# COMP 633 Parallel Computing Fall 2021

http://www.cs.unc.edu/~prins/Classes/633/



## **Parallel computing**

- What is it?
  - multiple processors cooperating to solve a single problem
  - hopefully faster than using a single processor!
- Why is it needed?
  - greater compute performance

### Where is performance needed?

- sometimes performance is required in time-critical tasks
  - timely and accurate weather forecast
  - obstacle detection for self driving cars
- sometimes performance gives a competitive advantage
  - from Walmart to Wall Street
    - data mining of trends
    - delivery logistics
    - real-time analytics (high frequency trading)
  - engineering, manufacturing, and pharmaceuticals
    - vehicle crash simulations, material properties prediction, drug design
- sometimes performance is the only way to answer a question
  - scientific progress using mathematical modeling and numerical simulation
    - human genome assembly
    - computational science and the timely Nobel prize

## Why can't we just build a faster single processor ?

- Moore's "Law"
  - processor performance per \$ doubles every two years !



## **Transistor miniaturization and performance**

#### Dennard scaling

- transistor switching power  $\infty$  transistor size
- shrinking transistor size
  - decreases switching power
  - decreases switching time (higher clock frequency)
  - increases number of transistors per unit area
- so for the same power and space budget we get
  - faster arithmetic operations
  - pipelined arithmetic
  - more and larger caches
  - $\Rightarrow$  increased performance
- Limits to Dennard Scaling
  - as transistor size approaches quantum mechanical limits
    - increasing leakage current
    - exponential power increase!



#### Parallelism is now the principal source of performance

- Processor evolution after 2004 (Intel)
  - multiple cores per socket
  - lower per-core performance
  - similar power per chip
    - per-core "turbo" mode
  - vector units and larger caches
  - multiple and higher performance off-chip memory interfaces



processor performance characteristics

#### Moore's "law"

- performance per socket is still increasing but no longer exponentially
- power/cooling per socket is the limiting factor
- Factors limiting parallel computing
  - overall system power
  - inconveniently slow speed of signal propagation!

## Parallel computing at various scales



## **Top supercomputers (2020)**



#### Sunway TaihuLight

National Research Center for Parallel Computer Engineering and Technology in Wuxi, CN

| Rank | System   | Cores      | Rmax<br>(TFlop/s) | Rpeak<br>(TFlop/s) | Power<br>(kW) |
|------|--|------------|-------------------|--------------------|---------------|
| 1    | <b>Supercomputer Fugaku</b> - Supercomputer Fugaku, A64FX 48C<br>2.2GHz, Tofu interconnect D, Fujitsu<br>RIKEN Center for Computational Science<br>Japan                           | 7,299,072  | 415,530.0         | 513,854.7          | 28,335        |
| 2    | Summit - IBM Power System AC922, IBM POWER9 22C<br>3.07GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR<br>Infiniband, IBM<br>DOE/SC/Oak Ridge National Laboratory<br>United States | 2,414,592  | 148,600.0         | 200,794.9          | 10,096        |
| 4    | <b>Sunway TaihuLight</b> - Sunway MPP, Sunway SW26010 260C<br>1.45GHz, Sunway, NRCPC<br>National Supercomputing Center in Wuxi<br>China  | 10,649,600 | 93,014.6          | 125,435.9          | 15,371        |

## What are the parallel computing challenges?

- Parallel computing involves many aspect of computer science
  - new algorithms must be designed
  - new algorithm analysis techniques must be used
  - new programming models and languages must be learned
  - memory operation and performance must be understood
  - communication costs and network behavior must be considered
  - different operating systems, services, and I/O
  - different debugging and performance monitoring
  - novel and continuously changing hardware

- ...

## Summary: Why study parallel computing?

- It is useful and it is used
- It involves new algorithms and analytic techniques
- Future computing will increasingly be predicated on the use of parallelism
- To understand what is feasible and what is not

### How else is parallelism used?

- Parallelism may improve reliability
  - high availability
  - high assurance
- Parallelism may be inherent in the problem
  - (G)UIs
  - distributed systems
    - >80 processors in a modern luxury car
- Parallelism is a simple load scaling approach
  - server farms

#### ... but these are not the focus of this course!

## Parallel Computing vs. Distributed Computing

- Parallel Computing (COMP 633)
  - Multiple processors cooperating to solve a single problem
  - Key concepts
    - Design and analysis of scalable parallel algorithms
    - Programming models
    - Systems architecture and hardware characteristics
    - Performance analysis, prediction, and measurement
- Distributed Systems (COMP 734)
  - Providing reliable services to multiple users via a system consisting of multiple processors and a network
  - Key concepts
    - Services & protocols
    - Reliability
    - Security
    - Scalability

## Parallel Computing vs. Concurrent Algorithms

- Parallel Computing (COMP 633)
  - Multiple processors cooperating to solve a single problem
  - Key concepts
    - Design and analysis of scalable parallel algorithms
    - Programming models
    - Systems architecture and hardware characteristics
    - Performance analysis, prediction, and measurement
- Distributed and Concurrent Algorithms (COMP 735)
  - Specification of fundamental algorithms and proofs of their correctness and performance properties
    - Mutual exclusion
    - Readers and writers
  - Key concepts
    - Lower and upper bounds, impossibility proofs
    - Formal methods
    - Wait-free and lock-free methods

## **Course Introduction**

- Organization and content of this course
  - prerequisites
  - source materials
  - course grading
  - what will be studied
- Introductory examples

### **Organization of the course**

- Course web page
  - Syllabus
    - Prerequisites
    - Learning Objectives
    - Honor Code
    - Topics
  - Online discussion Piazza
  - Source materials reading assignments
  - Assignments and grading
  - Computer usage
- Reading assignment for next time
  - Parallel Random Access Machine (PRAM) model and algorithms
    - sections 1, 2, 3.1 (pp 1-8)
- Sign up for Piazza
  - using link on web page

## What will we study?

- Course is organized around different models of parallel computation
  - shared memory models [main focus]
    - PRAM
    - Loop-level parallelism, threads, tasks (OpenMP, Cilk)
    - Accelerators (Cuda)
  - distributed memory models [secondary focus]
    - bulk-synchronous processing (BSP, UPC), message passing (MPI)
  - data-intensive models [cursory treatment]
    - MapReduce/Hadoop, spark
- For each model we examine
  - algorithm design techniques
  - cost model and performance prediction
  - how to express programs
  - hardware and software support
  - performance analysis
  - advantages and limitations of the model including realism, applicability and tractability

#### by studying some examples in detail

# Let's try it right now!

• Vector summation

- given vector V[1..n] compute 
$$s = \sum_{i=1}^{n} V_i$$
  
e.g. for n = 8  
 $s = V_1 + V_2 + ... + V_7 + V_8$ 

- sequential algorithm
  - n-1 additions: optimal
    - e.g. sum from left to right
  - sequential running time
    - T(n) = O(n)

## Example 1: DAG model of parallel computation



# **Execution of a DAG "program"**

- definition
  - an operation is ready if all of its children are leaves
- parallel execution step
  - simultaneously evaluate all ready operations and replace each with its value
- program execution
  - perform parallel execution steps until no operations remain



# **Complexity metrics for DAG model**

- Work complexity of a DAG program
  - total number of operations performed
    - = # interior vertices in DAG
- Step complexity of a DAG program
  - number of execution steps
    - = length of longest path in DAG

|        | work | steps |
|--------|------|-------|
| Prog 1 | 7    | 7     |
| Prog 2 | 7    | 3     |



20

 $V_1$ 

## Asymptotic complexity metrics for DAG model

#### • Asymptotic complexity

- problem size n
- W(n) asymptotic work complexity
- S(n) asymptotic step complexity
- T\*(n) optimal asymptotic sequential time complexity
- Definition
  - A DAG program is work efficient if  $W(n) = O(T^*(n))$



## Asymptotic complexity metrics for DAG model

#### • Asymptotic complexity

- problem size n
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#### • Definition

- A DAG program is work efficient if  $W(n) = O(T^*(n))$ 



## Execution of DAG programs with fixed resources

- At most p operations evaluated simultaneously in a DAG program H
  - models execution using p "processors"
- Definition
  - $-T_p(n)$  is the time to execute H using p processors
    - n problem size
    - p maximum number of nodes that may be evaluated concurrently in each timestep
  - $T_1(n) = W(n)$
  - $T_{\infty}(n) = S(n)$

But what is  $T_2(8)$  for prog 2?



### **Evaluation order**

- Determining evaluation order to minimize  $T_p(n)$  is NP-hard!
- Simple non-optimal greedy evaluation order
  - at each step
    - p or fewer operations ready  $\Rightarrow$  evaluate all ready nodes
- more than p operations ready  $\Rightarrow$  evaluate any p ready nodes
- Running time using greedy strategy can be bounded



## "fast" parallel programs give good speedup

- Definition
  - a *fast* parallel program has step complexity S(n) that is asymptotically smaller than work complexity W(n)

$$S(n) = o(W(n))$$
 means  $\lim_{n \to \infty} \frac{S(n)}{W(n)} = 0$ 

 For a fixed number of processors p, a fast parallel program gives better speedup as problem size n is increased

$$\left\lceil \frac{W(n)}{p} \right\rceil \le T_p(n) \le \left\lfloor \frac{W(n)}{p} \right\rfloor + S(n)$$
$$\lim_{n \to \infty} T_p(n) = O\left(\frac{W(n)}{p}\right)$$

- asymptotically *optimal speedup* on large problems!

## But can't speedup indefinitely

- You can't speed up a parallel algorithm indefinitely using more processors
  - for a fixed problem size n, step complexity limits speedup

$$T_p(n) = O\left(\left\lfloor \frac{W(n)}{p} \right\rfloor + S(n)\right)$$

- prog 1 cannot be sped up at all using more processors!
  - $W(n) = \Theta(n)$
  - $S(n) = \Theta(n)$
- prog 2 requires  $\Omega(\lg n)$  steps regardless of the number of processors
  - $W(n) = \Theta(n)$
  - $S(n) = \Theta(\lg n)$

## **Consequences: work efficiency is paramount**

- A parallel program H that is *not* work efficient loses asymptotically!
  - for any given p, there exists a problem size  $n_0$  such that
    - an efficient sequential program using one processor on problems of size n > n<sub>0</sub> is faster than the parallel program H using p processors!
  - it doesn't help if H is fast
  - worst results on large problems!

$$T_p(n) = O\left(\left\lfloor \frac{W(n)}{p} \right\rfloor + S(n)\right)$$

## Example 2: Message-passing model

- p processors connected in a ring
  - each processor
    - runs the same program
    - has a unique processor id  $0 \le i < p$
    - can send a value to its left neighbor
- summation of V[0..p-1] using p processors
  - assume  $V_i$  is in s on processor i at start
  - program terminates with  $s = \sum_{j \in 0..p-1} V_j$  on processor 0



#### **Summation program**

for h := 1 to (lg p)
x := s
for j := 1 to 2<sup>h-1</sup> do
 send value of x to left and receive new value for x from right
s := s + x



### Analysis of summation program

```
for h := 1 to (lg p)
x := s
for j := 1 to 2<sup>h-1</sup> do
    send value of x to left and receive new value for x from right
s := s + x
```

#### • Let

- t<sub>a</sub> time to perform addition
- t<sub>c</sub> time to perform communication

$$T_{p}(n) = \sum_{h=1}^{\lg p} (t_{a} + 2^{h-1}t_{c})$$
$$= (\lg p) \cdot t_{a} + (p-1) \cdot t_{c}$$

• Is this good performance?

### What's wrong?

- poor network?
  - network *diameter* is large thus values have to travel far
  - so communication time is huge compared to addition time
  - a smaller diameter network might do better
- bad communication strategy?
  - "cut-through" routing would be superior
- poor utilization of the processors?
  - only a few processors are performing useful additions!
- problem size too small?
  - this is the real problem!

#### Summation of n values with p processors

#### • Each processor holds n/p values





## Summation of n values using p processors

• Analysis

- excellent performance can be achieved
  - for arbitrary p,  $t_a$ ,  $t_c$
  - asymptotically optimal speedup with sufficiently large n
    - overheads and inefficiencies can be amortized!

#### For next week Tuesday

- read the PRAM handout
  - secns 1,2, 3.1 (pp 1-8)