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PID: $\qquad$
COMP 410 Spring 2019

## Midterm Exam

This exam is closed book, notes, calculators, cell phones, classmates, smart watches, everything but your own brain. You have 75 minutes to complete the exam. Do all your work on these exam pages. Please sign here (and print your name up top of each page) pledging that the work you submit is your own:

Signature: $\qquad$

Q1 (4\%): Consider a node M in a minimum binary heap; M is stored in the heap array at index 73.
a) At what array index will we find the parent of node M ?
answer: $\qquad$
b) At what array index will we find the right child of node M ?
answer: $\qquad$
Q2 (2\%): What is the maximum number of nodes that might be in a complete binary tree with height K , if we also have that the tree is not a full binary tree:
a) $2^{\wedge}(\mathrm{K}+2)-1$
b) $2^{*}(K+1)$
c) $2^{\wedge} \mathrm{K}-1$
d) $2^{\wedge}(K+1)$
e) $2^{\wedge}(K+1)-2$
answer: $\qquad$

For Q3 through Q9, fill in the table cells with the best (tightest, closest) Big Oh time complexities. If you think an answer is " $O(M \log k$ )" (for example), you may just write "M $\log k$ ", leave off $O(\ldots)$.

Q3 (3\%) Fill in the table with worst-case time complexity for list (array implementation) of $N$ items

| operation | add at $i$ | remove at $i$ | get ith |
| :---: | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q4 (3\%) Fill in the table with worst-case time complexity for stack (array implementation) of N items

| operation | push | pop | top |
| :---: | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q5 (3\%) Fill in with worst-case time complexity for binary search tree of N items (vanilla BST, not being balanced)

| operation | add | delete | contains |
| :---: | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q6 (3\%) Fill in with average-case time complexity for binary search tree of $N$ items (vanilla BST, not being balanced)

| operation | add | delete | contains |
| :---: | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q7 (3\%) Fill in the table with worst-case time complexity for queue (doubly linked cells) of N items

| operation | enque | deque | front |
| :--- | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q8 (3\%) Fill in the table with average-case time complexity for min binary heap of N items

| operation | add | getMin | delMin |
| :--- | :--- | :--- | :--- |
| Big Oh | a) | b) | c) |

Q9 (8\%) Fill in this table comparing sort methods for $N$ items. Use theoretical Big Oh notation

| Time complexity | Worst case | Average case |
| :--- | :--- | :--- |
| bubble sort (on an array) <br> N items |  |  |
| sort N items with a <br> minimum binary heap | a) | b) |
| BST sort N items (vanilla |  |  |
| BST, not being balanced) | e) | d) |
| put N items into linked <br> list, keep it sorted each <br> insert (inSort operation) | g) | f) |

## Name (print):

Q10 (12\%) True or False ( T / F ):
a) $\qquad$ If $P$ has worst case time complexity $O(\log N)$ then $P$ also has worst case time $O(N)$
b) $\qquad$ Making a binary heap of $N$ items by calling the insert operation $N$ times is never as efficient as using the "magic" build operation
c) $\qquad$ Garbage collection in Java makes it impossible to run out of run-time stack space during execution.
d) $\qquad$ The run-time stack is dynamic memory from which objects are allocated on calls to "new"
e) $\qquad$ The principle of time/space trade off says that if a program runs efficiently in time then it must use storage (space) inefficiently
f) ___ Any program that uses recursion can be rewritten to use no recursion and still produce the same results
g) $\qquad$ Items put into a priority queue will never come out in LIFO order
h) $\qquad$ Pre-order traversal on the tree that represents a minimum binary heap always produces the elements in increasing priority sequence
i) $\qquad$ Array representation for a general binary tree is always fast to use, and space efficient
j) $\qquad$ For any set of unique data elements, if we insert these elements into an empty BST in different orders, we can get different final BST structures
k) $\qquad$ An N -ary tree is a tree with every node (except leaves) having exactly N children.
I) $\qquad$ In practical terms, it is possible for a recursive function to fail to produce results, when an iterative version of that function will succeed in producing correct results

Q11 (3\%): Consider this code fragment for function bubb:

```
public static long bubb(int N) {
answer:
    int[] arr = new int[N];
    for (int n=0; n<N; n++) { arr[n]=genRandInt(); }
    for (int i=0; i<N; i++) {
        for (int k=0; k<i*i; k++) { bubblesort( arr ); }
}
```

$\qquad$

If we limit N to being a positive integer (not 0 ), and assume bubblesort has worst case complexity each time it runs, what is a good "Big Oh" complexity for the worst case execution time of function bubb ?

Q12 (3\%): Consider this code fragment for function mash:

```
public static long mash(int N) {
    int x = 2;
    for (int i=N; i>0; i--) {
        for (int j=i; j<i+3; j++) {
            for (int k=0; k<i; k++) {x *= i + j*k;} } }
}
```

If we limit N to being a positive integer (not 0 ), what is a good "Big Oh" complexity for the worst case execution time of function mash?

## Name (print):

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Q13 (8\%) Consider this 3-ary tree


Here are your answer choices:

1) mark harm goal joy pen boat age zoo wind team tarheel sim
2) goal harm joy pen mark boat zoo age wind team sim tarheel
3) mark harm boat team tarheel sim zoo pen goal joy age wind
4) goal pen joy harm zoo age wind boat sim tarheel team mark
5) mark harm boat team goal joy age wind tarheel pen zoo sim
6) none of the above
a) which sequence is a breadth-first traversal?
b) which sequence is a pre-order traversal?
c) which sequence is an in-order traversal? $\qquad$
d) which sequence is a post-order traversal?

Q14 (3\%): Consider this code fragment for function magic:

```
public static long magic(int N) {
if (N <= 1) return 2;
return magic(N-1) * magic(N-1);
}
```

answer:
$\qquad$

If we limit N to being a positive integer (not 0 ), what is a good "Big Oh" complexity for the worst case execution time of function magic ?

Q15 (3\%) Consider the program code to the right:
Which of these is most accurate when "main" is run?
a) the amount of run-time stack space that might be needed is finite
b) the amount of run-time stack space that might be needed is finite, but unbounded
c) the amount of run-time stack space that might be needed is infinite
answer: $\qquad$


```
function main ( ) {
```

function main ( ) {
var x = getUserInput();
var x = getUserInput();
var result = foo(x);
var result = foo(x);
alert(result);
alert(result);
}
}
function foo ( n ) {
function foo ( n ) {
if (n<=1) return 1;
if (n<=1) return 1;
return n * foo(n-1);
return n * foo(n-1);
}

```
}
```

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Q16 (3\%) Consider the program code to the right:
Which of these is most accurate when "main" is run?
a) the amount of run-time stack space that might be needed is finite
b) the amount of run-time stack space that might be needed is finite, but unbounded
c) the amount of run-time stack space that might be needed is infinite
answer: $\qquad$

```
function main ( ) {
    var x = 7683910024;
    var result = foo(x);
    alert(result);
}
function foo ( n ) {
    if (n==1) return 1;
    return n * foo(n-2);
}
```

Q17 (3\%) Consider the data structure represented at right
a) $(T / F)$ $\qquad$ This could be a binary heap
b) $(T / F)$ $\qquad$ This could be a BST (not being balanced)
c) $(T / F)$ $\qquad$ This could be a doubly linked list


Q18 (4\%) Consider the data structure/sequence represented at right
a) $(T / F)$ $\qquad$ This could be a queue
b) $(T / F)$ $\qquad$ This could be a stack
c) $(T / F)$ $\qquad$ This could be a priority queue (done as list)
d) $(T / F)$ $\qquad$ This could be a BST (not being balanced)


Q19 (5\%): Binary Search Tree (not being balanced)
Starting with an initially empty Binary Search Tree (vanilla, not being balanced), show the tree that results after inserting the following string values in the order given left to right:
input, cpu, port, disk, usb, ram, net, keys, audio, screen
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Q20 (5\%) Consider the heap H shown to the right:
Show (in box below) the heap that results after a delMin( ) operation


Q21 (5\%) Consider the heap H shown above right (in previous question):
Show (in the box below) the heap that results after add(5) followed by add(2)


## Name (print):

Q22 (3\%): Lets add an operation to STACK. The operation is max, and it will return the largest element stored in the stack. If we implement a STACK with an array, which of the following expressions gives the most accurate description of the worst case time complexity of the max operation?
a) $\mathrm{O}(1)$
b) $\mathrm{O}(\mathrm{N})$
answer: $\qquad$
c) $\mathrm{O}(2 \mathrm{~N})$
d) $\mathrm{O}\left(\mathrm{N}^{\wedge} 2\right)$
e) $O\left(2^{\wedge} N\right)$

Q23 (3\%): Consider this way to sort. You are given $N$ integers in an array, the data source array. You are also told that the integer values will be in the range 0 to K inclusive, that there are no duplicate values, and that $\mathrm{N}<\mathrm{K}$. To sort them smallest to largest, you build another array of boolean with subscripts 0 to K.. You set every element in the boolean array to false. You go through the data source array and for each element you use the integer value stored as a subscript into the boolean array and mark that slot true. Finally, to get the sorted sequence, you go through the boolean array from subscript 0 up and print the subscript for every element that contains true

Which of the following expressions is the best description of the worst case time complexity for this sort :
a) $\mathrm{O}(2 \mathrm{~N})$
b) $\mathrm{O}\left(\mathrm{N}^{\wedge} 2\right)$
answer: $\qquad$
c) $\mathrm{O}\left(\mathrm{N}^{*} \mathrm{~K}\right)$
d) $\mathrm{O}(\mathrm{N}+\mathrm{K})$
e) $\mathrm{O}\left(\mathrm{N}^{\wedge} 2+\mathrm{K}\right)$
f) $\mathrm{O}\left(\mathrm{N}+\mathrm{K}+\left(\mathrm{N}^{\wedge} 2\right) / \mathrm{K}\right)$

Q24 (5\%): Consider the BST B (basic, not balanced) below. Show its structure after "delete ( 18 )" is complete. Show your final tree in the box:


