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# **An Algorithm for Scheduling Certifiable Mixed-Criticality Sporadic Task Systems**

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- Tasks are in **multiple criticality levels** on safety-related embedded systems
- **Certification** is required for each criticality
- Classic real-time scheduling algorithms don't work efficiently

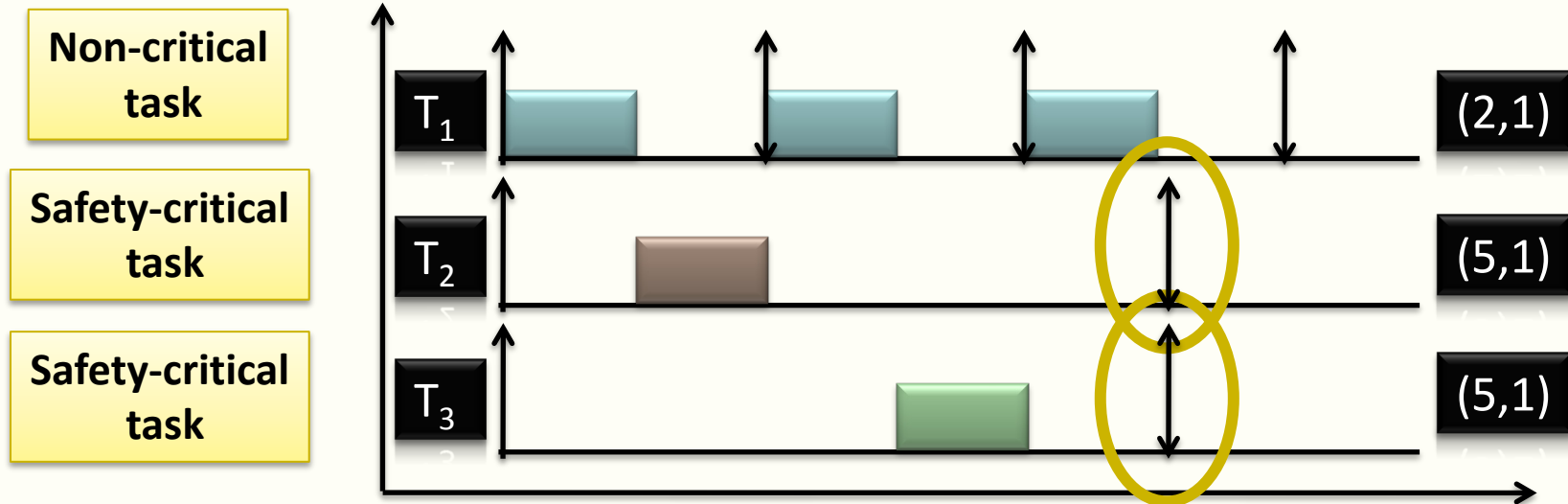


# Motivation: An Example

## ■ Typical real-time system model

### Certification:

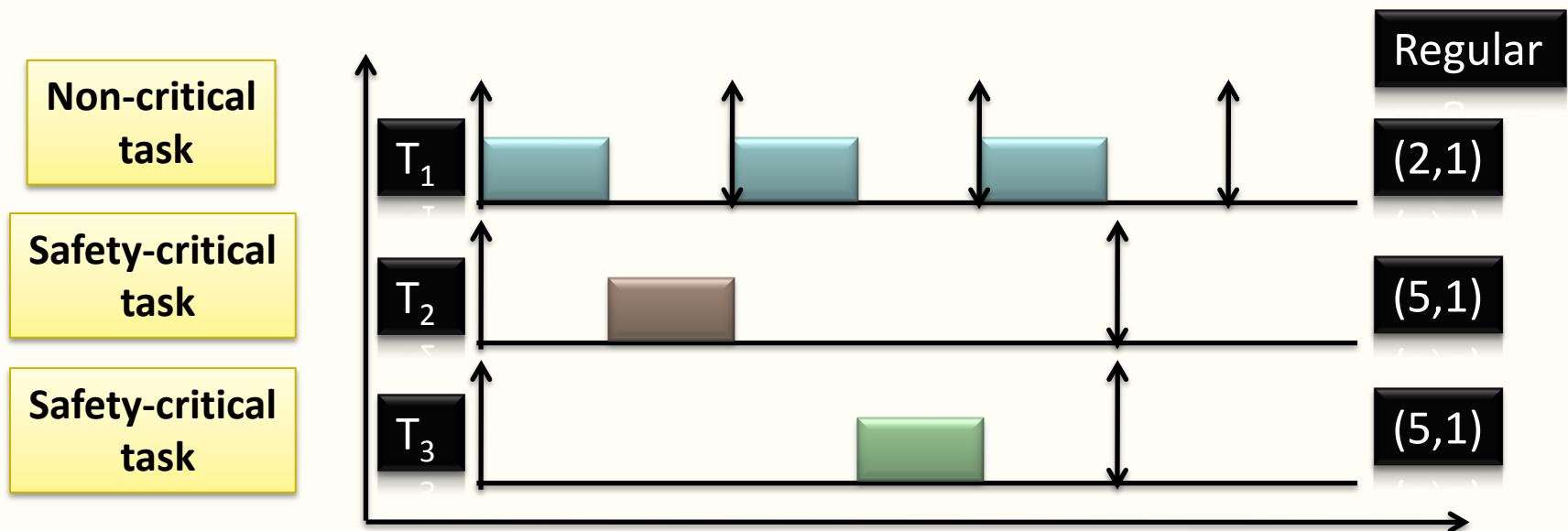
Checking temporal correctness of safety-critical tasks





# Motivation: An Example

- The problem with certification
  - The WCET is **estimated**
  - Schedulability relies on the **estimation**

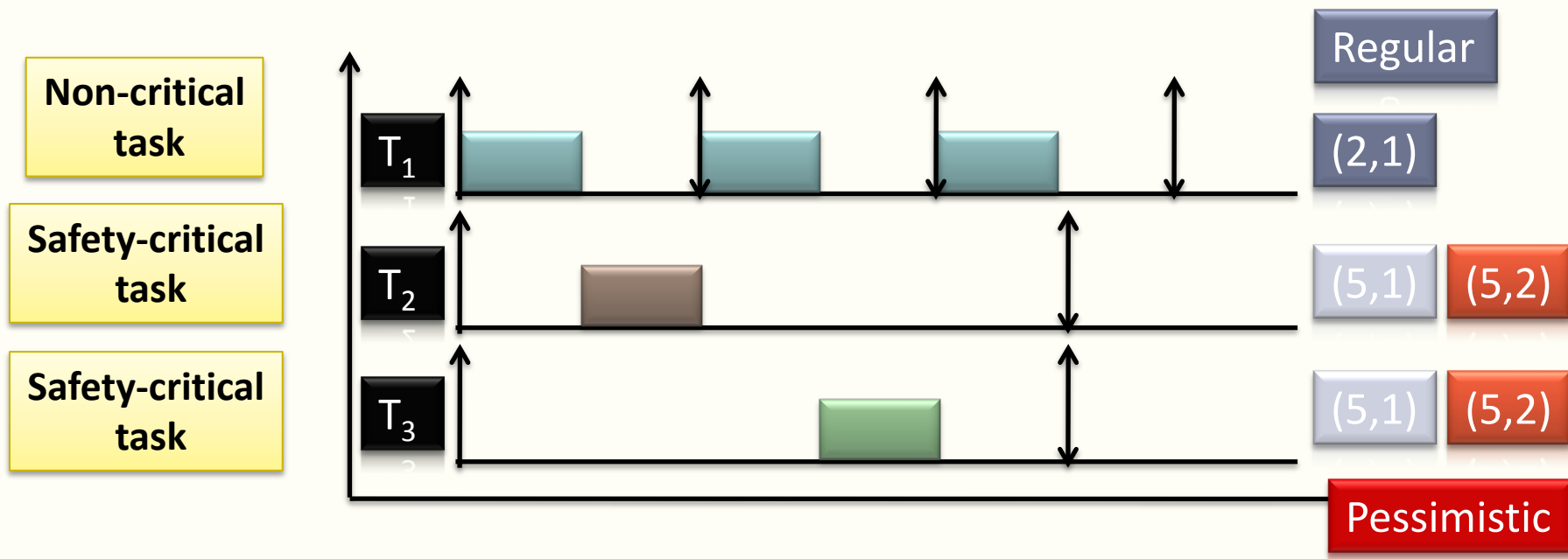




# Motivation: An Example

## ■ The problem with certification

Certifiers may use  
**more pessimistic** estimations

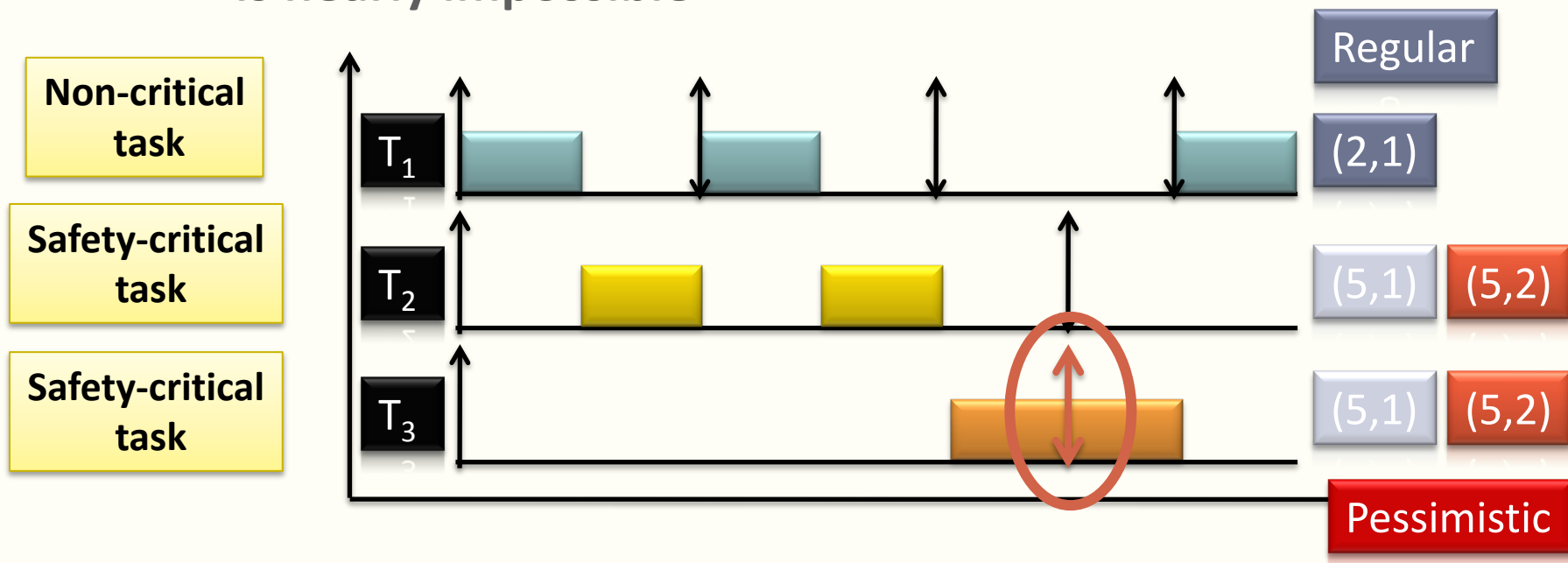




# Motivation: An Example

## ■ The problem with certification

- In this case, the system fails to pass certification
  - ◆ Though we know that  $T_2$  and  $T_3$ 's using so much time is nearly impossible

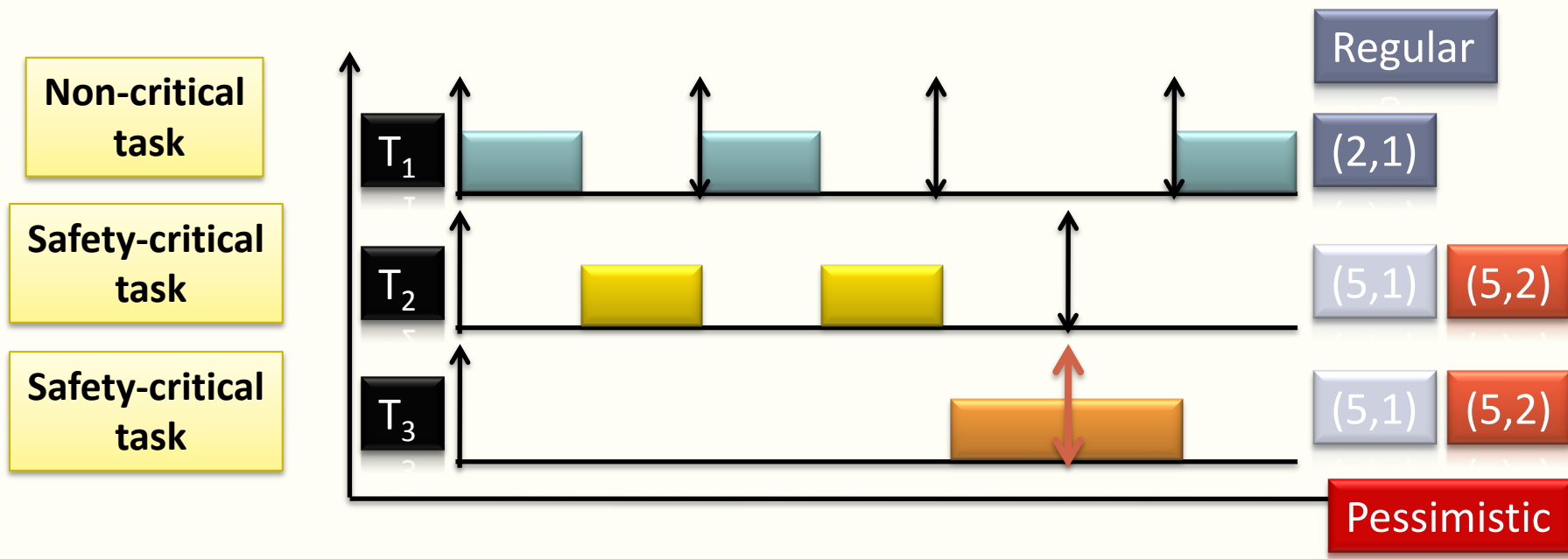




# Motivation: An Example

## ■ The problem with certification

We can use **criticality monotonic** to pass the certification

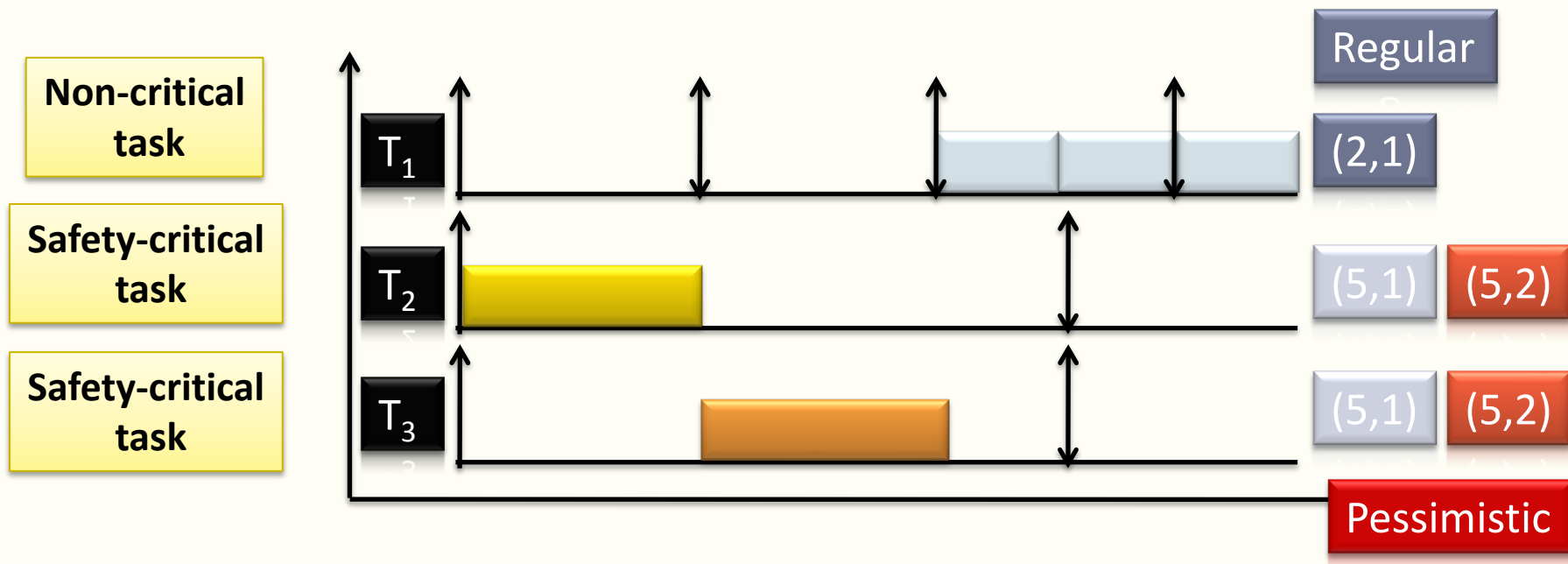




# Motivation: An Example

## ■ The problem with certification

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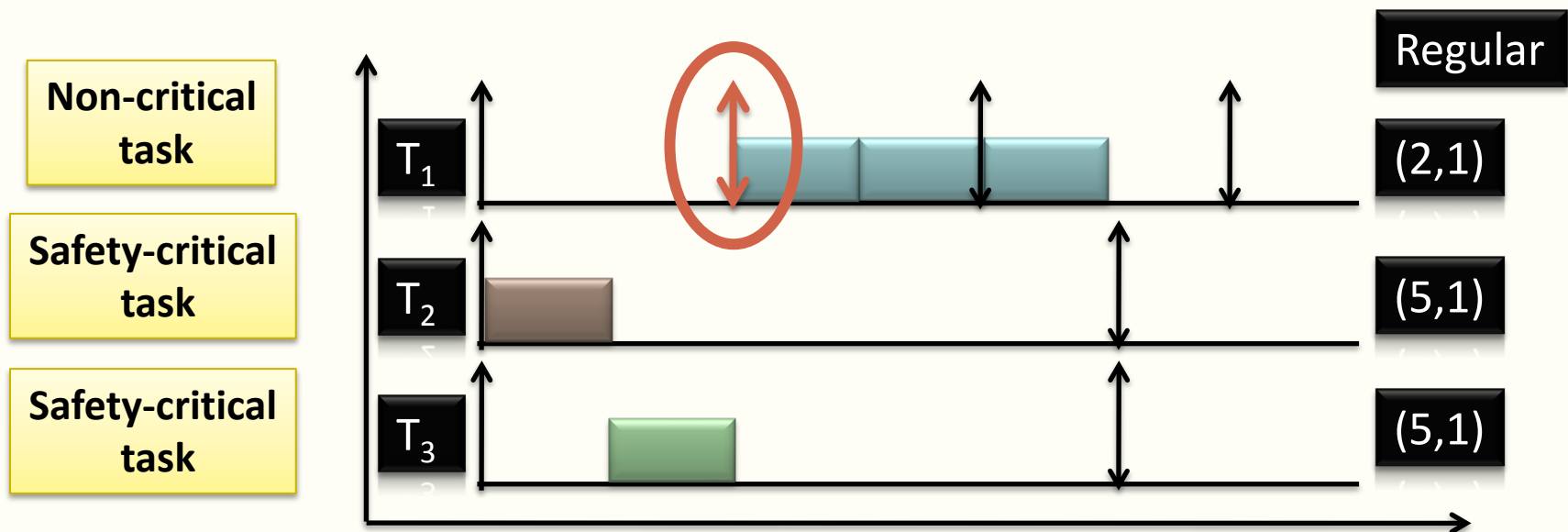




# Motivation: An Example

## ■ The problem with certification

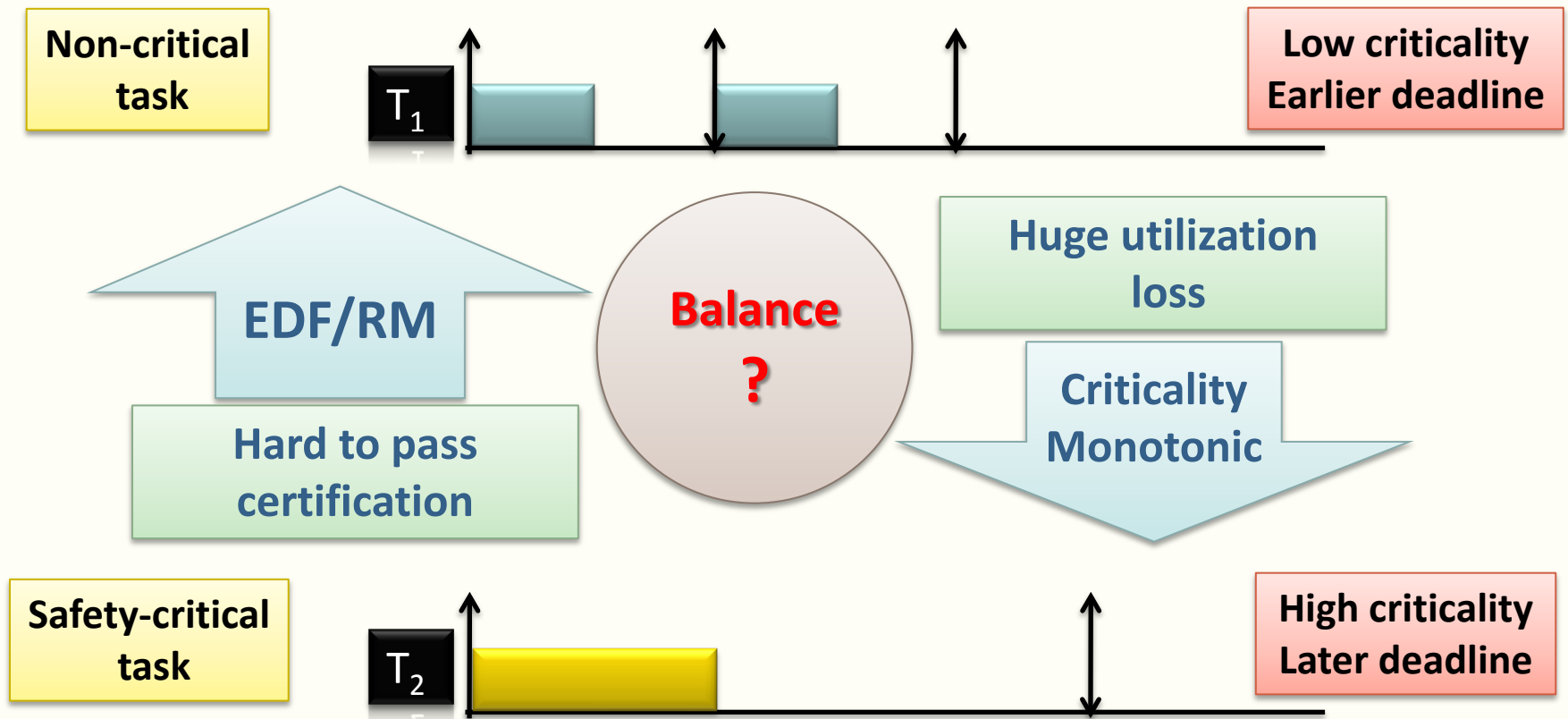
We can use **criticality monotonic** to pass the certification





# Motivation: Dilemma

## ■ Urgency and importance may differ

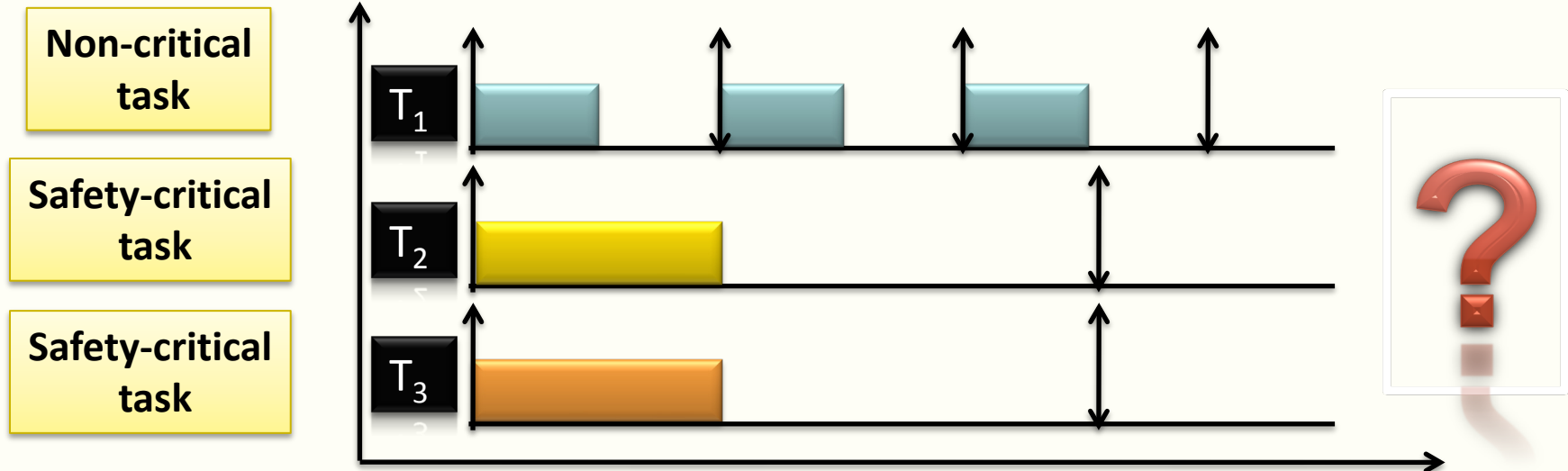




# Motivation: Balance

## Balanced Schedule:

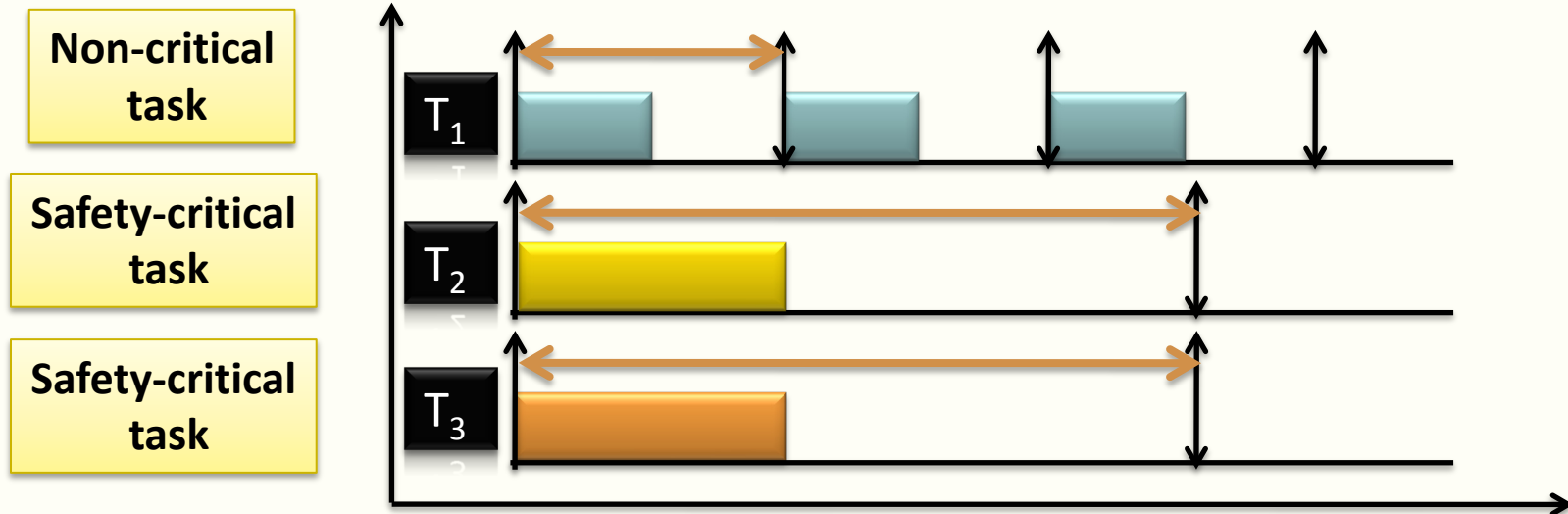
With **pessimistic** estimations, it passes certification;  
With **normal** estimations, it guarantees schedulability.





- Formal definition of the **mixed-criticality sporadic task system**

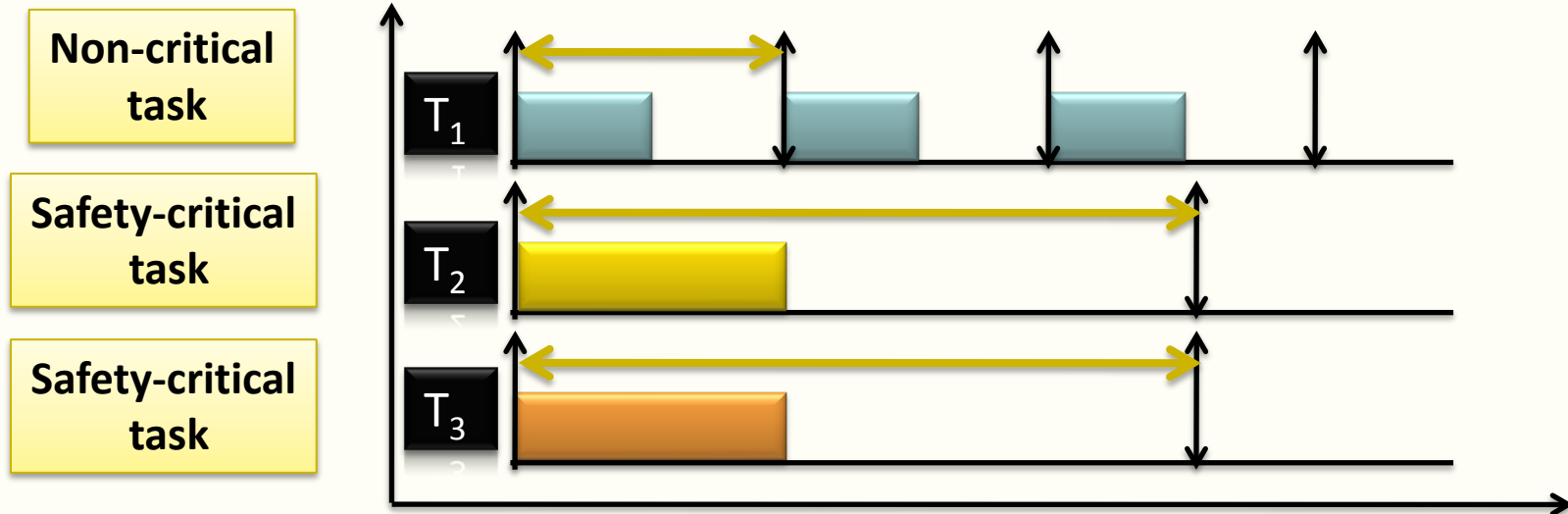
Period:  $T_i$





- Formal definition of the **mixed-criticality sporadic task system**

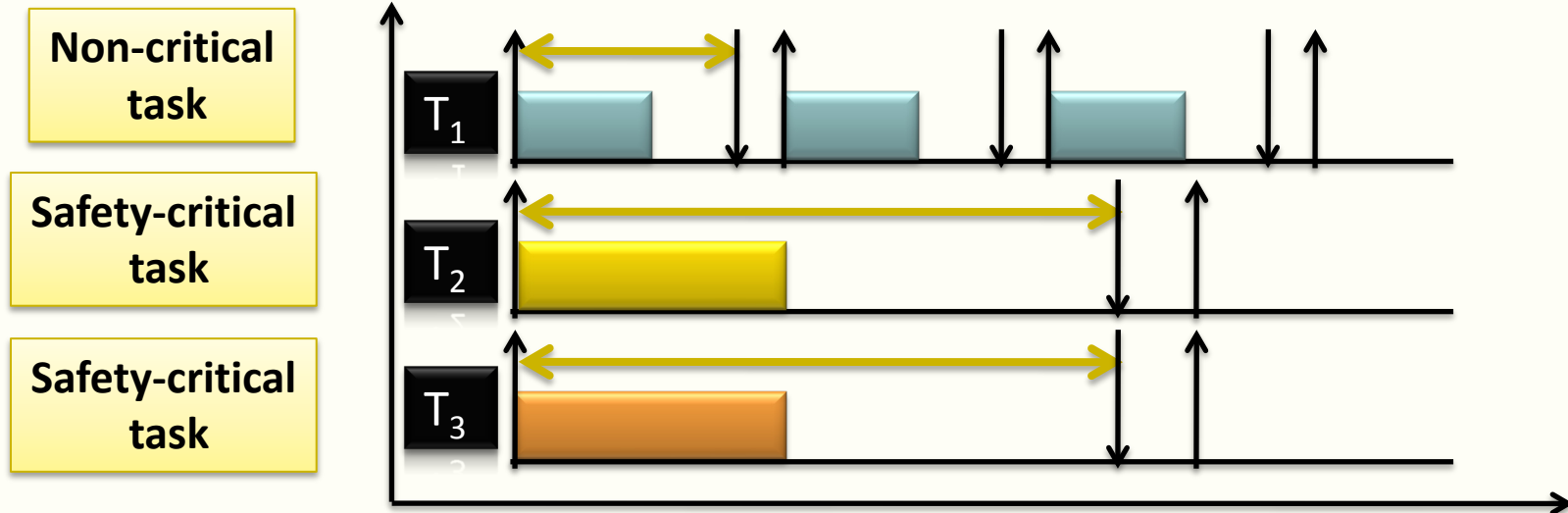
Deadline:  $D_i$





- Formal definition of the **mixed-criticality sporadic task system**

Deadline:  $D_i$





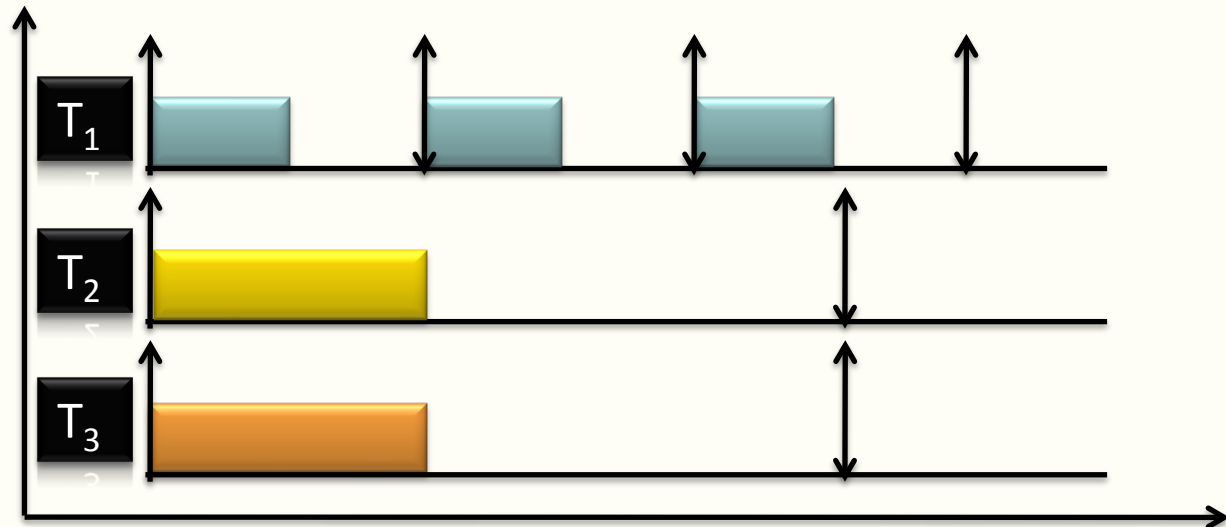
- Formal definition of the **mixed-criticality sporadic task system**

Criticality:  $x_i$

$x_1 = \text{LOW}$

$x_2 = \text{HIGH}$

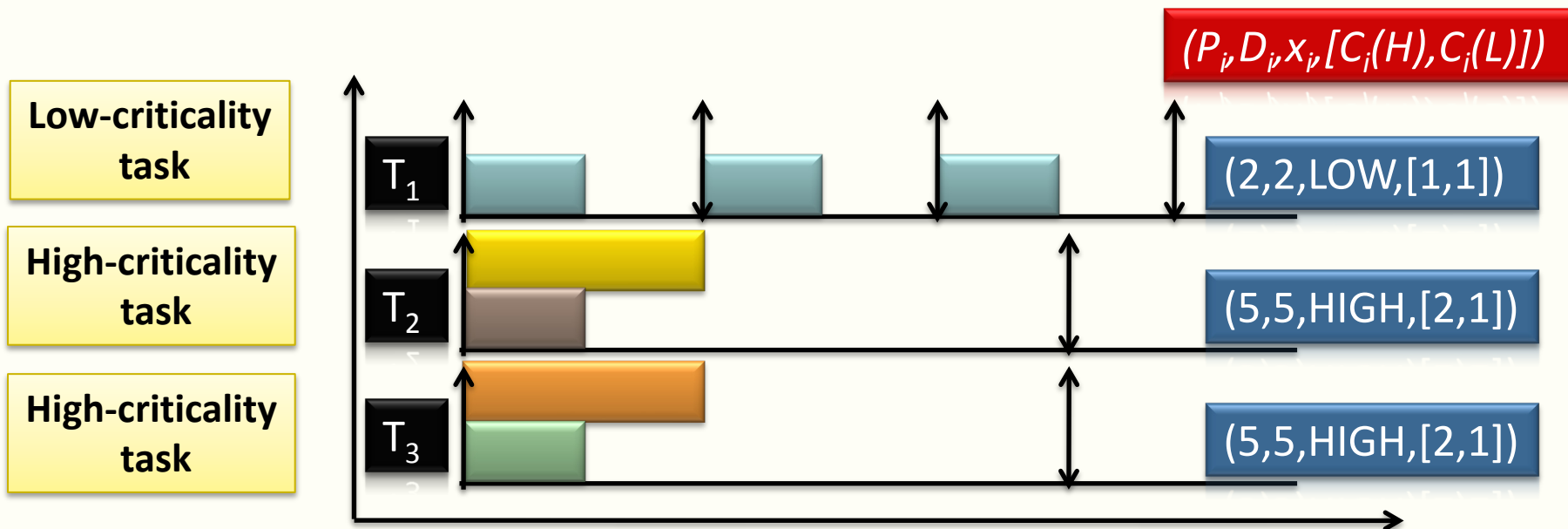
$x_3 = \text{HIGH}$





- The key idea is to specify **multiple WCETs** for different criticality levels

WCET at each criticality:  $[C_i(A), C_i(B), \dots ]$

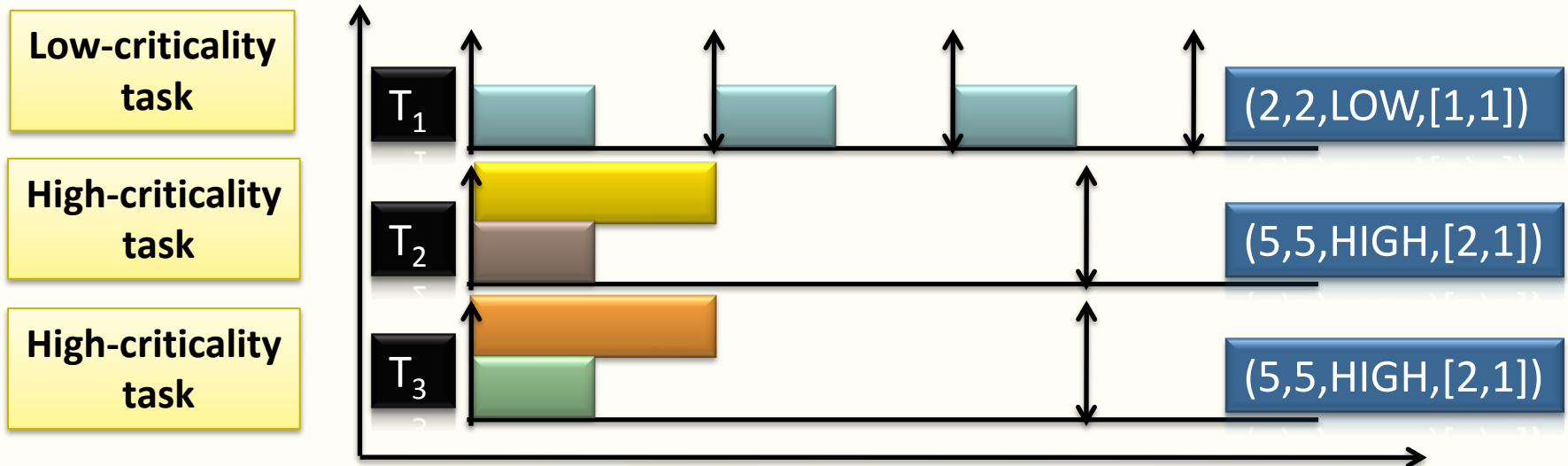






## ■ Correctness of **mixed-criticality schedule**

Temporal correctness of a schedule:  
All tasks **at level X and above** should meet their deadlines if **no task exceeds its level-X WCET**

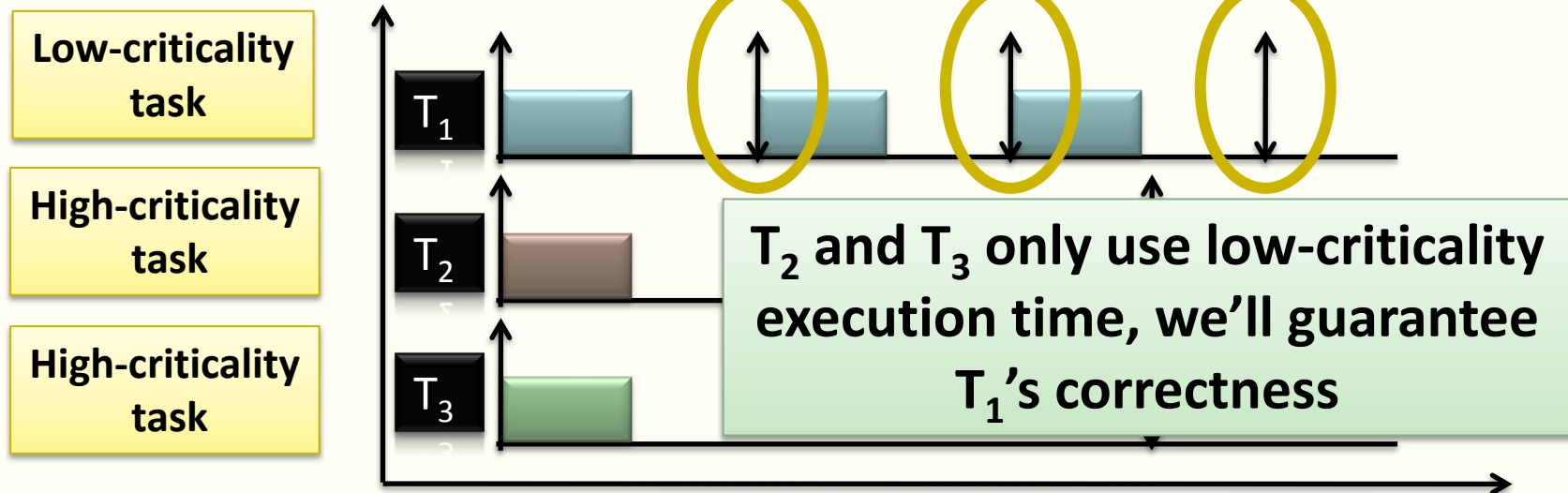




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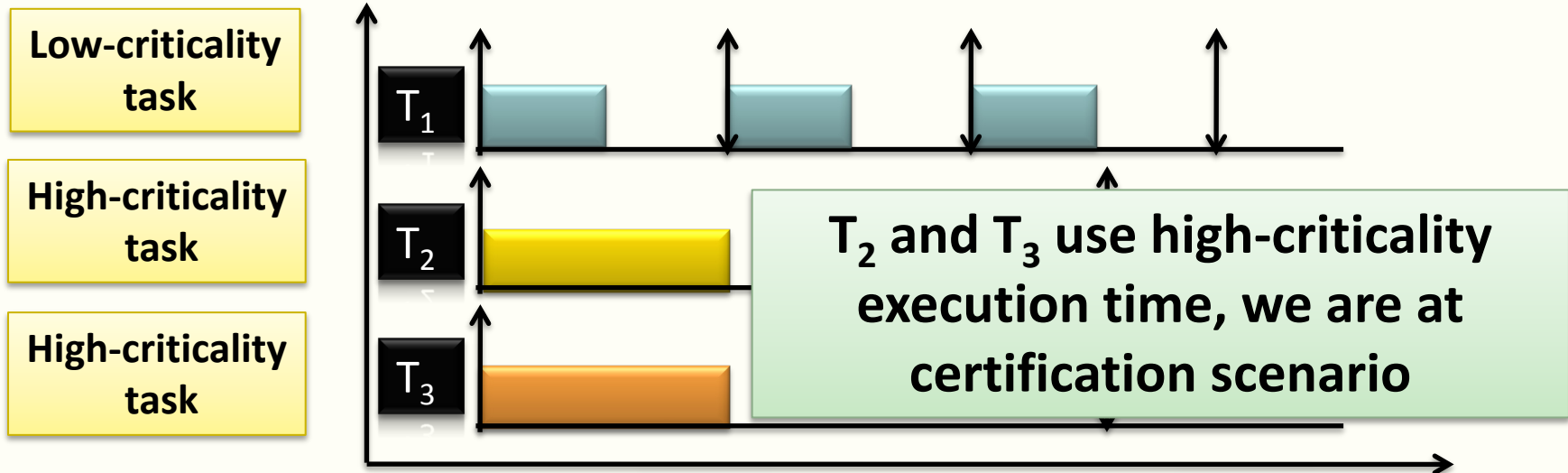




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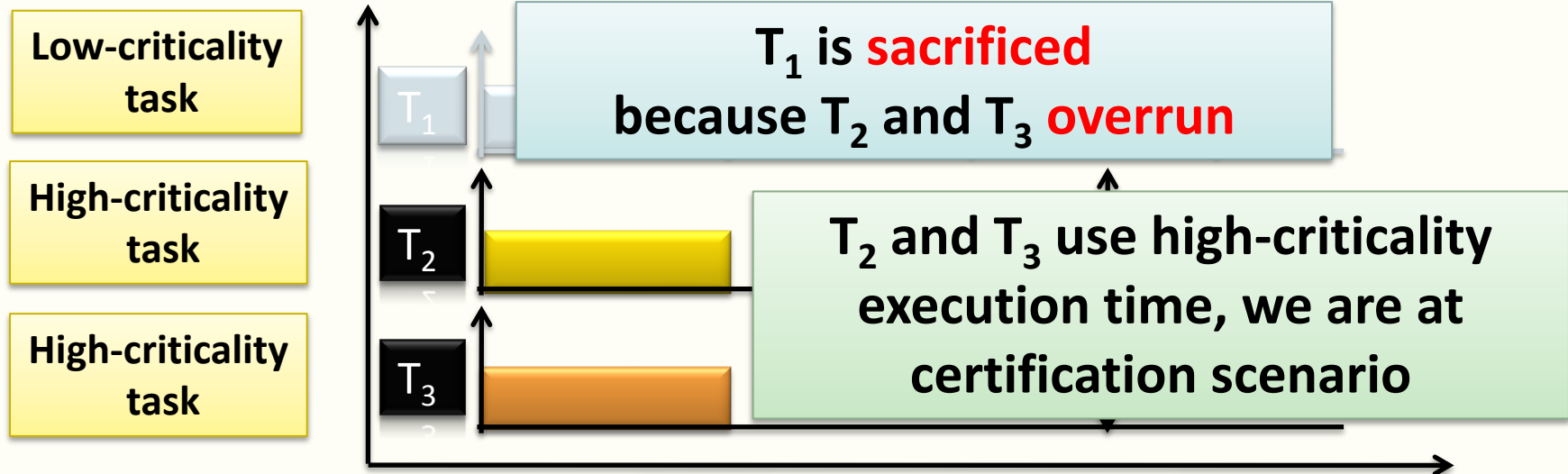




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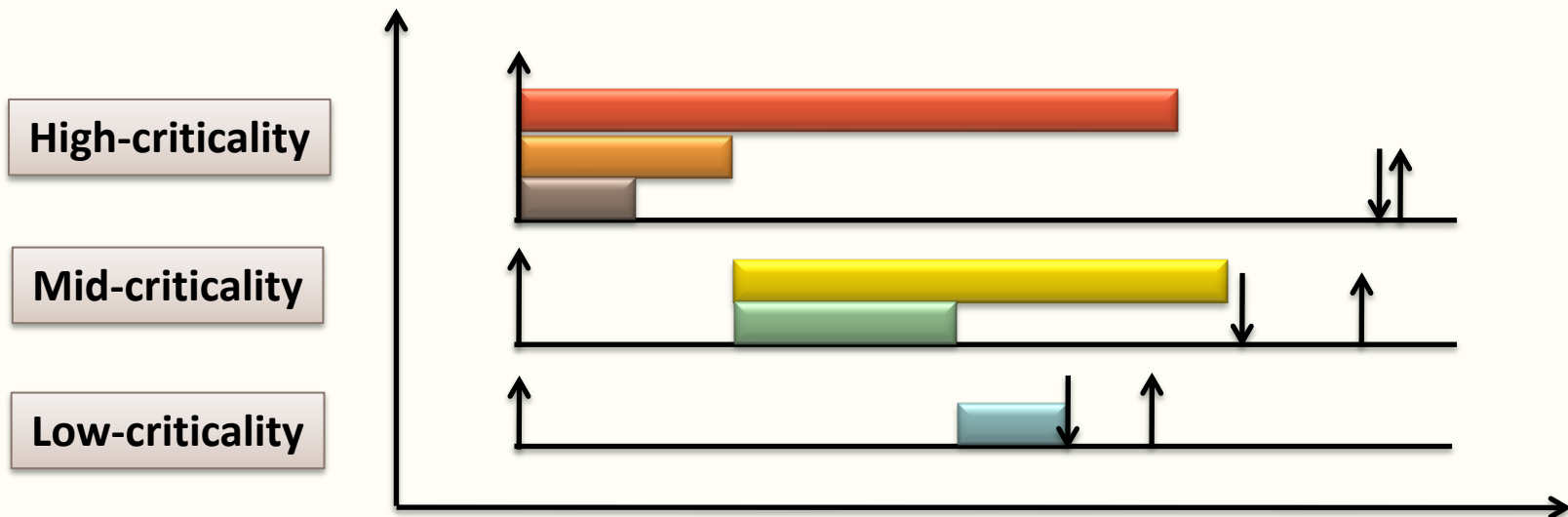




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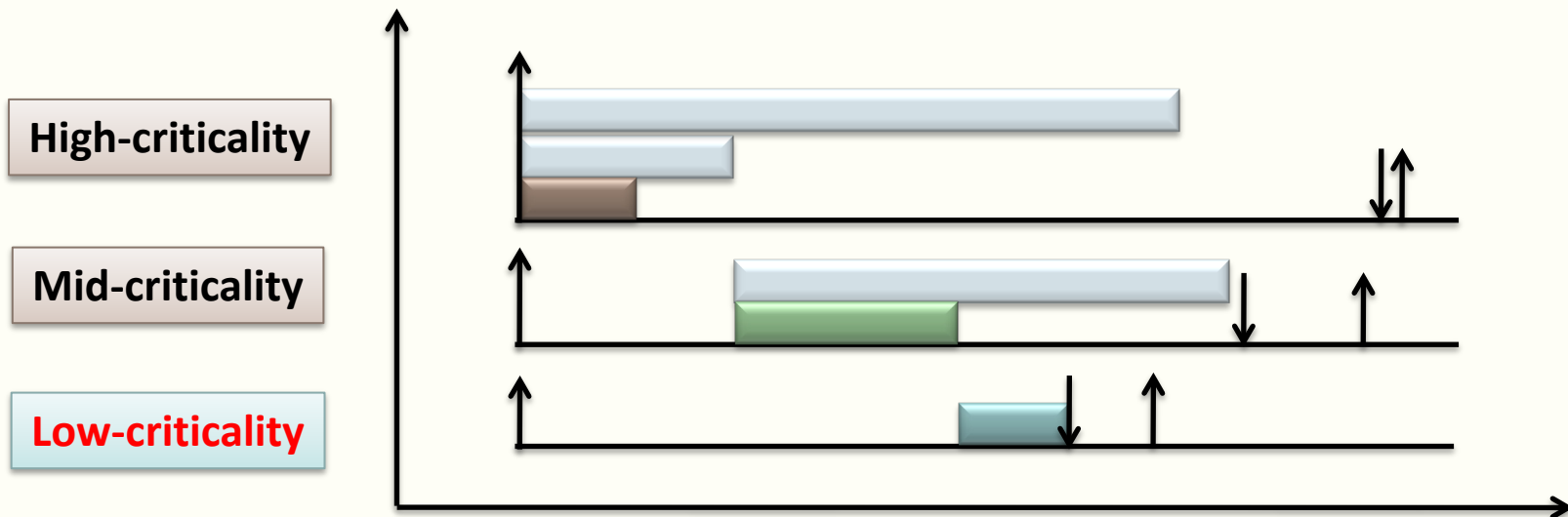




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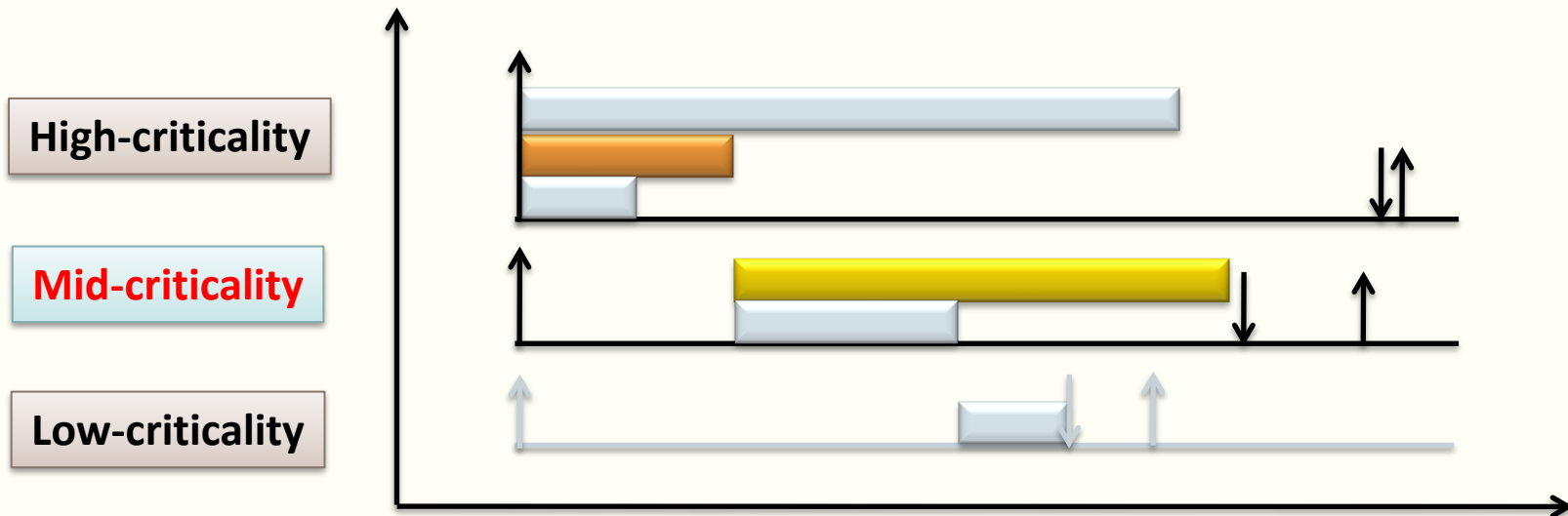




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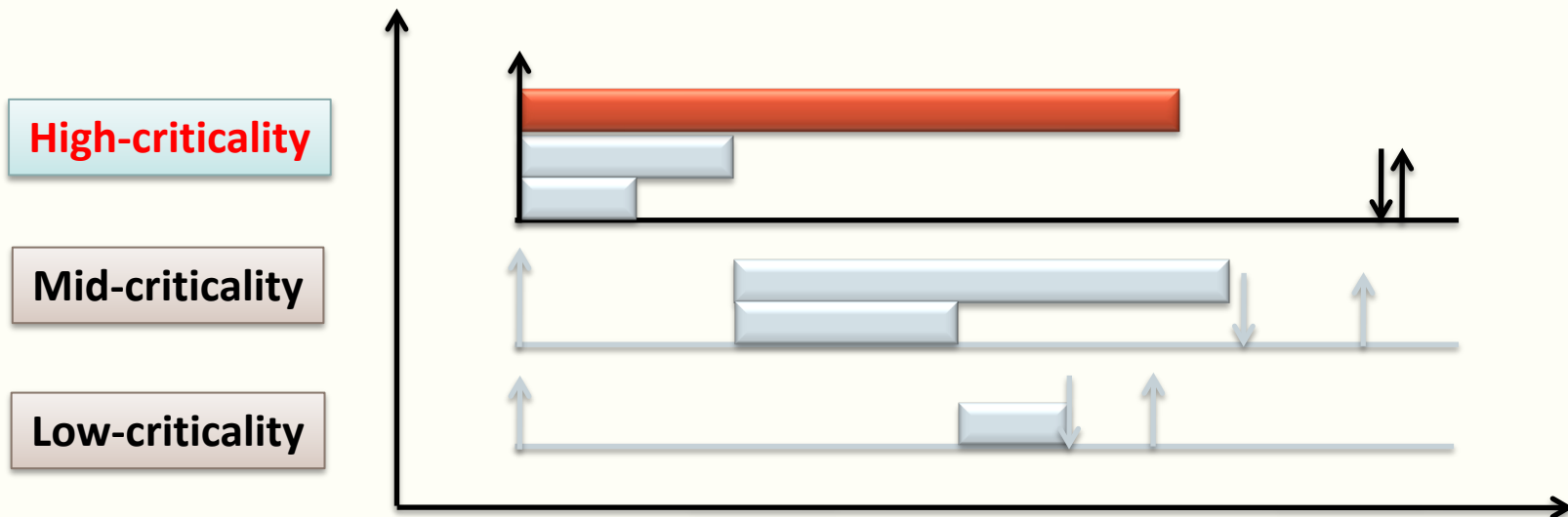




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**Temporal correctness of a schedule:**

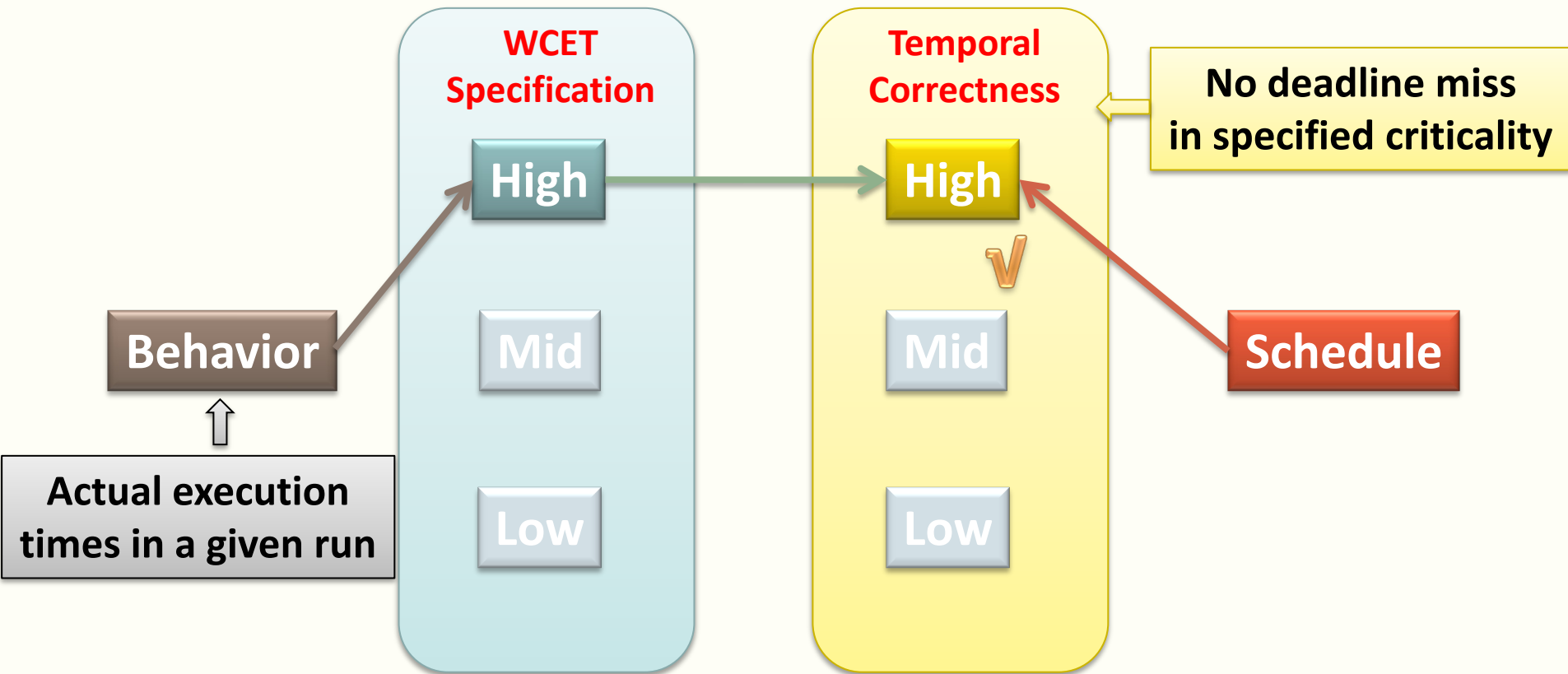
All tasks **at level X and above** should meet their deadlines if **no task exceeds its level-X WCET**





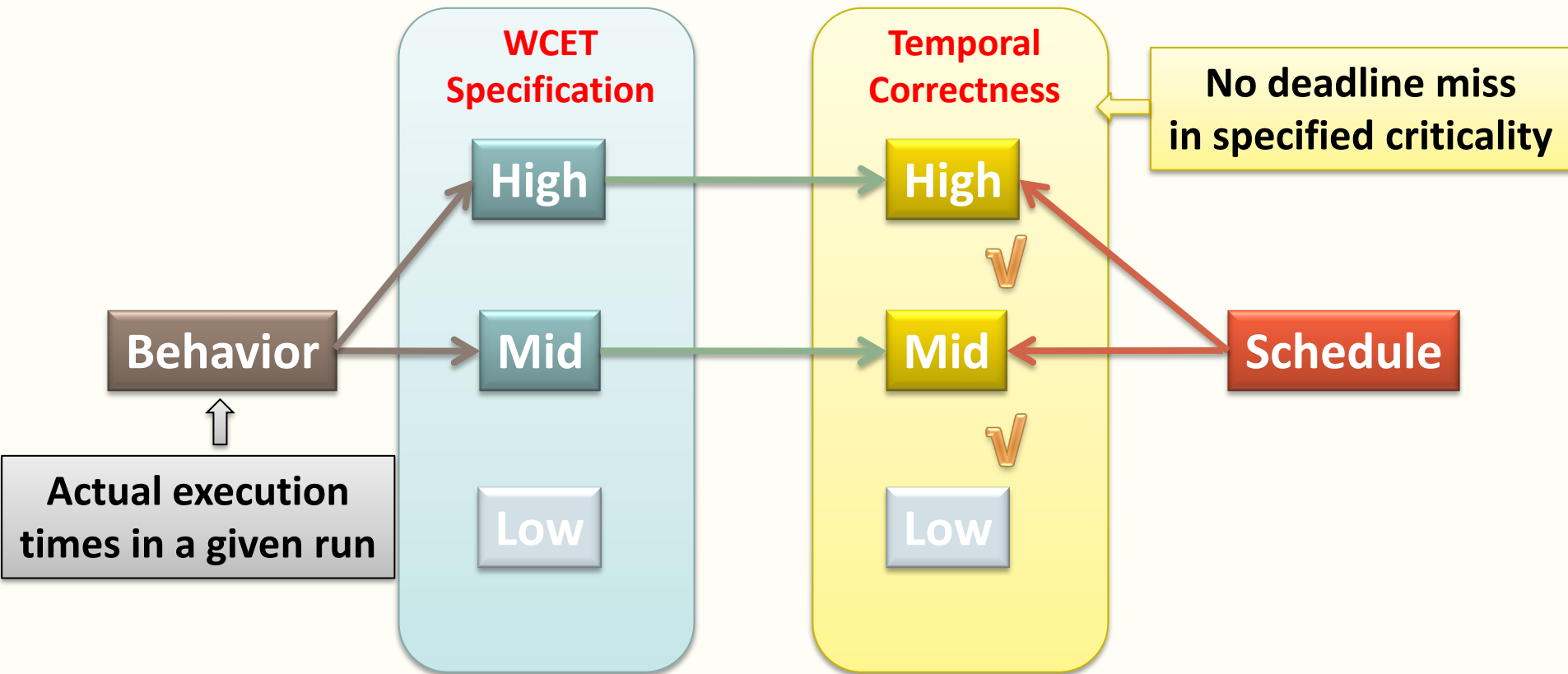


## ■ Informal interpretation of correctness



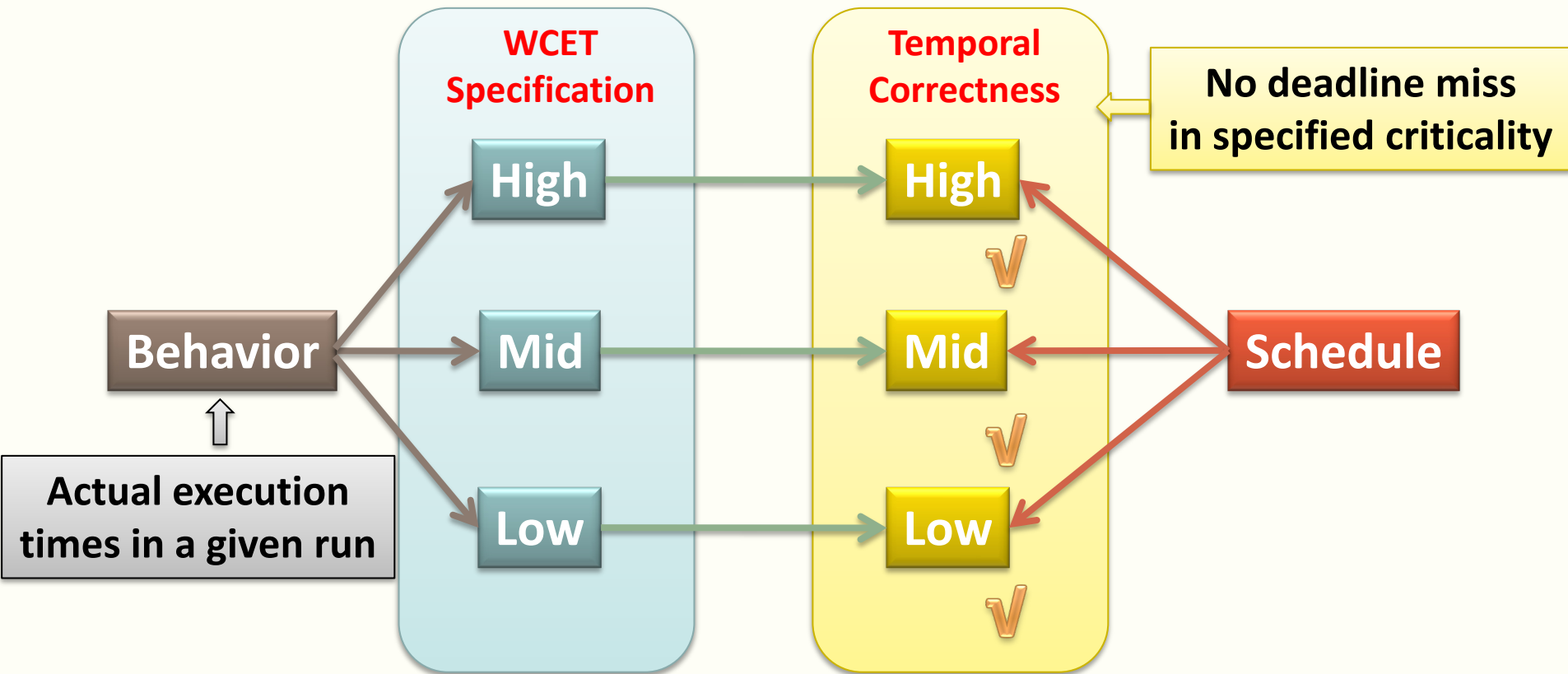


## ■ Informal interpretation of correctness





## ■ Informal interpretation of correctness





- The problem of scheduling mixed-criticality **independent jobs** has been solved
  - *Baruah, Li, and Stougie*. RTAS 2010
  - *Li and Baruah*. EMSOFT 2010
- We call our solution “OCBP algorithm”
  - Own Criticality-Based Priority algorithm



- OCBP algorithm generates a **static priority list** for a set of mixed-criticality **independent jobs**
  - It requires **specified release-time** and **deadline** for each job
  - It guarantees mixed-criticality correctness
  - It has a speedup factor 1.618 for two-criticality job sets
    - ◆ More criticality levels has higher speedup factor
    - ◆ Scheduling optimally is NP-hard in the strong sense
  - It runs in  $O(n \log n)$  time in the number of jobs



- In this paper, we apply OCBP algorithm to the mixed-criticality **sporadic** task systems
  - Speedup factors are maintained
  - A sufficient load-based schedulability test is also maintained



# OCBP Algorithm on Jobs

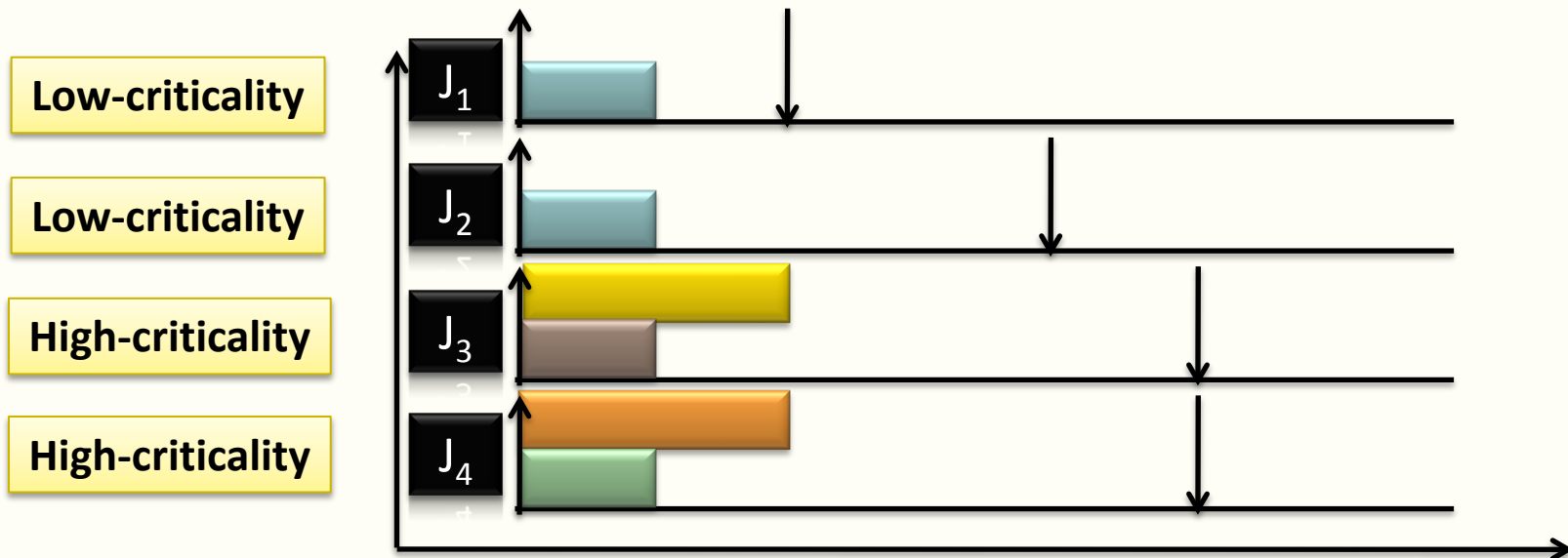
- The principle of OCBP algorithm is to recursively find the **lowest-priority job**
  - Very similar to “Audsley’s Approach”
  - If a **level-X** job would meet its deadline as the lowest-priority job, when **all jobs** execute at their **level-X WCETs**, then this job can be assigned lowest priority
    - ◆ Repeat this procedure to get a full priority list
    - ◆ When such lowest-priority job can not be found, claim the job set unschedulable



# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority job**

Determine if a job can get **the lowest priority**:  
Compute maximum time demand in **its criticality**



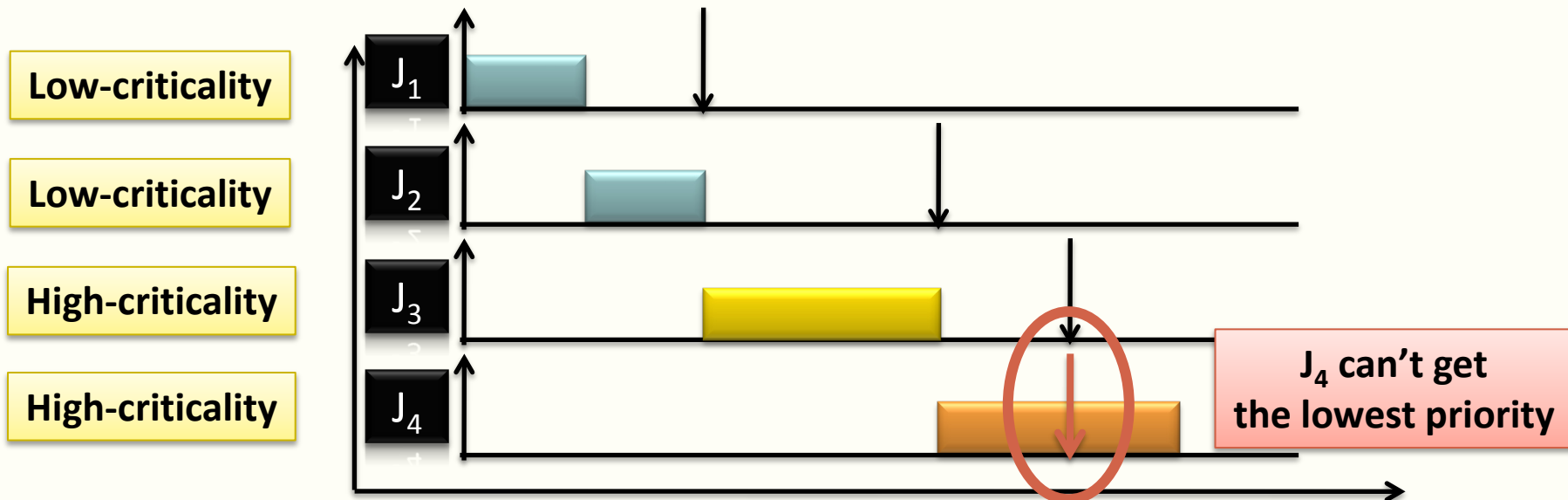




# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority** job

For  $J_4$ , the maximum possible time demand (in the worst case) exceeds its deadline

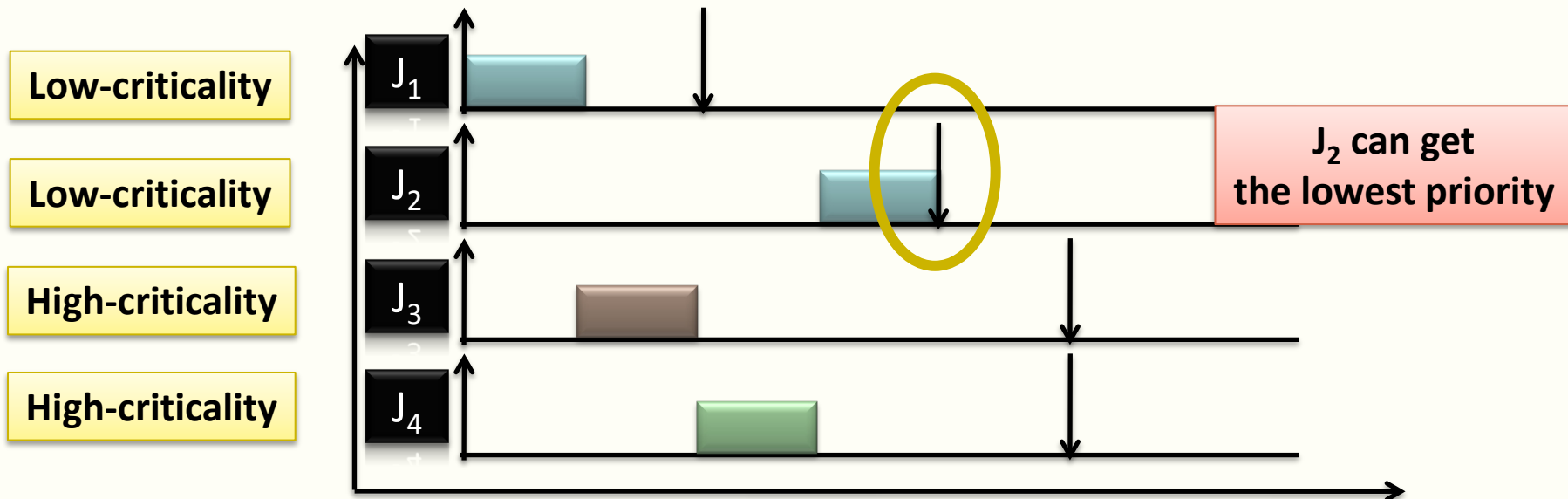




# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority** job

For  $J_2$ , the maximum time demand is smaller (if  $J_3$  or  $J_4$  overruns,  $J_2$  **can** miss its deadline)

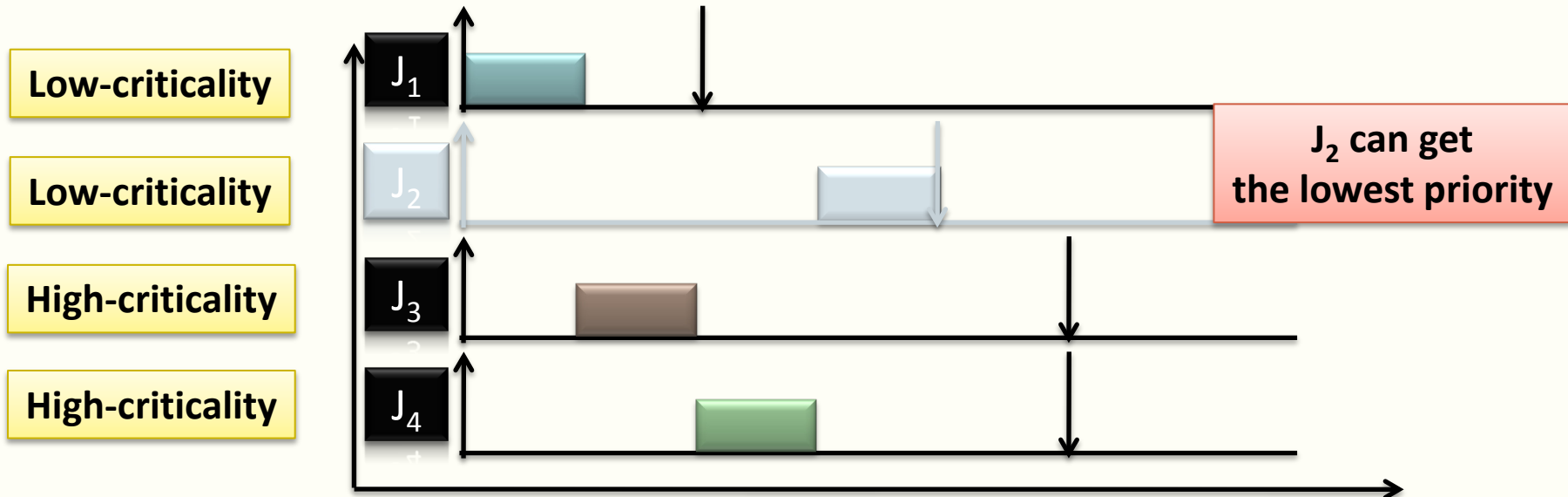




# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority** job

Assign  $J_2$  the lowest priority,  
and delete it from the job set

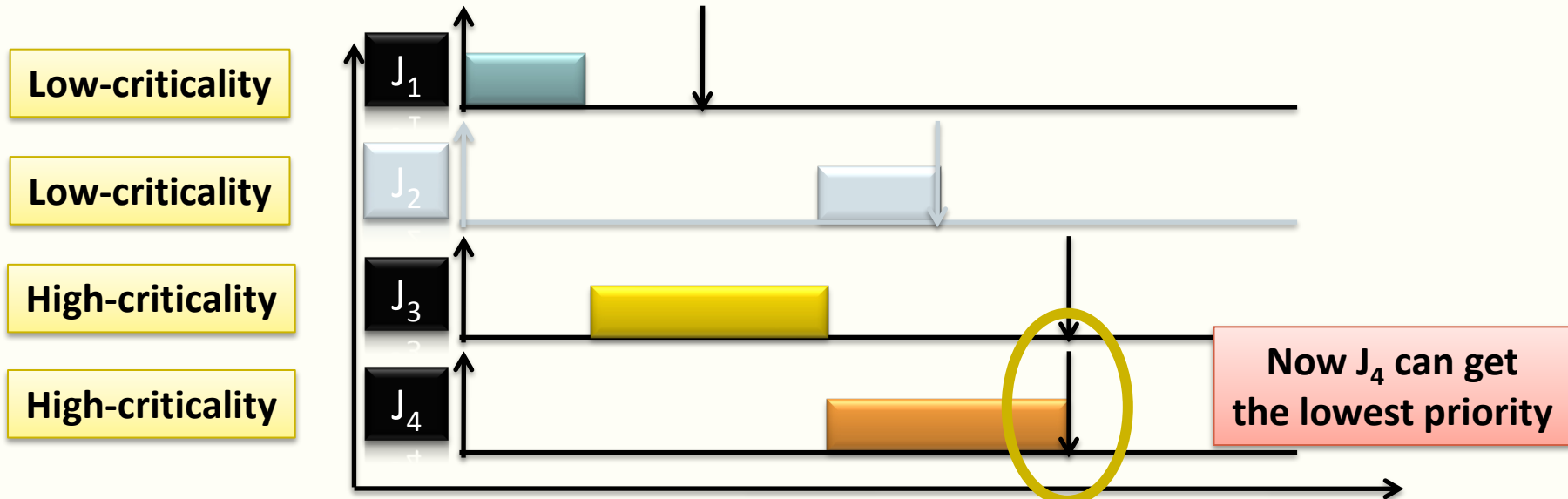




# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority** job

Now the maximum time demand for  $J_4$  decreases  
( $J_2$  won't affect  $J_4$  now)



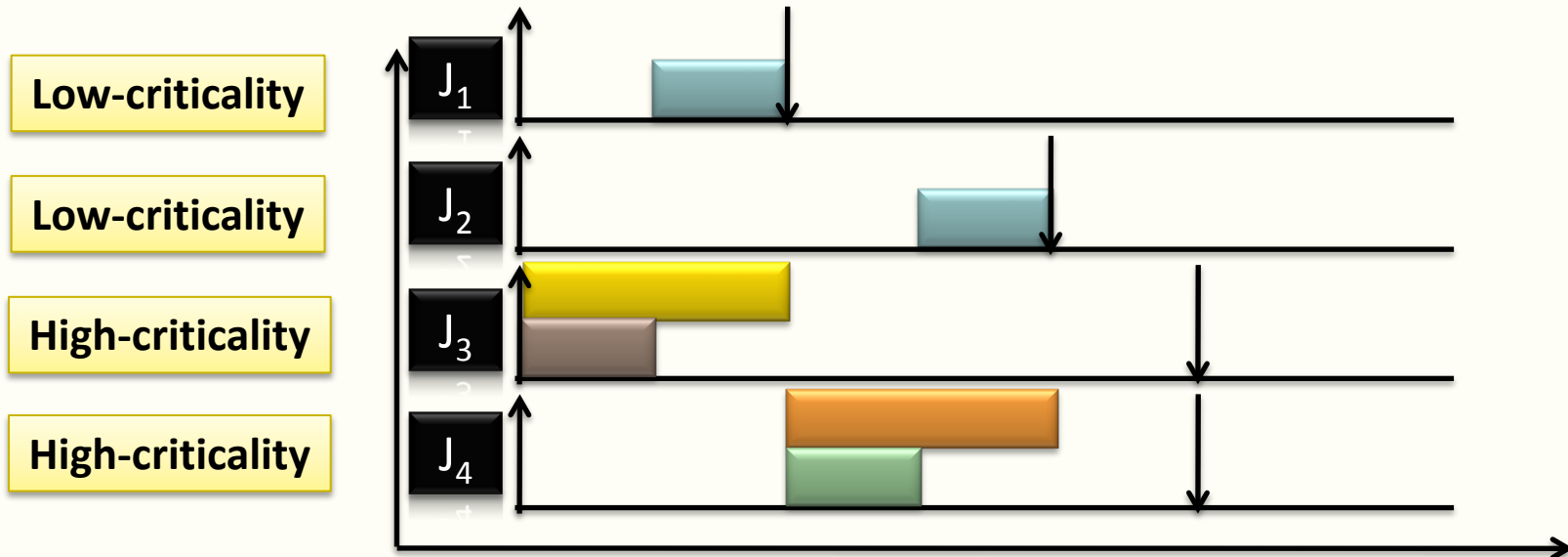


# OCBP Algorithm on Jobs

- The principle of OCBP algorithm is to recursively find the **lowest-priority job**

Repeat the procedure, we can get a priority list:

$$J_3 < J_1 < J_4 < J_2$$





# From Jobs to Sporadic Tasks

- **Sporadic tasks have infinite jobs**
  - But the processor can't be infinitely busy
    - ◆ We assume that the processor isn't fully utilized
- **To apply the job-oriented OCBP algorithm, we consider jobs in **the longest busy interval****
  - The number of jobs in the longest busy interval is bounded
    - ◆ The number of jobs is pseudo-polynomial to the number of tasks



# From Jobs to Sporadic Tasks

- We run OCBP algorithm in the beginning of the longest busy interval
  - We specify every job to get **the earliest possible** release-time and deadline
    - ◆ Assuming that the sporadic tasks run periodically
- A priority list for all jobs in the longest busy interval will be generated
  - This priority list may be eventually erroneous
    - ◆ Because jobs are **not** released immediately



# From Jobs to Sporadic Tasks

- We proved that the priority list can be erroneous only after the following two **violations**:
  - When the processor is **idle**
  - When a high-priority job is released, and **preempts a low-priority job**





# From Jobs to Sporadic Tasks

- We proved that the priority list can be erroneous only after the following two **violations**
- We also proved that when the violation happens, we can **re-compute** the priority list
  - Use OCBP algorithm again
  - The re-computation will always generate a valid priority list



# From Jobs to Sporadic Tasks

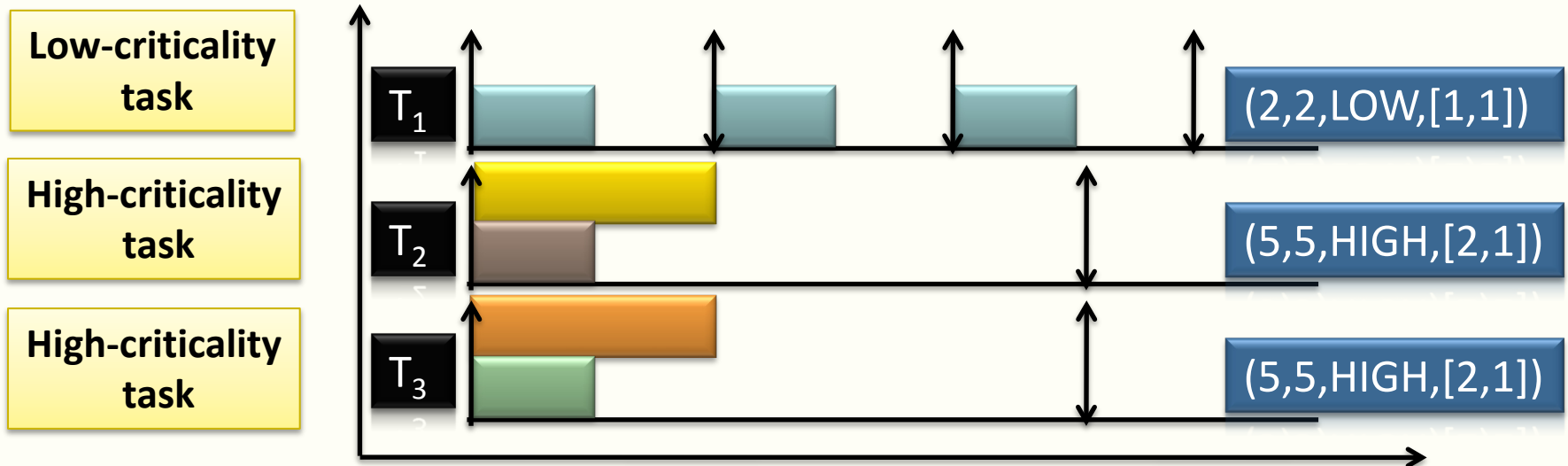
- We proved that the priority list can be erroneous only after the following two **violations**
- We also proved that when the violation happens, we can **re-compute** the priority list

Inductively, we've proved that:  
For a mixed-criticality sporadic system,  
if OCBP algorithm succeeds in the beginning,  
there exists a **correct scheduling algorithm**



# OCBP Algorithm on Tasks

- An example of running OCBP algorithm on mixed-criticality sporadic tasks



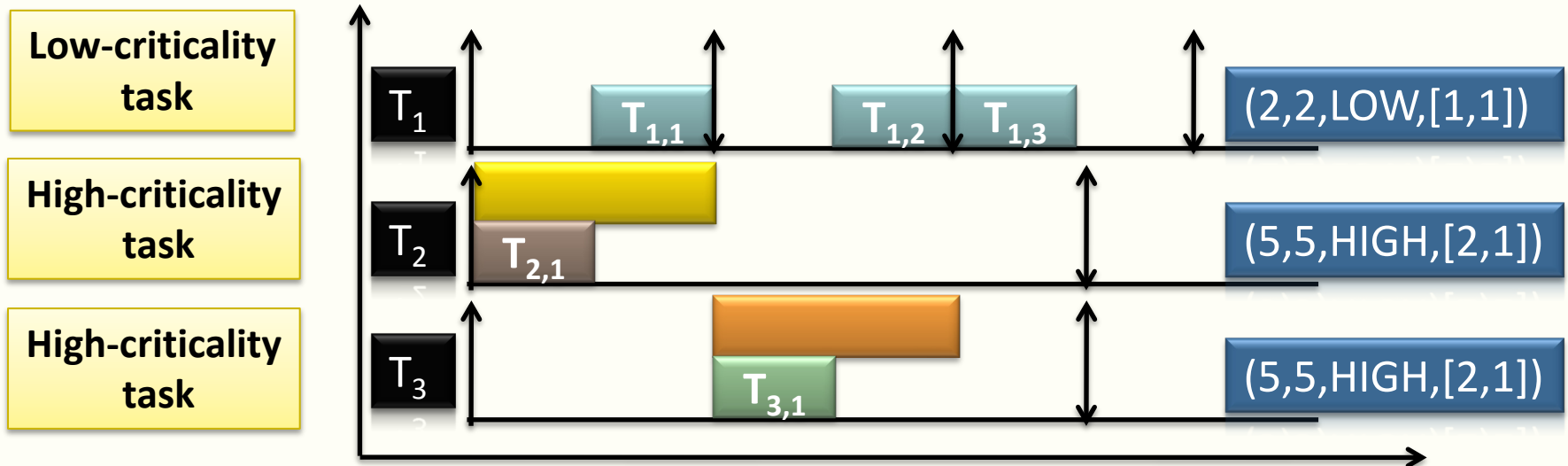


# OCBP Algorithm on Tasks

- Example of running OCBP algorithm in the beginning

A priority list (in the beginning):

$$T_{2,1} < T_{1,1} < T_{3,1} < T_{1,2} < T_{1,3}$$

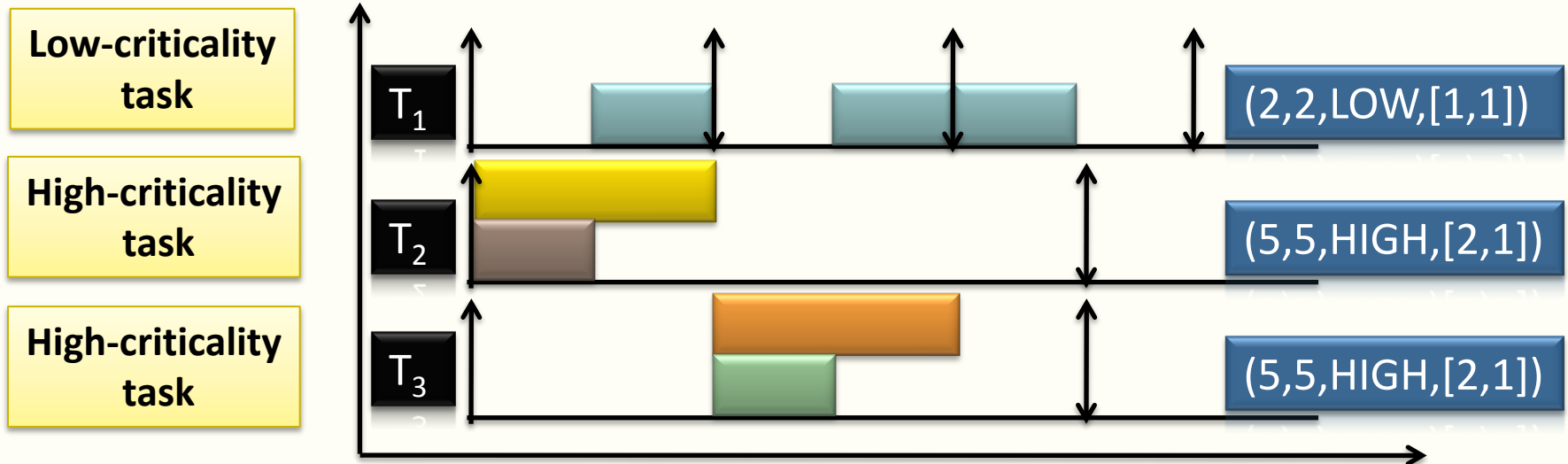




# OCBP Algorithm on Tasks

- Example of executing tasks following the OCBP priority list

When **no violation happens**,  
follow  $T_{2,1} < T_{1,1} < T_{3,1} < T_{1,2} < T_{1,3}$

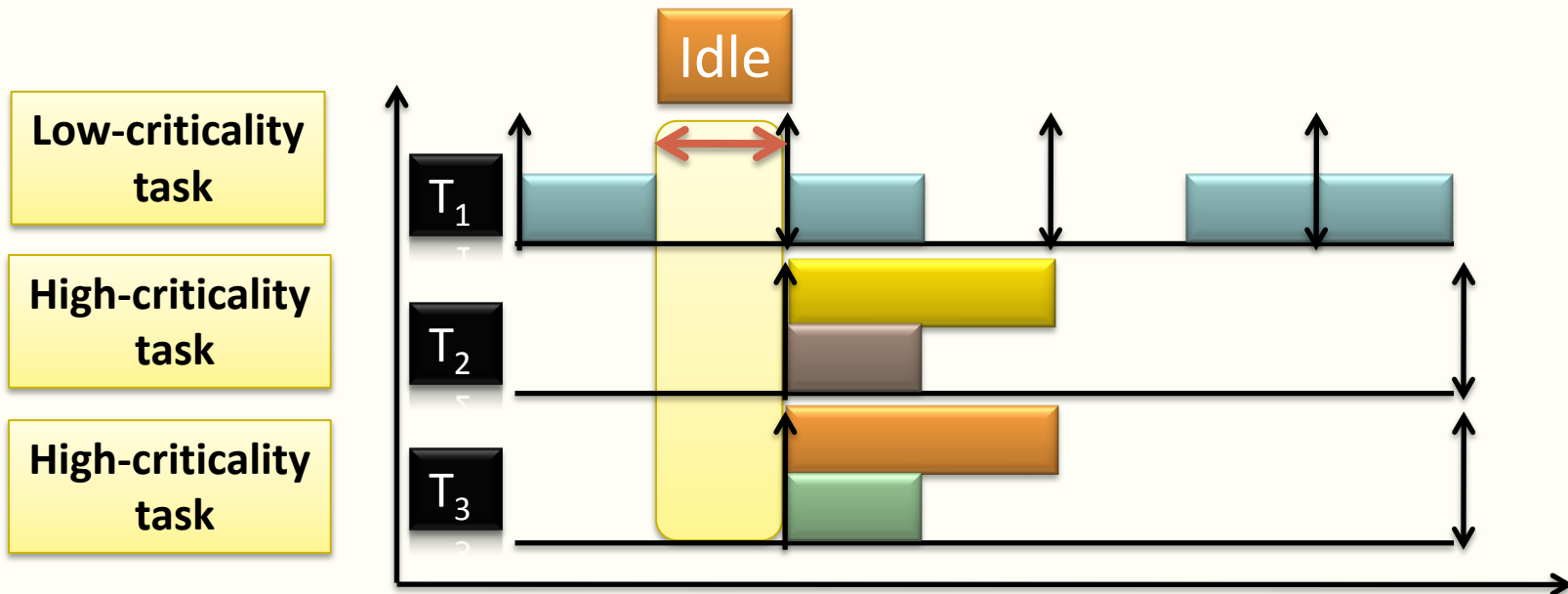




# OCBP Algorithm on Tasks

- Example showing when a violation happens

Violation: When the processor is **idle**



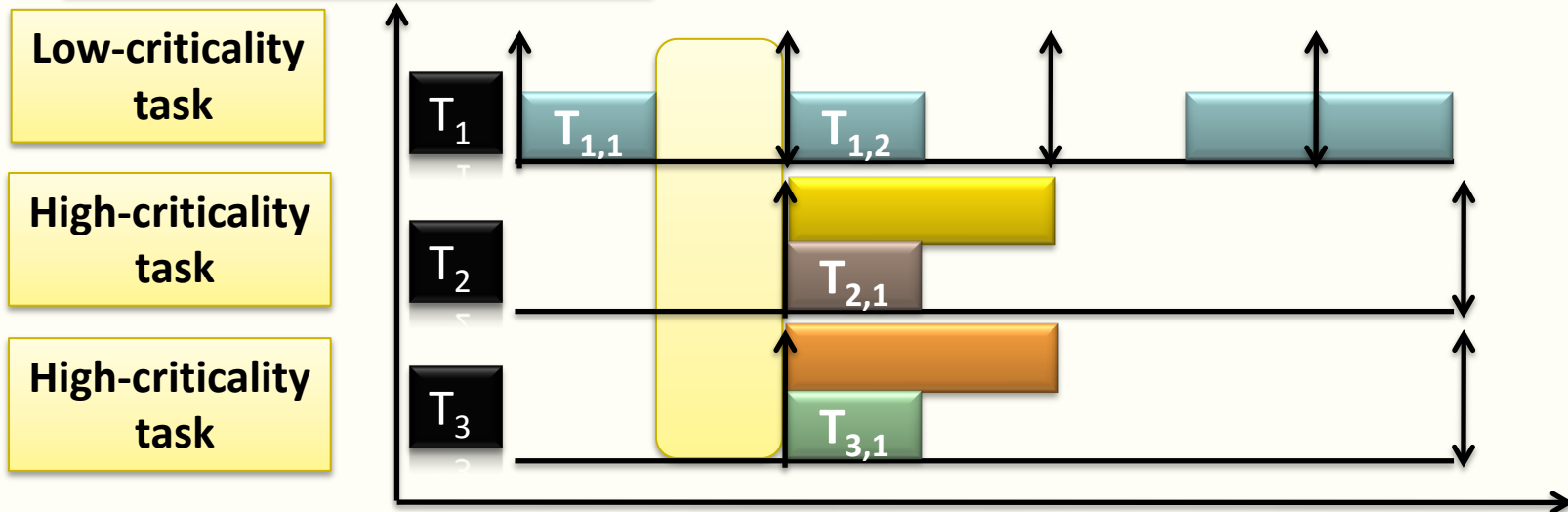


# OCBP Algorithm on Tasks

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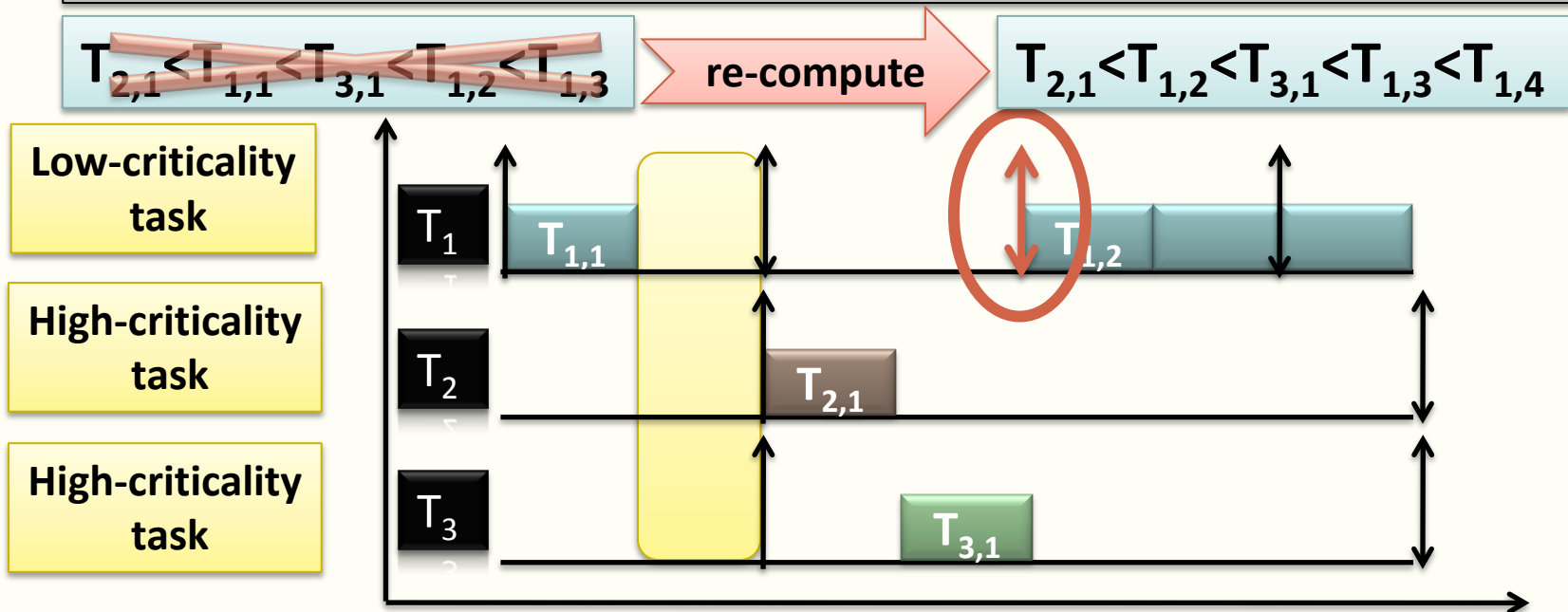




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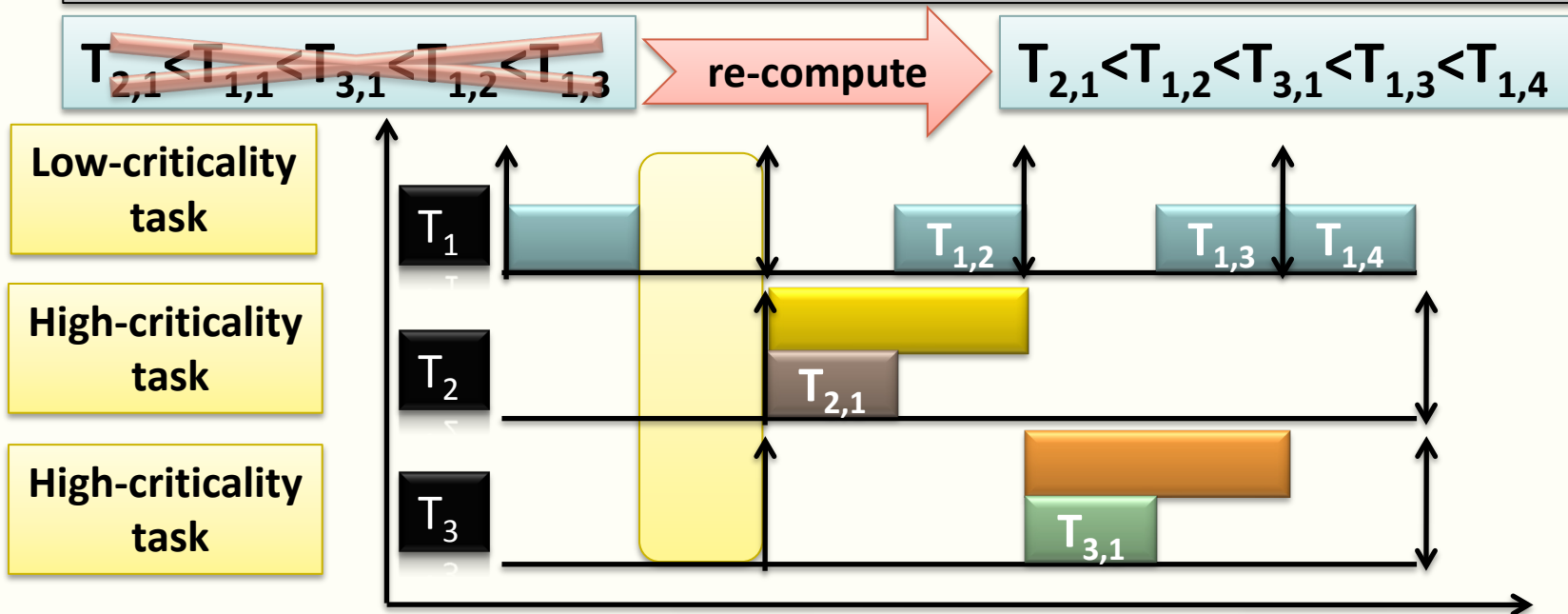




# OCBP Algorithm on Tasks

## ■ Example showing when a violation happens

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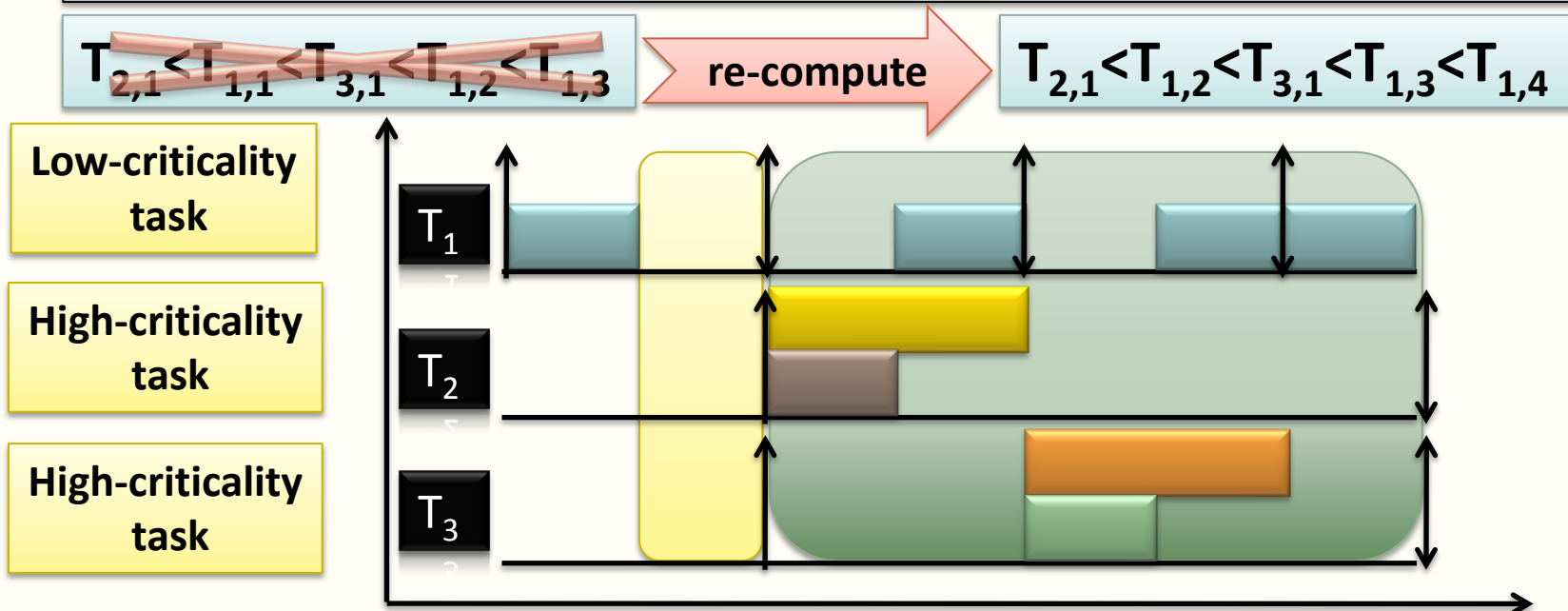




# OCBP Algorithm on Tasks

- The re-computation is **valid**

Violation: When the processor is **idle**

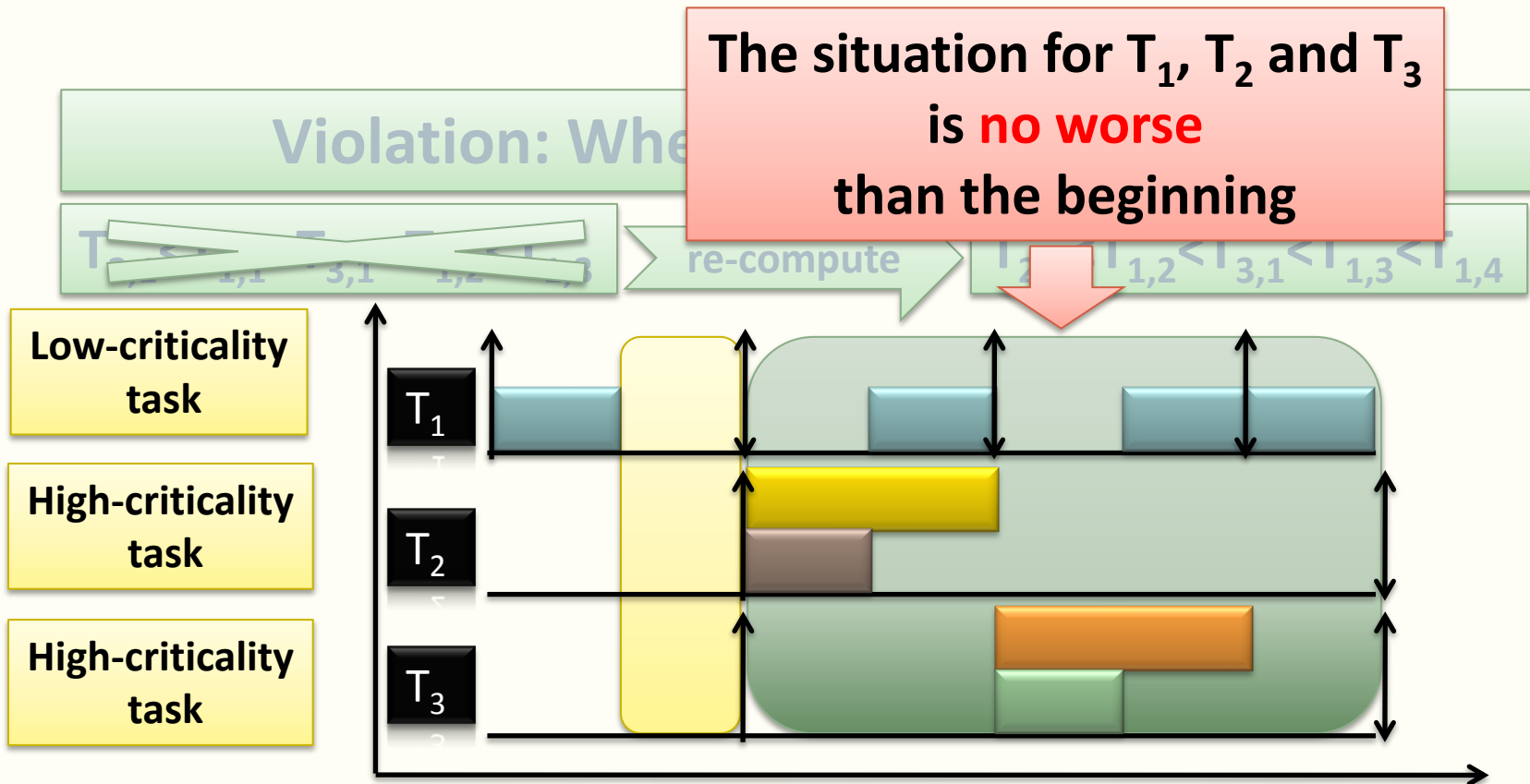




# OCBP Algorithm on Tasks

- The re-computation is **valid**

The situation for  $T_1$ ,  $T_2$  and  $T_3$   
is **no worse**  
than the beginning

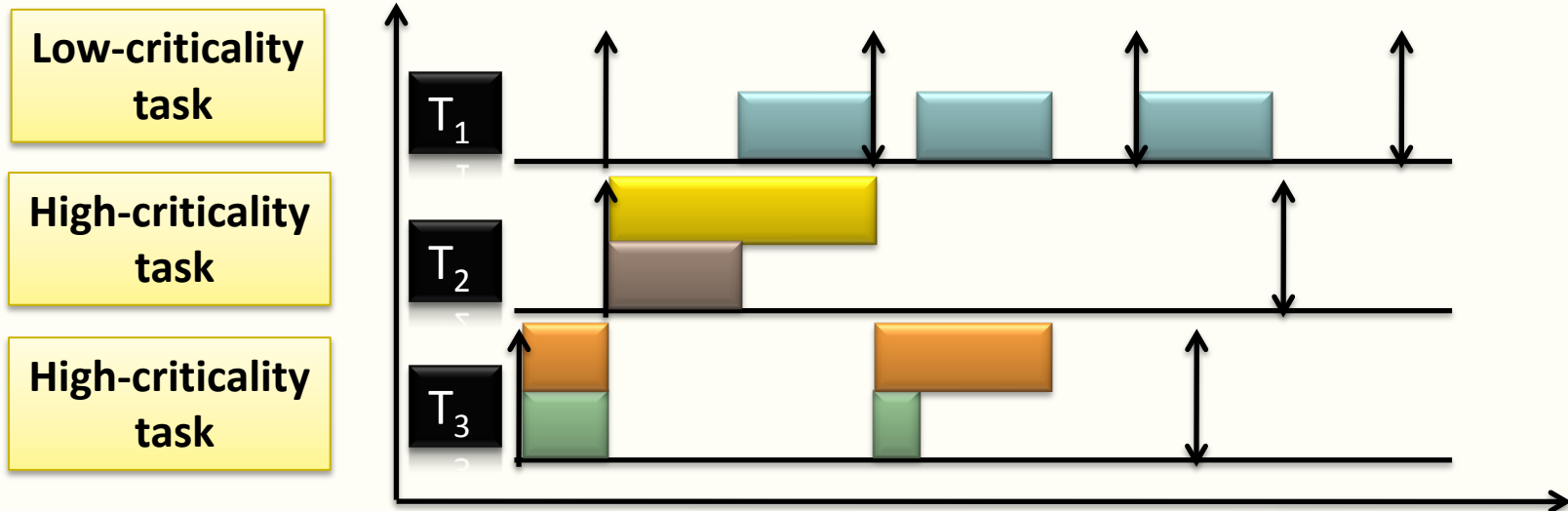




# OCBP Algorithm on Tasks

- Example showing when a violation happens

Violation: When a high-priority job is released, and **preempts a low-priority job**



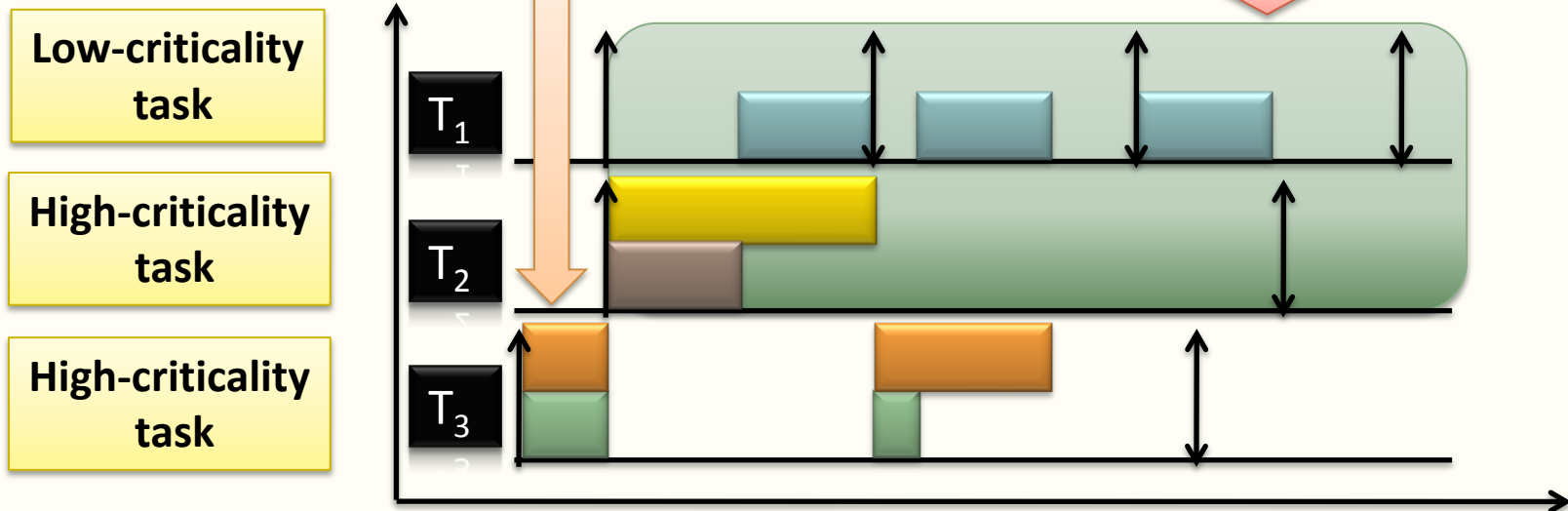


# OCBP Algorithm on Tasks

- The re-computation is also **valid**

$T_{3,1}$  is guaranteed to **meet its deadline** when  $T_{1,1}$  and  $T_{2,1}$  preempt it

The situation for  $T_{1,1}$  and  $T_{2,1}$  is **no worse** than the beginning





## ■ Our scheduling algorithm for mixed-criticality sporadic task system

- Attempt to compute a priority list for jobs in the longest busy interval using OCBP algorithm

- ◆ The schedulability will be determined

Offline

- Execute jobs according to the priority list
- If any following violations happens, re-compute the priority list using OCBP algorithm

- ◆ When the processor is idle

Run-time

- ◆ When a high-priority job preempts a low-priority job



## ■ Speedup factor

- $\Phi=1.618$  for OCBP algorithm with two criticalities
  - ◆  $\Phi=2$  for EDF with two criticalities
  - ◆  $\Phi=\infty$  for criticality-monotonic
- The result for multiple criticalities is available at
  - ◆ *Baruah et al.* MFCS 2010



## ■ **Schedulability test**

- **OCBP algorithm is itself a schedulability test**
  - ◆ It runs in pseudo-polynomial time to number of tasks
- **We also proved that for any two-criticality system**

$$l_{LO}^2 + l_{HI} \leq 1$$

**is a sufficient schedulability test**

- ◆ This schedulability test dominates currently known EDF schedulability test for mixed-criticality systems





# Performance Measurement

- **Run-time performance**
  - Every time a new job arrives, re-computation may happen
  - The re-computation could require pseudopolynomial time in the worst case



- **Scheduling algorithm with better run-time performance**
- **Multiprocessor scheduling**
- **Non-preemptions**

# Thank you



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# Load-Based Schedulability Test

## ■ Schedulability test

- For any two-criticality system

$$l_{LO}^2 + l_{HI} \leq 1$$

is schedulability test for OCBP

- And  $l_{LO} + l_{HI} \leq 1$

is schedulability test for EDF

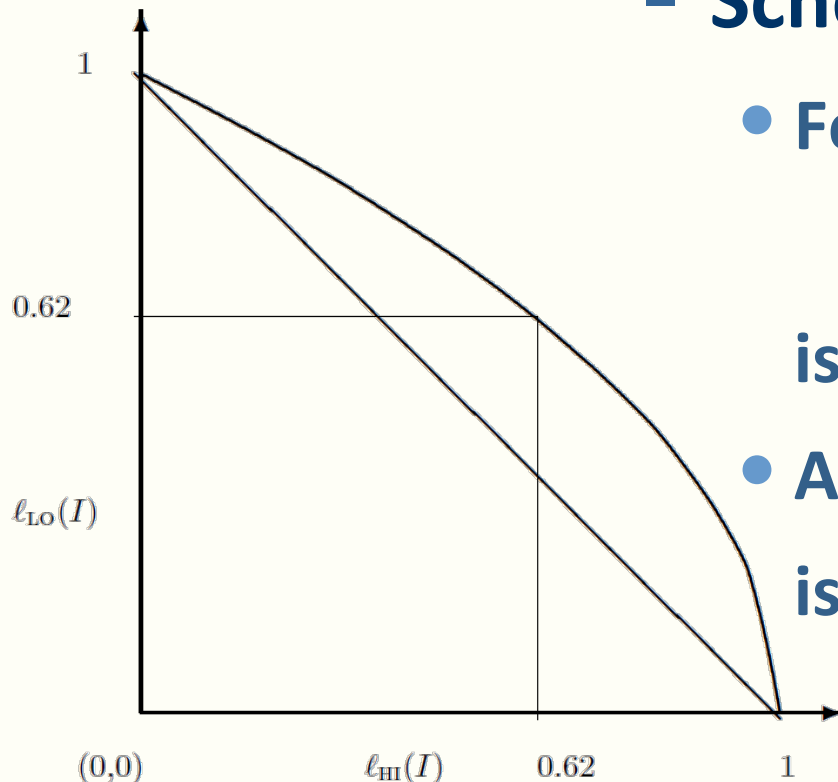
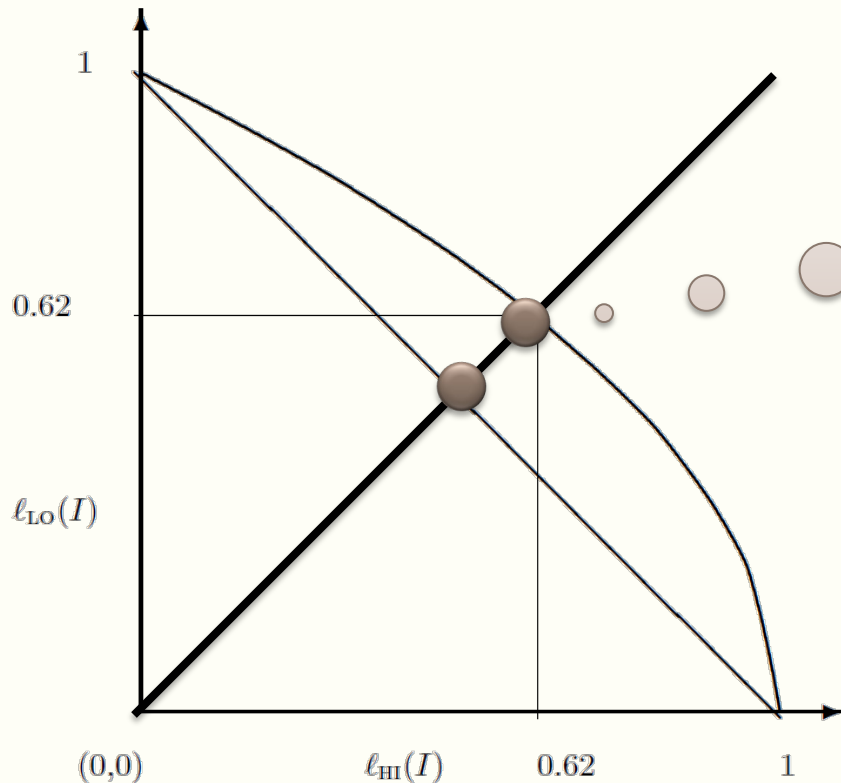


Figure 1: Bound on the LO-criticality load ( $l_{LO}$ ) as a function of HI-criticality load ( $l_{HI}$ ).



# Load-Based Schedulability Test

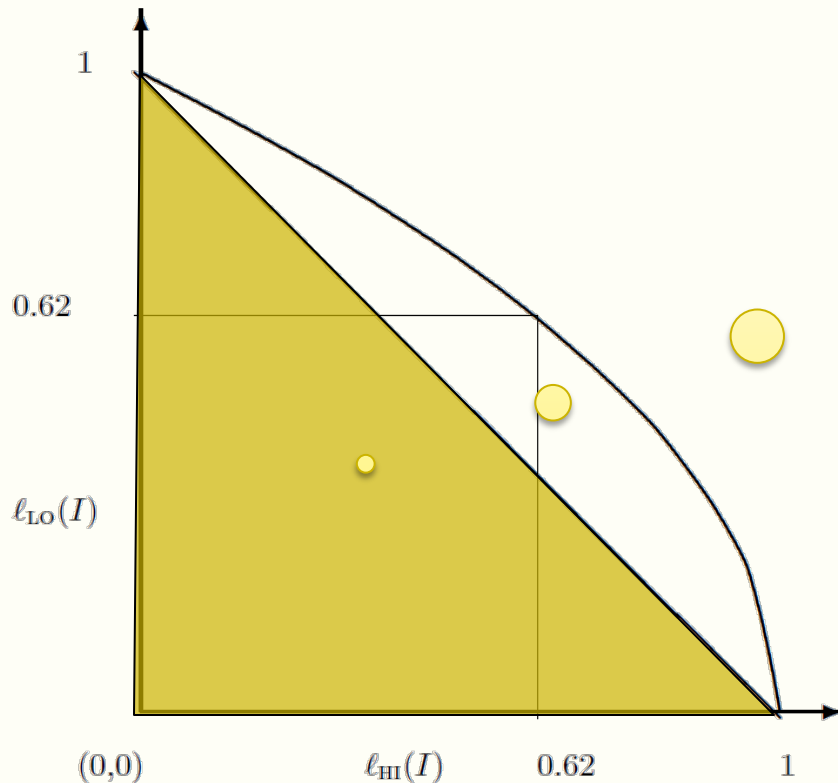


Our previous  
speedup  
factor result

Figure 1: Bound on the LO-criticality load ( $\ell_{LO}$ ) as a function of HI-criticality load ( $\ell_{HI}$ ).



# Load-Based Schedulability Test



EDF can  
definitely  
schedule

Figure 1: Bound on the LO-criticality load ( $\ell_{LO}$ ) as a function of HI-criticality load ( $\ell_{HI}$ ).



# Load-Based Schedulability Test

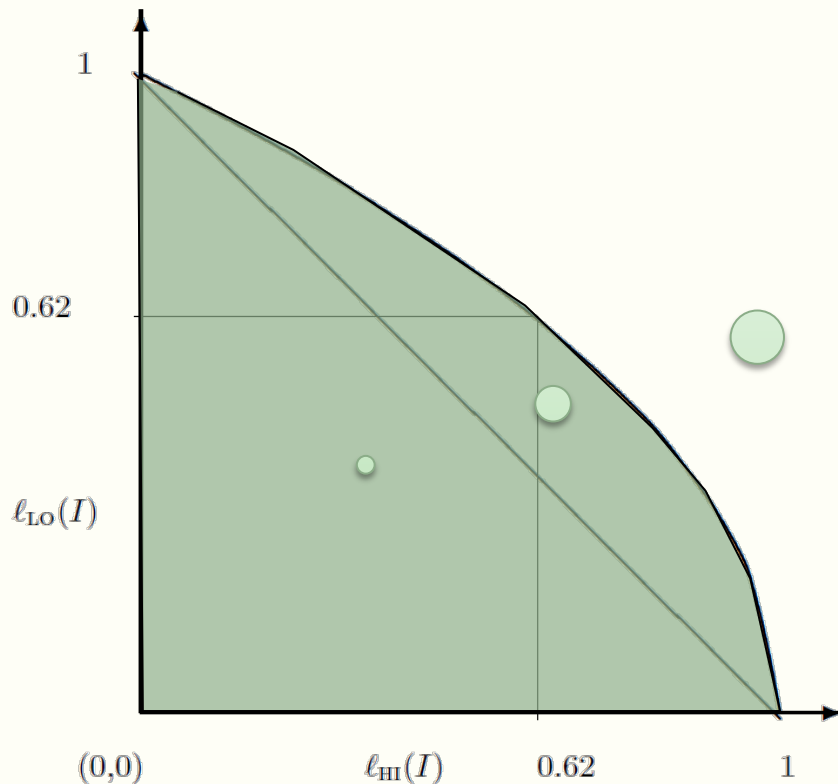


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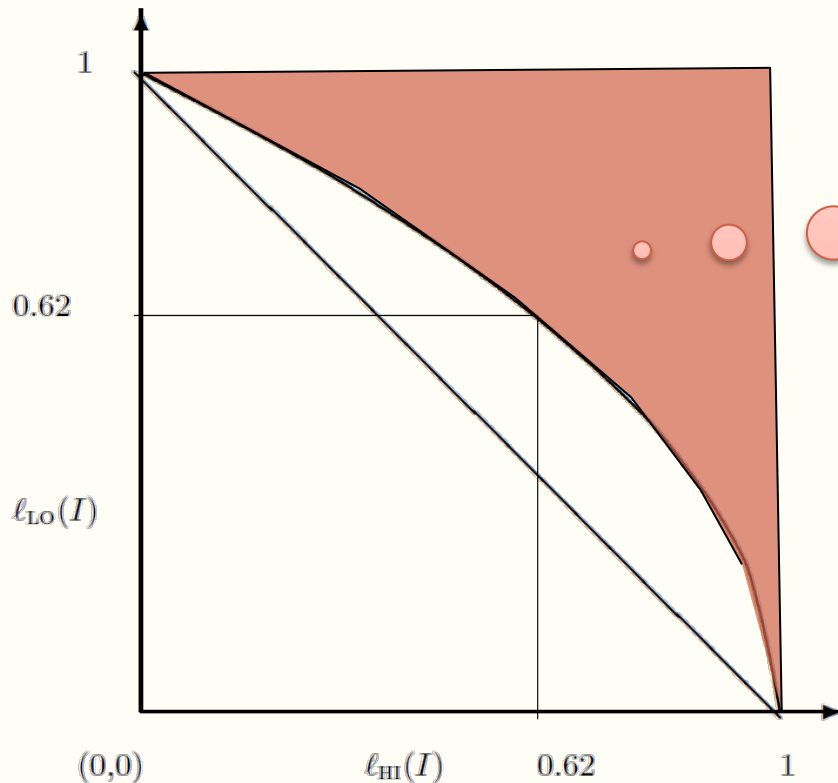


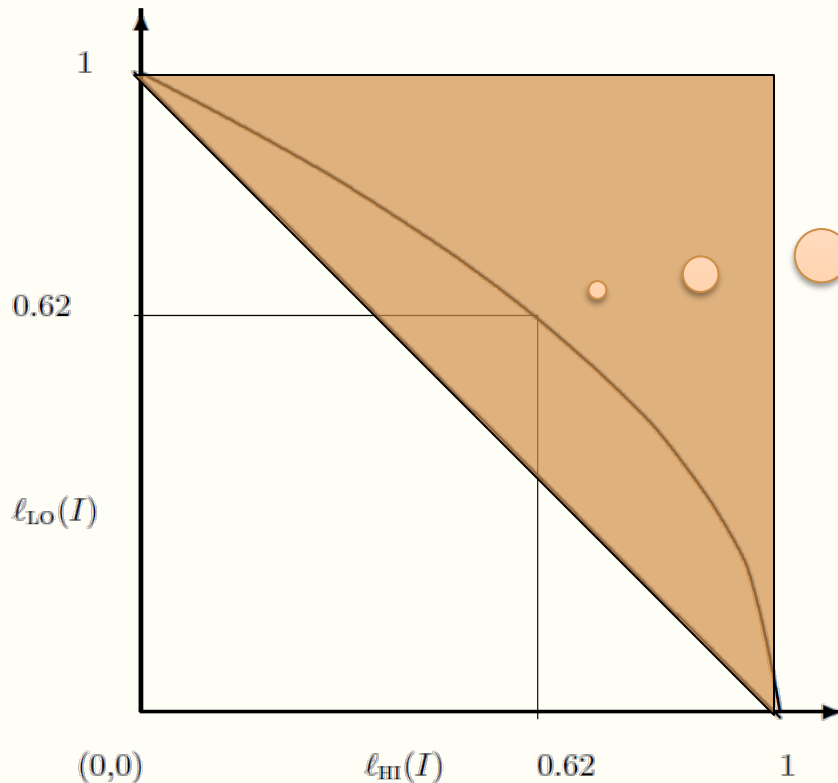
Figure 1: Bound on the LO-criticality load ( $\ell_{LO}$ ) as a function of HI-criticality load ( $\ell_{HI}$ ).

We can try  
OCBP as a test





# Load-Based Schedulability Test



No known  
test exists for  
EDF

Figure 1: Bound on the LO-criticality load ( $\ell_{LO}$ ) as a function of HI-criticality load ( $\ell_{HI}$ ).