Color

Phillip Otto Runge (1777-1810)
Overview

- The nature of color
- Color processing in the human visual system
- Color spaces
- Adaptation and constancy
- White balance
- Uses of color in computer vision
What is color?

• Color is a psychological property of our visual experiences when we look at objects and lights, *not* a physical property of those objects or lights (S. Palmer, *Vision Science: Photons to Phenomenology*)

• Color is the result of interaction between physical light in the environment and our visual system

Wassily Kandinsky (1866-1944), Murnau Street with Women, 1908
Why do we see light at these wavelengths? Because that’s where the sun radiates electromagnetic energy.
Any source of light can be completely described physically by its spectrum: the amount of energy emitted (per time unit) at each wavelength 400 - 700 nm.

Relative spectral power

Wavelength (nm.)
Some examples of the spectra of light sources

A. Ruby Laser  
B. Gallium Phosphide Crystal  
C. Tungsten Lightbulb  
D. Normal Daylight

© Stephen E. Palmer, 2002
The Physics of Light

Some examples of the reflectance spectra of surfaces

<table>
<thead>
<tr>
<th>Wavelength (nm)</th>
<th>% Light Reflected</th>
</tr>
</thead>
<tbody>
<tr>
<td>Red</td>
<td>400</td>
</tr>
<tr>
<td>Yellow</td>
<td>400</td>
</tr>
<tr>
<td>Blue</td>
<td>400</td>
</tr>
<tr>
<td>Purple</td>
<td>400</td>
</tr>
</tbody>
</table>

© Stephen E. Palmer, 2002
Interaction of light and surfaces

- Observed color is the result of interaction of light source spectrum with surface reflectance
- Spectral radiometry
  - All definitions and units are now “per unit wavelength”
  - All terms are now “spectral”
The human eye is a camera!

- **Iris** - colored annulus with radial muscles
- **Pupil** - the hole (aperture) whose size is controlled by the iris
- **Lens** - changes shape by using ciliary muscles (to focus on objects at different distances)
- **What’s the “film”?**
  - photoreceptor cells (rods and cones) in the **retina**
Density of rods and cones

Rods and cones are *non-uniformly* distributed on the retina

- Rods responsible for intensity, cones responsible for color
- **Fovea** - Small region (1 or 2°) at the center of the visual field containing the highest density of cones (and no rods).
- Less visual acuity in the periphery—many rods wired to the same neuron
Rod / Cone sensitivity

Why can’t we read in the dark?

Slide by A. Efros
Three kinds of cones:

- Ratio of L to M to S cones: approx. 10:5:1
- Almost no S cones in the center of the fovea
Color interpolation in human visual system

Brewster’s colors: evidence of interpolation from spatially offset color samples

Scale relative to human photoreceptor size: each line covers about 7 photoreceptors

Source: F. Durand
Rods and cones act as filters on the spectrum

- To get the output of a filter, multiply its response curve by the spectrum, integrate over all wavelengths
  - Each cone yields one number

- Q: How can we represent an entire spectrum with 3 numbers?
- A: We can’t! Most of the information is lost.
  - As a result, two different spectra may appear indistinguishable
    » such spectra are known as **metamers**
Spectra of some real-world surfaces

metamers
Metamers
Standardizing color experience

• We would like to understand which spectra produce the same color sensation from people under similar viewing conditions

• Color matching experiments
Color matching experiment 1

Source: W. Freeman
Color matching experiment 1

Source: W. Freeman
Color matching experiment 1

Source: W. Freeman
Color matching experiment 1

The primary color amounts needed for a match

Source: W. Freeman
Color matching experiment 2

Source: W. Freeman
Color matching experiment 2

Source: W. Freeman
Color matching experiment 2

Source: W. Freeman
We say a "negative" amount of $p_2$ was needed to make the match, because we added it to the test color’s side.

The primary color amounts needed for a match:

Source: W. Freeman
Trichromacy

• In color matching experiments, most people can match any given light with three primaries
  • Primaries must be independent
• For the same light and same primaries, most people select the same weights
  • Exception: color blindness
• Trichromatic color theory
  • Three numbers seem to be sufficient for encoding color
  • Dates back to 18th century (Thomas Young)
Grassman’s Laws

• Color matching appears to be linear

• If two test lights can be matched with the same set of weights, then they match each other:
  • Suppose \( A = u_1 P_1 + u_2 P_2 + u_3 P_3 \) and \( B = u_1 P_1 + u_2 P_2 + u_3 P_3 \).
    Then \( A = B \).

• If we mix two test lights, then mixing the matches will match the result:
  • Suppose \( A = u_1 P_1 + u_2 P_2 + u_3 P_3 \) and \( B = v_1 P_1 + v_2 P_2 + v_3 P_3 \).
    Then \( A + B = (u_1 + v_1) P_1 + (u_2 + v_2) P_2 + (u_3 + v_3) P_3 \).

• If we scale the test light, then the matches get scaled by the same amount:
  • Suppose \( A = u_1 P_1 + u_2 P_2 + u_3 P_3 \).
    Then \( kA = (ku_1) P_1 + (ku_2) P_2 + (ku_3) P_3 \).
Linear color spaces

• Defined by a choice of three primaries
• The coordinates of a color are given by the weights of the primaries used to match it

*Matching functions*: weights required to match single-wavelength light sources

- Mixing two lights produces colors that lie along a straight line in color space
- Mixing three lights produces colors that lie within the triangle they define in color space
How to compute the color match for any color signal for any set of primary colors

- Pick a set of primaries, \( p_1(\lambda), p_2(\lambda), p_3(\lambda) \)
- Measure the amount of each primary, \( c_1(\lambda_0), c_2(\lambda_0), c_3(\lambda_0) \) needed to match a monochromatic light, \( t(\lambda_0) \) at each spectral wavelength \( \lambda_0 \) (pick some spectral step size). These are the color matching functions.

Source: W. Freeman
Using color matching functions to predict the matches for a new spectral signal

We know that a monochromatic light of wavelength $\lambda_i$ will be matched by the amounts $c_1(\lambda_i), c_2(\lambda_i), c_3(\lambda_i)$ of each primary.

And any spectral signal can be thought of as a linear combination of very many monochromatic lights, with the linear coefficient given by the spectral power at each wavelength.

$$\vec{t} = \begin{pmatrix} t(\lambda_1) \\ \vdots \\ t(\lambda_N) \end{pmatrix}$$

Source: W. Freeman
Using color matching functions to predict the primary match to a new spectral signal

Store the color matching functions in the rows of the matrix, \( C \)

\[
C = \begin{pmatrix}
c_1(\lambda_1) & \cdots & c_1(\lambda_N) \\
c_2(\lambda_1) & \cdots & c_2(\lambda_N) \\
c_3(\lambda_1) & \cdots & c_3(\lambda_N)
\end{pmatrix}
\]

Let the new spectral signal be described by the vector \( t \).

\[
\vec{t} = \begin{pmatrix}
t(\lambda_1) \\
\vdots \\
t(\lambda_N)
\end{pmatrix}
\]

Then the amounts of each primary needed to match \( t \) are:

\[
\vec{e} = C\vec{t}
\]

The components \( e_1, e_2, e_3 \) describe the color of \( t \). If you have some other spectral signal, \( s \), and \( s \) matches \( t \) perceptually, then \( e_1, e_2, e_3 \), will also match \( s \) (by Grassman’s Laws)

Source: W. Freeman
Linear color spaces: RGB

- Primaries are monochromatic lights (for monitors, they correspond to the three types of phosphors)
- *Subtractive matching* required for some wavelengths

\[
p_1 = 645.2 \text{ nm} \\
p_2 = 525.3 \text{ nm} \\
p_3 = 444.4 \text{ nm}
\]
4.20 COMPARISON OF CONE PHOTOCURRENT RESPONSES AND THE COLOR-MATCHING FUNCTIONS. The cone photocurrent spectral responsivities are within a linear transformation of the color-matching functions, after a correction has been made for the optics and inert pigments in the eye. The smooth curves show the Stiles and Burch (1959) color-matching functions. The symbols show the matches predicted from the photocurrents of the three types of macaque cones. The predictions included a correction for absorption by the lens and other inert pigments in the eye. Source: Baylor, 1987.
Linear color spaces: CIE XYZ

- Established in 1931 by the International Commission on Illumination
- Primaries are imaginary, but matching functions are everywhere positive
- 2D visualization: draw \((x,y)\), where \(x = X/(X+Y+Z)\), \(y = Y/(X+Y+Z)\)

Matching functions

http://en.wikipedia.org/wiki/CIE_1931_color_space
Uniform color spaces

- Unfortunately, differences in x,y coordinates do not reflect perceptual color differences
- CIE u’v’ is a projective transform of x,y to make the ellipses more uniform

**McAdam ellipses:** Just noticeable differences in color
Uniform color spaces

• Unfortunately, differences in x,y coordinates do not reflect perceptual color differences
• CIE u’v’ is a projective transform of x,y to make the ellipses more uniform
• Next generation: CIE L*a*b* (Koenderink: “an awful mix of magical numbers and arbitrary functions that somehow ‘fit’ the eye measure”)
Nonlinear color spaces: HSV

- Perceptually meaningful dimensions: Hue, Saturation, Value (Intensity)
- RGB cube on its vertex
Color perception

- Color/lightness constancy
  - The ability of the human visual system to perceive the intrinsic reflectance properties of the surfaces despite changes in illumination conditions

- Instantaneous effects
  - Simultaneous contrast: background color affects perceived color of the target
  - Mach bands

- Gradual effects
  - Light/dark adaptation
  - Chromatic adaptation
  - Afterimages
Lightness constancy

White in light and in shadow

J. S. Sargent, The Daughters of Edward D. Boit, 1882
Lightness constancy

http://web.mit.edu/persci/people/adelson/checkershadow_illusion.html
Lightness constancy

- Possible explanations
  - Simultaneous contrast
  - Reflectance edges vs. illumination edges

http://web.mit.edu/persci/people/adelson/checkershadow_illusion.html
Simultaneous contrast/Mach bands

Source: D. Forsyth
Chromatic adaptation

• The visual system changes its sensitivity depending on the luminances prevailing in the visual field
  • The exact mechanism is poorly understood

• Adapting to different brightness levels
  • Changing the size of the iris opening (i.e., the aperture) changes the amount of light that can enter the eye
  • Think of walking into a building from full sunshine

• Adapting to different color temperature
  • The receptive cells on the retina change their sensitivity
  • For example: if there is an increased amount of red light, the cells receptive to red decrease their sensitivity until the scene looks white again
  • We actually adapt better in brighter scenes: This is why candlelit scenes still look yellow

http://www.schorsch.com/kbase/glossary/adaptation.html
Chromatic adaptation
Useful reference

White balance

• When looking at a picture on screen or print, we adapt to the illuminant of the room, not to that of the scene in the picture
• When the white balance is not correct, the picture will have an unnatural color “cast”

http://www.cambridgeincolour.com/tutorials/white-balance.htm
White balance

• **Film cameras:**
  • Different types of film or different filters for different illumination conditions

• **Digital cameras:**
  • Automatic white balance
  • White balance settings corresponding to several common illuminants
  • Custom white balance using a reference object

http://www.cambridgeincolour.com/tutorials/white-balance.htm
White balance

- Von Kries adaptation
  - Multiply each channel by a gain factor
  - Note that the light source could have a more complex effect, corresponding to an arbitrary 3x3 matrix
White balance

- **Von Kries adaptation**
  - Multiply each channel by a gain factor
  - Note that the light source could have a more complex effect, corresponding to an arbitrary 3x3 matrix

- **Best way: gray card**
  - Take a picture of a neutral object (white or gray)
  - Deduce the weight of each channel
    - If the object is recoded as $r_w$, $g_w$, $b_w$
      use weights $1/r_w$, $1/g_w$, $1/b_w$
White balance

- Without gray cards: we need to “guess” which pixels correspond to white objects
- Gray world assumption
  - The image average $r_{\text{ave}}, g_{\text{ave}}, b_{\text{ave}}$ is gray
  - Use weights $1/r_{\text{ave}}, 1/g_{\text{ave}}, 1/b_{\text{ave}}$
- Brightest pixel assumption
  - Highlights usually have the color of the light source
  - Use weights inversely proportional to the values of the brightest pixels
- Gamut mapping
  - Gamut: convex hull of all pixel colors in an image
  - Find the transformation that matches the gamut of the image to the gamut of a “typical” image under white light
- Use image statistics, learning techniques
White balance by recognition

- Key idea: For each of the semantic classes present in the image, compute the illuminant that transforms the pixels assigned to that class so that the average color of that class matches the average color of the same class in a database of “typical” images.

Mixed illumination

• When there are several types of illuminants in the scene, different reference points will yield different results

[Images: Moonlit Sky, Indoor Lighting]

Reference: moon
Reference: stone

http://www.cambridgeincolour.com/tutorials/white-balance.htm
Spatially varying white balance

Input  Alpha map  Output

Uses of color in computer vision

Color histograms for indexing and retrieval

Uses of color in computer vision

Skin detection

Uses of color in computer vision

Image segmentation and retrieval

Uses of color in computer vision

Robot soccer


Source: K. Grauman
Uses of color in computer vision

Building appearance models for tracking

Uses of color in computer vision

Judging visual realism