

Rate-Based Execution Models For Real-Time Multimedia Computing

Proportional Share Resource Allocation

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Rate-Based Execution Models For Real-Time Multimedia Computing

Outline

- ◆ Rate Based Execution: The case against Liu & Layland style models of real-time computing
- ◆ A Liu & Layland extension for rate-based execution?
- ◆ Fluid-flow models of resource allocation for real-time services
- ◆ Proportional share CPU scheduling
- ◆ On the duality of proportional share and traditional Liu & Layland style resource allocation

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Proportional Share Resource Allocation

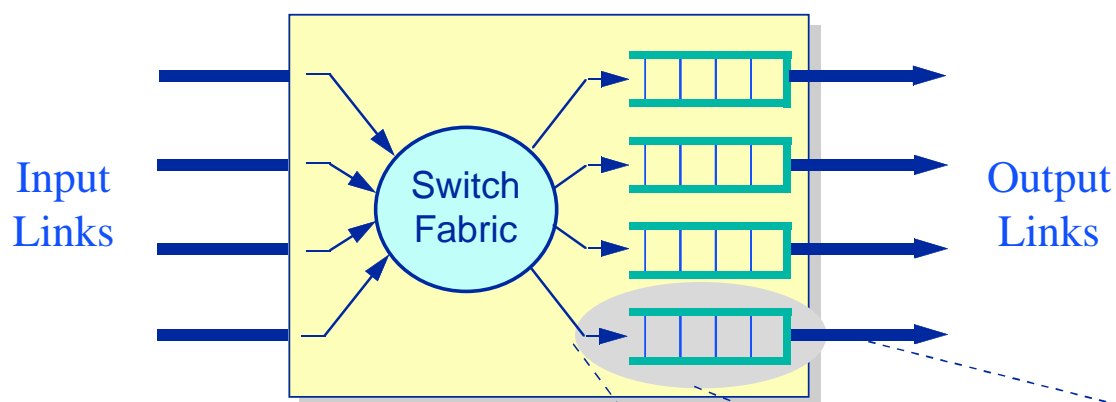
Outline

- ◆ Fluid-flow resource allocation models
 - » Packet scheduling in a network
- ◆ Proportional share resource allocation models
 - » CPU scheduling in an operating system
- ◆ On the duality of proportional share and traditional real-time resource allocation models
 - » How to make a provably real-time general purpose operating system

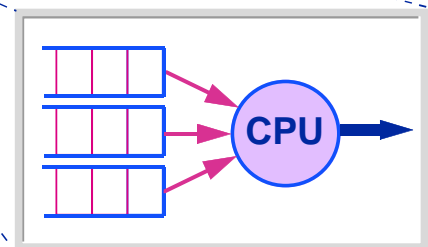
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Fluid-Flow Resource Allocation Models

Packet/Cell scheduling in a network



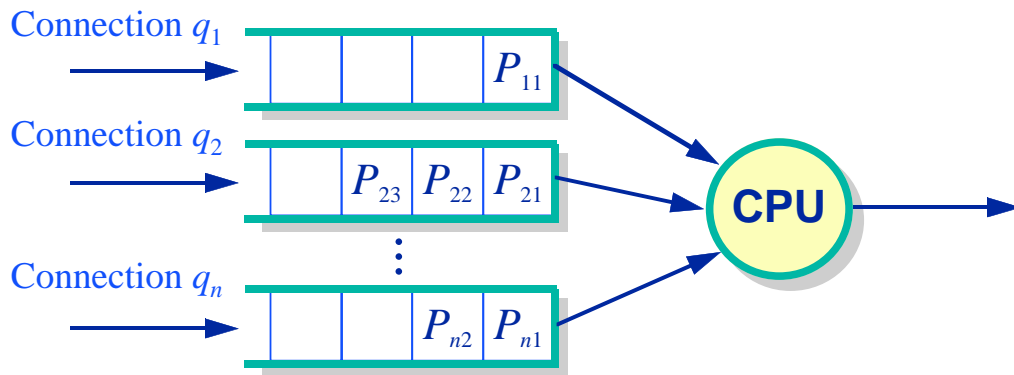
- ◆ Consider a network switch with output link buffering
 - » 1 output queue per logical network connection



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Fluid-Flow Resource Allocation Models

Packet/Cell scheduling in a network

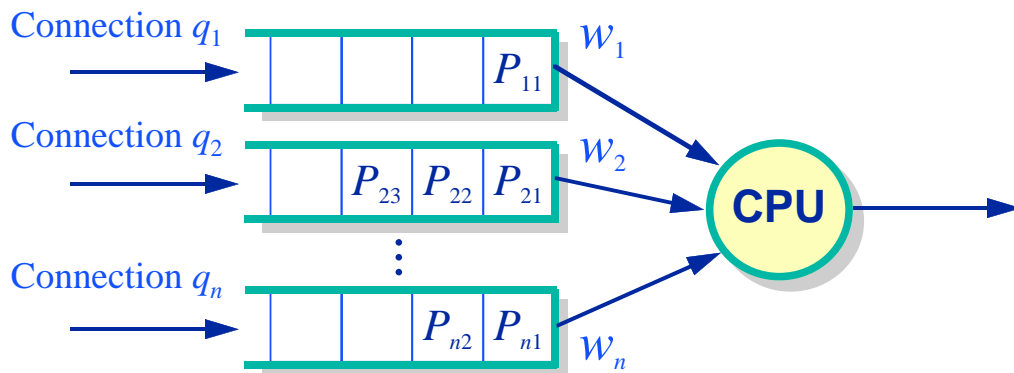


- ◆ Generalized processor sharing (GPS)
 - » service proceeds in *bit-by-bit rounds*
 - » service 1 bit from queue i during each round
 - » provides *fair* allocation
 - » provides *isolation* from other connections

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Fluid-Flow Resource Allocation Models

Generalized processor scheduling



- ◆ Connections can be differentiated by integer weights
 - » w_i bits transmitted from connection i during each round
 - » each connection receives a *fair share* of the link's capacity

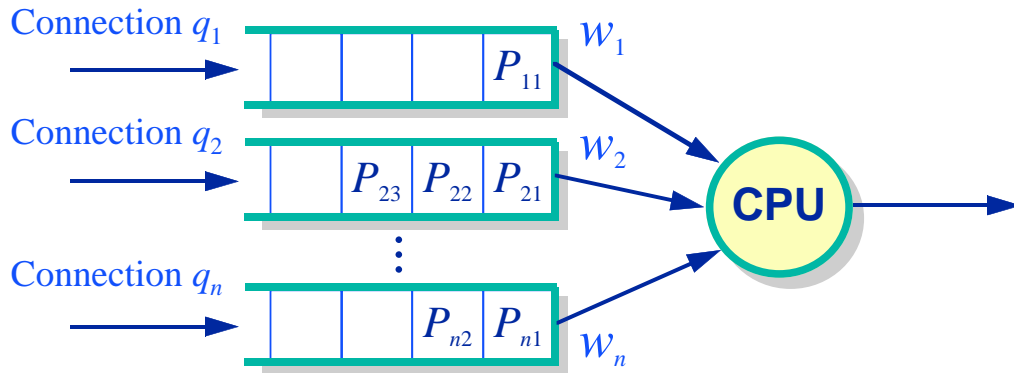
$$\frac{S_i(t_1, t_2)}{S_j(t_1, t_2)} \geq \frac{w_i}{w_j}$$

where $S_i(t_1, t_2)$ is the number of bits transmitted from connection i during $[t_1, t_2]$

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Approximations to GPS

Packet-by-packet generalized processor sharing (PGPS)

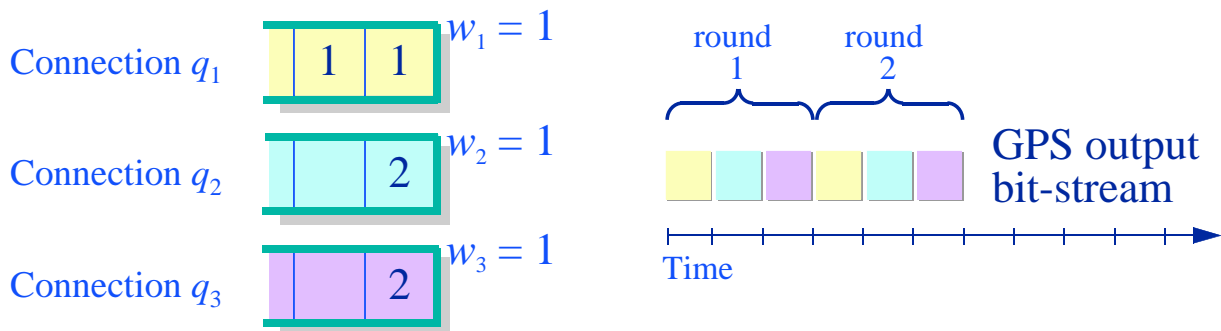


- ◆ Transmit packets as whole units rather than bit-by-bit
- ◆ Simulate GPS by scheduling packets by *finish number*
 - » the time a packet would have completed transmitted in a GPS system
- ◆ Packets with smaller finish number are scheduled before packets with larger finish numbers

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Packet-by-Packet GPS

Finish numbers example

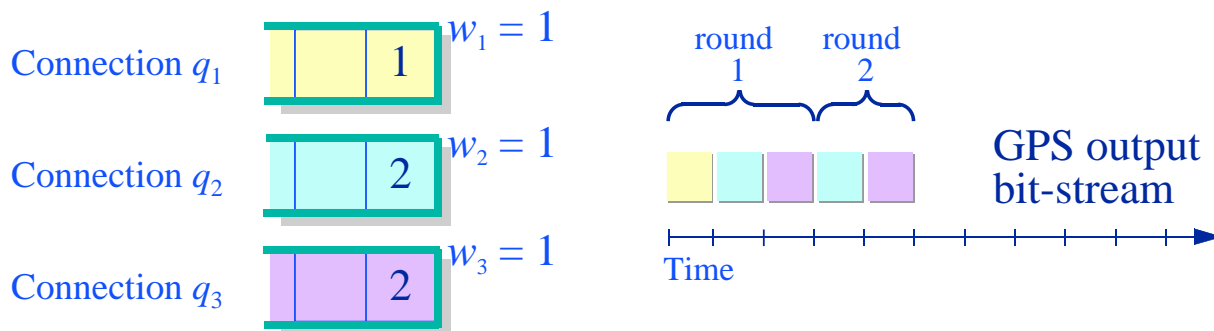


- ◆ Model GPS as proceeding in *rounds*
 - » $\sum_i w_i$ bits are transmitted in each round
 - » *finish number* = round number in which the last bit of a packet is transmitted

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Packet-by-Packet GPS

Finish numbers example

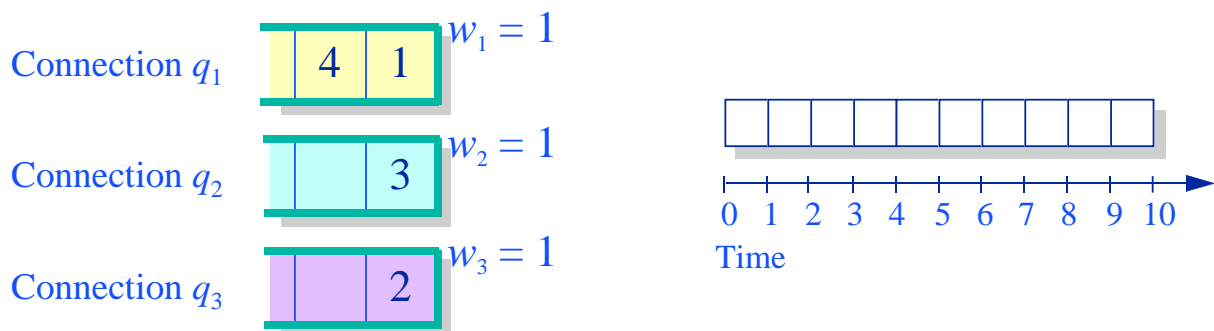


- ◆ Rounds proceed at a variable rate depending on the availability of work
 - » thus finish numbers do not necessarily deterministically map onto real-time values

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Packet-by-Packet GPS

Finish numbers example



- ◆ Finish numbers of packets are:

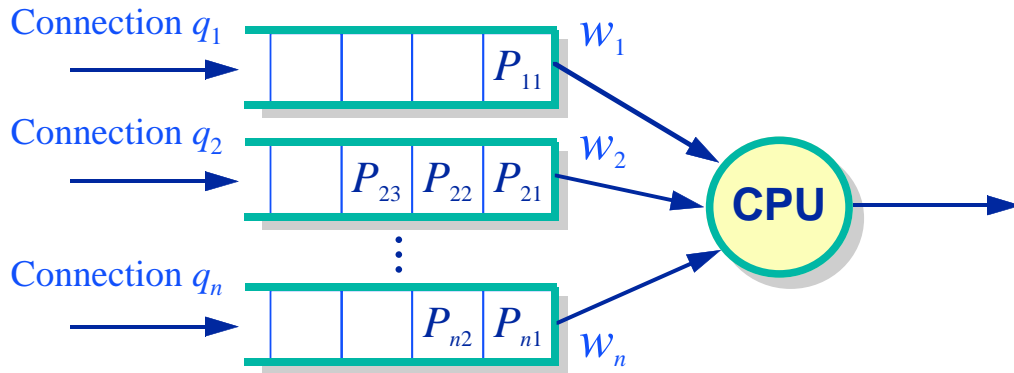
- » $P_{11} =$ » $P_{12} =$
- » $P_{21} =$
- » $P_{31} =$

(Assume the second packet from connection q_1 arrives at time 4)

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Packet-by-Packet to GPS

Finish number computation



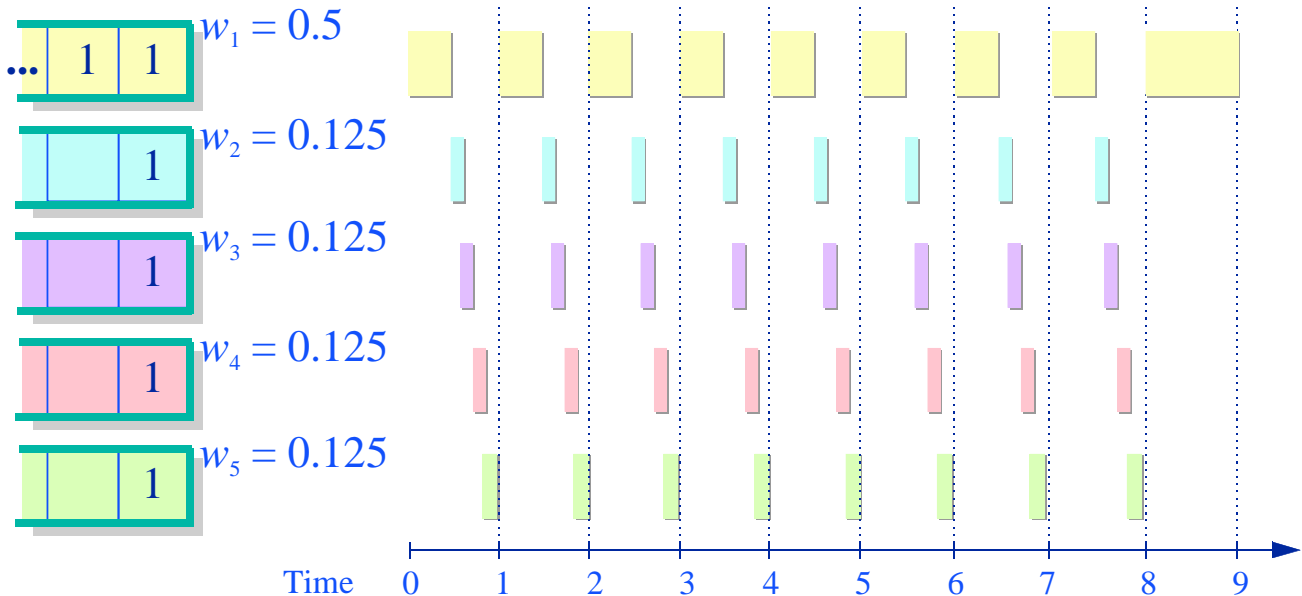
- ◆ Transmit packets by *finish number* F

$$F_{ik} = \max(F_{ik-1}, R(t)) + p_{ik}/w_i$$

- » where t is the arrival time of the packet
- » $R(t)$ is the round number at time t
- » p_{ik} is the size of packet P_{ik}

Packet-by-Packet GPS Example

Comparison with GPS

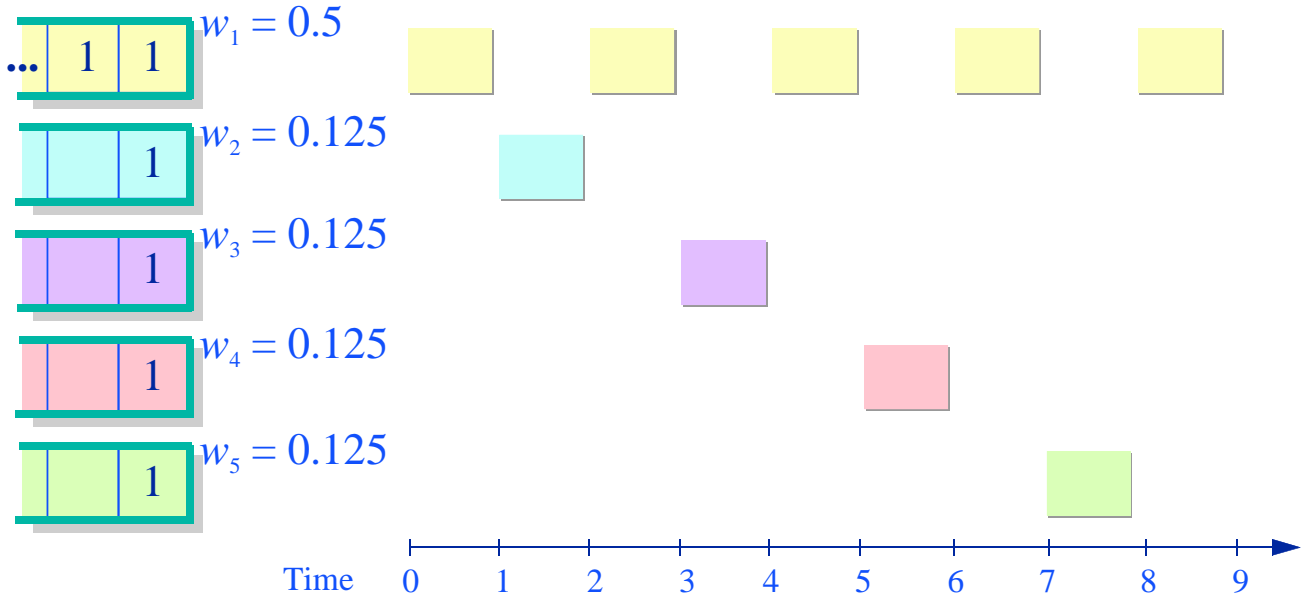


- ◆ GPS schedule for 5 connections

- » Packets for connection 1 arrive every 2 time units

Packet-by-Packet GPS Example

Comparison with GPS

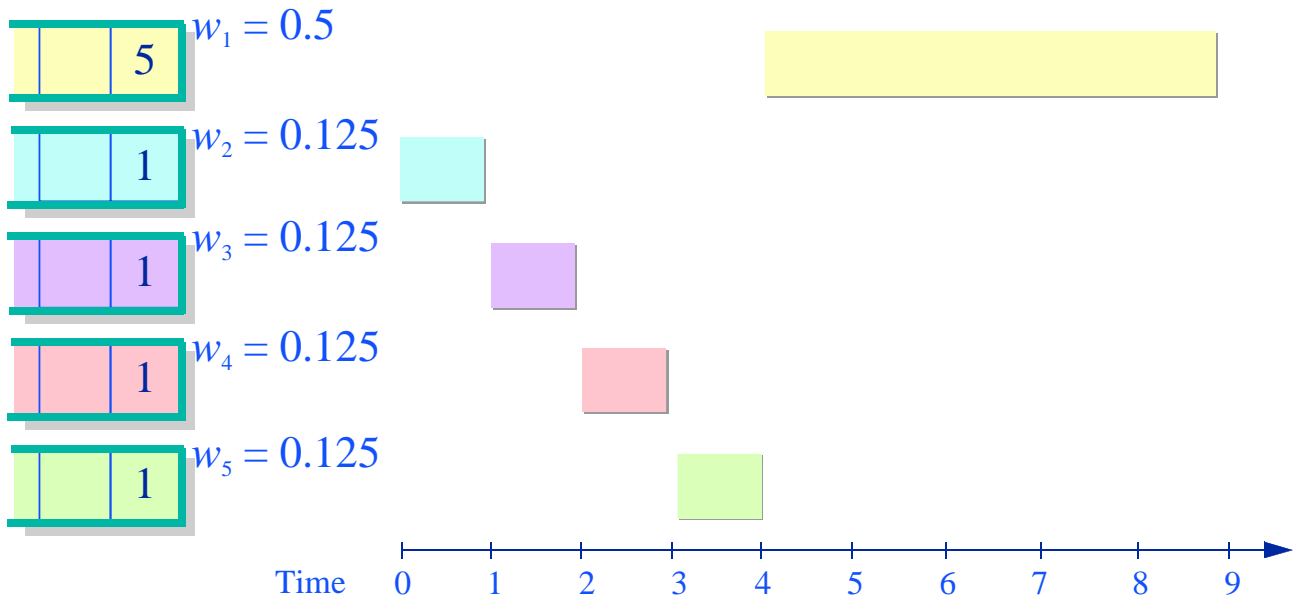


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Packet-by-Packet GPS Example

Comparison with GPS

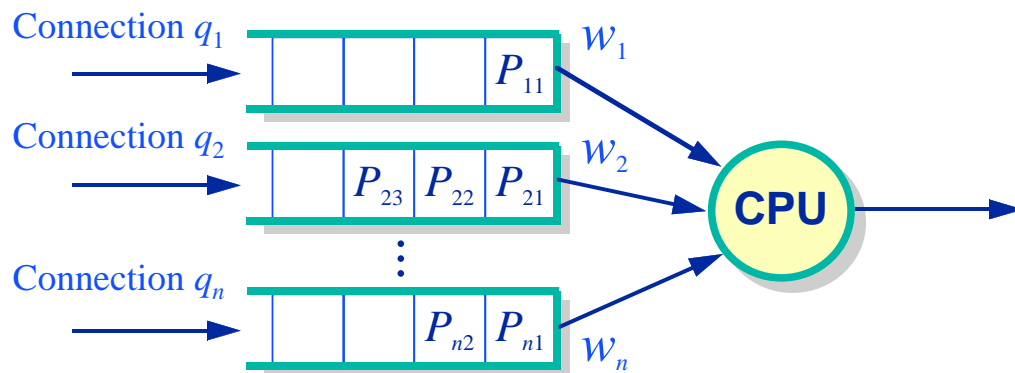


- ◆ Example: PGPS schedule for 5 connections
 - » connection 1 has a single packet that is 5 times as large

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Packet-by-Packet to GPS

Summary



- ◆ PGPS allocates link capacity *fairly* and *uniformly*
 - » a connection is guaranteed to receive a share of the link's capacity equal to

$$\frac{w_i}{\sum_j w_j}$$

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Packet-by-Packet GPS

What does this have to do with real-time?!

- ◆ Under certain assumptions about the distribution of packet arrivals...
- ◆ Connections can achieve bounded end-to-end delay in a network of PGPS scheduled switches
- ◆ And this bound is (asymptotically) independent of:
 - » the number of connections in the network
 - » the number of switches in the network

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