

### A Theory of Rate-Based Execution

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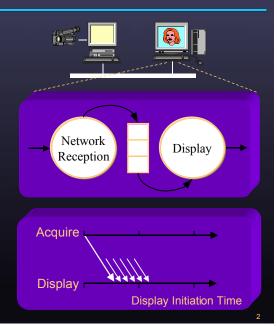
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#### A Theory of Rate-Based Execution Goals

- Extend the Liu and Layland theory of real-time processor scheduling to:
  - -Support notions of execution rate that are more general than periodic or sporadic execution
  - -Support integrated real-time device and application processing
  - -Support responsive non-real-time computing

#### A Theory of Rate-Based Execution What's wrong with the Liu & Layland model?

- Loosely speaking, nothing is periodic or sporadic in a distributed system
- The essential problem seems to be the requirement that the arrival process be somehow constrained



## Rate-Based Execution

- Schedule tasks at the *average rate* at which they are expected to be invoked
  - -Make buffering a first-class concept in the model
  - -Understand the fundamental relationships between feasibility, response time, and processing rate
- Develop a model of tasks wherein:
  - -Tasks complete execution before a well-defined deadline
  - -Tasks make progress at application-specified rates
  - -No constraints are placed on the external environment

# 1

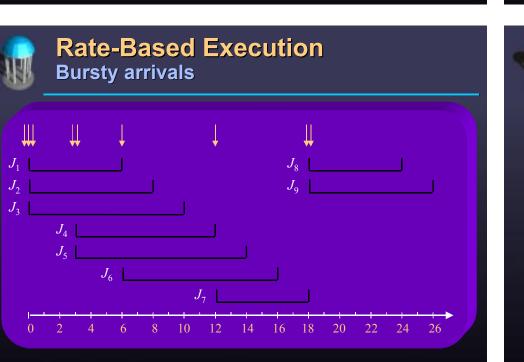
#### Rate-Based Execution Formal model

- Process make progress at the rate of processing *x* events every *y* time units, each event is processed within *d* time units
- For task *i* with rate specification  $(x_i, y_i, d_i)$ , the *j*<sup>th</sup> event for task *i*, arriving at time  $t_{i,j}$ , will be processed by time

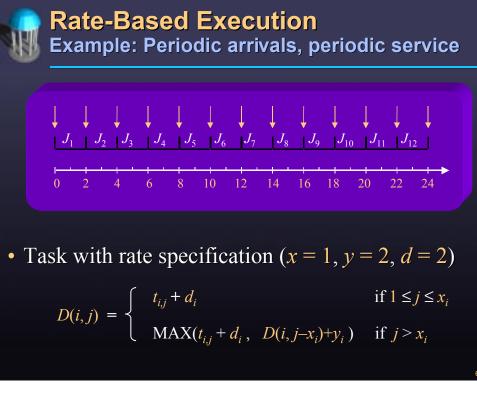
 $D(i,j) = \begin{cases} t_{i,j} + d_i & \text{if } 1 \le j \le x_i \\ MAX(t_{i,j} + d_i, D(i, j - x_i) + y_i) & \text{if } j > x_i \end{cases}$ 

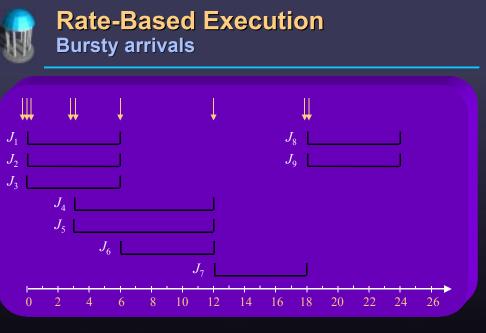
– Deadlines occur at least *d* time units after a job is released

-Deadlines separated by at least *y* time units



• Task with rate specification (
$$x = 1, y = 2, d = 6$$

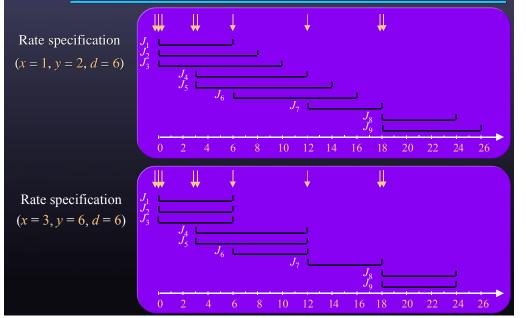




• Task with rate specification (x = 3, y = 6, d = 6)



#### **Rate-Based Execution** Comparison of different rate specifications



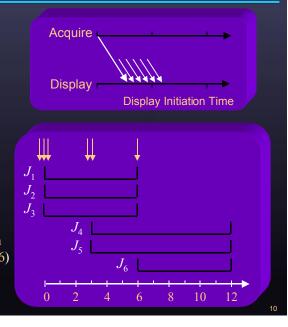
#### A Theory of Rate-Based Execution Feasibility under preemption constraints

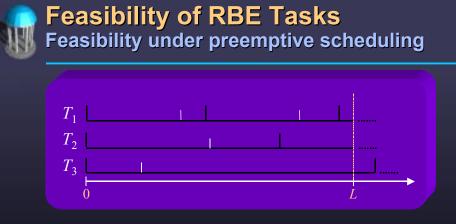
- Feasibility conditions for periodic and sporadic tasks, for all other known execution environments, also hold for *RBE* tasks
  - -Feasibility under non-preemptive scheduling
  - -Feasibility under scheduling with critical sections
  - -Feasibility under scheduling with interrupt handlers
- Thus feasibility is not inherently a function of release times
  - -Under deadline-driven scheduling, feasibility is a function of the implementation of a task set
  - -Under static-priority scheduling, feasibility is a function of the behavior of the external environment

#### Using RBE Tasks What problems do they solve?

RBE tasks provide a more natural way of modeling inbound packet processing of fragmented messages

> Rate specification (x = 3, y = 6, d = 6)

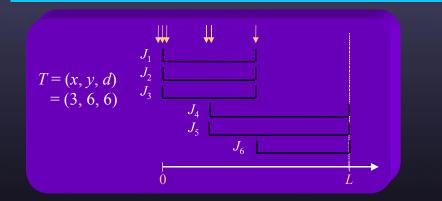




• Feasibility conditions of *RBE* tasks with rate specifications (*x*, *y*, *c*, *d*) are precisely the same as for periodic tasks

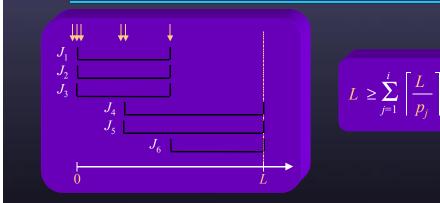
$$\forall L, L > 0: L \ge \sum_{i=1}^{n} \left\lfloor \frac{L - d_i + y_i}{y_i} \right\rfloor x_i c_i$$

#### A Theory of Rate-Based Execution On the relationship to periodic tasks



• But can't an RBE task be modeled as *x* instances of a periodic task (with some appropriate precedence relationship between instances)?

#### A Theory of Rate-Based Execution A corollary on static priority scheduling



- Under a static priority scheduling scheme, the processor demand in any interval can be unbounded
  - Thus event driven, rate-based execution is not possible under static priority scheduling schemes

#### A Theory of Rate-Based Execution Summary

- Traditional Liu & Layland theory is not directly applicable to distributed real-time systems
- The theory of scheduling periodic & sporadic tasks applies verbatim to RBE tasks
  - Polynomial & pseudo-polynomial time schedulability conditions exist for
    - » Preemptive scheduling
    - » Non-preemptive scheduling
    - » Scheduling with interrupt handlers
    - » Scheduling with critical sections
  - The *earliest-deadline-first* scheduling algorithm is optimal

#### A Theory of Rate-Based Execution Summary

- The feasibility of a set of "periodic tasks" was never inherently a function of the periodic arrival requirement
  - The only requirement is that exist a minimal separation between deadlines
- But if static priority scheduling methods are employed then (in the worst case) periodic arrivals are required
  - -Static priority methods require a well-behaved external environment
  - -Deadline methods require a well-behaved operating system