



THE UNIVERSITY
of NORTH CAROLINA
at CHAPEL HILL

Global Mixed-Criticality Scheduling on Multiprocessors

Haohan Li **Sanjoy Baruah**

Department of Computer Science

The University of North Carolina at Chapel Hill



- **Scheduling mixed-criticality task systems**
 - Sporadically releasing
 - Identical multiprocessors
 - Global scheduling
 - Two criticality levels
 - Implicit deadlines



- **Mixed-criticality sporadic task model**
 - **Period: P_i**
 - ◆ $P_1=3, P_2=6$





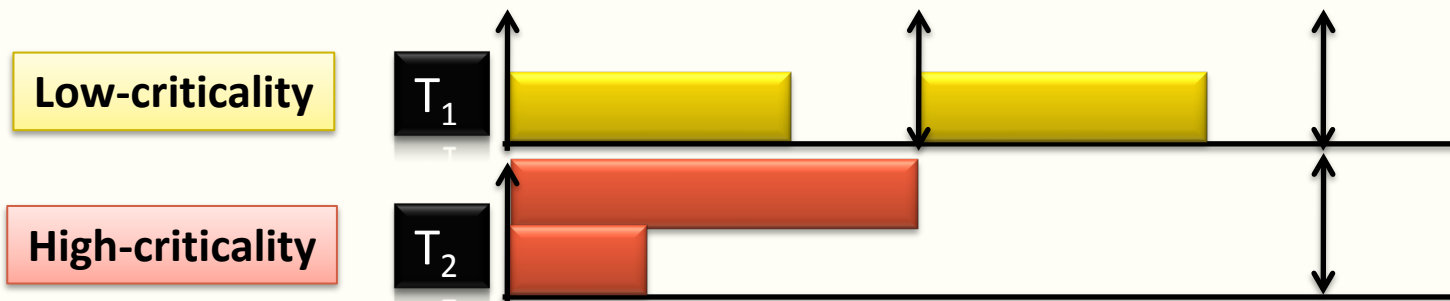
■ Mixed-criticality sporadic task model

- Period: P_i
 - ◆ $P_1=3, P_2=6$
- WCET: $C_i(LO), C_i(HI)$
 - ◆ For T_1 : $C_1(LO)=2$
 - ◆ For T_2 : $C_2(LO)=1, C_2(HI)=3$



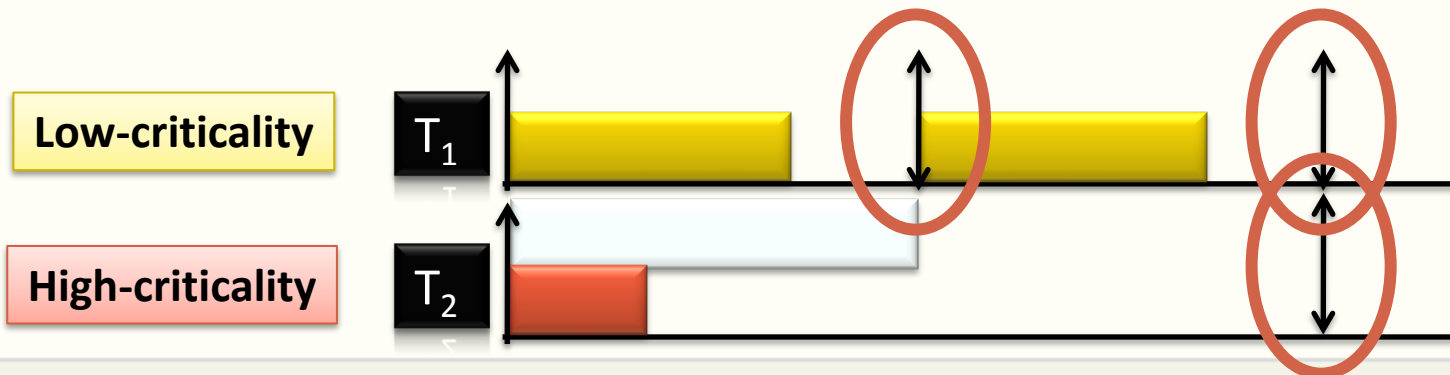


- **Mixed-criticality sporadic task model**
 - If every job uses up to **low-criticality WCET**, all **deadlines** must be met



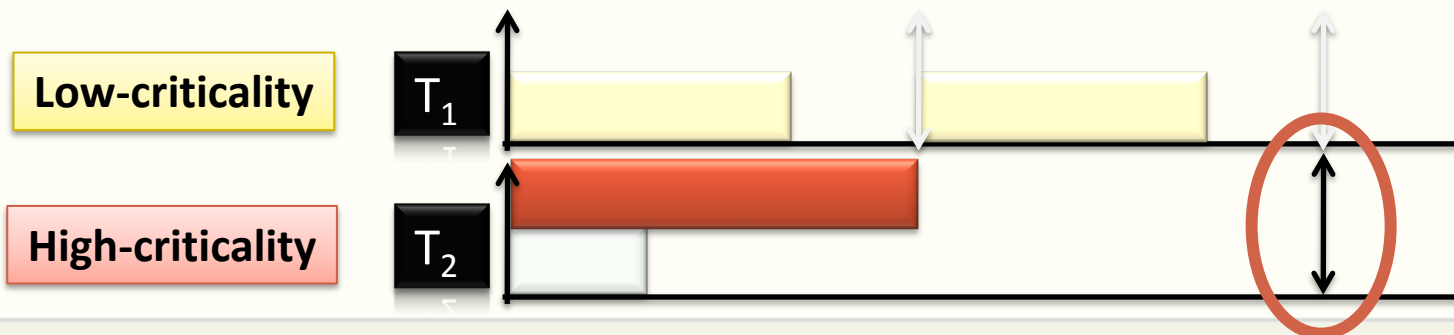


- **Mixed-criticality sporadic task model**
 - If every job uses up to **low-criticality WCET**, all **deadlines** must be met



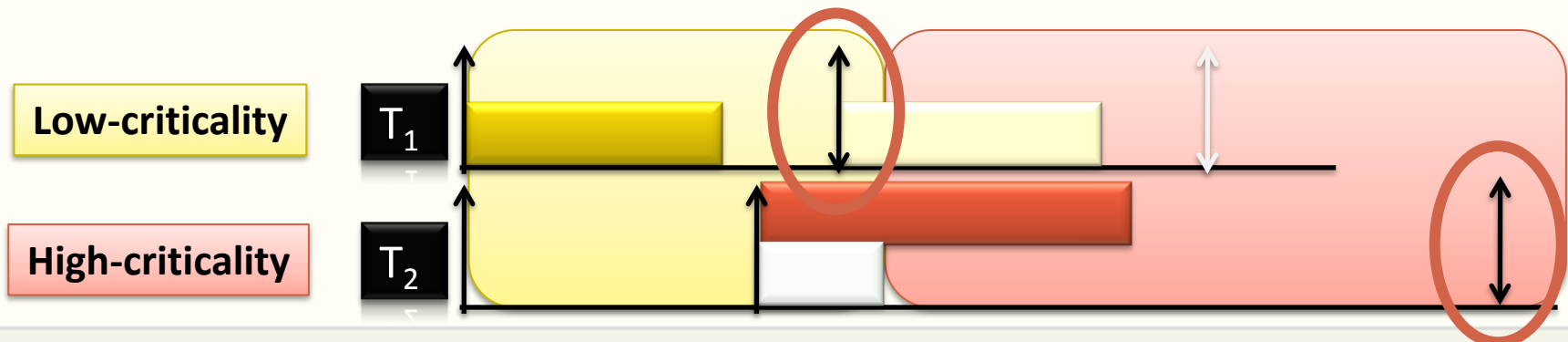


- **Mixed-criticality sporadic task model**
 - If every job uses up to **low-criticality WCET**, **all deadlines** must be met
 - If some job uses **more than low-criticality WCET**, **only high-criticality deadlines** must be met





- **Mixed-criticality sporadic task model**
 - If every job uses up to low-criticality WCET, all deadlines must be met
 - If some job uses more than low-criticality WCET, only high-criticality deadlines must be met
 - Execution times are only known at **run-time**





■ EDF-VD

- *Mixed-Criticality Scheduling of Sporadic Task Systems*, Baruah et al., ESA 2011
 - ◆ Earliest Deadline First with Virtual Deadlines
 - ◆ An EDF-based **mixed-criticality** scheduling algorithm for **implicit-deadline** systems on **uniprocessor**
 - ◆ Speed-up factor is at most $(\sqrt{5+1})/2 \approx 1.618$



■ fpEDF

- *Optimal Utilization Bounds for the Fixed-Priority Scheduling of Periodic Task Systems on Identical Multiprocessors*, Baruah, TC 2004
 - ◆ Fixed Priority Earliest Deadline First
 - ❖ Fixed-job-priority scheduling algorithm
 - ◆ An EDF-based **global** scheduling algorithm for **implicit-deadline** systems on **multiprocessors**
 - ◆ Speed-up factor is at most 2

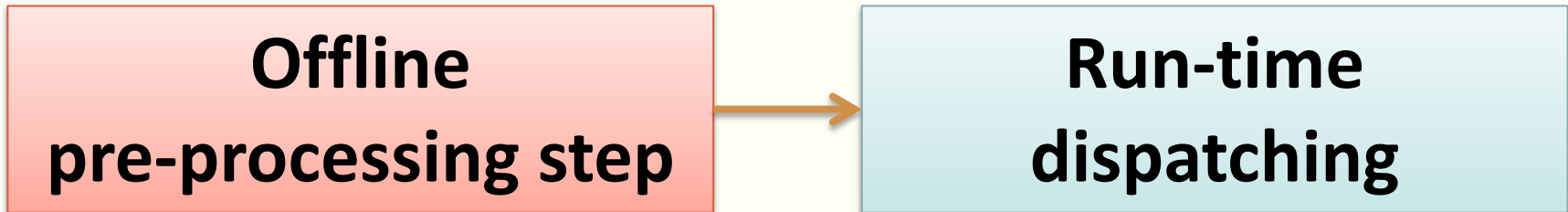


A **global preemptive** algorithm for scheduling **mixed-criticality implicit-deadline** systems on **identical multiprocessors**

- Proving that speed-up factor is at most $\sqrt{5+1} \approx 3.236$
- Experiments to show effectiveness

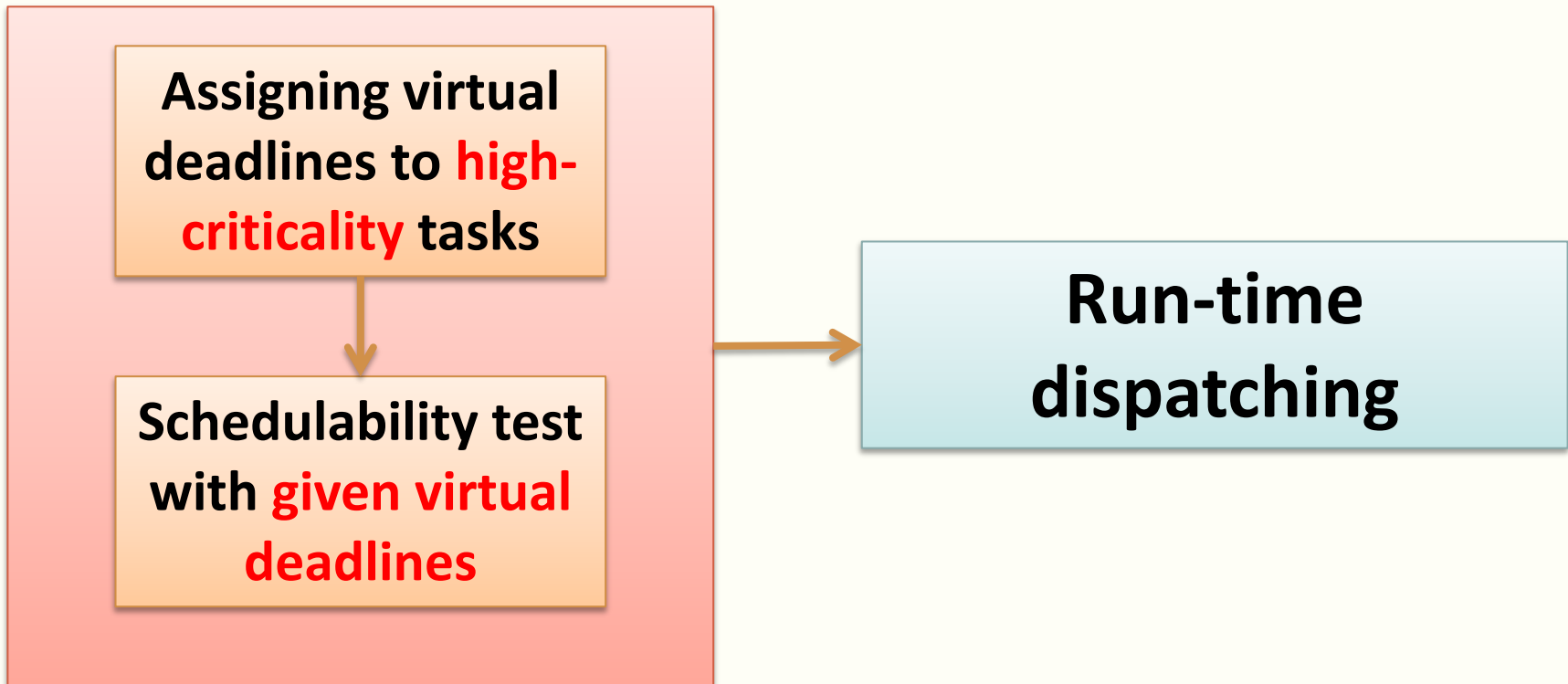


Scheduling Algorithm



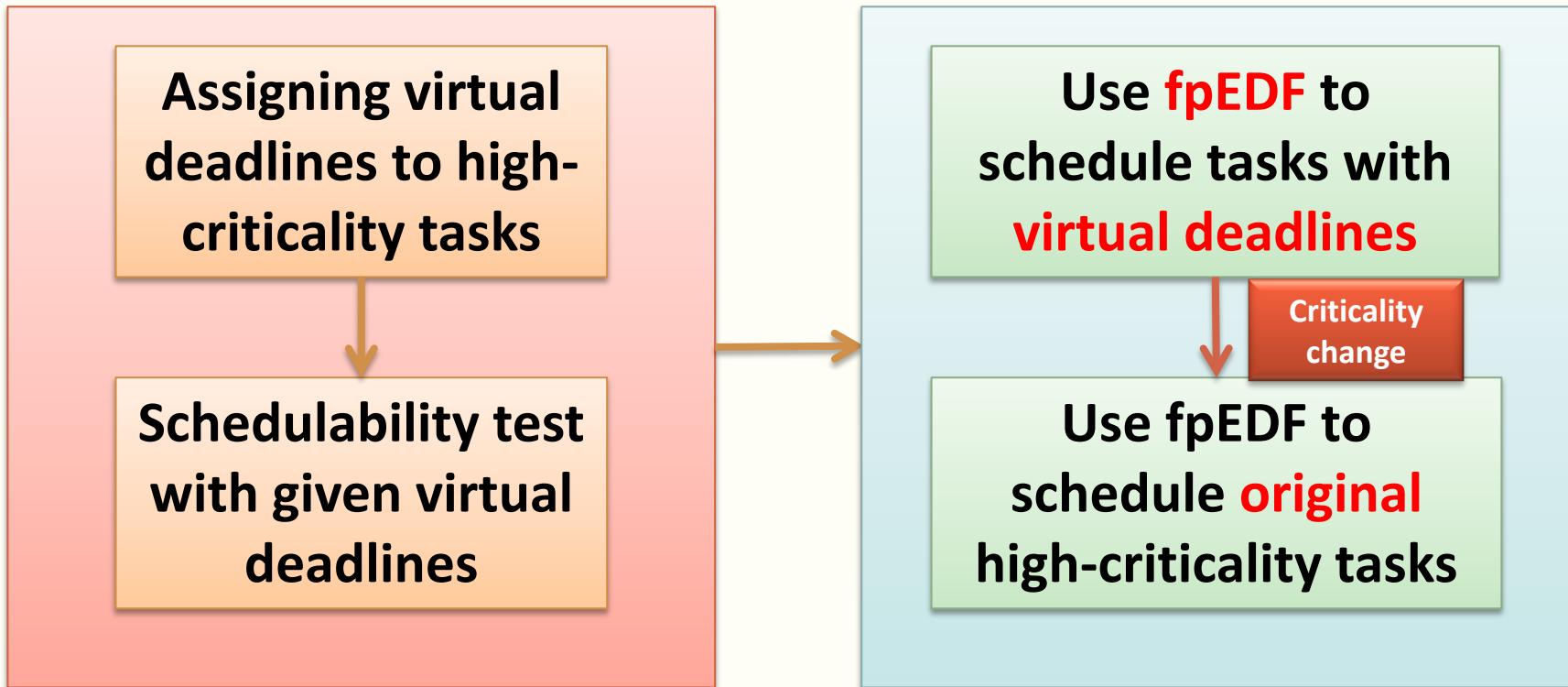


Scheduling Algorithm



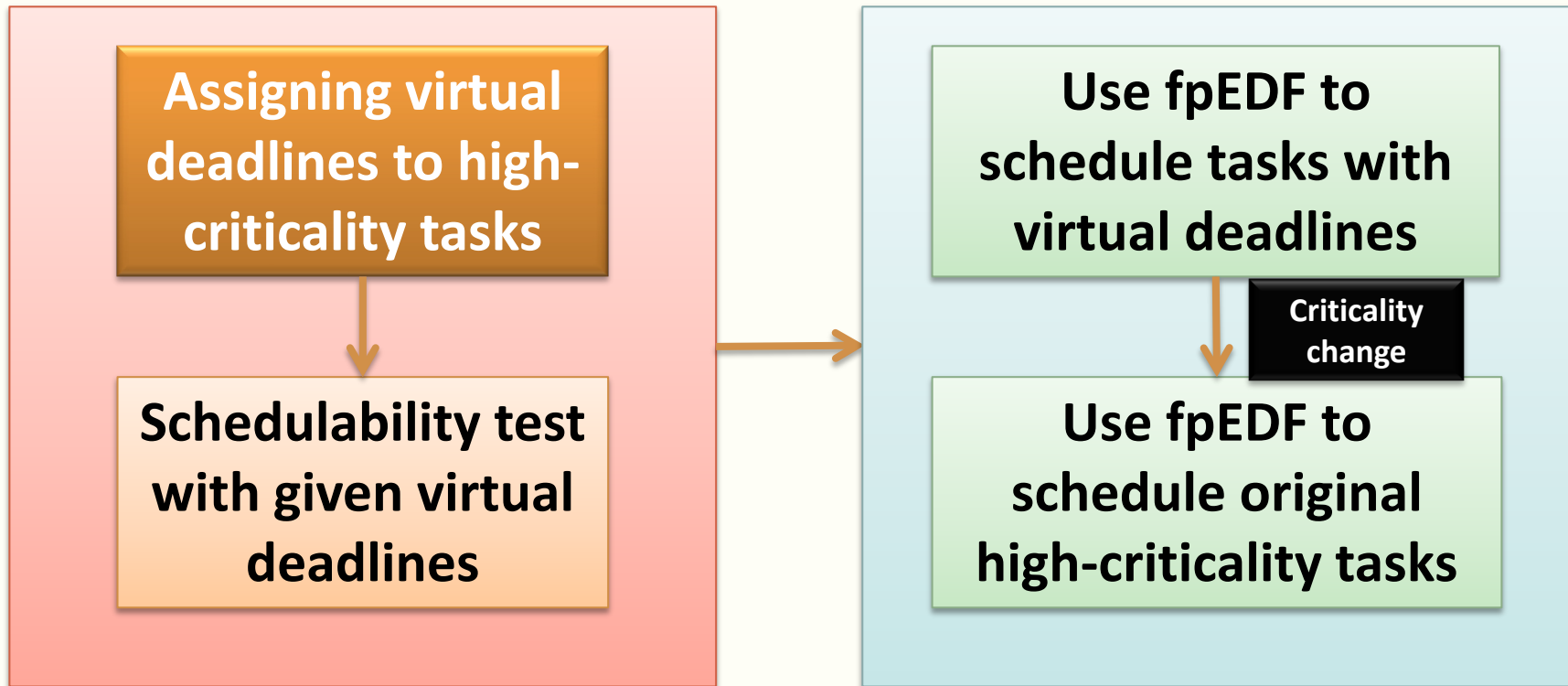


Scheduling Algorithm





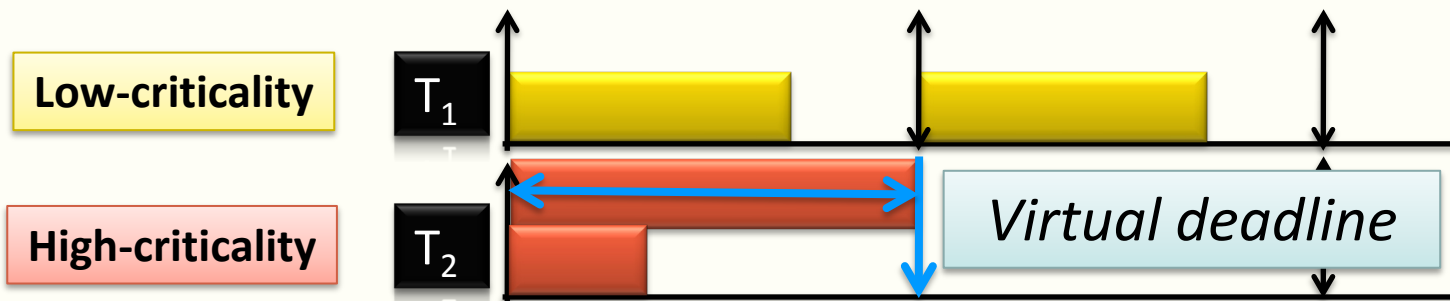
Scheduling Algorithm





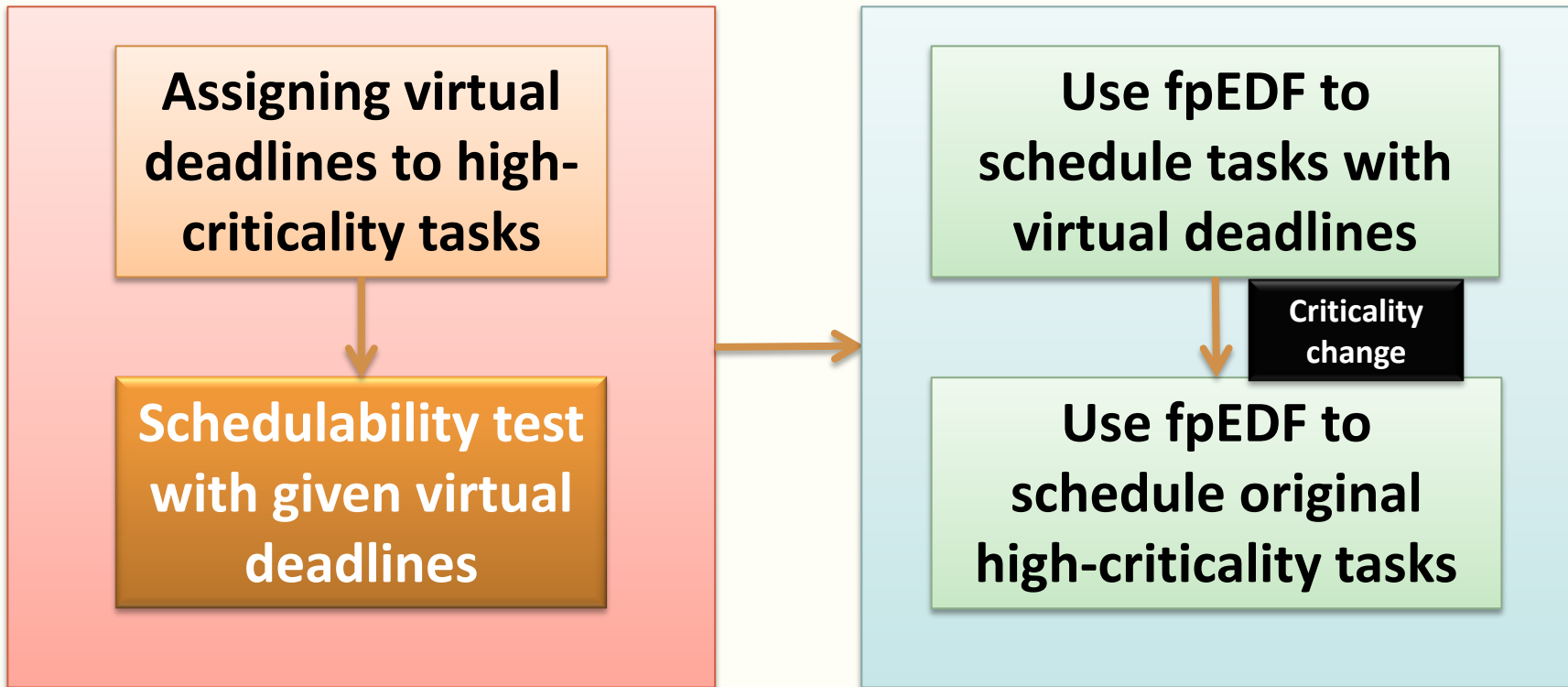
Scheduling Algorithm

- Assigning virtual deadlines to high-criticality tasks
 - Virtual deadlines are assigned **proportionally** to original deadlines with factor x ($0 < x < 1$)
 - ◆ In the example, assume that $x=1/2$, then the virtual deadline is $xP_2=1/2*6=3$



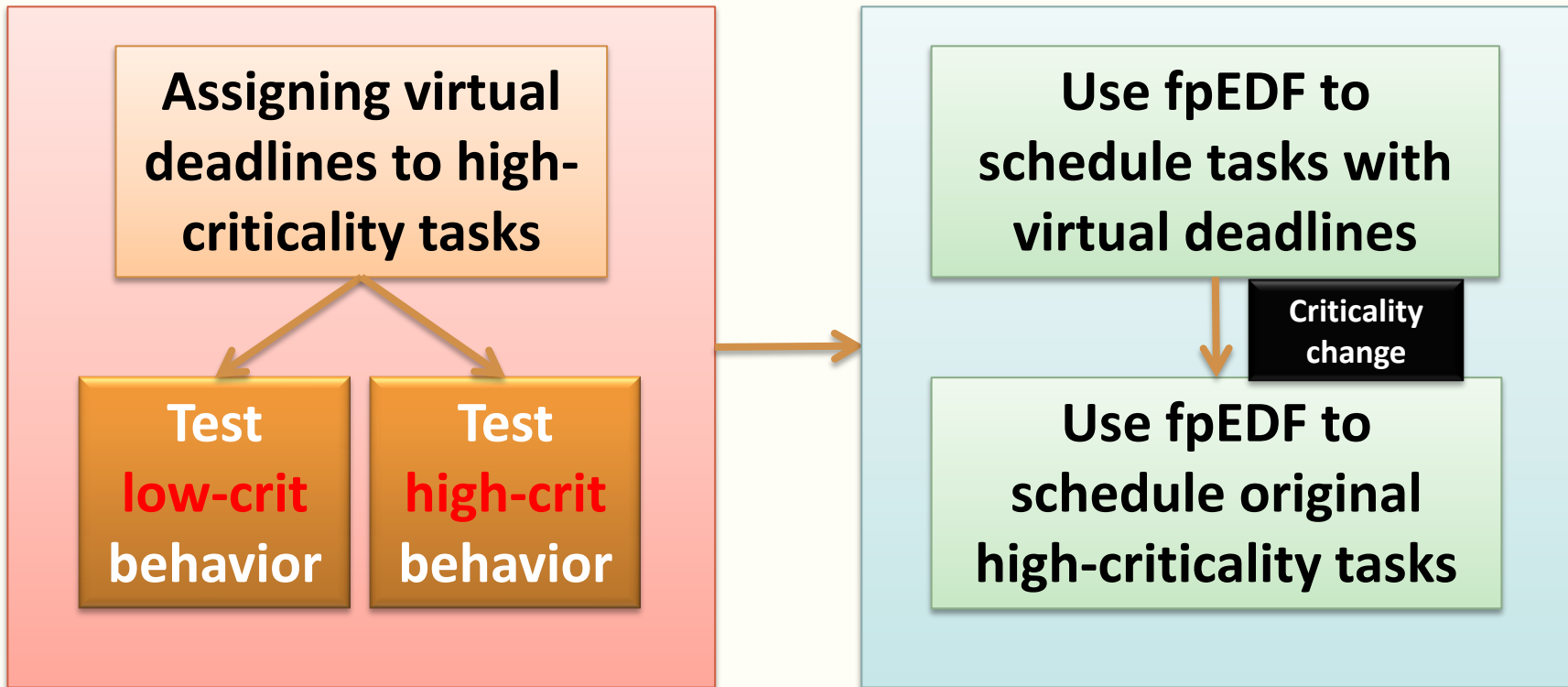


Scheduling Algorithm





Scheduling Algorithm

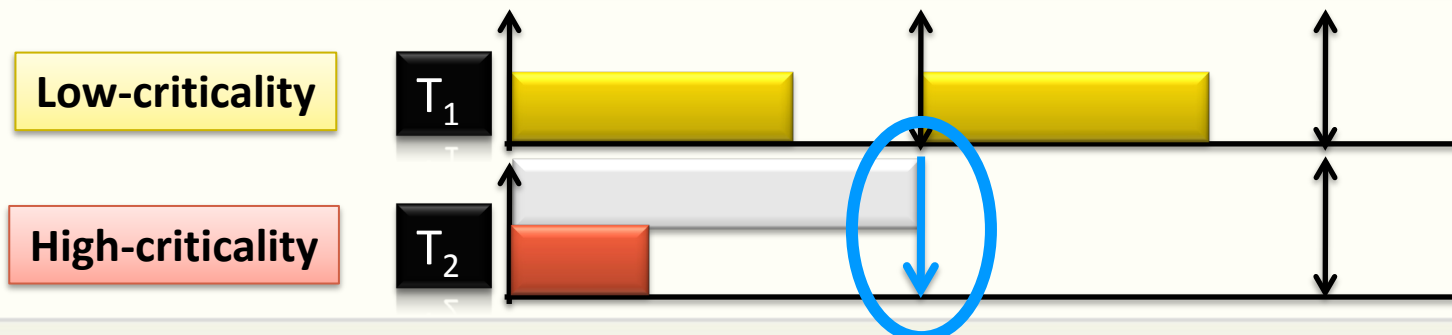




Scheduling Algorithm

- **Schedulability test with given virtual deadlines**
 - **Low-criticality sufficient schedulability condition**
 - ◆ at low-criticality, the virtual system with **virtual periods** is schedulable

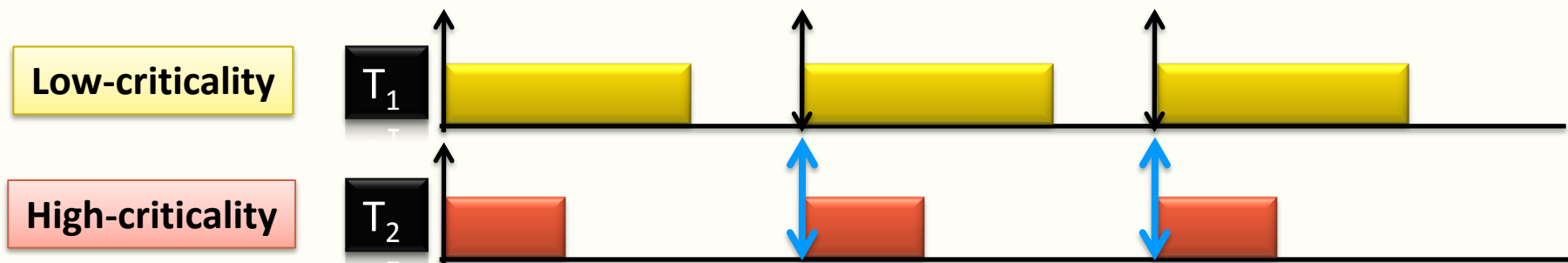
Assuming that in low-criticality behavior, all high-criticality tasks must **be completed by their virtual deadlines**





Scheduling Algorithm

- **Schedulability test with given virtual deadlines**
 - **Low-criticality sufficient schedulability condition**
 - ◆ at low-criticality, the virtual system with **virtual periods** is schedulable
 - ◆ The virtual periods of high-crit tasks will be xP_i
 - ◆ Test the virtual system with **fpEDF's schedulability condition**





Scheduling Algorithm

- **Schedulability test with given virtual deadlines**
 - **High-criticality sufficient schedulability condition**
 - ◆ at high-criticality, the virtual system with **remaining periods** and **high-crit WCETs** is schedulable

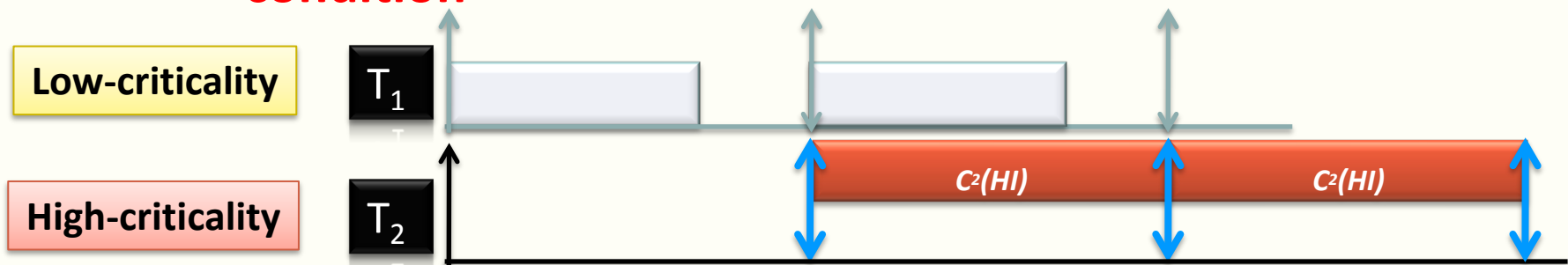
Only high-crit demand is left after criticality change





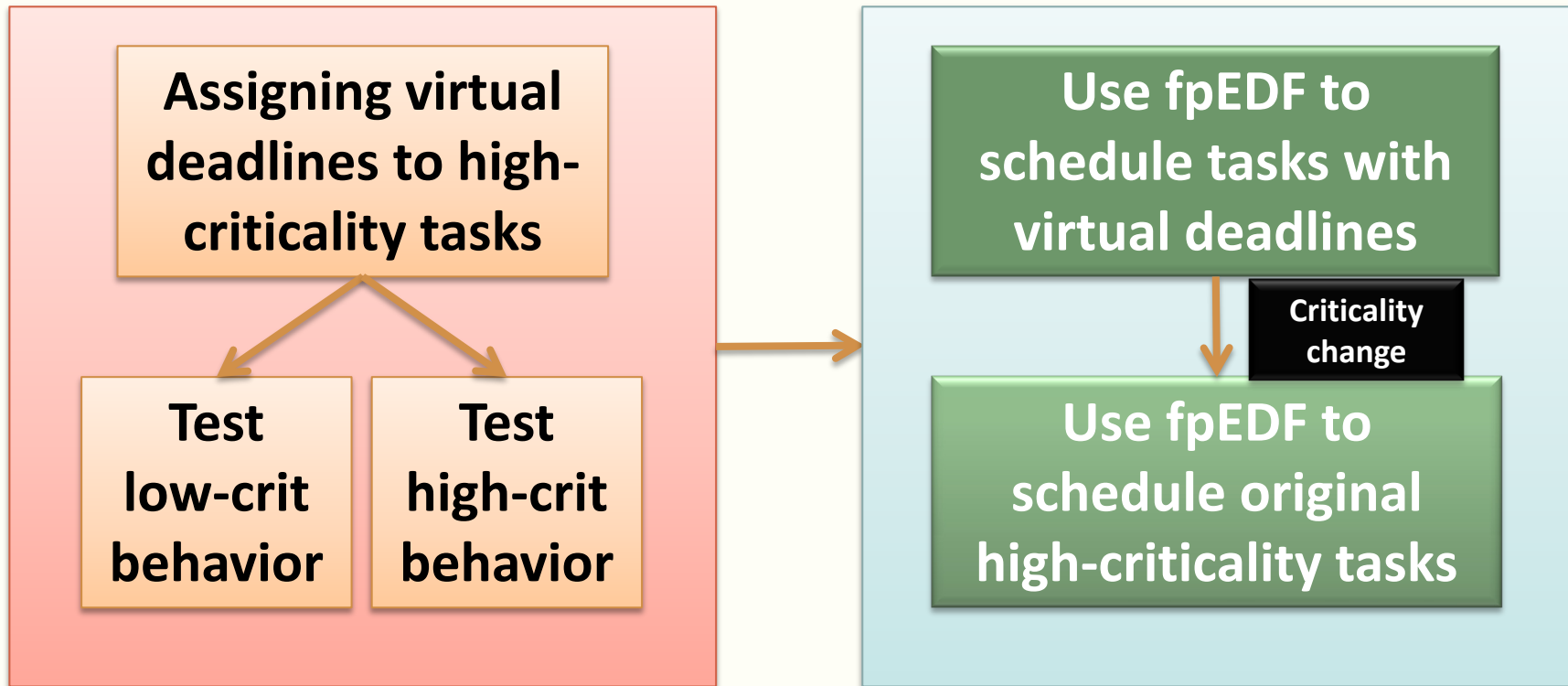
Scheduling Algorithm

- **Schedulability test with given virtual deadlines**
 - **High-criticality sufficient schedulability condition**
 - ◆ at high-criticality, the virtual system with **remaining periods** and **high-crit WCETs** is schedulable
 - ◆ The virtual periods and virtual WCET of high-crit tasks will be $(1-x)P_i$ and $C_i(HI)$
 - ◆ Test the virtual system with **fpEDF's schedulability condition**





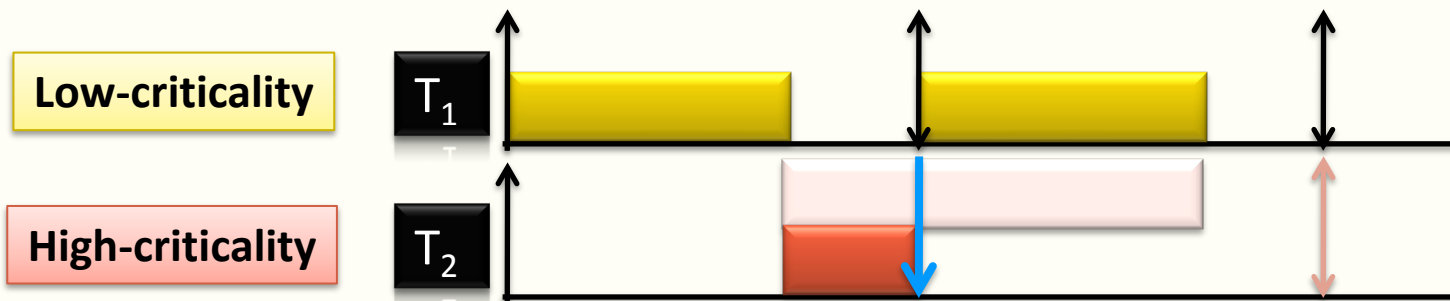
Scheduling Algorithm





Scheduling Algorithm

- Run-time dispatching
 - Use **fpEDF** to schedule tasks with **virtual deadlines**

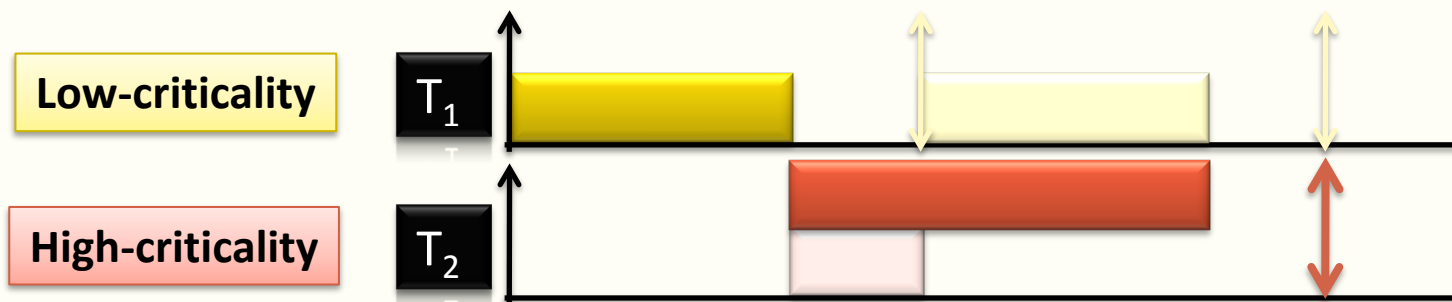




Scheduling Algorithm

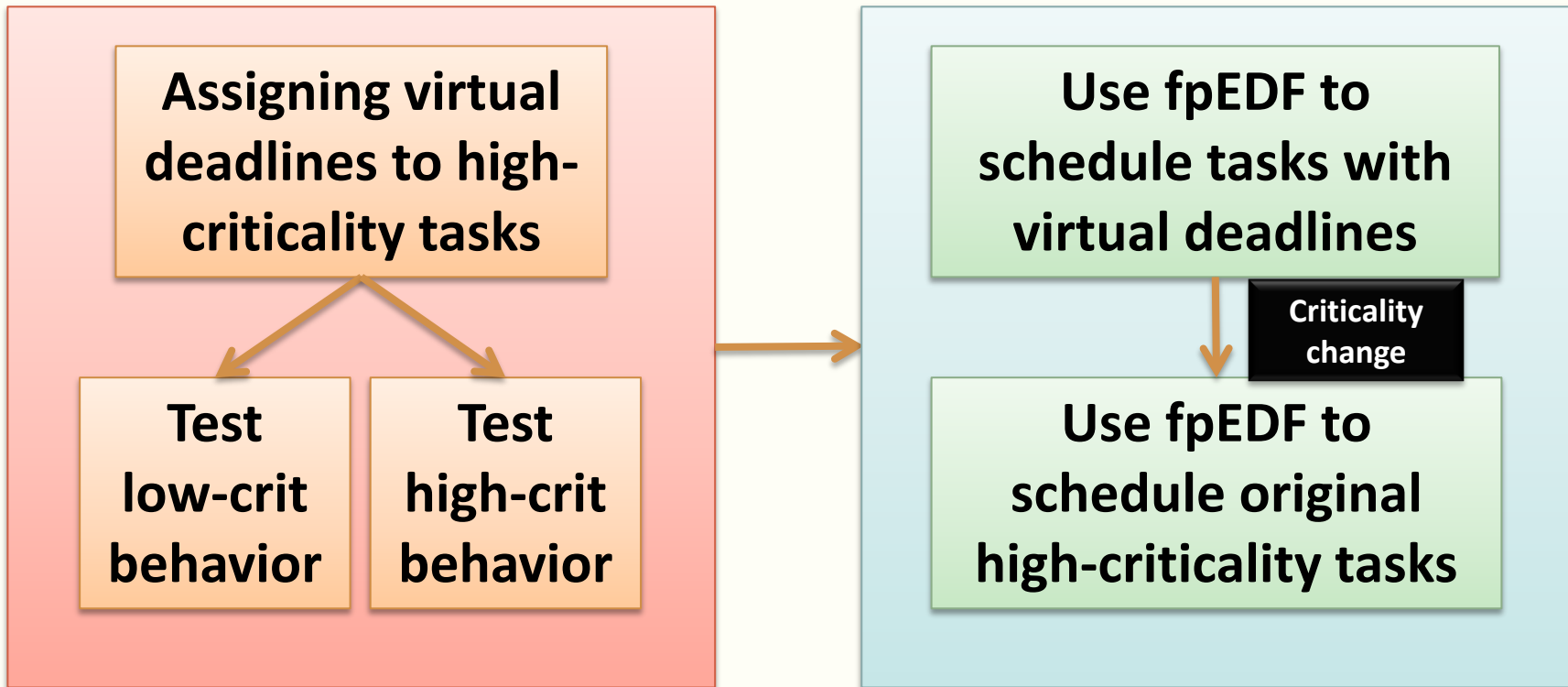
■ Run-time dispatching

- Use fpEDF to schedule tasks with virtual deadlines
- If **high-crit behavior detected**, drop low-crit tasks and use fpEDF to schedule high-crit tasks with **original deadlines**



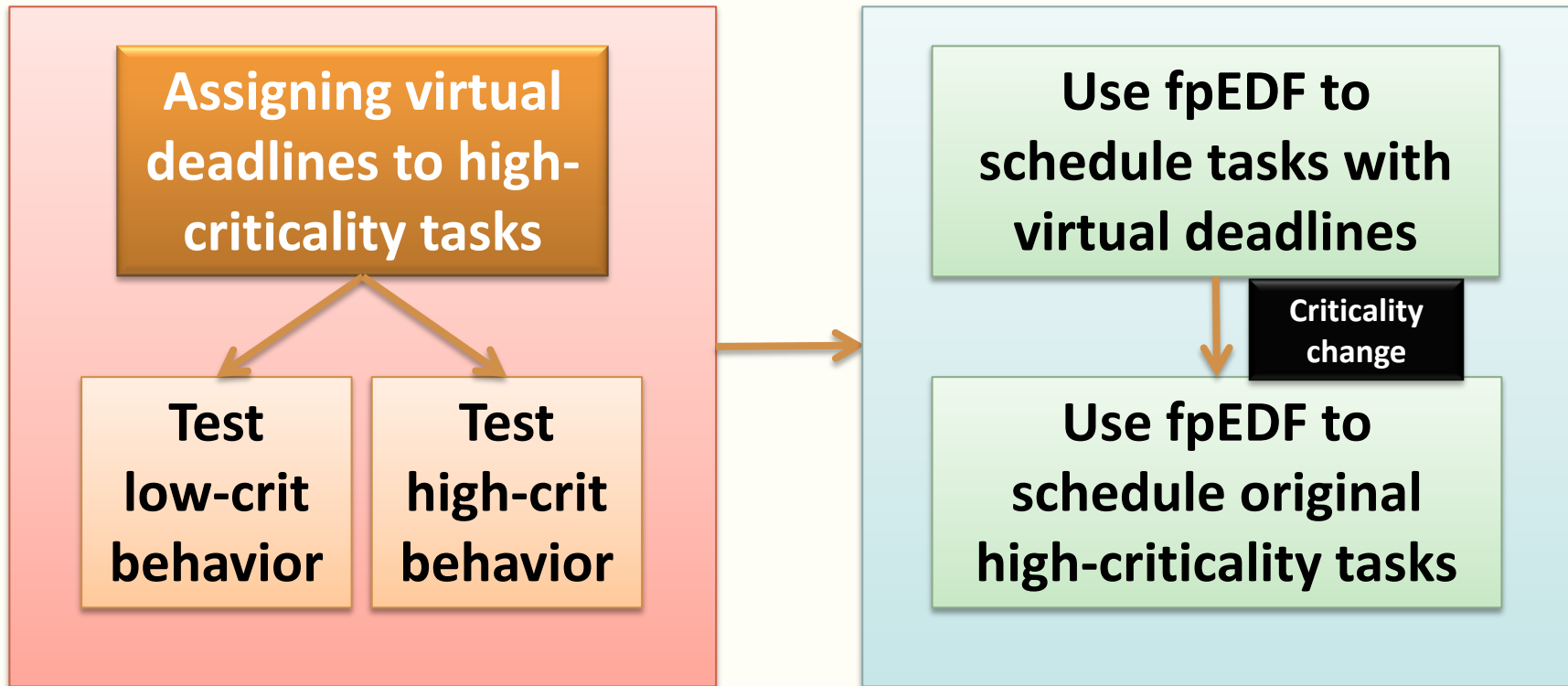


Scheduling Algorithm





Scheduling Algorithm

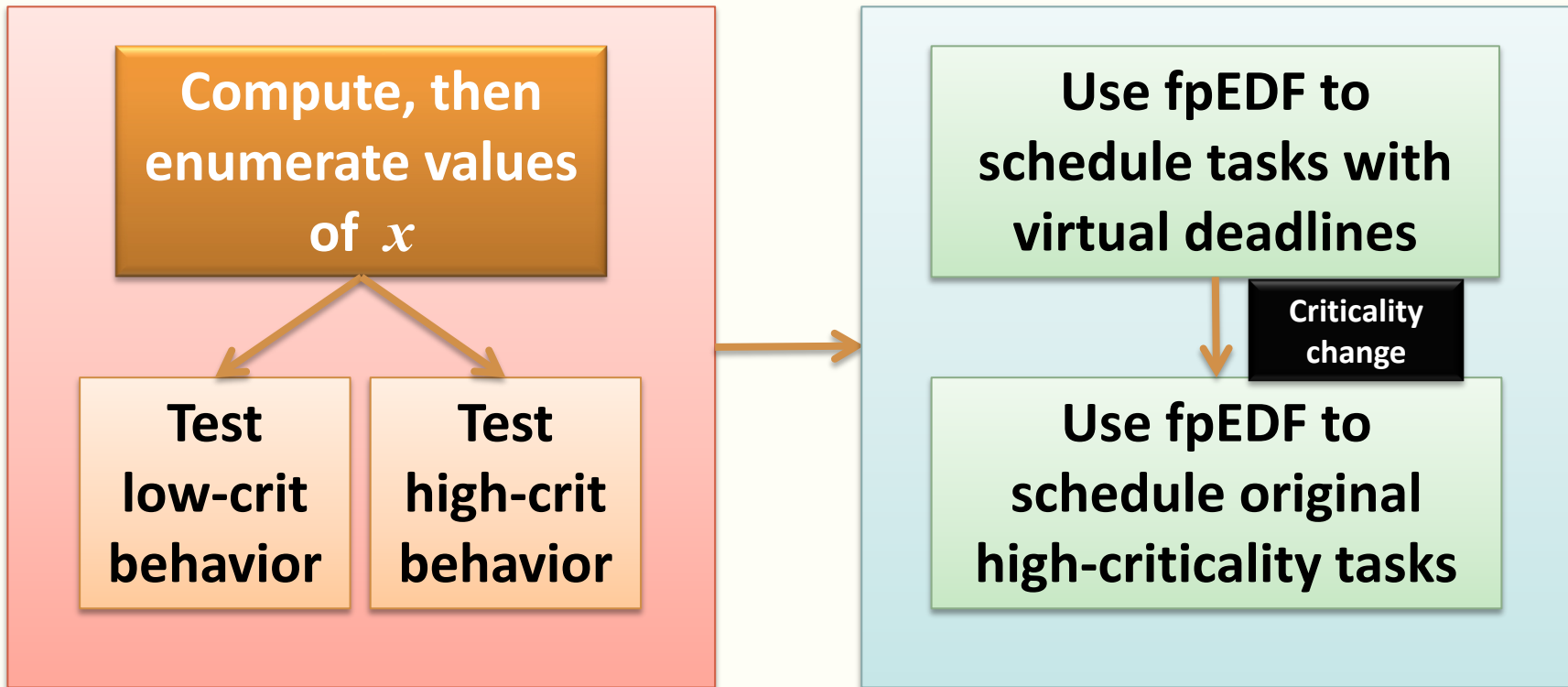




- **The selection of x**
 - **Computation from theoretical analysis**
 - ◆ *Fig. 2 and Theorem 3 in the paper*
 - ◆ Does not always generate a proper x
 - ◆ Guarantees the speed-up factor
 - **Enumeration as a pragmatic improvement**
 - ◆ The possible values of x are finite
 - ◆ If none of them passes the test, report unschedulable

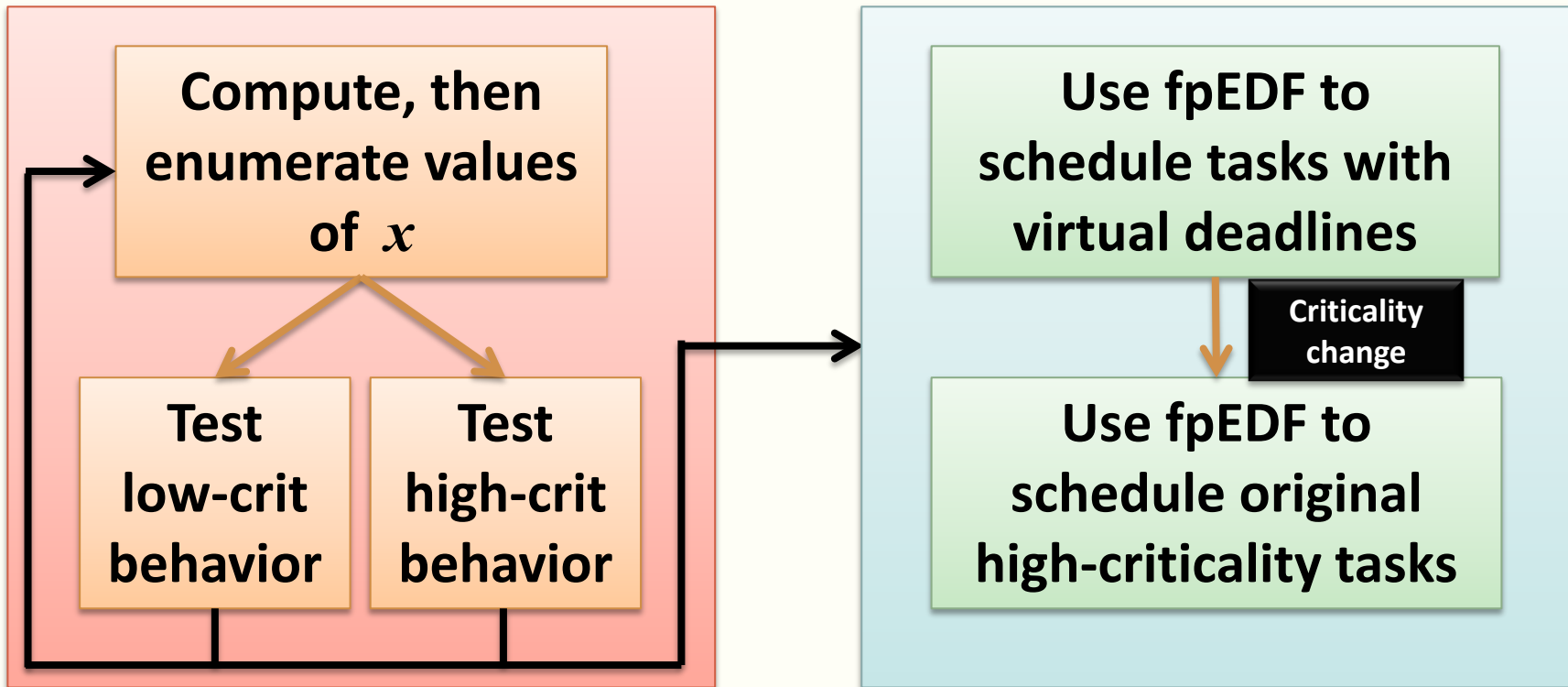


Scheduling Algorithm





Scheduling Algorithm





■ Simulation experiments

- Generate random MC implicit-deadline tasks with given utilization in low and high criticality

- ◆ Utilization is defined as the maximum fraction of time demand in each criticality

- ◆ $U(LO)=2/3+1/6=5/6$

- ◆ $U(HI)=3/6$



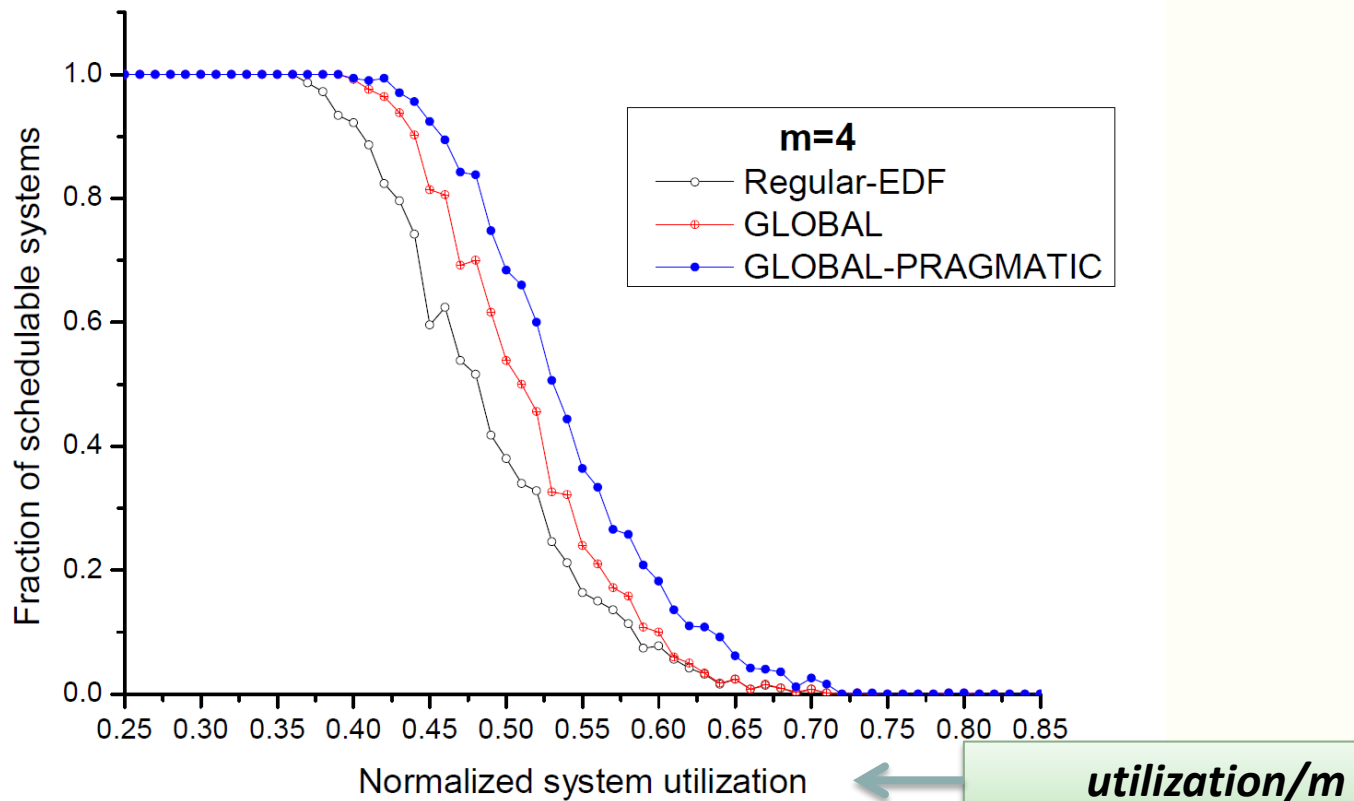


■ Simulation experiments

- Generate random MC implicit-deadline tasks with given utilization in low and high criticality
 - ◆ The task generation algorithm is in *Fig. 4*
- Compare 3 algorithms
 - ◆ Regular-EDF: *Worst-case reserving to meet all deadlines*
 - ◆ GLOBAL: *Using computed x only*
 - ◆ GLOBAL-PRAGMATIC: *Using computed and enumerated x*

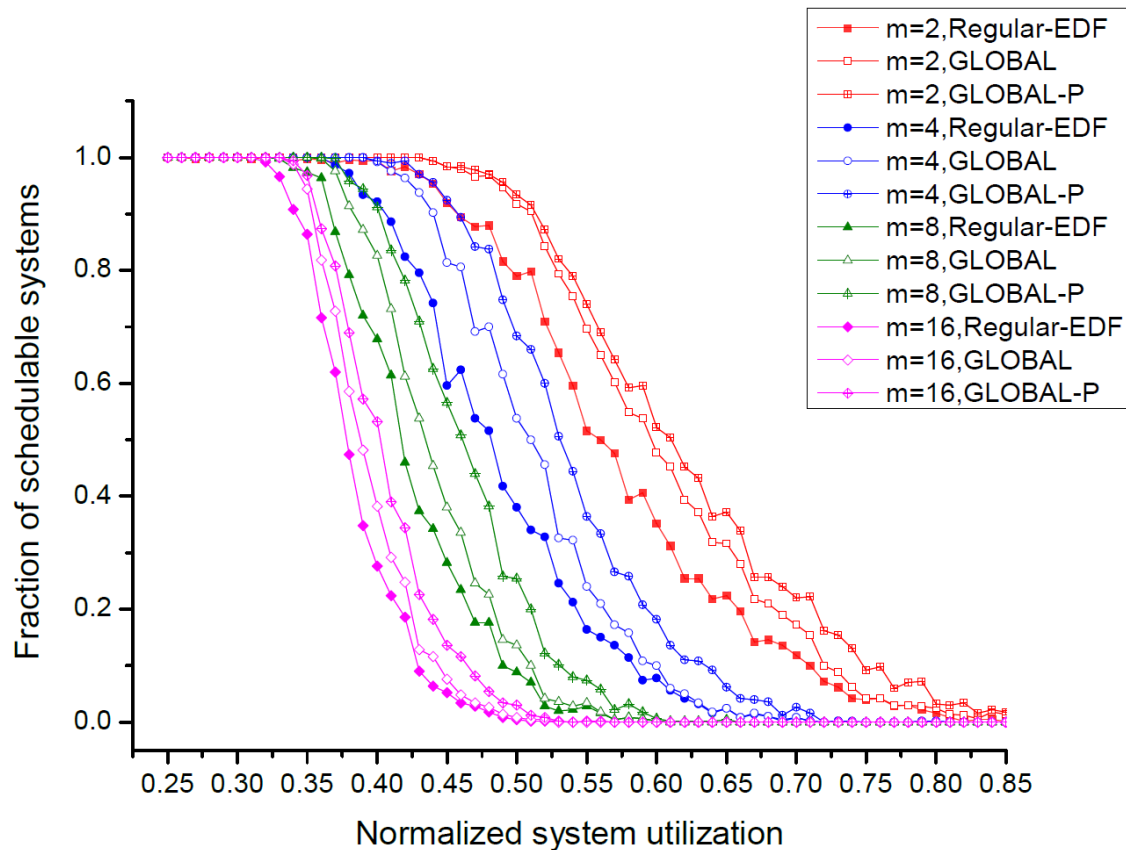


■ Experimental results





■ Experimental results





- **Global mixed-criticality scheduling**
 - Global-EDF with virtual deadlines
 - Schedulability test on two virtual systems
 - Selected virtual deadlines
 - Speed-up factor *3.236*, and experiments
- **Future work**
 - More criticality levels
 - Better scheduling strategies

Thank you



THE UNIVERSITY
of NORTH CAROLINA
at CHAPEL HILL