x))^{251}}{x^{100} (\arctan(x))^{400}} = -1$$

The formula for the slope of  $x^3$

$$\frac{d}{dx} x^3 = 3x^2$$

An illustration of the chain rule

$$\frac{d}{dx} \sin(x^3) = 3x^2 \cos(x^3)$$

A partial derivative

$$\frac{d}{dy} x^2 y^3 = 3x^2 y^2$$

A 5th-order Taylor polynomial expanded about  $x=0$

$$\text{TAYLOR}(e^x, x, 0, 5) = 0.008333333x^5 + 0.04166666x^4 + 0.1666666x^3 + 0.5x^2 + x + 1$$

A 7th-order Taylor polynomial

$$\text{TAYLOR}(\ln(\cos(ax)), x, 0, 7) = -0.02222222a^6 x^6 - 0.08333333a^4 x^4 - 0.5a^2 x^2$$

An antiderivative of  $x^2$  with respect to  $x$

$$\int x^2 dx = 0.333333x^3$$

An antiderivative of cosine(x) with respect to  $x$

$$\int \cos(x) dx = \sin(x)$$

An antiderivative obtained by substitution

$$\int x^2 \cos(ax^3 + b) dx = \frac{0.333333 \sin(b) \cos(ax^3)}{a} + \frac{0.333333 \cos(b) \sin(ax^3)}{a}$$

A definite integral for  $x$  going from  $a$  to  $b$

$$\int_a^b x^2 dx = 0.333333b^3 - 0.333333a^3$$

An integral having an infinite integration limit

$$\int_{a^2}^{\infty} \frac{1}{x^2} dx = \frac{1}{a^2}$$

An integral having an endpoint singularity

$$\int_0^{b^2} \frac{1}{\sqrt{x}} dx = 2|b|$$

A 2-dimensional integral over a quarter disk

$$\int_0^r \int_0^{\sqrt{r^2-x^2}} xy dy dx = 0.125r^4$$

The formula for the sum of an arithmetic series

$$\sum_{k=0}^n k = 0.5n(n+1)$$

The formula for the sum of successive cubes

$$\sum_{k=0}^n k^3 = 0.25n^2(n+1)^2$$

The formula for the sum of a geometric series

$$\sum_{k=0}^n a^k = \frac{a^{n+1}}{a-1} - \frac{1}{a-1}$$

The sum of an infinite series

$$\sum_{k=0}^{\infty} 2^{-k} = 2$$

A sum for which iteration would be slow

$$\sum_{k=-123456788}^{123456789} \frac{k}{370370367} = 0.333333$$

The product of successive even integers

$$\prod_{k=1}^n 2k = 2^n n$$