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Scalable Algorithms For Interactive Visualization Of Curved Surfaces*

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Technical Paper

Abstract

We present efficient parallel algorithms for interactive display of higher order surfaces on current graphics systems. At each frame, these algorithms approximate the surface by polygons and rasterize them over the graphics pipeline. The time for polygon generation for each surface primitive varies between successive frames and we address issues in distributing the load across processors for different environments. This includes algorithms to statically distribute the primitives to reduce dynamic load imbalance as well a **distributed wait-free** algorithm for machines on which re-distribution is efficient, e.g. shared memory machine. These algorithms have been implemented on different graphics systems and applied to interactive display of trimmed spline models. In practice, we are able to obtain almost linear speed-ups (as a function of number of processors). Moreover, the distributed wait-free algorithm is faster by 25 – 30% as compared to static and dynamic schemes.

Keywords: Surface tessellation, Load balancing, Real-time rendering, Simulation-based Design, Splines.

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1 Introduction

Higher order surfaces are commonly used to represent models for computer graphics, geometric modeling and CAD/CAM. These include rational spline surfaces, algebraic surfaces and generalized implicit models. In particular, rational spline surfaces are typically used to represent solids in engineering design. Splines also find application in modeling body parts for medical imaging and molecules for drug design. Large scale models consisting of tens of thousands of such surfaces are commonly used to represent shapes of automobiles, submarines, airplanes, building architectures, sculptured models, mechanical parts and in applications involving surface fitting over scattered data or surface reconstruction. Many applications like interactive walkthroughs and design validation, need to interactively visualize these surface models [11], which means we must render it at more than 15 frames a second. Current renderers of sculptured models on commercial graphics systems, while faster than ever before, are not able to render them in real time for applications involving virtual worlds, walkthroughs and other immersive technologies.

A number of techniques including polygonization, ray-tracing, scan-line conversion and pixel-level subdivision have been proposed for rendering splines. However, in practice, only the algorithms based on polygonization [13] are able to achieve close to interactive display on common graphics systems. At each frame, these algorithms approximate the surface using triangles and render those triangles using the graphics pipeline. A typical graphics pipeline is shown in Fig. 1. Most graphics vendors package all this functionality into a single unit, with access only at the front end. In addition to this unit, graphics systems also include extra general purpose host CPUs, that can input triangles to this unit.

Since we are interested in surface display, our focus is on efficiently utilizing the extra processing power for tessellating the surfaces into triangles. Systems that generate off-line triangular approximation of surfaces need to generate a large number of triangles to ensure good image quality. Although high-end graphics systems can now render millions of polygons per second [5, 3], this is nearly not enough for interactive display of large surface model. To ensure that the graphics unit is not bottlenecked up with too many triangles, ideally we would like to generate the triangles that are likely to be important on screen [13]. This implies, the set of triangles used to approximate a surface in different frames can be quite different. Thus the cost of tessellating a surface varies dynamically.

In this paper, we mainly deal with one class of surfaces: trimmed spline surfaces, and demonstrate our algorithm on the model of a notional submarine storage and handling system shown in Fig. 2. (It has 38,000 trimmed Bézier surfaces, a class of trimmed spline surfaces). The general algorithm, though, is applicable to all objects with dynamically varying load.

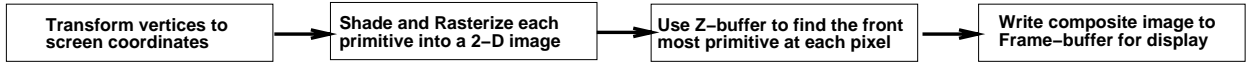


Figure 1: Graphics Pipeline

Recently, a number of polygonization based trimmed spline renderers have been proposed in the literature [1, 2, 19, 15, 13, 10]. These algorithms use the host CPUs to approximate the surfaces with polygons, and employ standard graphics hardware to render these polygons.

Figure 2: Submarine Storage and Handling System

As we deal with large models composed of tens of thousands of surfaces, current single CPU graphics systems are not fast enough to polygonize large models at interactive frame rates. As a result, interactive algorithms for rendering utilize multi-processor configurations. The algorithms for tessellating spline surfaces are relatively simple to parallelize. However, the distribution of surfaces along different processors is important for the overall performance. The time to polygonize each surface varies as a function of the user’s viewing position. Furthermore, for many of these spline rendering algorithms, polygon generation is often a bottleneck on systems with high end graphics engines. This means the triangle pipeline is often idle.

In this paper, we present static and dynamic load balancing algorithms for interactive display of large models defined using higher order surfaces. The **main contributions** are:

1. **Balancing static and dynamic load:** We present a static allocation scheme for distributing the model across multiple processors and reduce dynamic load imbalance. The resulting algorithm takes into account, visibility computations (like view-frustum culling) and highly varying transformations. It works well on graphics systems, where re-distributing primitives between processors can be prohibitively slow. It also exploits frame-to-frame coherence. In particular, it is based on the observation that such load exhibits spatial coherence. Primitives on same part of the screen tend to have similar statistical load. We also extend it to configurations, where re-allocation is efficient, e.g. shared memory machines. We present a **scalable, wait-free** algorithm to re-distribute primitives, whenever the load becomes imbalanced. This algorithm is **distributed**, in the sense that there exists no ‘master’ processor spending resources on load-balancing. Further, the overhead of performing load balancing is small.

2. **Greedy rendering:** We present a greedy rendering technique to update the scene as a function of viewpoint. The resulting algorithm lowers the system latency for rendering higher order surfaces and is very important for head-mounted displays and walkthrough applications, where a lagging image can induce motion-sickness. The resulting algorithm uses the concept of greedy rendering, which is akin to progressive refinement to improve the quality of the image whenever the user stops moving.

The resulting algorithms have been implemented on different graphics systems and have been applied to a number of models. On an SGI-Onyx (RE2) with 4 host CPUs, our overall algorithm can render large models at 50 – 100 times better frame rates than the micro-coded implementation of the SGI-GL library that uses the graphics unit to polygonize the surfaces and render the resulting polygons. Much of it is due to greedy rendering that tries to keep up with the user movement by rendering what it can. Having quoted this bottom-line figure, it is important to clarify that, algorithmically, we are, in fact, comparing apples to oranges. Due to their micro-coded implementation, GL routines are not able to make much use of multiple CPUs. In addition, they do not store triangles, but rather generate them for each frame. Also, our tessellation algorithm itself is more efficient than the one used by GL [13]. In practice, our parallelization technique is able to obtain close to 85% of the ideal speed-up. Our static load-allocation scheme improves the average frame rate by about 10% as compared to a round robin allocation scheme. The distributed load management algorithm improves the speed-ups to 25 – 30% on shared-memory graphics systems. We include tables and graphs later in the paper that demonstrate our speed-ups on some specific models.

1.1 Related Work

Load-imbalance is an old and well studied problem in parallel and distributed computing. [6] offers an excellent survey on load-balancing techniques. If the load is known à priori, it can be optimally allocated to processors in an off-line process, spending little time at run-time to manage load. For dynamic loads, a much more dynamic algorithm is warranted. In the graphics literature a number of algorithms have been proposed for polygonal models and for parallel ray-tracing. In [18, 20, 16] algorithms dividing the primitives in terms of screen-regions are presented. Moreover, [17, 4, 22] balance the load in object space. However, these techniques cannot be applied to rendering of higher-order surfaces, as the rendering-cost of a spline surface varies significantly across frames. For dynamic load-balancing, in the presence of shared-memory, distributed computing literature presents a number of algorithms to arbitrate shared accesses with consistency [14, 21, 8]. Indeed, for each sequential data structure there exists a shared implementation that requires no locks [8]. For example, [8] present a hierarchy of shared objects, with wait-free accesses. However, the objects presented in these papers are more general and do not result in significant performance improvement. Moreover, many of these implementations rely on the existence of atomic ‘test and set’ like instructions, which may not be available on all graphics systems.

The rest of the paper is organized in the following manner. We briefly review the algorithm for spline tessellation in Section 2. The static load-balancing technique is presented in Section 3. In Section 4 we present the load re-distribution algorithm. We consider the

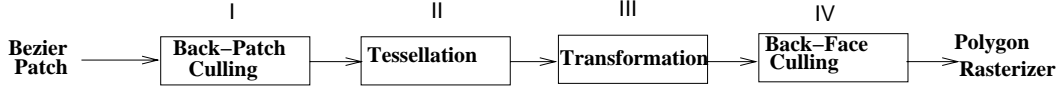


Figure 3: Spline rendering Pipeline

problem of real-time display and present the greedy rendering algorithm in Section 5. We discuss its implementation and performance in Section 6.

2 Spline Rendering

The spline surfaces are rendered based on the algorithm presented in [12]. Given a trimmed spline model, the algorithm represent them as trimmed Bézier surfaces using knot-insertion algorithm. At run-time it tessellates each surface into an appropriate number of triangles at each frame (see Fig. 3). Although the actual method of this tessellation is not the subject of this paper, a brief introduction is in order. A Bézier surface \mathbf{F} of degree $m \times n$ defined by parameters $u, v \in [0, 1]$, is specified by a mesh of control points $C_{ij}, 0 \leq i \leq m, 0 \leq j \leq n$:

$$\mathbf{F}(u, v) = \sum_{i=0}^m \sum_{j=0}^n C_{ij} B_i^m(u) B_j^n(v)$$

where the Bernstein polynomial B is given by

$$B_i^n(t) = \binom{n}{i} t^i (1-t)^{n-i}$$

In addition, trimmed spline surfaces have two dimensional closed curves defined on the domain. Only those points of the domain that are enclosed by these curves map to the final surface.

A brief overview of the tessellation algorithm [12] is given below.

1. Perform view-frustum and back-facing surface visibility to eliminate hidden surface. We compute a bounding box around each Bézier surface. If the bounding box does not lie on the screen, the surface is not tessellated. Similarly, we use a bound on the normals to determine if all the normals face away from the user. For solid models, all such back-facing surfaces can be culled away. These techniques help us to quickly reduce the number of surface that need to be tessellated.
2. For each frame, given the viewing matrix, compute the required tessellation step sizes n_{u_p}, n_{v_p} for each surface p , and n_{t_c} for each trimming curve c . These numbers are computed such that the resulting tessellation satisfies the user's quality constraints on the size of resulting triangles, or their deviation from the actual surface.
3. Tessellate each surface p into quads, choosing tessellants $\frac{1}{n_{u_p}}$ and $\frac{1}{n_{v_p}}$ apart along the u and v parametric axes respectively. Similarly, tessellate trimming curve c into n_{t_p} piecewise linear segments.

4. Trace the segments of the trimming curves on the quad to compute all intersections. Generate triangles for the surface by triangulating the polygons generated by intersection of the quads and the trimming curves. For each quad un-trimmed by the curve, use the diagonal to triangulate it.

Any triangulation-based surface rendering algorithm first needs to allocate resources to generate these triangles. The desirable tessellation is computed and the vertices and normals are evaluated. The total time is, therefore a function of the number of triangles generated. The performance of triangle rendering is system dependent and typically a function of the number of triangles and the size and distribution of these triangles on the screen.

It is possible to compute a very fine triangulation à priori and to render all the triangles for each frame. In this case, almost no time is spent in triangle generation and all of the time is spent on rendering. However the number of triangles needed for close-up (zoomed) views of some surfaces can be extremely high (a few thousand) and for models consisting of thousands of surfaces, this requires hundreds of megabytes of storage, and the capability to render hundreds of millions of triangles per second. We can reduce the demand on triangles rendering capability by computing different levels of detail of each surface and at each phase choosing one of the approximations as a function of the viewing parameters. But the memory requirements only get worse.

On the other hand, we can compute, on-line, the minimum number of triangles required for a smooth image as a function of the viewing parameters (for each frame). The resulting algorithm is based on adaptive subdivision and takes considerable time in the triangle generation for each frame. As a result, it can be too slow for interactive performance on large-scale models.

3 Static Load Balancing

When the user zooms in to a small part of the model, that part occupies a significant part of the screen, and hence a significant part of the total tessellation cost. If that part of the cost is not fairly distributed between processors, some of them become bottlenecks. If we randomly distribute primitives, say in a round robin manner, to processors, load imbalances of more than 1:50 are not uncommon.

A number of load balancing algorithms reduce the problem to graph partitioning [7, 9]. All these algorithms assume the existence of a load-graph. To construct such a graph, we must first know the processing cost of each primitive. However, the rendering cost of a spline primitive is a function of parameters such as:

- the degree of surface
- the complexity of the trimming curves
- the screen size of the primitive

Though, the dependence of this cost on the viewing parameters makes it difficult to find an assignment which is optimal in all frames, primitives on same part of the screen tend to

have similar load. This observation of spatial coherence suggests the distribution of ‘nearby’ primitives to different processors.

To model our problem as a graph partitioning problem, each primitive is represented by a vertex of the graph. The vertices and edges are assigned weights so that sub-graph weights estimate rendering cost well. Initially, a complete graph with n vertices is constructed where n is the number of primitives. The weights are assigned as follows:

- **Vertex weight:** the sum of the estimated rendering cost of the surfaces in the primitive. This is a function of surface degrees, and the degrees of the trimming curves.
- **Edge weight:** the inverse of the geometric distance between the primitives of two vertices it connects.
- **Subgraph cost function:** For each edge, we calculate $W_e(W_{v1} + W_{v2})$, where W_e is the edge weight and W_{v1} , W_{v2} are the vertex weight of the vertices the edge connects. The cost function is the sum of the above function for every edge in the subgraph.

Our goal is to partition the graph into p disjoint subgraphs of almost equal weight, where p is the number of processors and the cost function in each subgraph is minimized.

Approximation algorithms such as simulated annealing has also been used for optimization. We use the heuristic that if two nearby primitives are in the same processors, the cost function of the subgraph for that processor is increased because the weight of the edge connecting them is high. The optimization algorithm moves one of these to a different processors with a high probability. In practice, this algorithm results in about 10% speedup as compared to round-robin distribution. Details on the implementation and performance of this algorithm are presented in Section 6.

4 Primitive Re-distribution

As mentioned earlier, in any given frame the processor load may not be balanced. This means that some processors may finish the tessellation of their work-load and become **idle** while others are still **busy** tessellating surfaces. This work-load is dynamic, in the sense that the cost to render the same set of surfaces changes with time. It is precisely due to this reason that a static primitive distribution cannot achieve satisfactory speedup. For systems with efficient inter-processor communication, primitive re-distribution results in much more balanced load, and with little overhead.

In this section we present two simple re-distribution algorithms. The first algorithm maintains a global queue of surfaces, arbitrating access to the queue using *locks*. The second algorithm improves this scheme by eliminating processor waits. Furthermore, it scales better as the number of available processors increases.

4.1 Global Queue (with locking)

Each element of the queue (Fig. 4) corresponds to N_p surfaces. Each processor deletes the element in the front of the queue and computes the tessellation for the corresponding

surfaces and renders the triangles. This step is repeated until the queue becomes empty. The granularity N_p of a queue element affects the processor utilization. In our experience, N_p should be a small fraction of N , the total number of surfaces to be rendered. Since, a 1 : 100 load imbalance can sometimes occur for static schemes, we use a value of $\frac{N}{100P}$, where P is the number of processors.

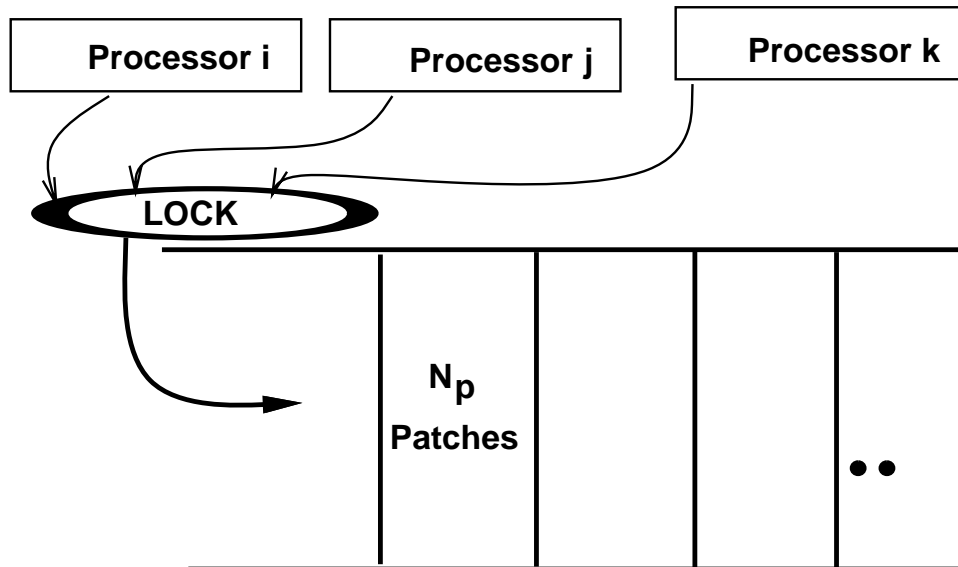


Figure 4: Global Queue, with locking as a potential bottleneck

A problem with this method is the fixed choice of granularity. Different values of N_p are required to achieve optimal speed-up for different environments and models. In addition, although, this algorithm performs better than the static distribution algorithm, the overhead of lock-maintenance and mutual-exclusion prevents us from making full use of dynamic load-balancing. Next, we propose an algorithm that reduces this overhead (based on **load stealing**). At each frame, each processor starts with an approximate work-load. As processors get idle, they steal surfaces from busy processors, computing the tessellation of those additional surfaces.

4.2 Load Stealing

Each processor p maintains its current work-load in a global structure labeled as *ActivityList*[p]. It is the list of surfaces, that are allocated to p for the current frame. At the beginning of simulation, this allocation is same as the static allocation presented in Section 3. At each frame, each processor runs its tessellation loop and updates its allocation.

4.2.1 Tessellation Loop

Due to temporal coherence, the rendering cost of a primitive does not vary significantly between successive frames. Hence the *ActivityList* for a processor at the previous frame is a good starting guess for a balanced *ActivityList* for the current frame. The basic idea of our

algorithm is to allow no additional overhead for busy processors. All the extra computation is done by the idle processors. Here is the basic tessellation loop:¹

```

While ( Next = Front of ActivityList is not End of list ){           :1
    Update Front;                                                    :2
    tessellate (SURFACE Next)                                         :3
    update triangles for Next                                         :4
}                                                                        :5
Find a busy processor  $p_b$ , Share its load.                            :6

```

In this algorithm, possible concurrent access to shared variables occur at line 6. The first contention at line 6 is between idle processors. Multiple processors may ‘find’ the same p_b . To reduce such contention, each processor maintains a list of other processors in a random order, and checks processors’ *ActivityLists* in that order. Of course, this does not guarantee mutual exclusion. This access is arbitrated by locks. Each processor has a lock, *LockList*, associated with it. Before an idle processor p_i checks the *ActivityList* of p_b ($i \neq b$), it secures a **non-blocking lock** on *LockList*[p_b]. Non-blocking lock ensures that if p_i cannot acquire *LockList*[p_b], there must exist another idle processor p_j currently sharing *ActivityList*[p_b]. A processor p_i , when idle, executes the following loop until all tessellators become idle:

```

for  $p_b$  in RandomList {                                             :61
    lock LockList[ $p_b$ ]                                             :62
    if lock not acquired, go on to next in RandomList                :63
    if (Front of ActivityList[ $p_b$ ] is not End of list)             :64
        Share load with processor  $p_b$                                :65
    unlock LockList[ $p_b$ ]                                           :66
    Perform Tessellation loop                                         :67
}                                                                        :68

```

4.2.2 Lock-free implementation

Once the idle processor used for sharing a busy processor’s load is fixed, the only possible concurrent shared variable access can occur at line 65. This contention is between the idle processor p_i and the selected busy processor p_b . Since it involves a busy processor, exclusion by locking is not an option, since we seek to introduce no overhead at the busy processors. That contention is resolved by letting the p_i update the *ActivityList* of p_b , asynchronously. It is possible that p_b reads the old *ActivityList*, and tessellates some surfaces that are taken off its *ActivityList* by p_i . This case is handled by letting p_i re-read the current position of p_b after updating its *ActivityList*, and not tessellate any surface of new *ActivityList*[p_i], that p_b may already have tessellated. The resulting algorithm is:

```

Delete the second half of unprocessed ActivityList[ $p_b$ ]           :651
Add it to ActivityList[ $p_i$ ]                                       :652
Read new Front[ $p_b$ ] ( $p_b$ ’s copy)                                  :653
Mark the Tessellation loop to start after new Front.                :654

```

¹To simplify the notation, we don’t index variables by the processor id, when it is clear from context.

There still exists a race condition, in that p_b could have read its *Front* (line 1) just before p_i updates its *ActivityList* (at line 651), and not yet written the new *Front* (line 2) when p_i reads it back (at line 653). If the cost of tessellating each primitive is not high, we can let the two processors duplicate the effort of tessellating one primitive, when this race condition occurs, since it is quite rare. Note that line 653 appears after line 652 by design, since it reduces the probability of race condition, assuming all processors are equally fast. However, the race condition can be eliminated using the following modification.

Busy processors write an additional binary shared variable, *ListTransient*. Each busy processor p sets its *ListTransient* to 1 before reading its *ActivityList*, and resets it to 0 after having updated its *Front*. Now, we let the idle processor busy-wait² for *ListTransient*[p_b] to be 0 before reading the new *Front* of p_b .

In practice, *ActivityList* is not implemented as a list of surface ids but as a list of id ranges. By design, the algorithm tends to keep adjacent surfaces on same processor. This means, a processor's work load does not consist of just a random list of surfaces, but, rather, a number of contiguously stored groups of surfaces.

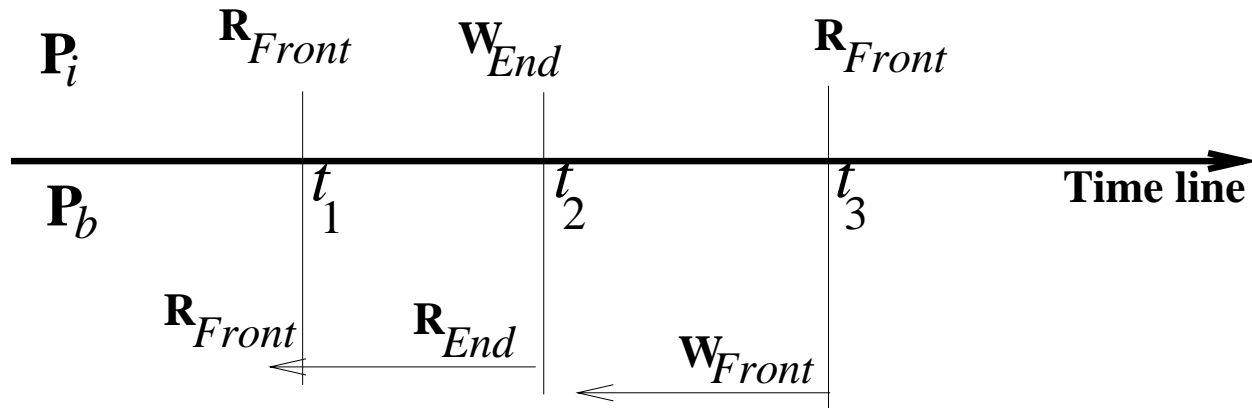


Figure 5: Timeline showing consistent behavior

The load-stealing algorithm must guarantee the following:

- (a) For a given frame, each element of the queue is read at least once.

In addition, for efficiency, we require that

- (b) each element is read exactly once.

It is easy to see that (a) is true, since at every instant an element lies in at least one of the queues of p_b and p_i . It is possible, though, that some elements lie in multiple queues for a time-interval. To see that (b) still holds, consider the time line shown in Fig. 5.

Suppose the idle processor, p_i , updates the queue of the busy processor, p_b , at time instant³ t_2 . At t_2 , p_b may have read element in p_i 's share, since it continues processing asynchronously. But the next time p_i checks its queue, it must read the new queue, and

²For multiple processors, busy-waiting is the right solution, because it does not induce context-switch.

³Individual memory reads and writes happen atomically.

stop. Thus the last element of p_i 's share that p_b reads must be read before t_2 . This implies that the *ListTransient* flag is set at t_2 . p_b reads the position of p_i 's *Front* after t_2 , say at t_3 . This implies that *ListTransient* must be reset at t_3 , which, in turn, implies that p_b must have updated the *Front* of it's queue before t_3 . Thus, at t_3 , p_i knows exactly which elements of its queue p_b ever reads.

Note that p_i is prone to starvation. But in practice, it does make progress when p_b proceeds to tessellate the surface(s) corresponding to the the *Front* of its queue.

5 Greedy Rendering

A fundamental component of real-time graphics is to have the image appear on screen in time. The quality of such image may not be of primary concern. In its most general sense, such applications are referred to time-critical rendering. We present a method to allocate the time spent in each frame in which all triangles must be sent down the rendering pipeline. This is an essential component of in-time rendering.

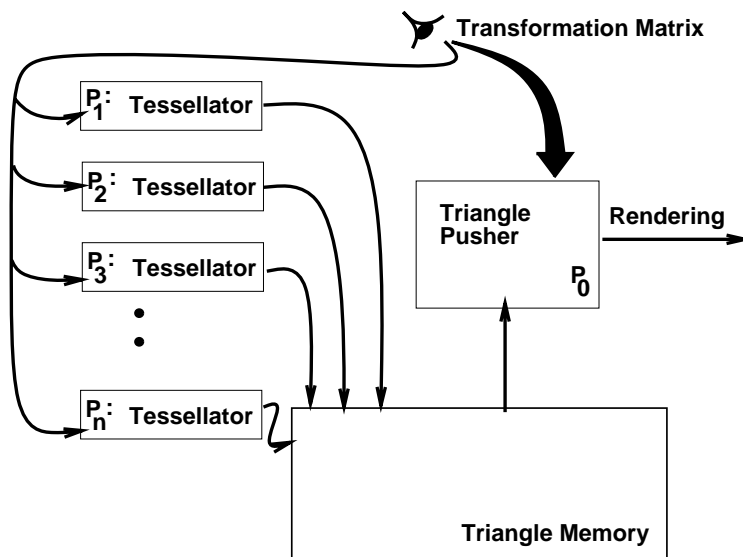


Figure 6: Greedy Rendering Technique

5.1 System Architecture

Fig. 6 shows our overall system architecture. A triangle pushing processor is allocated for the sole purpose of sending triangles down the rendering pipeline. This processor runs asynchronously with the tessellators. It has a ‘view’ of the current set of triangles to be rendered.

This triangle pushing processor executes the following loop:

```
Get Current Viewer Position           :P1
```

```

Compute and push transformation matrix           :P2
For each triangle in view                     :P3
    write triangle to the pipeline.             :P4

```

The triangle pusher never waits for any tessellators to finish. The tessellators, asynchronously generate triangles and update the pusher's view. The tessellators, however, themselves execute in synchrony: a tessellator goes on to frame number $i + 1$ only if all surfaces have been tessellated for frame i . The tessellators follow the algorithm presented in Section 4. Once a frame is complete, all tessellators read the then current view-matrix from a shared global variable, and use this matrix to generate new triangles. Clearly, if tessellation is slow, as is commonly the case, we almost always render sub-optimal number of triangle, as the tessellator *lag* behind the renderer by a few frames. The tessellators mostly generate triangles with an old view-matrix. This, in our experience, is not a major problem, due to coherence. The tessellators mostly lag by no more than 3 – 4 frames. And the view-matrix does not change significantly in 3 – 4 frames, meaning the 'old' triangles lead to a reasonably smooth image.

5.2 View Update

It is important to update the view in a fashion that the pusher never mixes old and new triangles. In addition, surfaces are not independent entities. The triangles for adjacent surfaces must match up at the surface boundaries to prevent cracks. We partition the adjacency graph of surfaces into connected components. The update of all members of a connected components occurs simultaneously. For each component c there exists a shared variable $ComponentTris(c)$. $ComponentTris(c)$ is a pointer to a list of triangle addresses. Each address corresponds to the triangles of a surface, which are stored contiguously in memory. The tessellator that generates triangles for surface i , of component c , stores the address of new triangles in $Newlist[i]$. Once the new triangles have been generated, and the pointer list set up, the tessellator that generates the last triangle of the group, writes the address of the new list in $ComponentTris(c)$.

```

Generate Triangles at address  $a$ 
 $Newlist[i] = a$ 
if for all surfaces in the component  $NewList[i]$  is non NULL
     $ComponentTris(c) = NewList$ 

```

To ensure that the pusher, does not read triangles from different list. It reads $ComponentTris(c)$ just once per frame, and saves it locally. Thus it either renders all new, or all old triangles. Modifying line P3 to reflect this:

```

 $List = ComponentTris(c)$ 
for each surface  $i$  in component  $c$ 
Render all triangles at  $List(i)$ 

```

5.3 General Environments

This method works well for environments consisting of a number of small solid models, resulting in a number of small components. In environments where this is not the case, we propose a more general technique:

1. Tessellate surface boundaries separately from the surface interior
2. Generate boundary strips between the boundary and surface interior
3. For each boundary with a different surface, generate boundary strips N_i with new interior tessellation and new boundary tessellation, and strips O_i with new interior tessellation and old boundary tessellation.
4. Maintain adjacency graph.
5. If an adjacent boundary has not been tessellated for the current frame, use O_i . If the adjacent boundary has been tessellated, use N_i . Again, the processor to tessellate a boundary second updates the address on behalf of both processors.

In practice, we have found it much more efficient, and hardly distracting, to render the images with cracks, and let the cracks ‘fill up’ when the user stops, and the tessellation catches up.

As a final note, let us emphasize that this method is not necessarily bound to multiple processor environments. For a given application, even single processors can allocate triangle pushing time per frame. For example, suppose it takes t_p seconds to process each triangle. For each frame the triangle pushing thread has an account of the number of triangles available for that frame, call it m . Suppose further that the desired frame rate is R frames per second. In each frame, then, the processor must allocate no more than $\frac{1}{R} - mt_p$ seconds per frame for triangle generation.

6 Implementation and Performance

On Pixel Plane 5, a heterogeneous message passing multicomputer, we implemented our static load balancing scheme presented in section 3 and compared its performance with random distribution. The architecture of this machine is shown in Fig. 7. Front-end geometry processing, such as transformation, clipping, and setup for rasterization, is performed on the Graphics Processors (GPs) which contain Intel i860 RISC microprocessors running at 40 MHz, 8 MB of main memory, and communications hardware. Triangle rasterization, and shading is performed on renderer units which contain arrays of 128 by 128 1-bit processors with local memory [5] and an instruction sequencer. The processing units are connected by a 160 million word per second ring communications network. The multiple processors shown in the left box are used for tessellation.

With a configuration of 25 GPs our load-distribution scheme shows an average speedup of 10%. We evaluated our algorithms on a number of models, including various parts of the

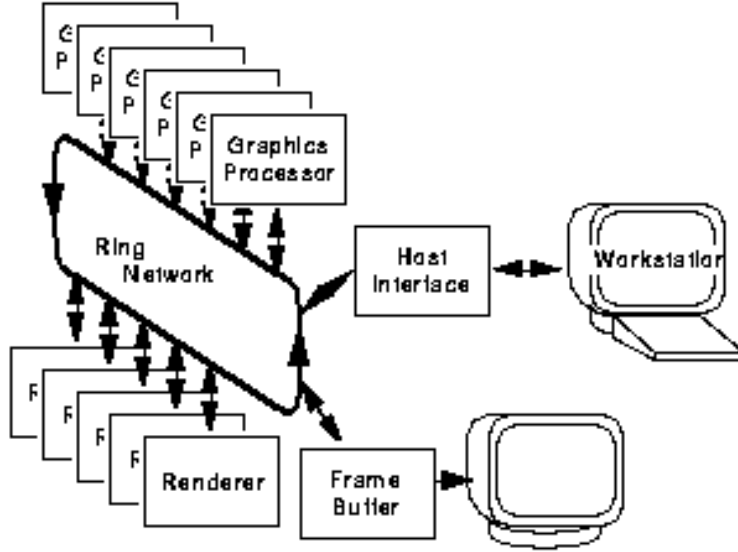


Figure 7: PixelPlanes Architecture

Model	# Surfaces	Round-Robin Distribution		Graph Partitioning	
		Frames/Sec	Utilization	Frames/Sec	Utilization
Torpedo	1201	10.80	72.6%	11.74	80.1%
Pivot	4101	15.41	61.9%	15.95	81%
Ship	3392	19.05	65.3%	19.86	78%

Table 1: Performance of Static Load-distribution Algorithm

submarine storage and handling system. Table 1 shows the increase in average processor utilization using the graph partitioning algorithm, and the actual speedup gained.

We also implemented our algorithms on Silicon Graphics Onyx with 4 host CPUs and Reality Engine II graphics. The memory (and address space) is shared by all processors. Each processor has a small on-chip cache. On this system, we implemented the ‘static’, ‘global queue’, and ‘load stealing’ load distribution schemes, and compared their performances. For large processor configurations we used a parallel Challenge machine, which has similar architecture. Fig. 8 shows three graphs with models of 5302, 10,604, and 15,906 trimmed spline surfaces respectively. Each graph shows the change of the tessellation rate⁴ with different number of processors. The graphs show that the global queue scheme provides 5% to 10% improvement over the static scheme, while the load stealing scheme provides another 10% to 20% improvement over the global queue scheme. In addition, as the number of processors increases, the load stealing scheme shows the best scaling behavior. The speedup is close to linear.

⁴Since greedy rendering proceeds asynchronously, the frame-update rate is hardly affected. The lag changes with the tessellation rate.

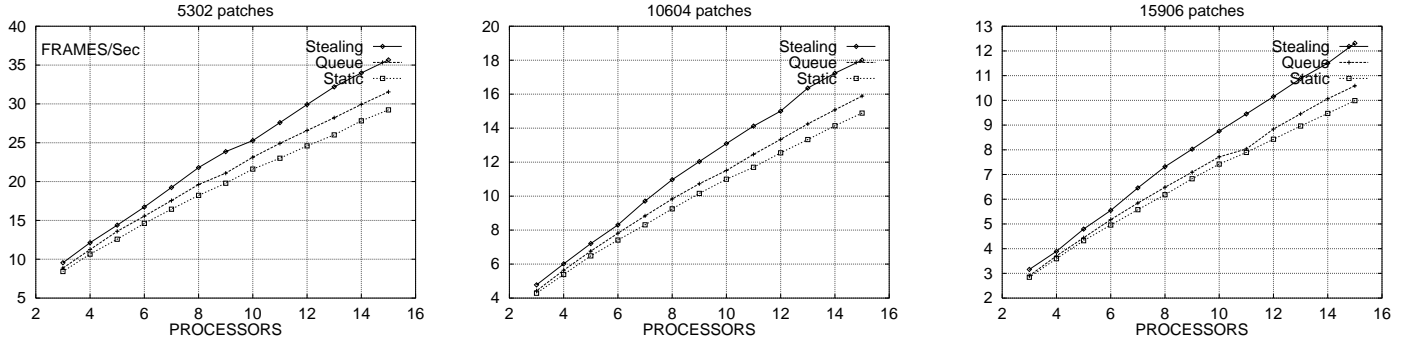


Figure 8: Performance Comparison of three load-balancing techniques

If a large number of processors are not available, or if the size of the model is large, the tessellation rate drops to under 5 frames per second. With greedy rendering, we are consistently able to render at the speed of about 4 times of the actual tessellation rate. Table 2 shows the performance of the greedy algorithm on a number of models. Column 5 shows the average number of frames the tessellators lag behind the triangle pusher, and represents the speed-up gained by the greedy algorithm. This speed-up comes at a minimal loss in image quality. The color plate shows the images corresponding to the worst lag in a user sequence for three parts of the submarine storage and handling system. As can be seen, even in the worst case, the lagging images are of reasonable quality. Thus this technique achieves about 5 times speedup with little visual erosion.

7 Conclusion

We have presented two techniques to distribute work across processors to speed up the rendering of dynamic objects. The greedy rendering technique can reduce image-jumps for most applications, thus reducing motion-sickness. The load-balancing technique can increase processor utilization to about 70-90%. If load-redistribution is not a feasible option, in our experience any significant load-balancing is difficult, and quite application specific. On the other hand, load-redistribution can have significant impact on update-rates. In particular, our load stealing algorithm is designed for shared memory machines. It restricts most of the load balancing algorithm to idle processors, thus freeing busy processors to continue to perform real work. For distributed memory machines, where enough communication

Model	# Surfaces	Tessellations/Sec	Updates/Sec	Average Lag
Dragon	5354	4.20	19.96	15.76
Car 1	5053	4.84	19.97	15.13
Car 2	8693	2.20	8.55	6.35

Table 2: Performance of the Greedy Rendering Algorithm

bandwidth is available for patch re-distribution, we should be able to extend our algorithm to request based 'load stealing', but overhead on the busy processors must increase.

Our over-all algorithm achieves almost two orders of magnitude improvement over the existing method of spline rendering on Reality Engine systems. As a result, our method makes it possible to interactively visualize models with tens of thousands of Bézier surfaces on high-end systems.

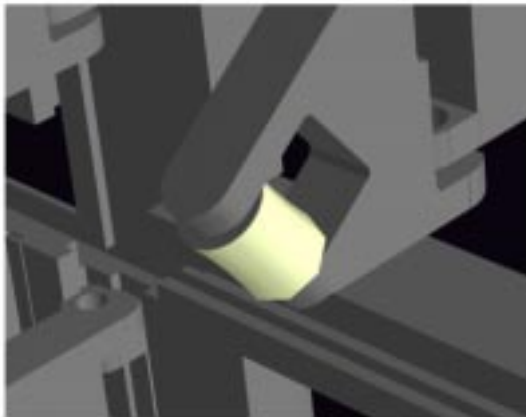
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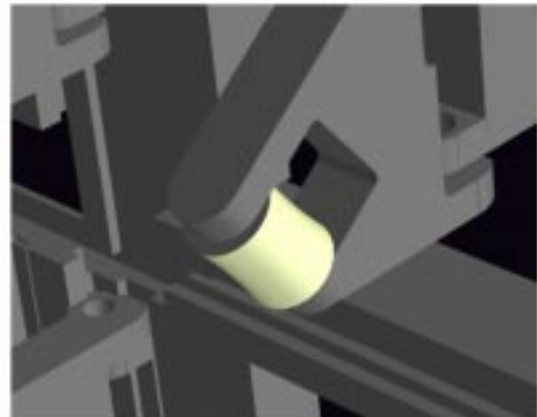
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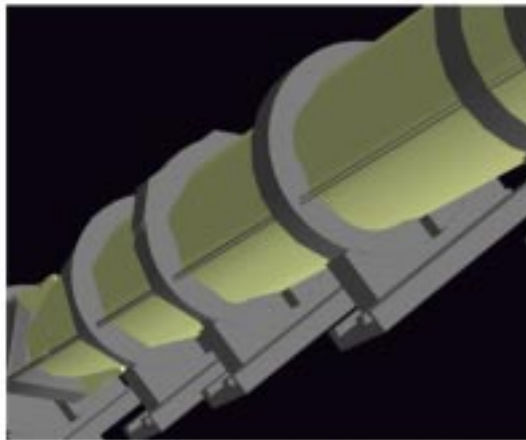
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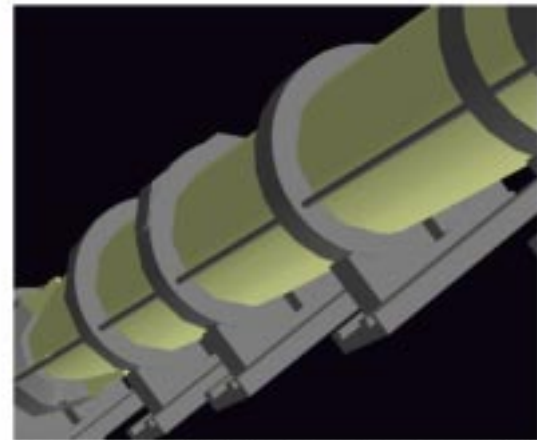
(a1) Pivot: Lagging Tessellation



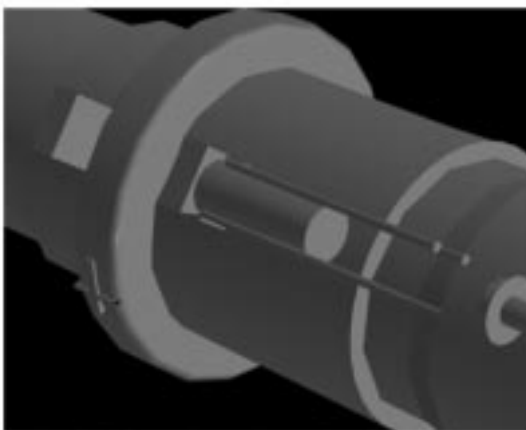
(a2) Pivot: Synchronized Tessellation



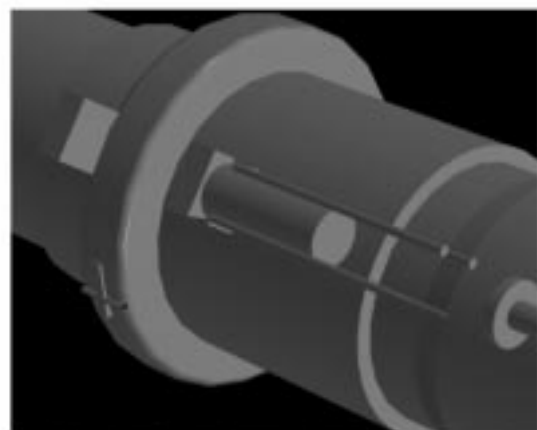
(b1) Line: Lagging Tessellation



(b2) Line: Synchronized Tessellation



(c1) Tube: Lagging Tessellation



(c2) Tube: Synchronized Tessellation

Color Plate I: Greedy Rendering