

Multi-Projector Techniques for Real-Time Visualizations in



Outline

O. Bimber



Outline

these slides:

www.uni-weimar.de/medien/AR



Introduction
Motivations and Applications



Geometric CorrectionPlanar, Non-Trivial, Complex Surfaces



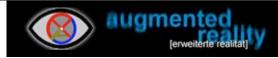
Radiometric Compensation Local and Global Light Effects



Advanced Techniques
View-Dependence, Multi-Focal Projection, Light
Transport



Outlook
Limitations and Future Work



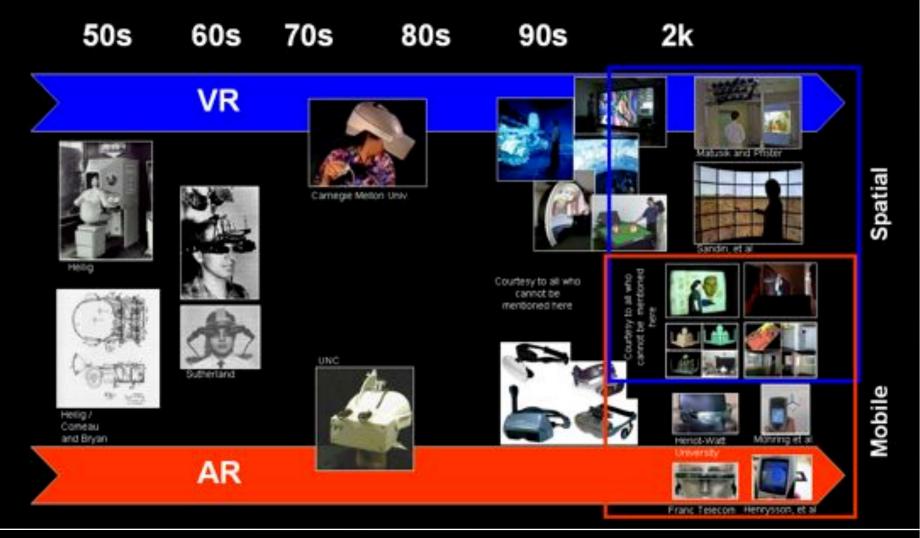
Introduction



Evolving Evolution



Evolving Evolution

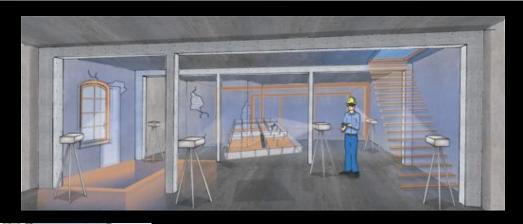




Motivation: Projection



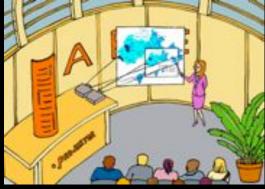
Motivation: Projection











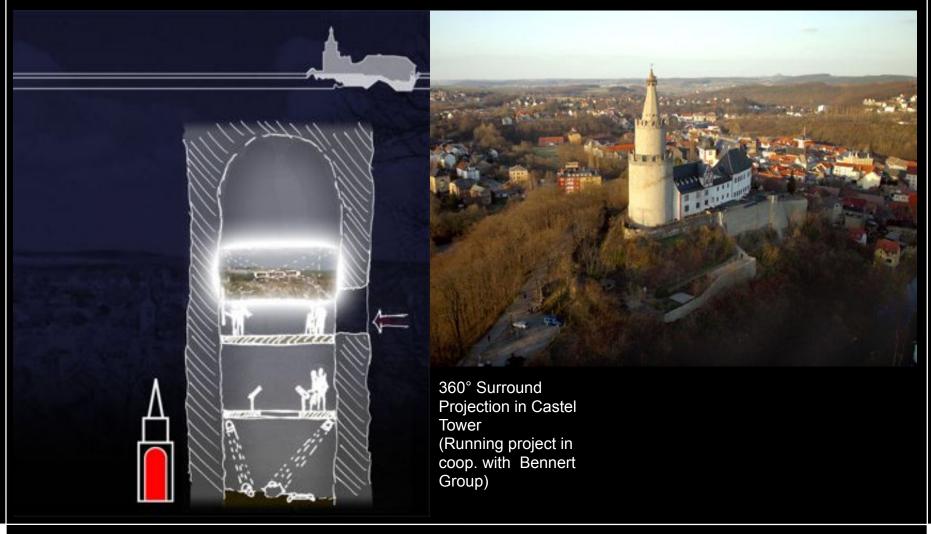




Application: Historic Sites and Museums



Application: Historic Sites and Museums





Application: Architectural Visualization



Application: Architectural Visualization





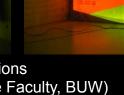




Bimber et al, IEEE/ACM ISMAR 2005



On-Site Architectural Visualizations (Running project in coop. with Architecture Faculty, BUW)





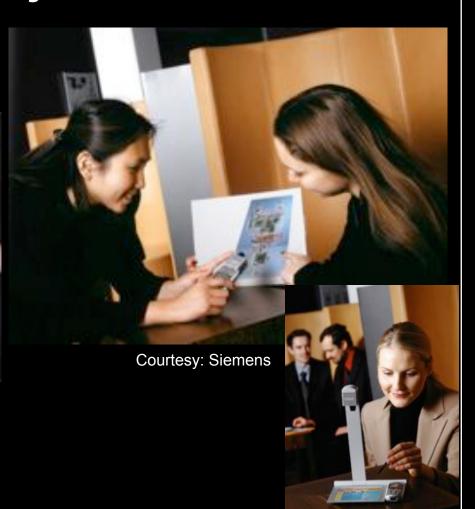
Application: Pocket Projectors



Application: Pocket Projectors



Courtesy: InFocus

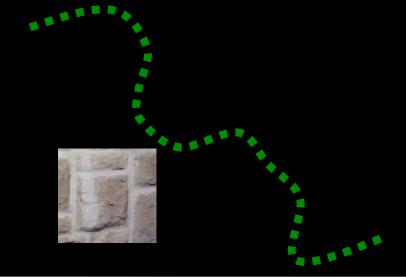




Principle





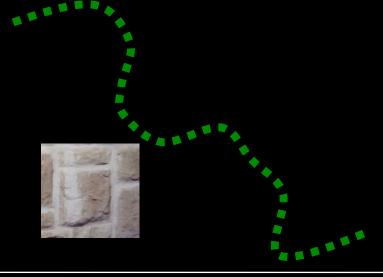


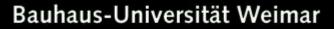


Principle

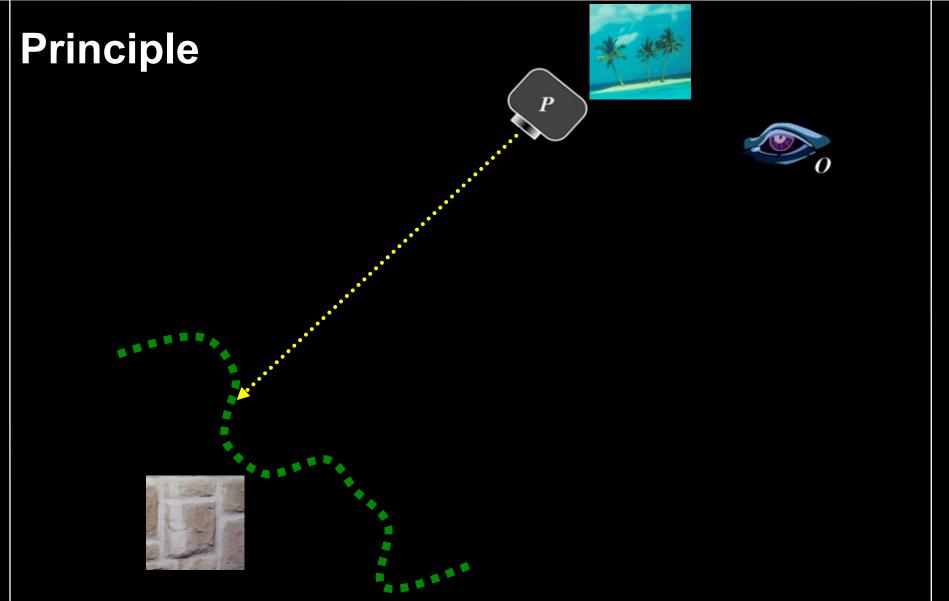




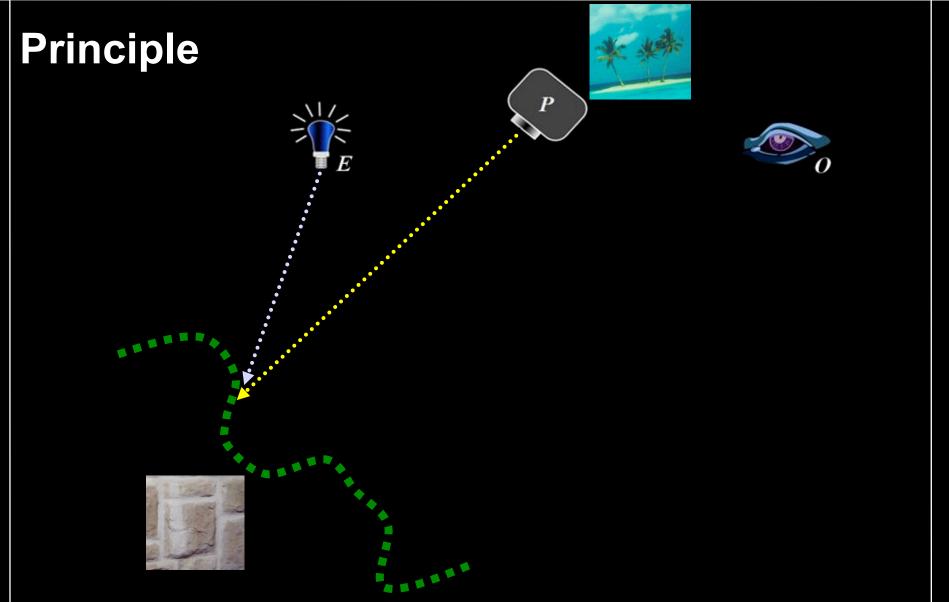




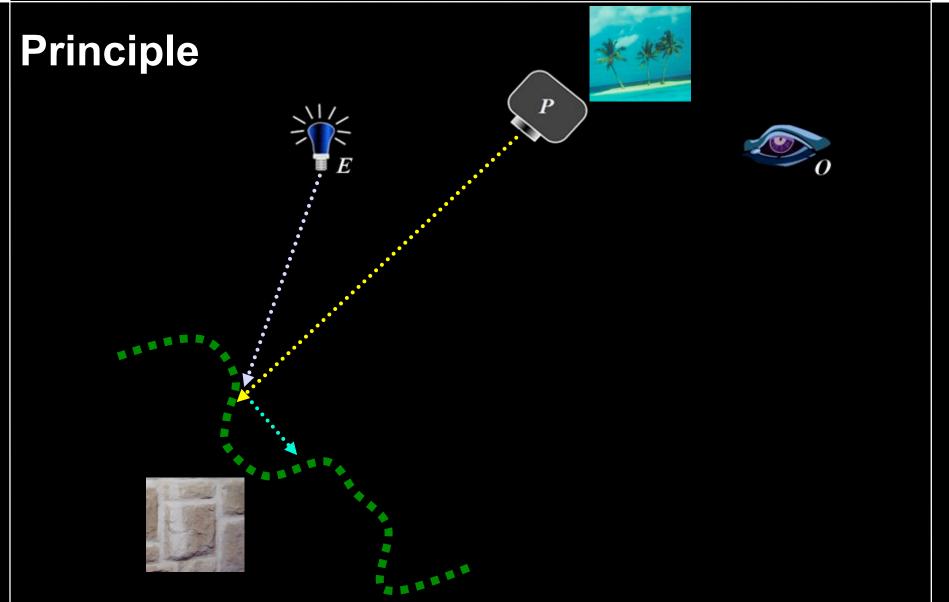




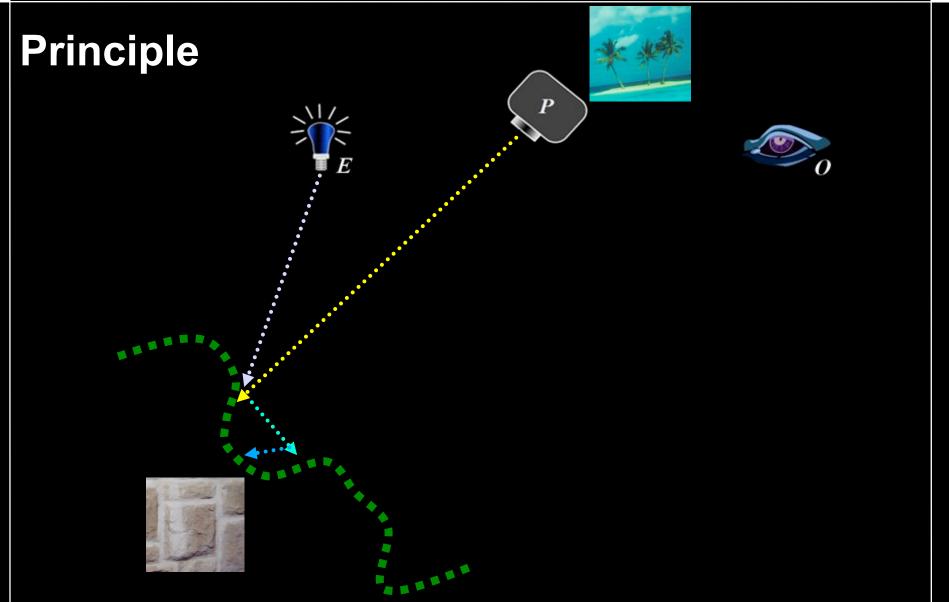




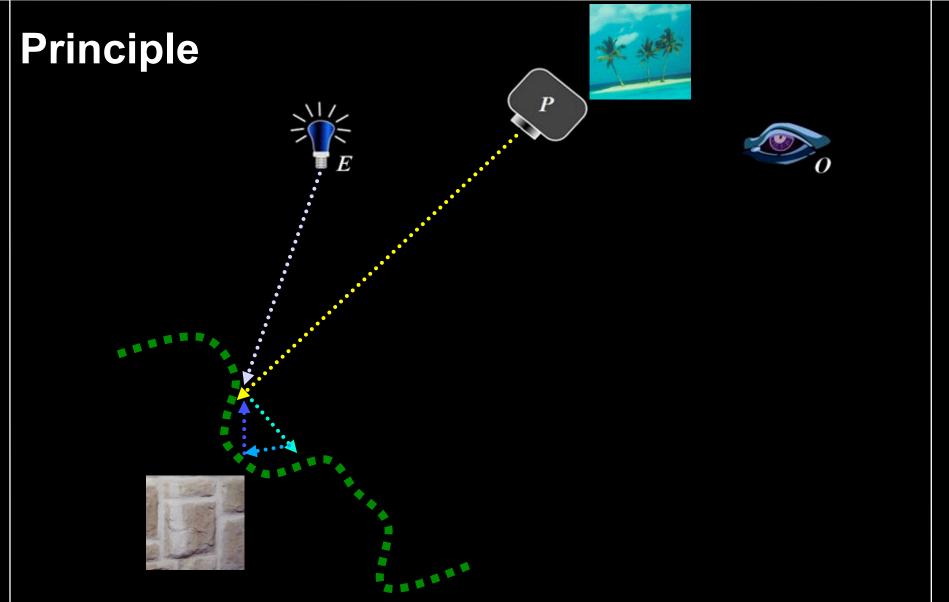




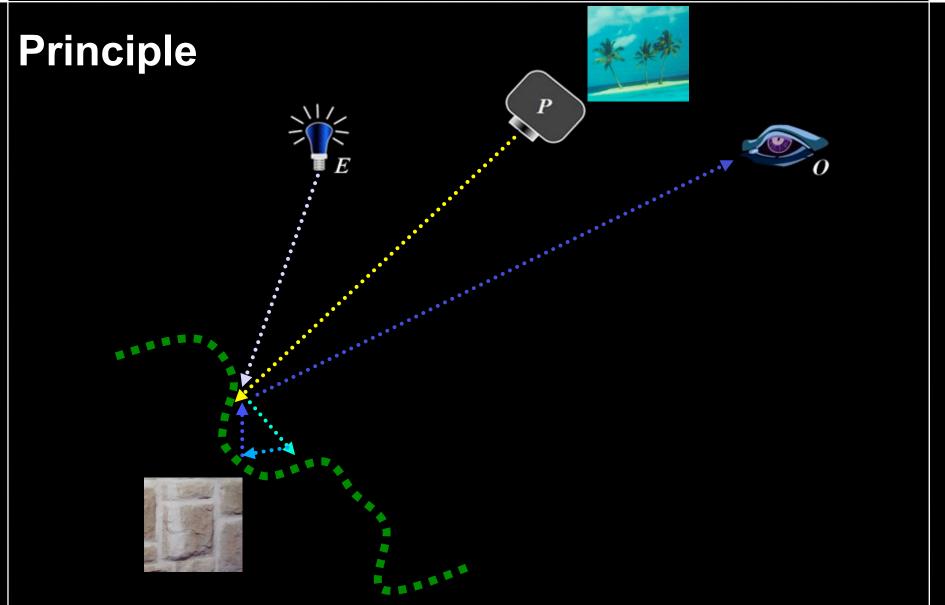




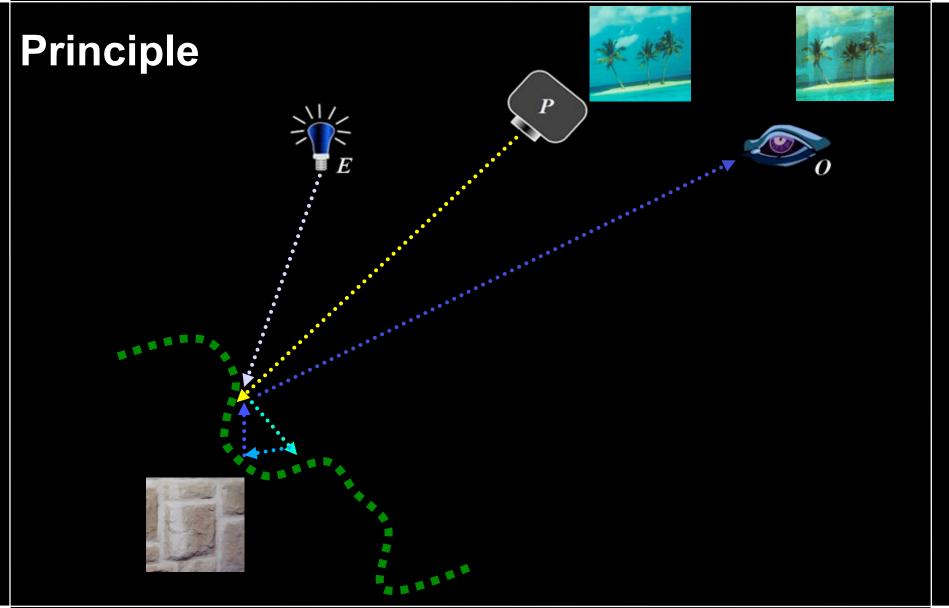




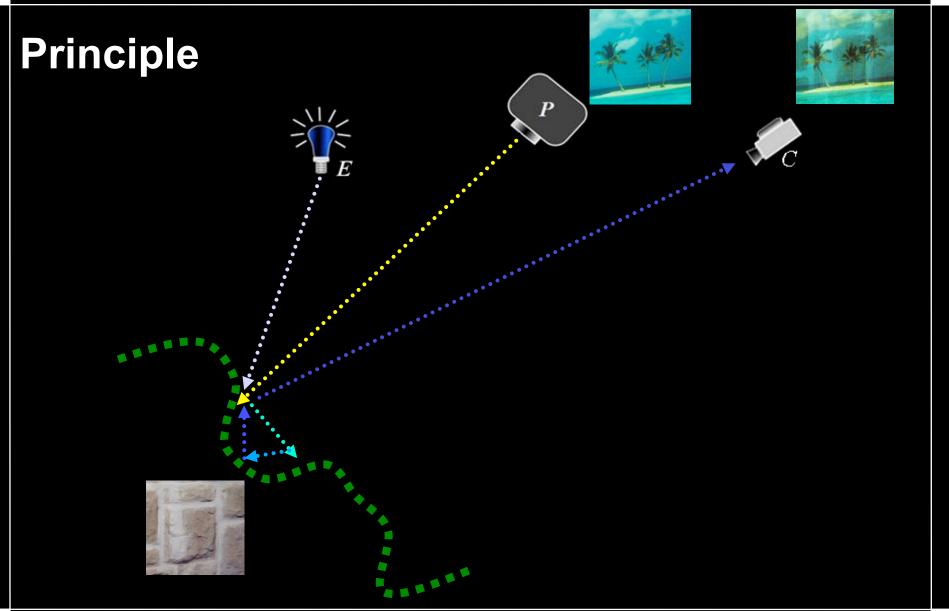




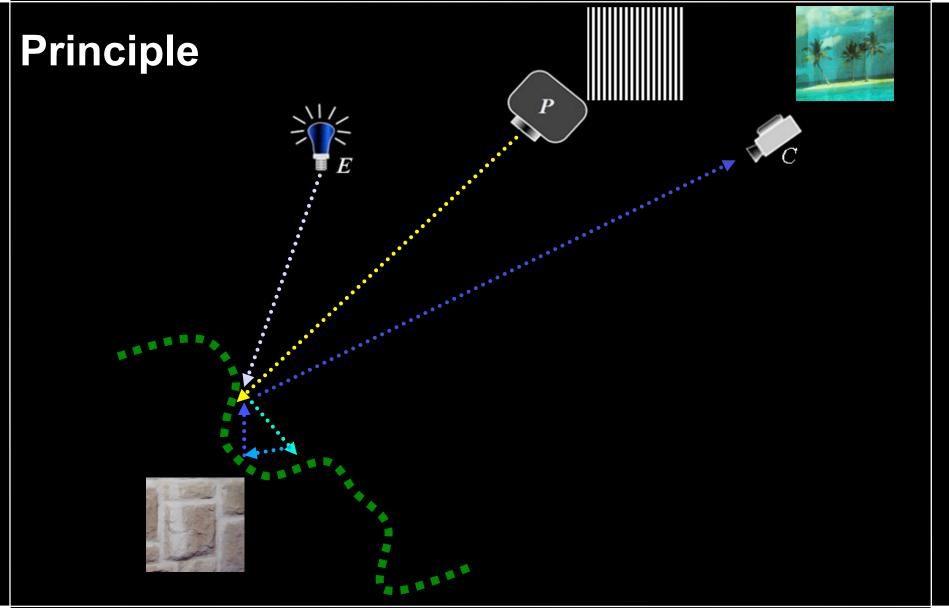




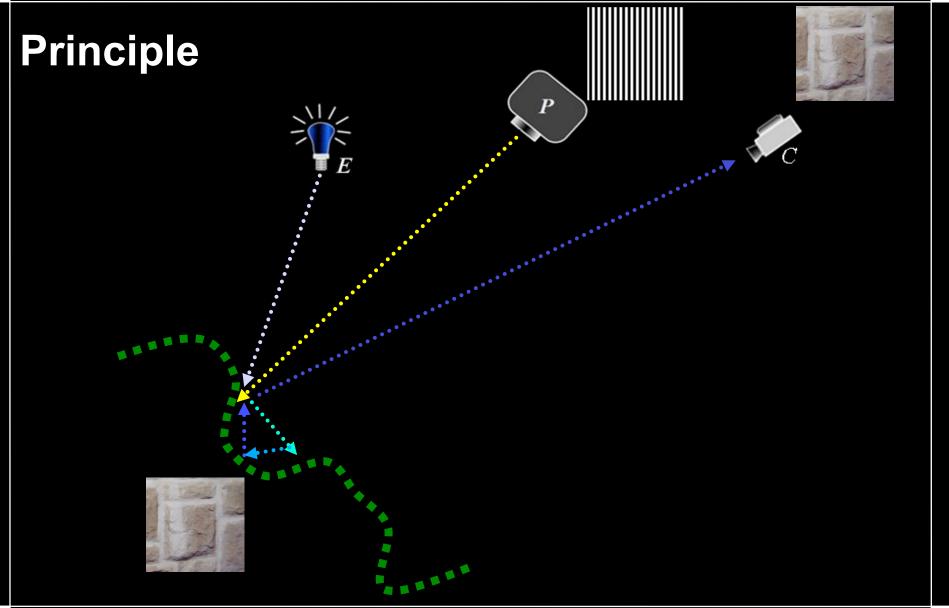




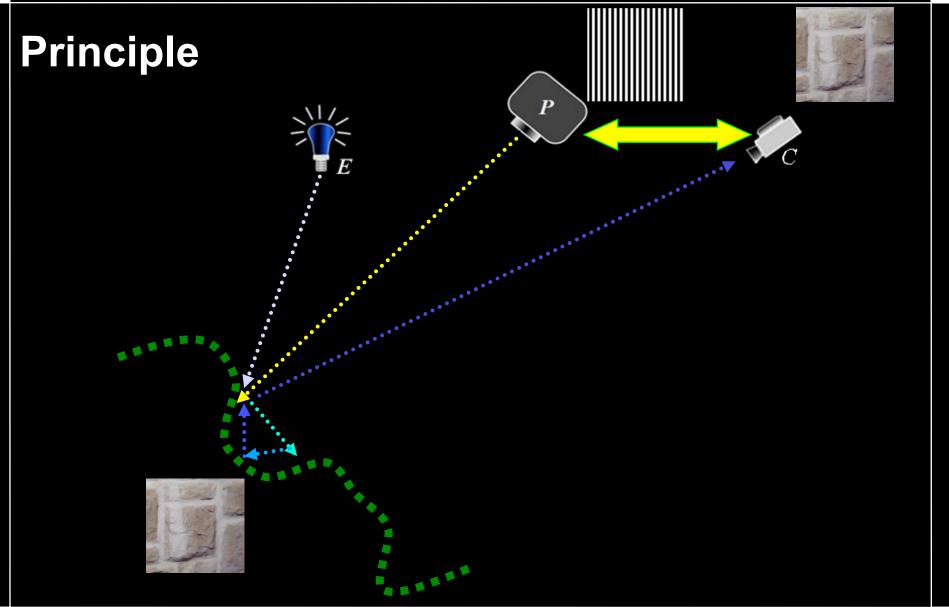




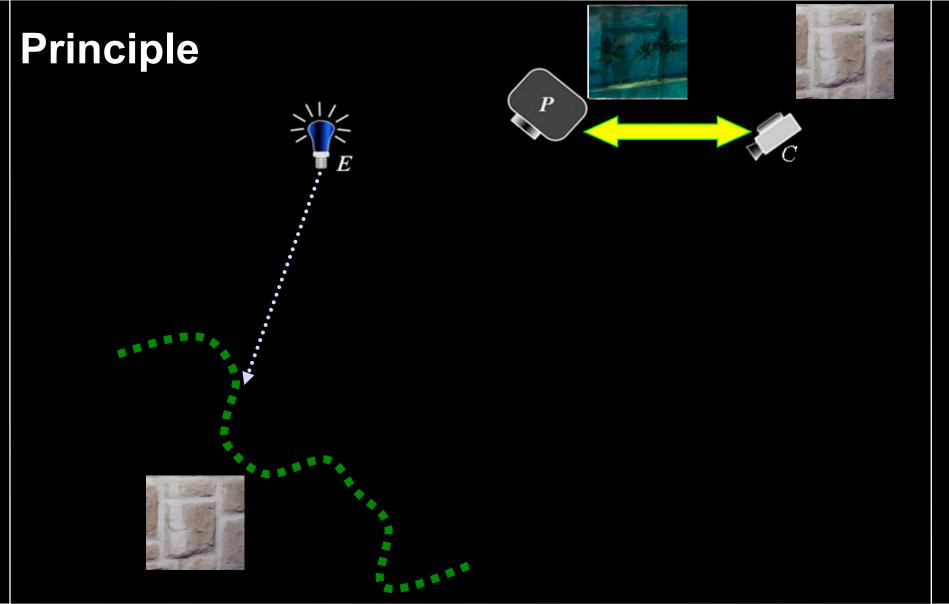




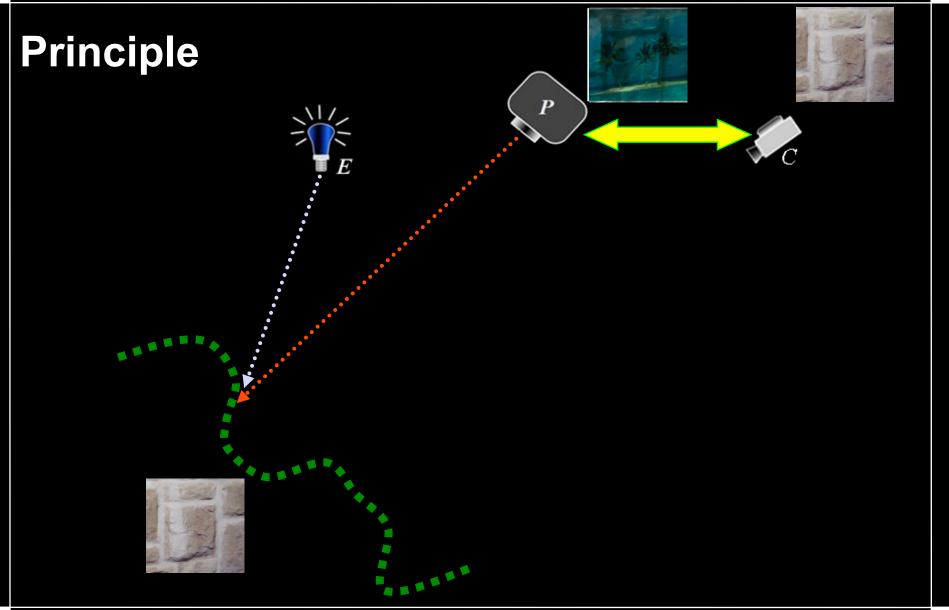




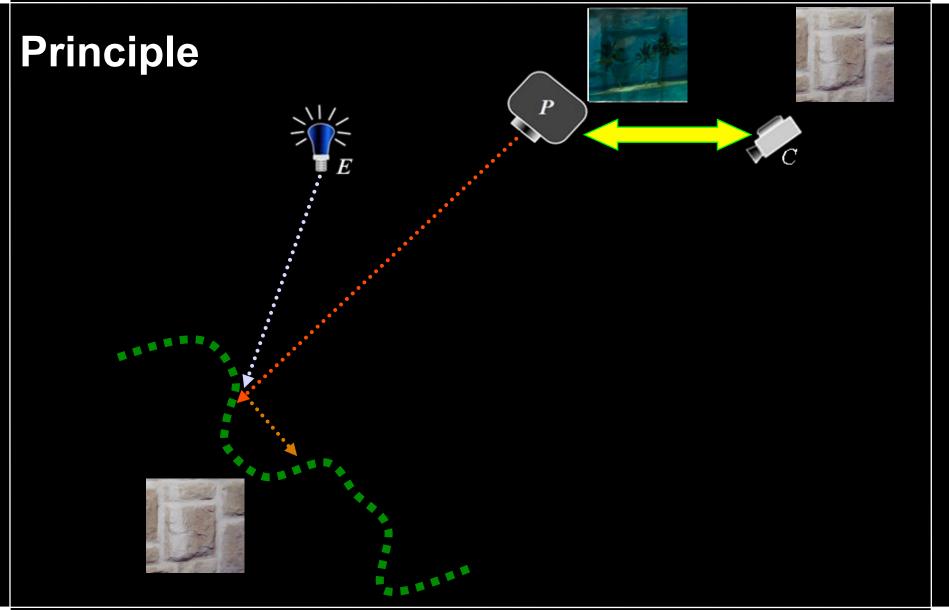




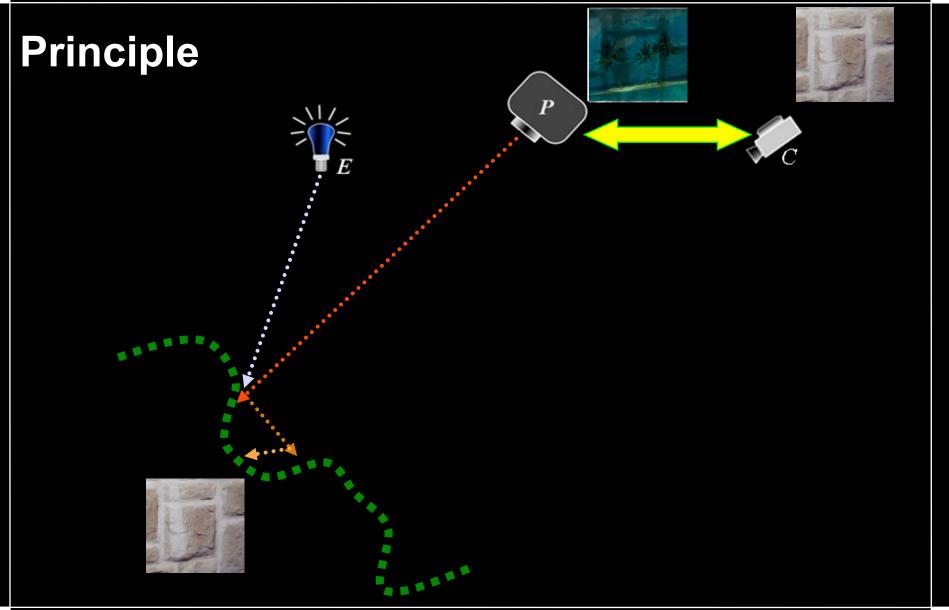




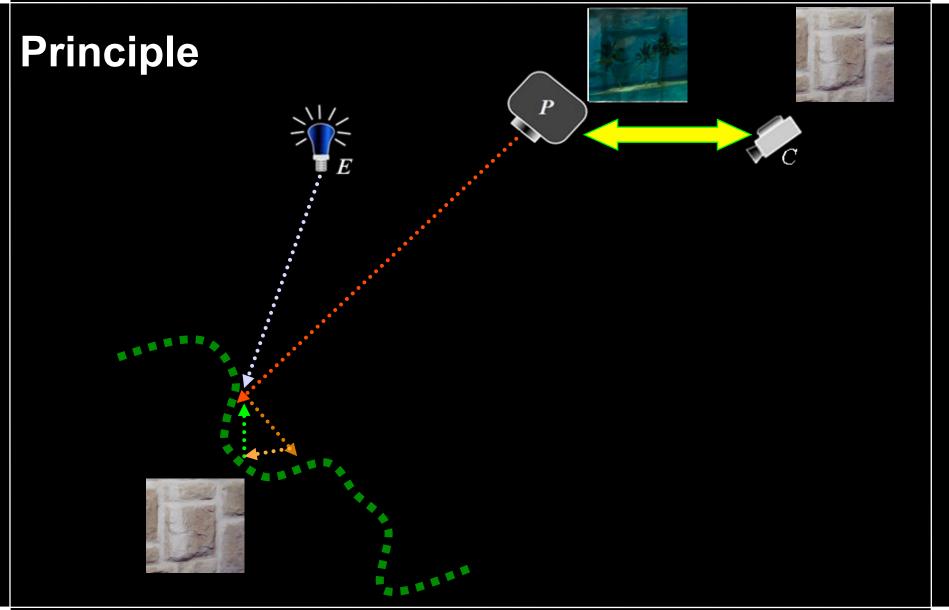




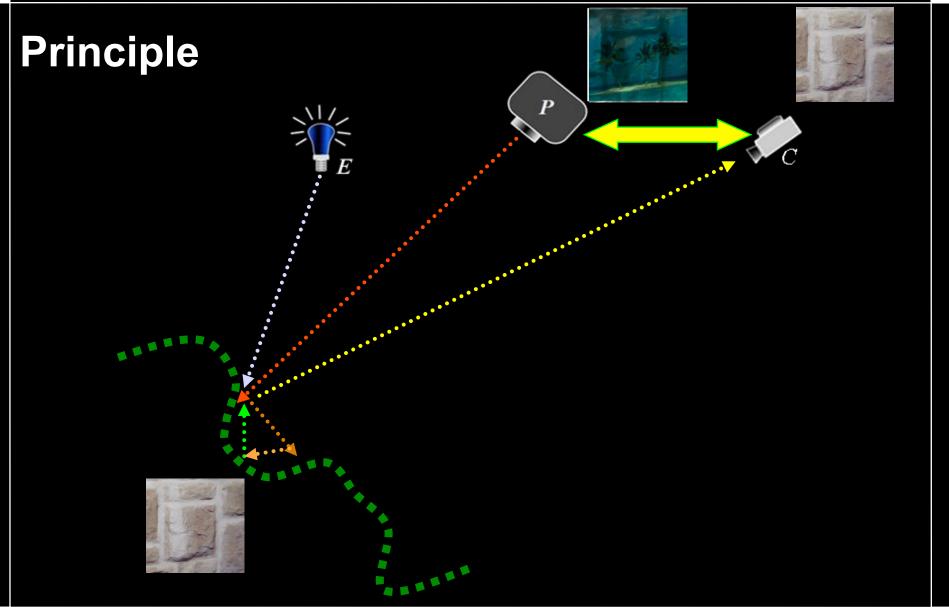




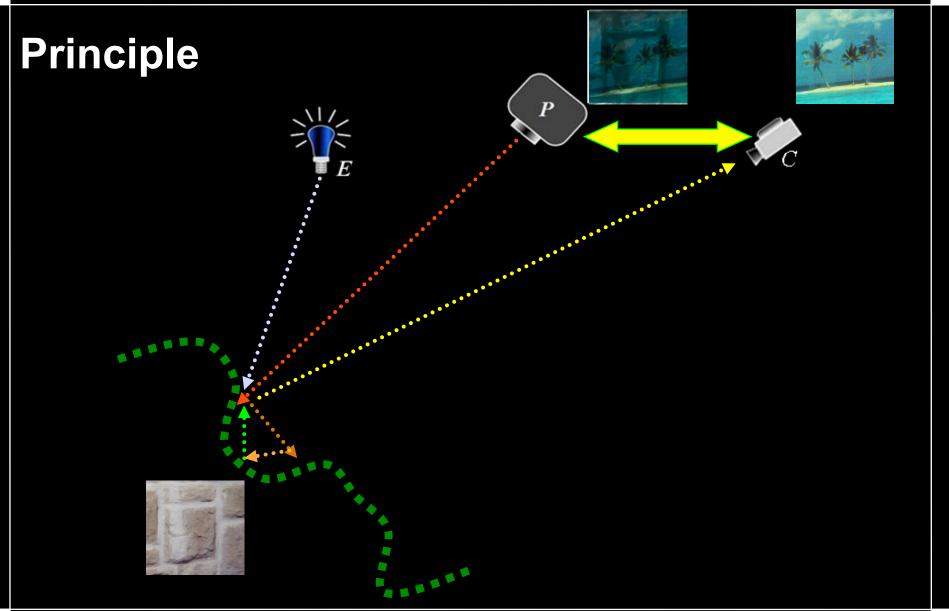




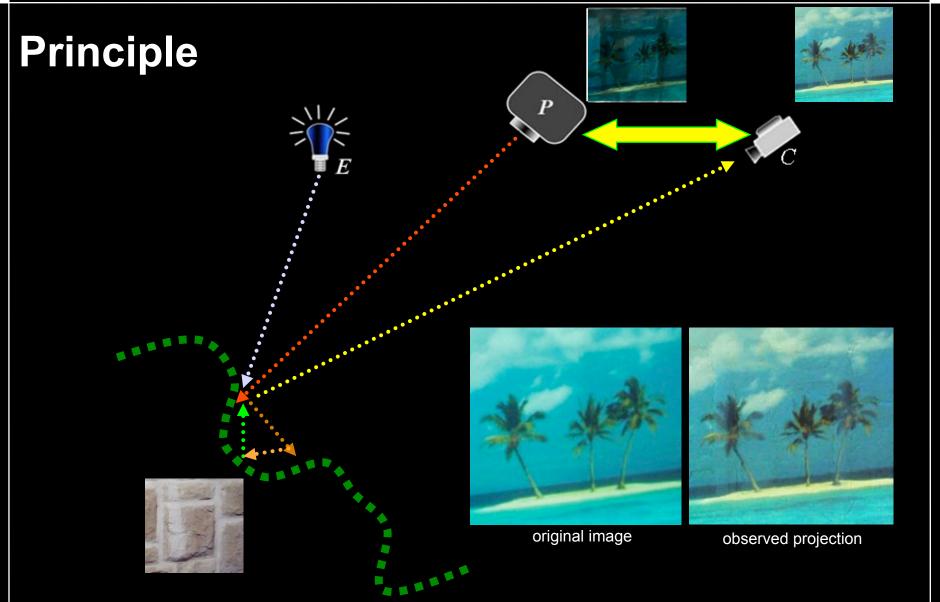








Bauhaus-Universität Weimar



O. Bimber

Multi-Projector Techniques for Real-Time Visualizations in Everyday Environments

04/01/06



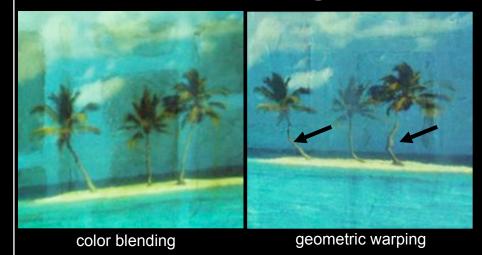
Some Challenges



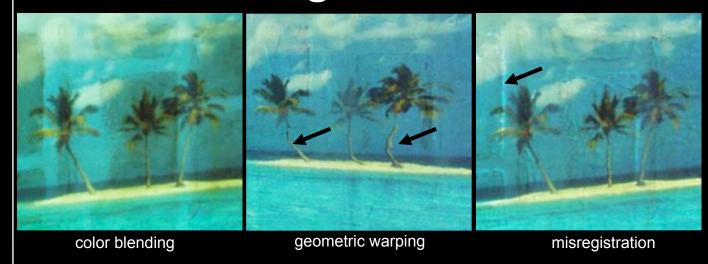


color blending

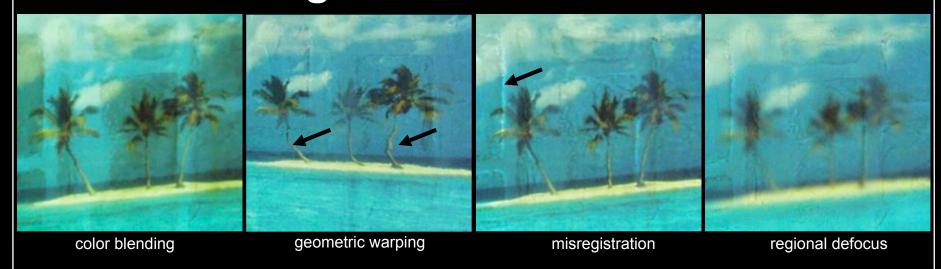




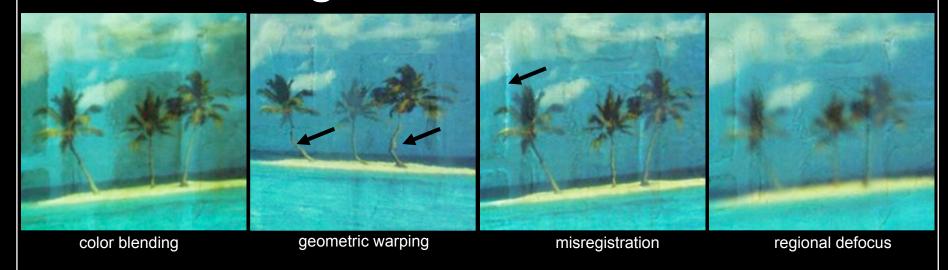


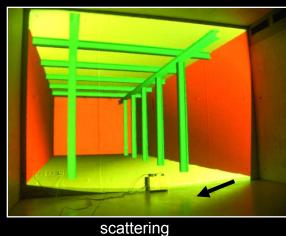




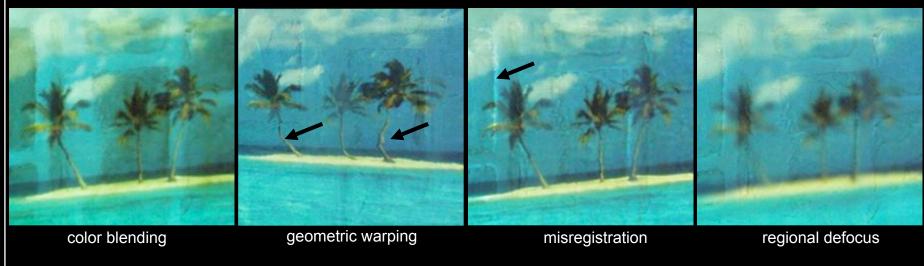


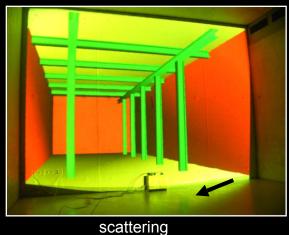










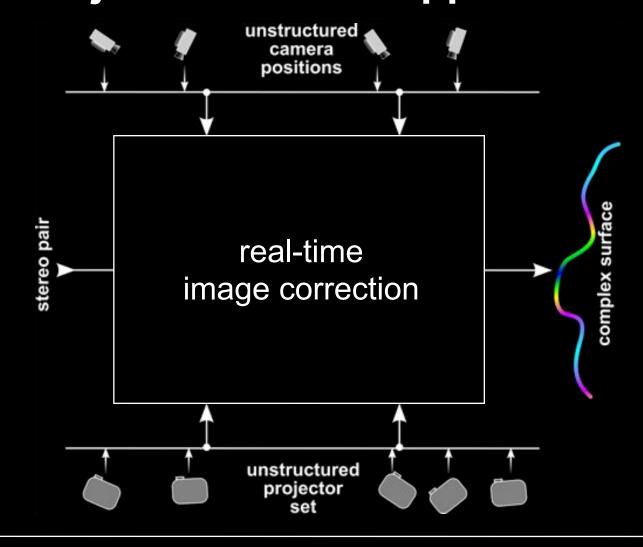




specular reflection, refraction, sub-surface scattering, inter-reflections, dispersion, diffraction, etc.

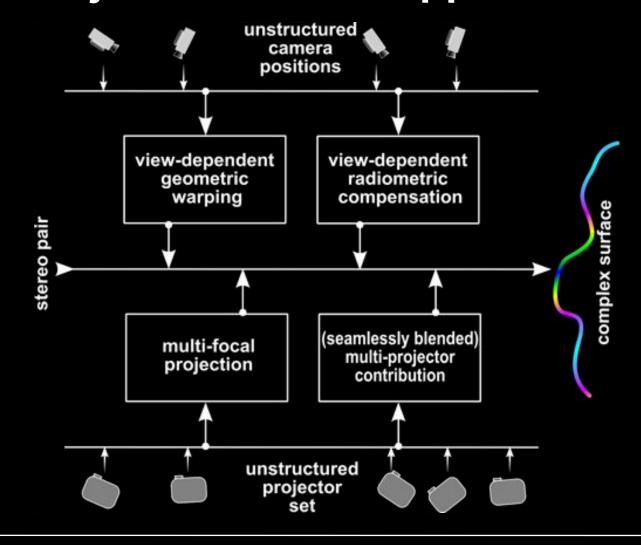


A Multi-Projector-Camera Approach





A Multi-Projector-Camera Approach





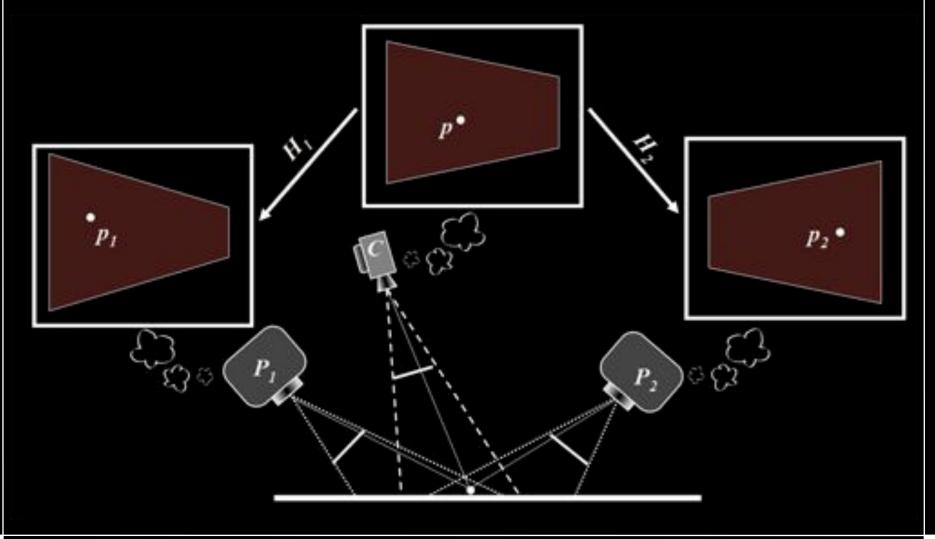
Geometric Correction



Planar Surfaces



Planar Surfaces





Homography

O. Bimber

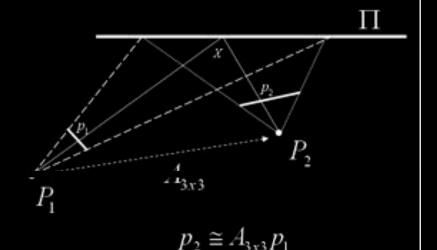


Homography

- homography is a mapping between two projections over a plane
- can map pixel coordinates from one perspective to another
- equation system has to be solved to determine 8 parameters of matrix A
- can be used directly in transformation pipeline by multiplying the following matrix after projection (without perspective division):

$$A_{4\times4} = \begin{bmatrix} a_{11} & a_{12} & 0 & a_{13} \\ a_{21} & a_{22} & 0 & a_{23} \\ 0 & 0 & 1 & 0 \\ a_{31} & a_{32} & 0 & 1 \end{bmatrix}$$

ensure intact depth values with (approximately)



$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \end{bmatrix} \begin{bmatrix} p_{1x} \end{bmatrix}$$

$$\begin{bmatrix} p_{2x} \\ p_{2y} \\ 1 \end{bmatrix} \cong \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} p_{1x} \\ p_{1y} \\ 1 \end{bmatrix}$$

$$p_{2x} = \frac{p_{1x}}{(a_{31}p_{1x} + a_{32}p_{1y} + p_{1w})} \in [-1,1]$$

$$A_{1x4} = \begin{bmatrix} a_{11} & a_{12} & 0 & a_{13} \\ a_{21} & a_{22} & 0 & a_{23} \\ 0 & 0 & 1 - |a_{31}| - |a_{32}| & 0 \\ a_{31} & a_{32} & 0 & 1 \end{bmatrix}$$

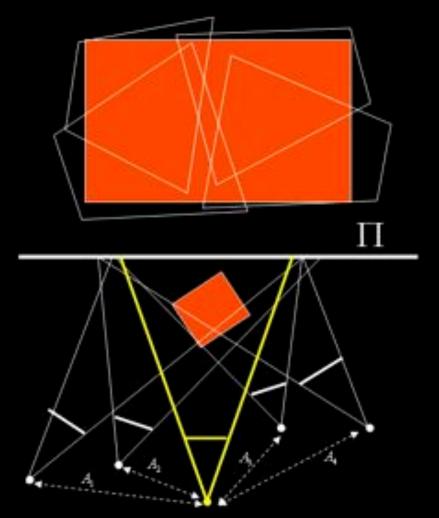


Multi-Projector Registration



Multi-Projector Registration

- registering multiple projectors onto a common planar surface
- map all perspective into a single target perspective via homographies
- target perspective can be camera perspective
 - automatic determination of matrix parameters via structured light
- rendering
 - render image for target perspective (if target perspective is **orthogonal** to plane, then it can be done with an off-axis projection of an observer!)
 - map pixels into individual projector views (i.e., multiply 4x4 version of homography matrix onto matrix stack [after projection] and ensure that depth values remain intact!)





Example: Tiled Projection Screens



Example: Tiled Projection Screens

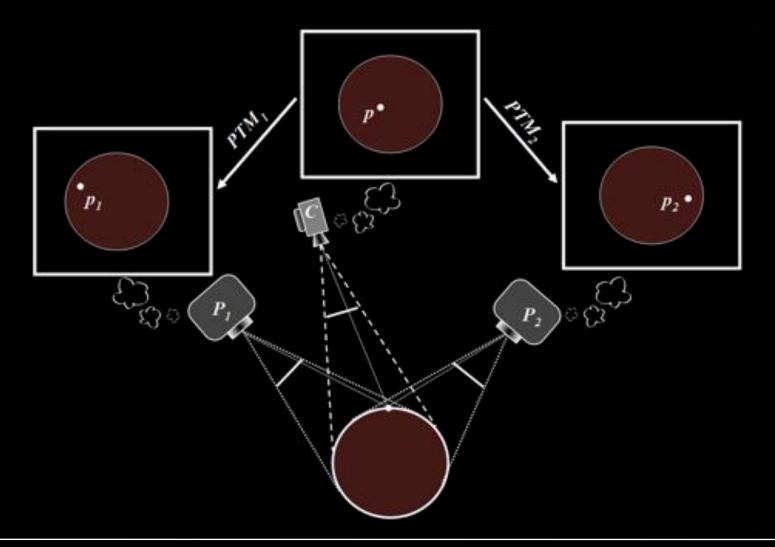




Non-Trivial Surfaces

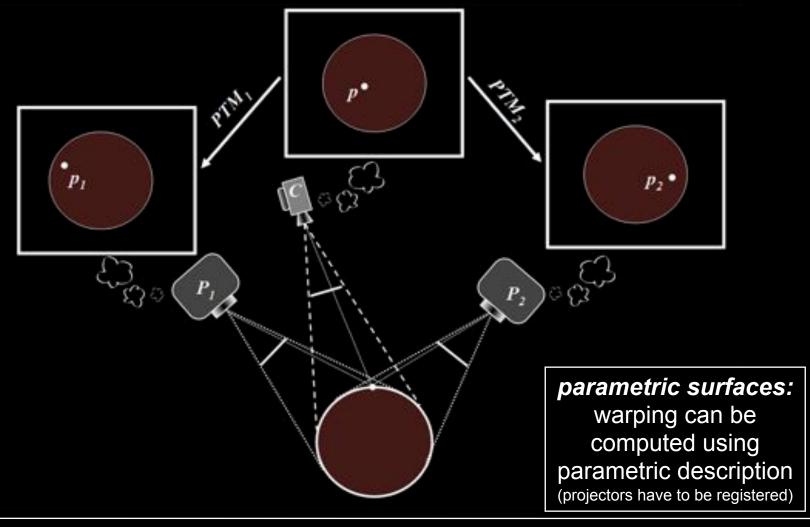


Non-Trivial Surfaces





Non-Trivial Surfaces



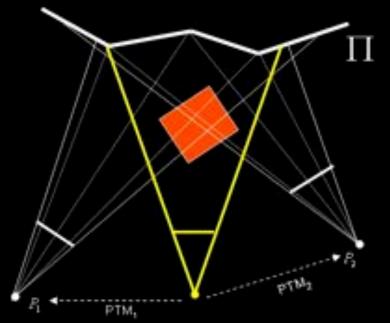


Projective Texture Mapping



Projective Texture Mapping

- given a geometric definition of the surface
 - scan or model
- determine intrinsic and extrinsic of projectors with respect to surface
 - measure projections of known 3D surface points on image plane of projector and solve equation system to determine parameters of matrix
- define virtual camera with same parameter for each projector
- render 3D model of surface, textured with images, from perspective of projectors/ virtual cameras
- texture coordinates can be automatically generated from target perspective via projective texture mapping



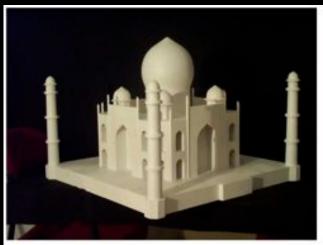
$$\begin{bmatrix} wx \\ wy \\ wz \\ w \end{bmatrix} = \begin{bmatrix} f & \cdot & \cdot & \cdot \\ \cdot & f & \cdot & \cdot \\ \cdot & \cdot & \cdot & 1 \\ \cdot & \cdot & \cdot & 1 \end{bmatrix} \begin{bmatrix} R_{11} & R_{12} & R_{13} & t_x \\ R_{21} & R_{22} & R_{23} & t_y \\ R_{31} & R_{32} & R_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

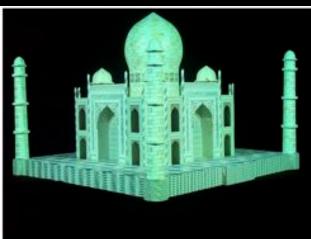


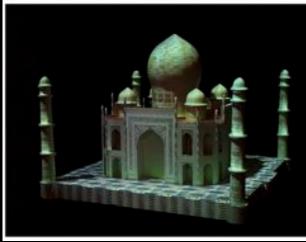
Example: Shader Lamps

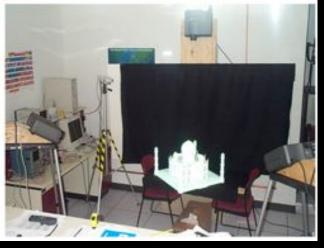


Example: Shader Lamps









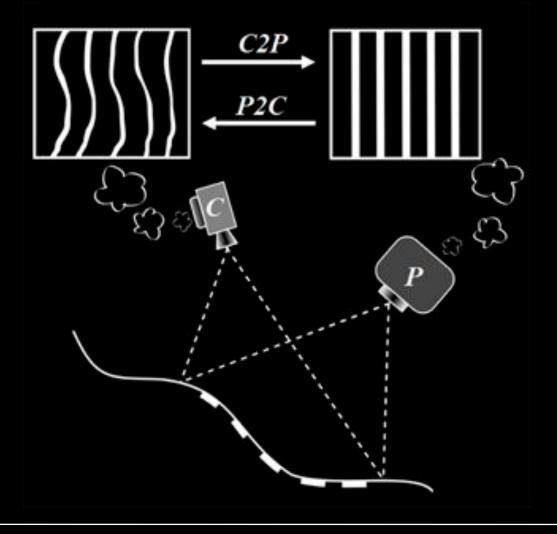
Courtesy: Raskar, et al., EGRW 2001



Complex Surfaces



Complex Surfaces



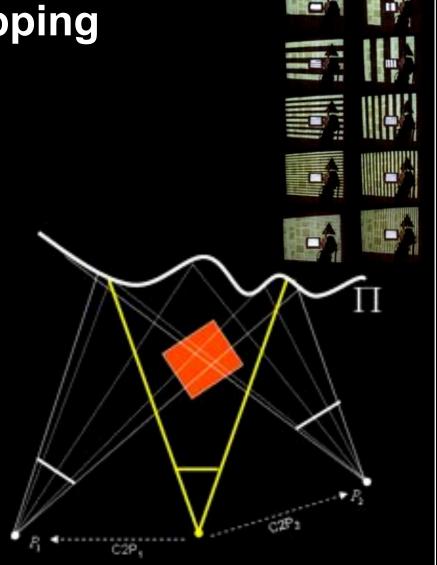


Pixel Displacement Mapping



Pixel Displacement Mapping

- registering projections to such a surface by determining their intrinsic and extrinsic is too imprecise
 - non-linear lens distortion
 - errors in measuring fiducials
- rendering of 3D surface representation from perspective of projector might be to slow
 - high geometric complexity of model
 - many triangles to render
 - project, raster, texture
- measure per-pixel mapping between projector perspectives and target perspective (e.g., camera)
- render image from target perspective and map it (look-up) into perspective of projectors (e.g., pixel-shading)





Pixel Displacement Mapping

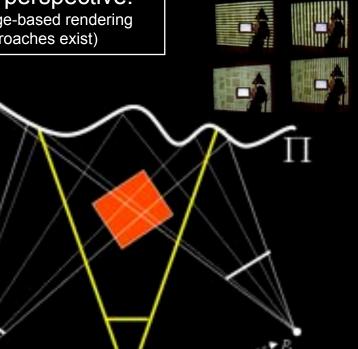
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problem:

works only for static target perspective! (but image-based rendering

approaches exist)

Ć2P.

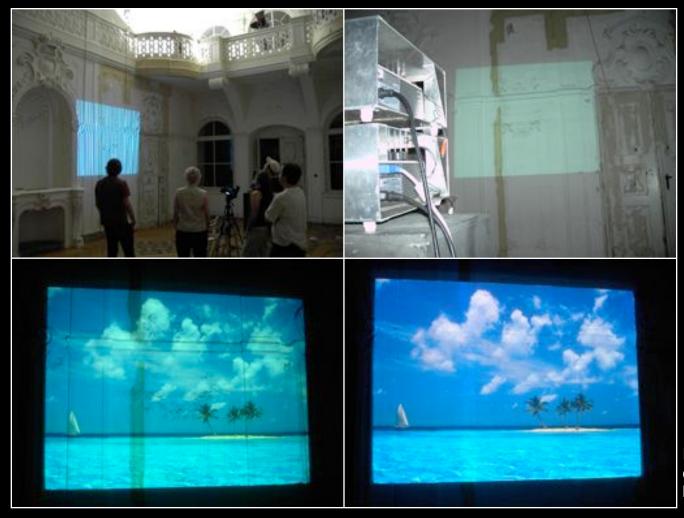




Example: Stucco Wall



Example: Stucco Wall



In coop. with castle Ettersburg



Example: Fossil Cast



Example: Fossil Cast



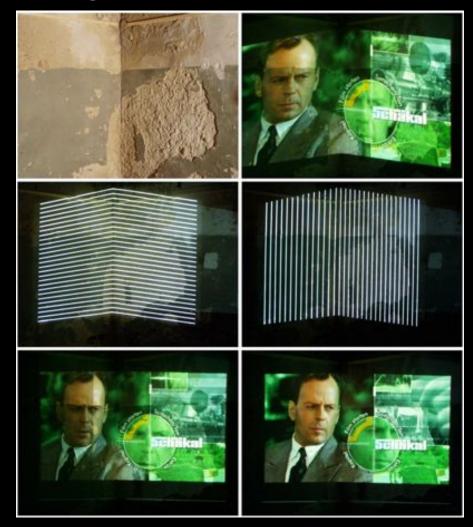
In coop. with Senckenberg Museum



Example: Scruffy Room Corner



Example: Scruffy Room Corner



Bimber et al., IEEE Computer 2005



Radiometric Compensation

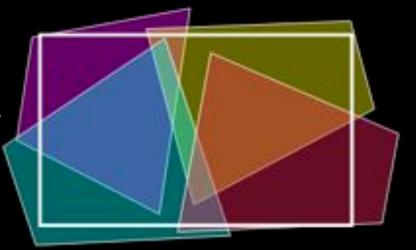


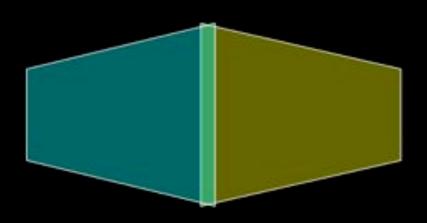
Photometric Calibration



Photometric Calibration

- regions of display surfaces that are illuminated by multiple projectors simultaneously appear brighter
- projectors can have different brightness and can cover a different color space
- result: inconsistent image (intensity and color)
- humans can perceive 2% difference in brightness and a color variation of 2nm
- variations in brightness is more critical than variation in color
- solutions: intensity blending and color space mapping
- these techniques are not explained here!
- we assume that projectors and cameras are linearized and color mapped



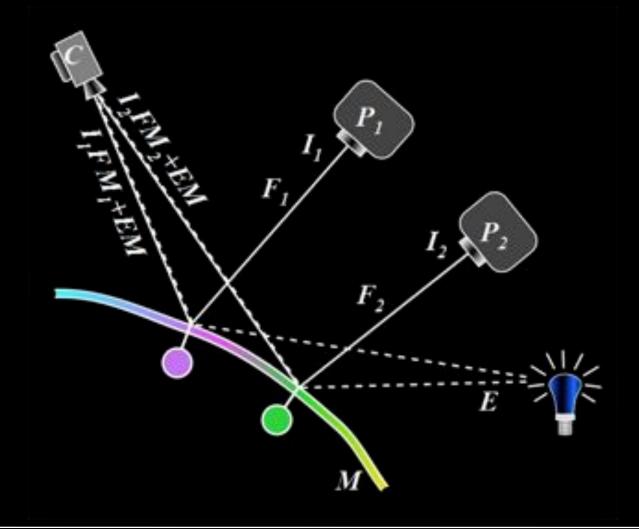




Compensating Local Light Effects

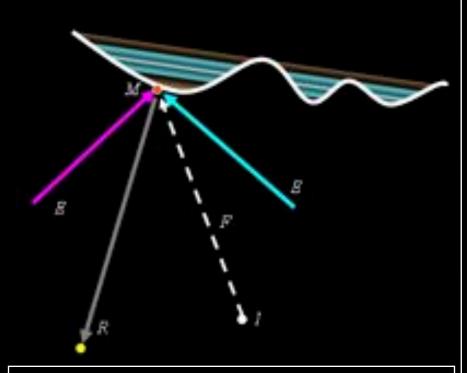


Compensating Local Light Effects









R=IFM+EM

I → projected image

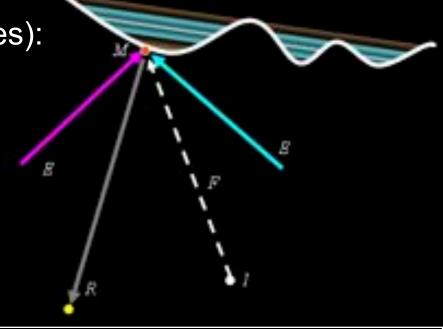
B → black-level

F → projector-2-surface form factor

E → environment light



determining parameters (textures):



R=IFM+EM

I → projected image

B → black-level

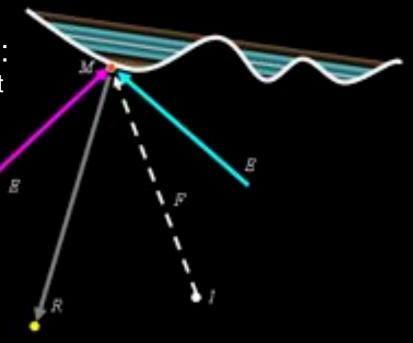
F → projector-2-surface form factor

E → environment light



determining parameters (textures):

(1) turn off environment light and project black flood image



R=IFM+EM

I → projected image

B → black-level

F → projector-2-surface form factor

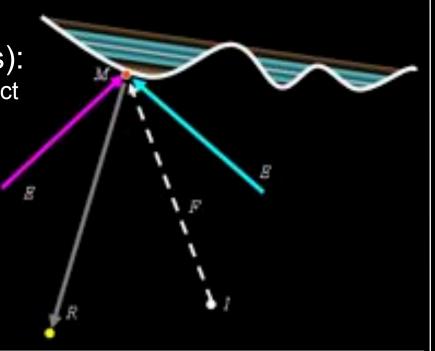
E → environment light



determining parameters (textures):

(1) turn off environment light and project black flood image

 $I=0,E=0 \rightarrow BFM$



R=IFM+EM

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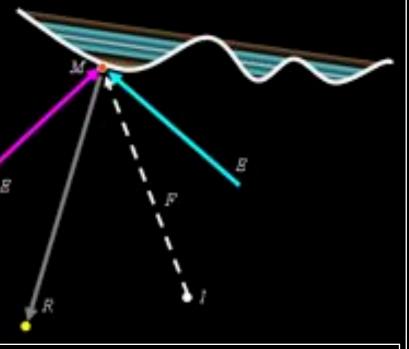


determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

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R=IFM+EM

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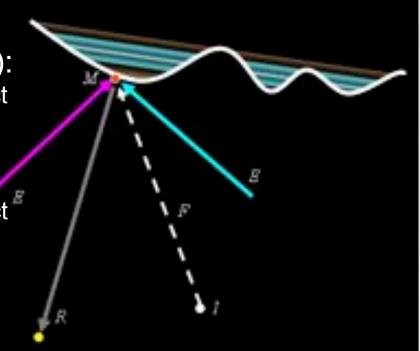
determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

$$l=0,E=1 \rightarrow EM \text{ (incl. BFM !)}$$



R=IFM+EM

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light



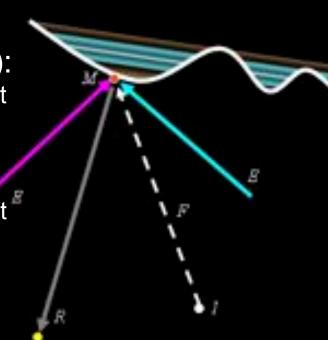
determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

(3) turn off environment light and



R=IFM+EM

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light



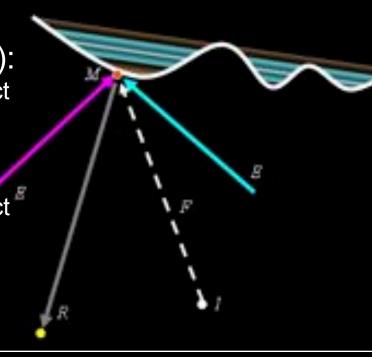
determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

(3) turn off environment light and project white flood image



R=IFM+EM

I → projected image

B → black-level

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determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

(3) turn off environment light and project white flood image



I → projected image

B → black-level

F → projector-2-surface form factor

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determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

(3) turn off environment light and project white flood image



I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light



determining parameters (textures):

(1) turn off environment light and project black flood image

$$I=0,E=0 \rightarrow BFM$$

(2) turn on environment light and project black flood image

(3) turn off environment light and project white flood image

compensation (per pixel):



I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

Bimber et al. IEEE

Computer 2005



Single Projector

determining parameters (textures):

- (1) turn off environment light and project black flood image
 - $I=0,E=0 \rightarrow BFM$
- (2) turn on environment light and project black flood image
 - **I=0,E=1** → **EM** (incl. **BFM**!)
- (3) turn off environment light and project white flood image

compensation (per pixel): I=(R-EM)/(FM)



- I → projected image
- B → black-level
- F → projector-2-surface form factor
- E → environment light
- M → surface reflectance (diffuse)



O. Bimber



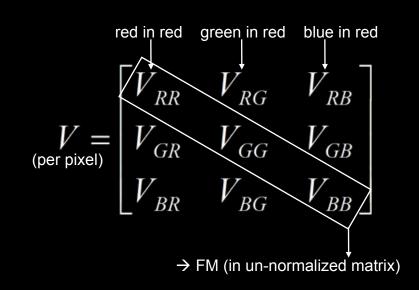
Nayar et al, CVPR 2004

red in red green in red blue in red
$$V_{RR} = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

R=V*I



Nayar et al, CVPR 2004

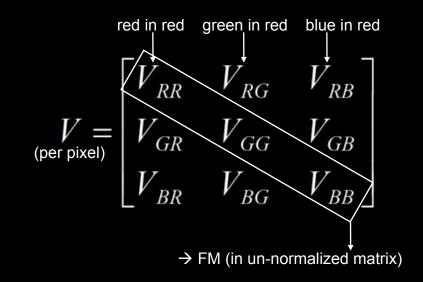


R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:



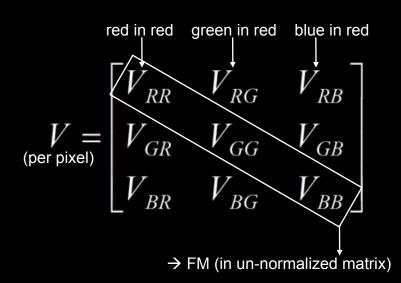




Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):





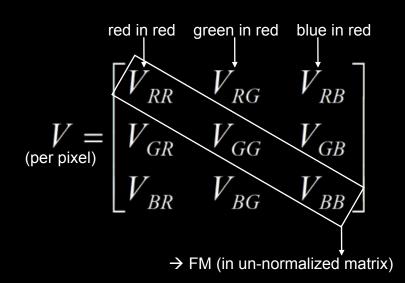


Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares







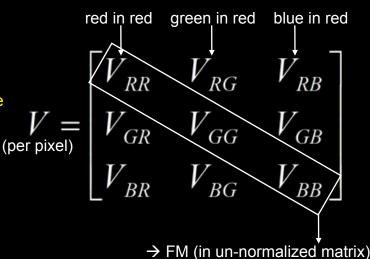
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determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):



R=V*I



Nayar et al, CVPR 2004

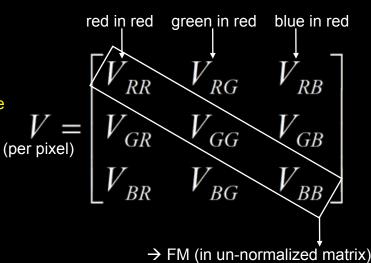
determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

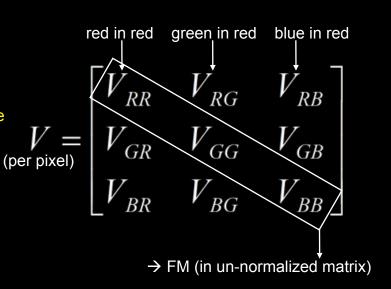
for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_i / \Delta I_i = \Delta C_i / \Delta R_i$



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

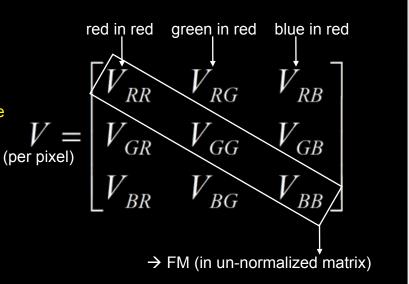
for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$ (since $V_{ii} = 1$, $\Delta I_i = \Delta C_i$)



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

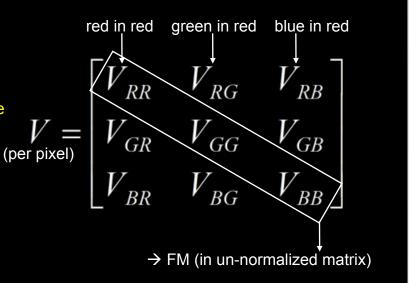
for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$

(since $V_{ii}=1$, $\Delta I_i=\Delta C_i$)

capture 6 images **C** (2 per color channel



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

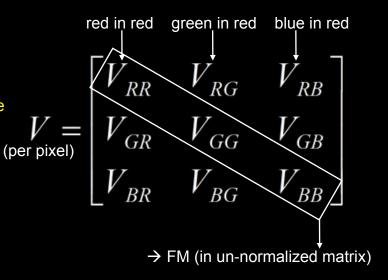
diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$

(since $V_{ii}=1$, $\Delta I_i=\Delta C_i$)

capture 6 images **C** (2 per color channel

to determine deltas)



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

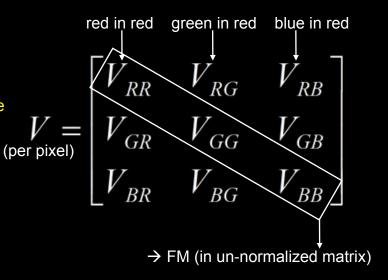
diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$

(since $V_{ii}=1$, $\Delta I_i=\Delta C_i$)

capture 6 images **C** (2 per color channel

to determine deltas)



R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

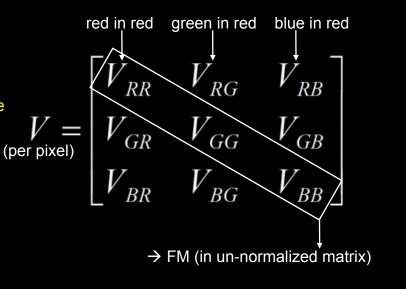
diagonals are 1 (unknown scaling)

off-diagonals are $\mathbf{V}_{ij} = \Delta \mathbf{C}_{j} / \Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{j} / \Delta \mathbf{R}_{i}$ (since $\mathbf{V}_{ii} = 1$, $\Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{i}$)

capture 6 images **C** (2 per color channel

to determine deltas)

compensation (per pixel):



I → projected image
 V → color mixing matrix
 (projector/camera/reflectance)

R=V*I



Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

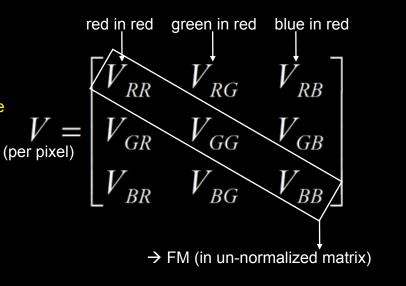
off-diagonals are $\mathbf{V}_{ij} = \Delta \mathbf{C}_{j} / \Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{j} / \Delta \mathbf{R}_{i}$ (since $\mathbf{V}_{ii} = 1$, $\Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{i}$)

capture 6 images **C** (2 per color channel

to determine deltas)

compensation (per pixel):

I=V-1*R (does not consider





Nayar et al, CVPR 2004

determining color mixing matrix V:

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images → least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $\mathbf{V}_{ij} = \Delta \mathbf{C}_{j} / \Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{j} / \Delta \mathbf{R}_{i}$ (since $\mathbf{V}_{ii} = 1$, $\Delta \mathbf{I}_{i} = \Delta \mathbf{C}_{i}$)

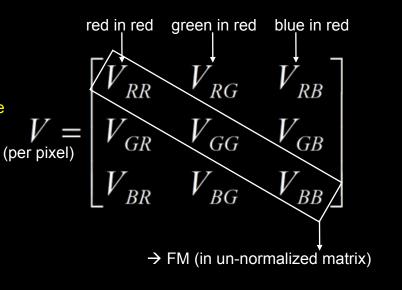
capture 6 images C (2 per color channel

to determine deltas)

compensation (per pixel):

I=V-1*R (does not consider

environment light!)



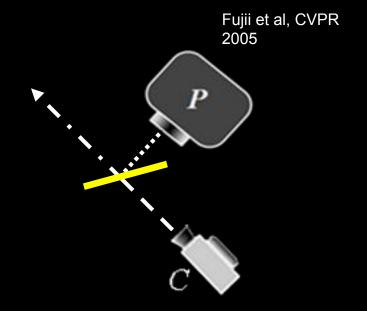
R=V*I



Dynamic Adaptation



Dynamic Adaptation



```
R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)
```

t → time index

I_t → projected image at t

 $V_0 \rightarrow un$ -normalized color mixing

matrix at t=0 (const.)

M_t → material at t

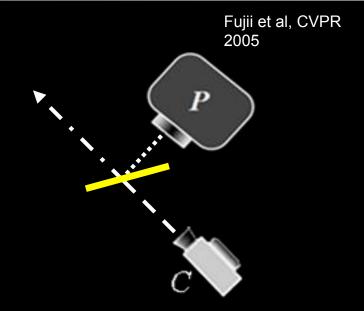
 $M_0 \rightarrow \text{material at t=0}$

E_t → environment light at t=0



Dynamic Adaptation

determining color mixing matrix V₀:



```
R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)
```

 $t \rightarrow time index$

 $I_t \rightarrow \text{projected image at t}$

V₀ → un-normalized color mixing

matrix at t=0 (const.)

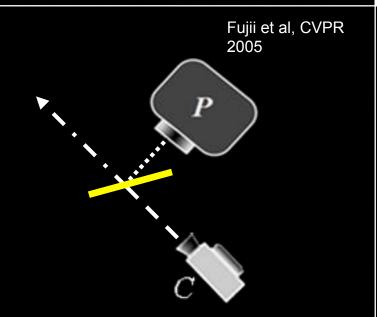
 $M_t \rightarrow material at t$

 $M_0 \rightarrow \text{material at t=0}$

 $E_t \rightarrow environment light at t=0$



determining color mixing matrix V₀: similar as before: **V**_{ij}= Δ **C**_j/ Δ **I**_i



```
R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)
```

 $t \rightarrow time index$

 $I_t \rightarrow \text{projected image at t}$

 $V_0 \rightarrow$ un-normalized color mixing

matrix at t=0 (const.)

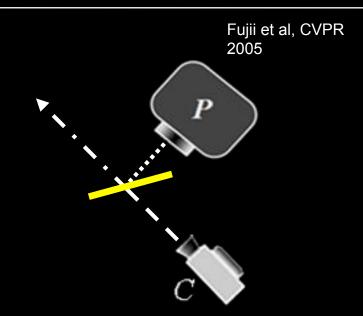
 $M_t \rightarrow material at t$ $M_0 \rightarrow material at t=0$

E, → environment light at t=0



determining color mixing matrix V₀:

similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_{j} / \Delta \mathbf{I}_{i}$ (un-normalized!)



$R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)$

 $t \rightarrow time index$

I_t → projected image at t

 $V_0 \rightarrow un$ -normalized color mixing

matrix at t=0 (const.)

 $M_t \rightarrow material at t$

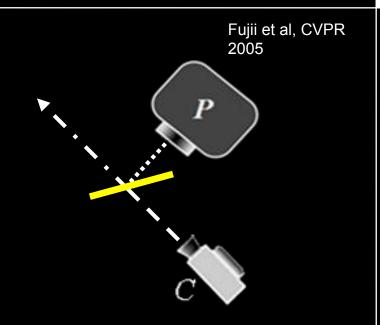
 $M_0 \rightarrow \text{material at t=0}$

E_t → environment light at t=0



determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment



```
R_{t}=M_{t}/M_{0}^{*}(E_{t}^{*}M_{0}^{+}V_{0}^{*}I_{t})
t \rightarrow \text{time index}
I_{t} \rightarrow \text{projected image at t}
```

V₀ → un-normalized color mixing matrix at t=0 (const.)

M₁ → material at t

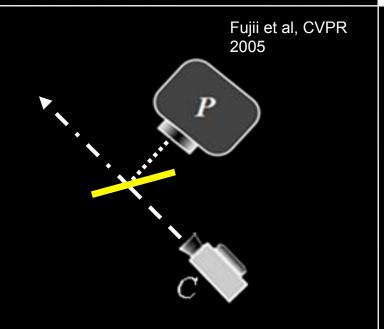
 $M_0 \rightarrow \text{material at t=0}$

 $E_t \rightarrow \text{environment light at t=0}$



determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:



```
R_t=M_t/M_0*(E_t*M_0+V_0*I_t)

t \rightarrow time index
I_t \rightarrow projected image at t
V_0 \rightarrow un-normalized color mixing
matrix at t=0 (const.)
M_t \rightarrow material at t
M_0 \rightarrow material at t=0
```

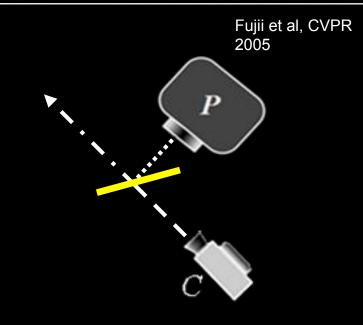
 $E_t \rightarrow$ environment light at t=0



determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:

 $E_0*M_0=C-V_0*I$ (project



```
R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)

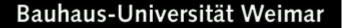
t \rightarrow time index

I_t \rightarrow projected image at t

V_0 \rightarrow un-normalized color mixing

matrix at t=0 (const.)

M_t \rightarrow material at t
```



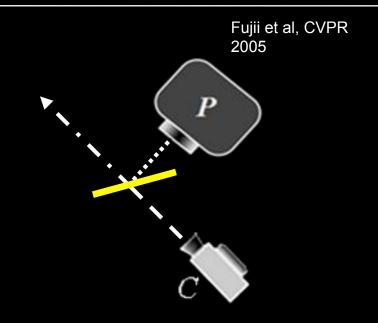


determining color mixing matrix V₀:

similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_{j} / \Delta \mathbf{I}_{i}$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:

 $E_0^*M_0=C-V_0^*I$ (project arbitrary I and capture C)



```
R_t = M_t / M_0^* (E_t^* M_0 + V_0^* I_t)

t \rightarrow time index
I_t \rightarrow projected image at t
V_0 \rightarrow un-normalized color mixing
matrix at t=0 (const.)
M_t \rightarrow material at t
M_0 \rightarrow material at t=0
E_t \rightarrow environment light at t=0
```

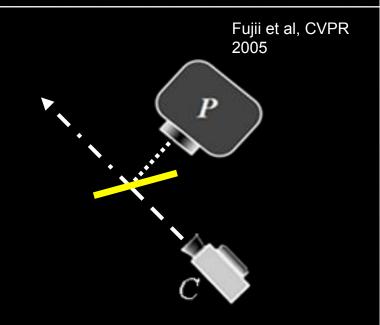


determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:

 $E_0^*M_0=C-V_0^*I$ (project arbitrary I and capture C)

compensation (per pixel at t):



```
R_t=M_t/M_0*(E_t*M_0+V_0*I_t)

t \rightarrow time index
I_t \rightarrow projected image at t
V_0 \rightarrow un-normalized color mixing
matrix at t=0 (const.)
M_t \rightarrow material at t
M_0 \rightarrow material at t=0
E_t \rightarrow environment light at t=0
```

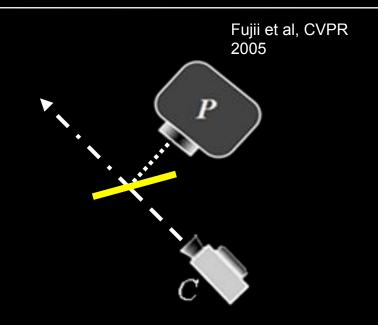


determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:

 $E_0^*M_0=C-V_0^*I$ (project arbitrary I and capture C)

compensation (per pixel at t): $I_{t}=V_{0}^{-1*}(\mathbf{R}^{*}\mathbf{M}_{0}/\mathbf{M}_{t-1}-\mathbf{E}_{t-1}^{*}\mathbf{M}_{0})$



```
R_t=M_t/M_0*(E_t*M_0+V_0*I_t)

t \rightarrow time index
I_t \rightarrow projected image at t
V_0 \rightarrow un-normalized color mixing
matrix at t=0 (const.)
M_t \rightarrow material at t
M_0 \rightarrow material at t=0
E_t \rightarrow environment light at t=0
```

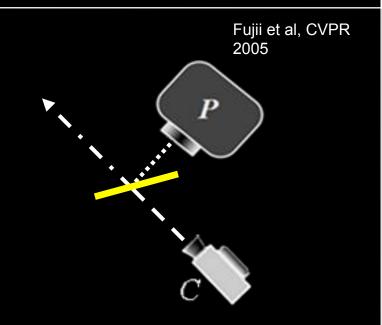


determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light E_0*M_0 at t=0:

 $E_0^*M_0=C-V_0^*I$ (project arbitrary I and capture C)

compensation (per pixel at t): $I_t=V_0^{-1*}(R^*M_0/M_{t-1}-E_{t-1}^*M_0)$ $\rightarrow E_{t-1}^*M_0$ approx. $E_0^*M_0$



```
R_t=M_t/M_0*(E_t*M_0+V_0*I_t)

t \rightarrow time index

I_t \rightarrow projected image at t

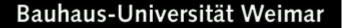
V_0 \rightarrow un-normalized color mixing

matrix at t=0 (const.)

M_t \rightarrow material at t

M_0 \rightarrow material at t=0

E_t \rightarrow environment light at t=0
```



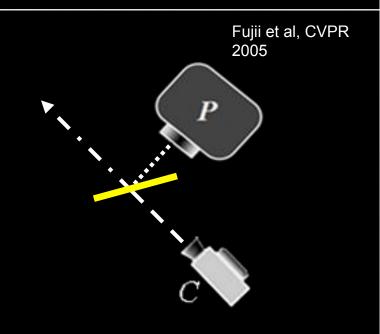


determining color mixing matrix V_0 : similar as before: $\mathbf{V}_{ij} = \Delta \mathbf{C}_j / \Delta \mathbf{I}_i$ (un-normalized!)

determine reflected environment light $E_0^*M_0$ at t=0:

E₀***M**₀=**C**-**V**₀***I** (project arbitrary I and capture C)

compensation (per pixel at t): $I_{t}=V_{0}^{-1*}(R^{*}M_{0}/M_{t-1}-E_{t-1}^{*}M_{0})$ $\rightarrow E_{t-1}^{*}M_{0} \text{ approx. } E_{0}^{*}M_{0}$ $\rightarrow M_{0}/M_{t-1}=C_{0}/C_{t-1}$



```
R_t=M_t/M_0*(E_t*M_0+V_0*I_t)

t \rightarrow time index

I_t \rightarrow projected image at t

V_0 \rightarrow un-normalized color mixing

matrix at t=0 (const.)

M_t \rightarrow material at t

M_0 \rightarrow material at t=0

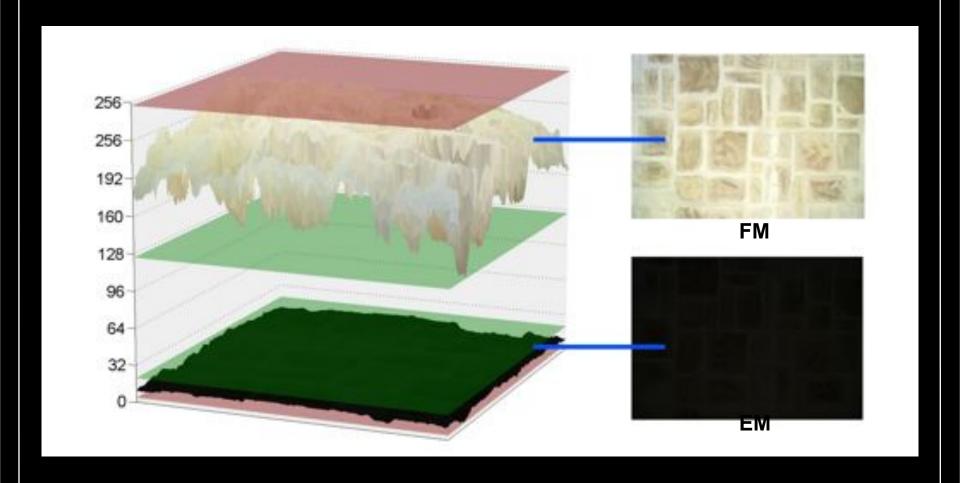
E_t \rightarrow environment light at t=0
```



Limited Dynamic Range and Brightness

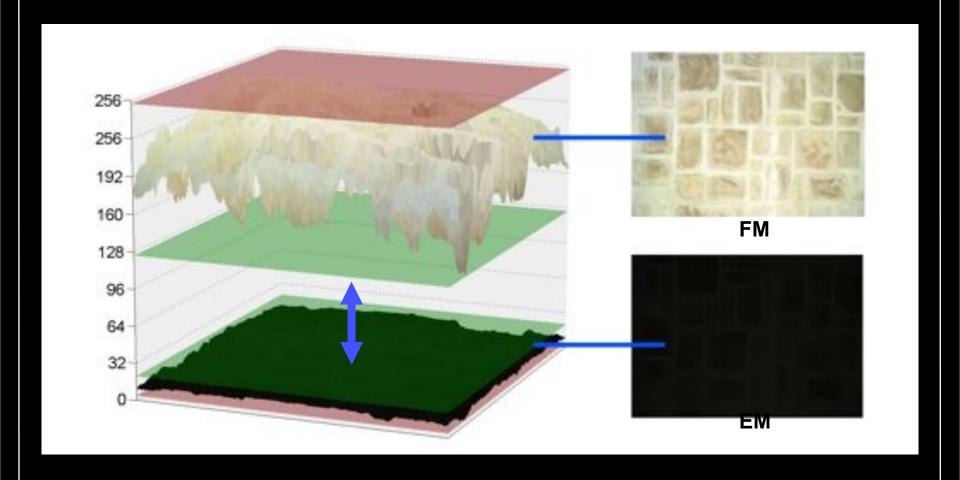


Limited Dynamic Range and Brightness



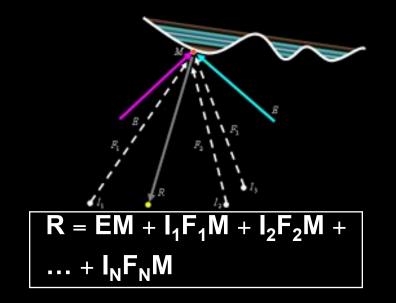


Limited Dynamic Range and Brightness



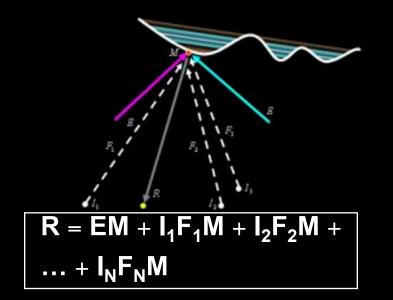








strategy: balance intensity load

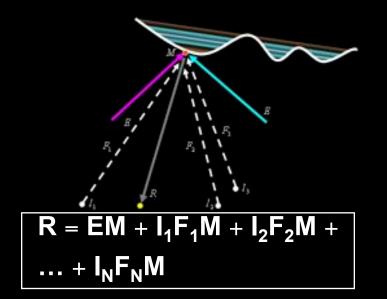




strategy: balance intensity load

 assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$

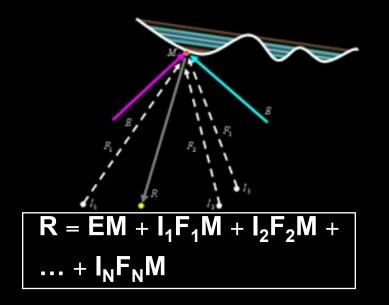




strategy: balance intensity load

 assume: total intensity is equally balanced among multiple low-capacity units

$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$



$$R = EM + I_{i}(F_{1}M + F_{2}M + ... + F_{N}M)$$

$$\rightarrow EM + I(F_{1} + F_{2} + ... + F_{N})M$$



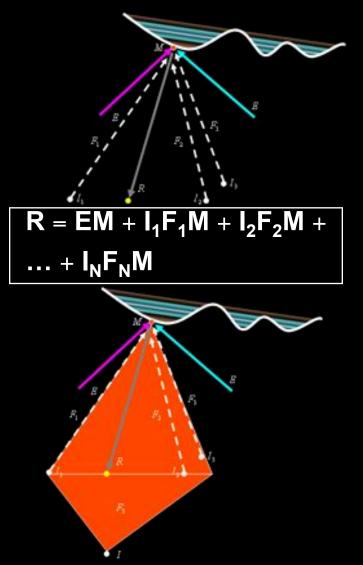
strategy: balance intensity load

 assume: total intensity is equally balanced among multiple low-capacity units

$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$

$$R = EM + Ii(F1M + F2M + ... + FNM)$$

$$\rightarrow EM+I(F1+F2+...FN)M$$





strategy: balance intensity load

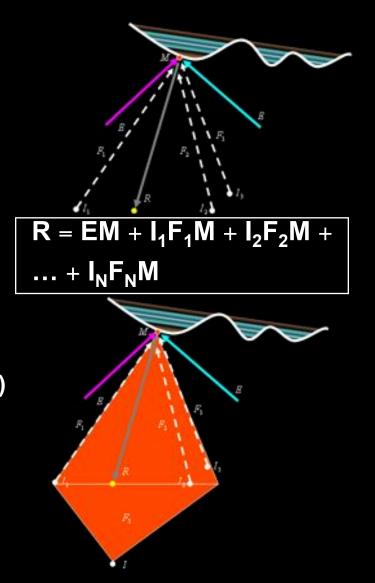
 assume: total intensity is equally balanced among multiple low-capacity units

$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$

 this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + Ii(F1M + F2M + ... + FNM)$$

$$\rightarrow EM+I(F1+F2+...FN)M$$





strategy: balance intensity load

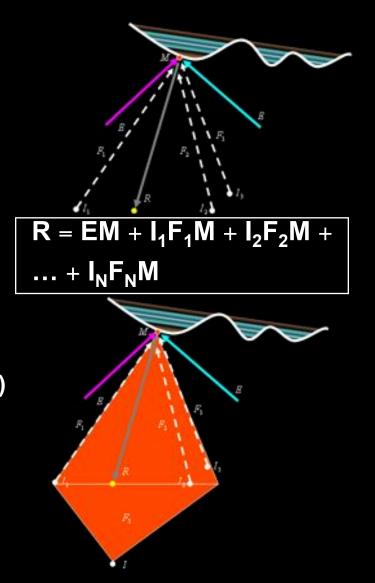
 assume: total intensity is equally balanced among multiple low-capacity units

$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$

 this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + Ii(F1M + F2M + ... + FNM)$$

$$\rightarrow EM+I(F1+F2+...FN)M$$





strategy: balance intensity load

 assume: total intensity is equally balanced among multiple low-capacity units

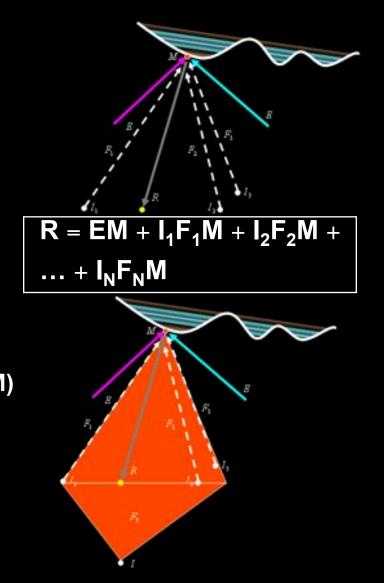
$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$

 this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + Ii(F1M + F2M + ... + FNM)$$

$$\rightarrow EM+I(F1+F2+...FN)M$$

compensation (per pixel):





strategy: balance intensity load

 assume: total intensity is equally balanced among multiple low-capacity units

$$I_{i} = I_{1} = I_{2} = \dots = I_{N}$$

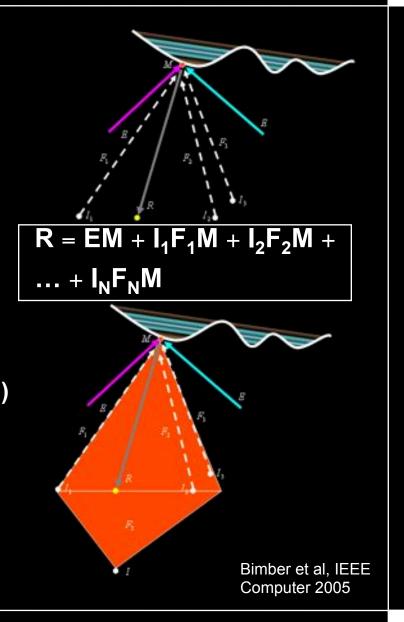
 this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + Ii(F1M + F2M + ... + FNM)$$

$$\rightarrow EM+I(F1+F2+...FN)M$$

compensation (per pixel):

$$\begin{split} \textbf{I}_i &= (\textbf{R-EM})/(\textbf{F}_1\textbf{M} + \textbf{F}_2\textbf{M} + \dots + \textbf{F}_N\textbf{M}) \\ &\quad \text{remember: } \textbf{F}_i\textbf{M} = \textbf{F}_i\textbf{M} - \textbf{B}_i\textbf{F}_i\textbf{M} & ! \\ &\quad \text{or } \textbf{B}\textbf{F}\textbf{M} = \textbf{B}_1\textbf{F}_1\textbf{M} + \dots + \textbf{B}_i\textbf{F}_i\textbf{M} \end{split}$$





Considering Human Visual Perception



Considering Human Visual Perception

threshold map (Ramasubramanian et al. Siggraph'99)

- computes for every pixel of an image R
 the amount of luminance difference that
 is imperceptible
- considers contrast, luminance and spatial frequency in local neighborhood



- compute and apply a single (global) scaling factor R'=R*α that minimizes the perceived error (Wang, et al. 2005, only monochrome, not real-time, single projector)
- coming soon: color, real-time, global and local adaptation, potentially multiple projectors



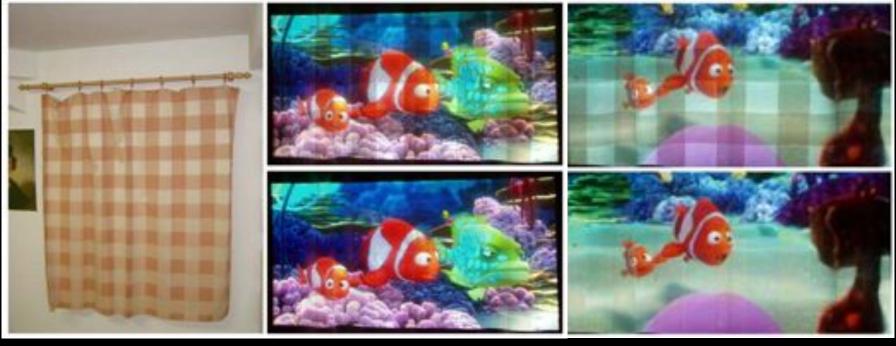




Example: Curtain



Example: Curtain



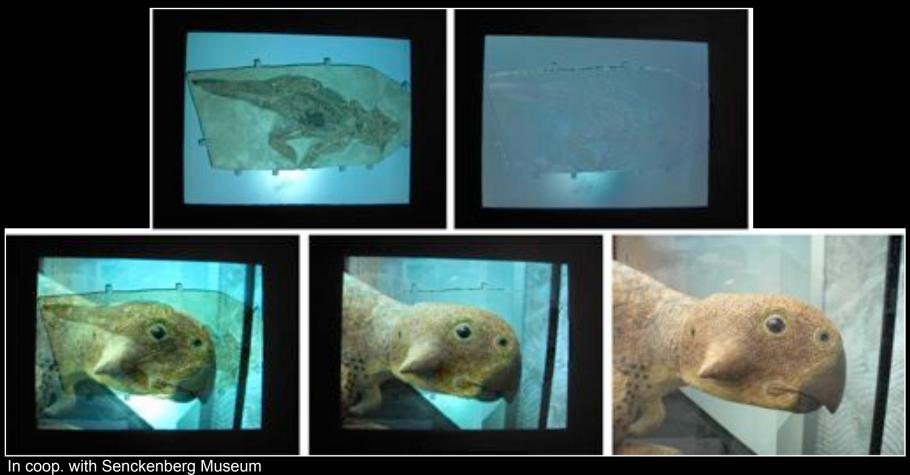
Bimber et al, IEEE Computer 2005



Example: Fossil



Example: Fossil



coop. with Selickenberg Museum



Example: Natural Stone Wall



Example: Natural Stone Wall







Bimber et al, IEEE Computer 2005 In coop. with Bennert Group



Example: Wallpaper



Example: Wallpaper



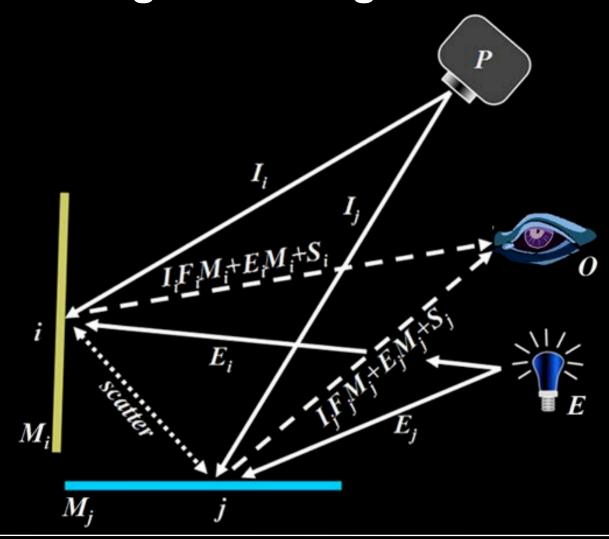
Bimber et al, IEEE Computer 2005



Compensating Global Light Effects



Compensating Global Light Effects

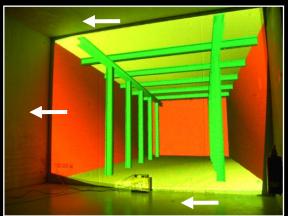


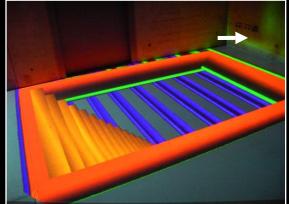


Compensating Diffuse Scattering



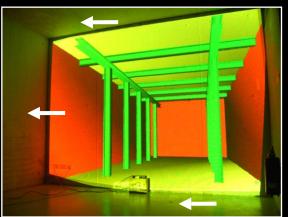
Bimber et al, IEEE/ACM ISMAR 2005

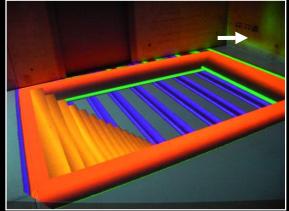




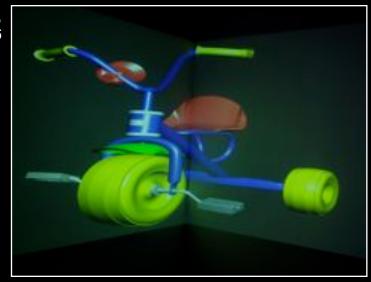


Bimber et al, IEEE/ACM ISMAR 2005



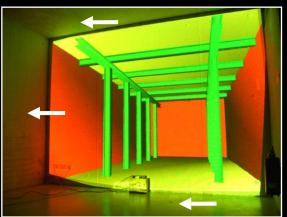


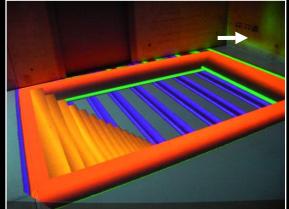
Bimber et al, IEEE VR, 2006



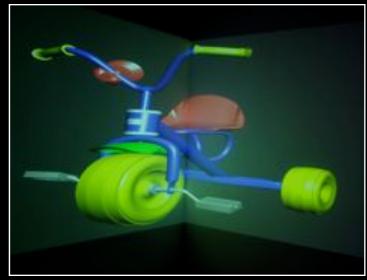


Bimber et al, IEEE/ACM ISMAR 2005



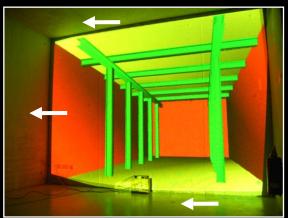


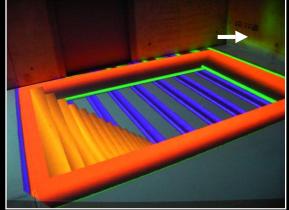
Bimber et al, IEEE VR, 2006





Bimber et al, IEEE/ACM ISMAR 2005





Bimber et al, IEEE VR, 2006



details:

IEEE VR talk on Wednesday morning (8:30am), session on tracking and projection displays

see demo!



Advanced Techniques View-Dependence

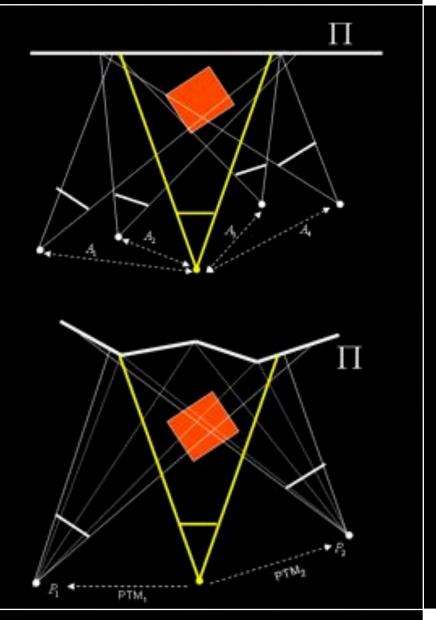


Non-Complex Surfaces



Non-Complex Surfaces

- view-dependent geometry correction can be compute if geometry is known
- for example:
 - planar/multi-plane: offaxis projection
 - parametric: warping via parametric description
 - scanned/modelled: projective texture mapping

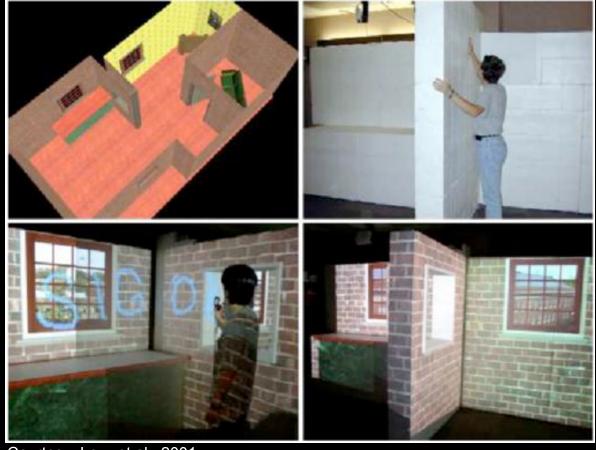




Example: Life-Sized Projector-Based Dioramas



Example: Life-Sized Projector-Based Dioramas



Courtesy: Low, et al., 2001



Complex Surfaces



Complex Surfaces

- if geometry is unknown image-based rendering helps
- sample geometric and radiometric parameters from multiple (source) camera (perspective)
- for novel (destination) camera
 - compute weighted penalties:

$$p_j = \alpha a_j + (1 - \alpha)b_j$$

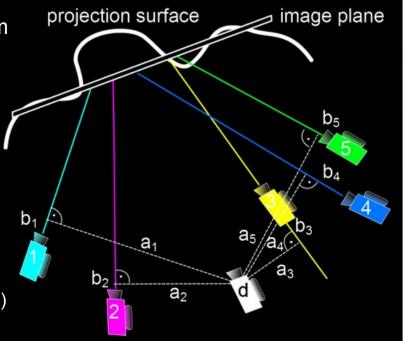
select k best perspectives (lowest penalties) and normalize them:

$$w_{j} = \left(1 - \frac{p_{j}}{\max_{pk}}\right) \frac{1}{p_{j}}$$
 interpolate new parameter textures (P_i2C_j, F_{ij}M, E_{ij}M)

and direction vector for destination perspective to render new IP:

$$t_d = \sum_{j=1}^{k} w_j t_j$$

- $t_d = \sum\nolimits_j^k w_j t_j$ lookups in F_{ij}M, E_{ij}...polated P_i2C_i
- lookups in IP with interpolated P_i2C_i





Example: Tracking and Stereo



Example: Tracking and Stereo



Bimber et al, IEEE/ACM ISMAR 2005



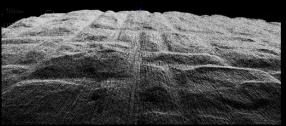
Depth and Occlusion

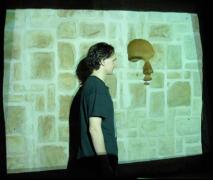


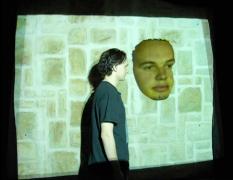
Depth and Occlusion













Bimber et al, IEEE/ACM ISMAR 2005



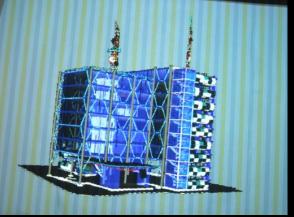


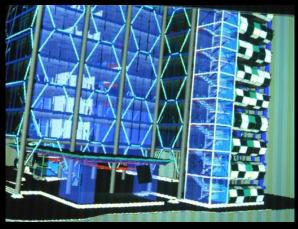
Example: Stereo on Wallpaper

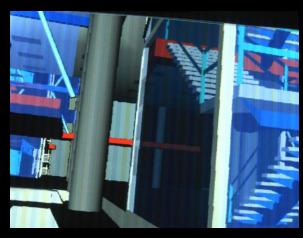


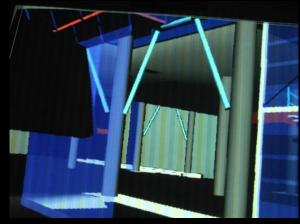
Example: Stereo on Wallpaper

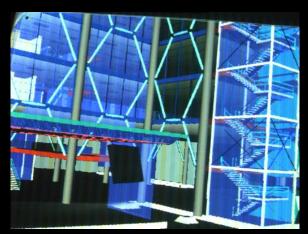












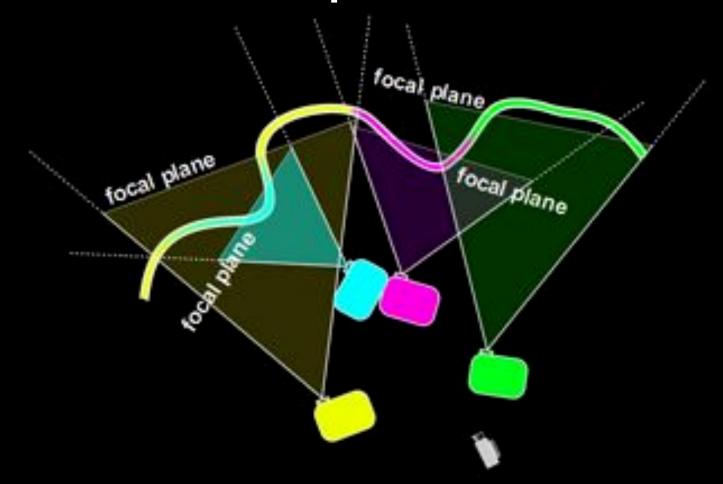
Bimber et al, IEEE/ACM ISMAR 2005



Advanced Techniques Multi-Focal Projection



Multi-Projector-Camera Technique that Increases Focal Depth





Determining Defocus



Determining Defocus

- structured light projection of grid point samples (2- dimensional phase shift)
 - pre-correction: geometric and radiometric correction (corrected grid points must be observed in camera)

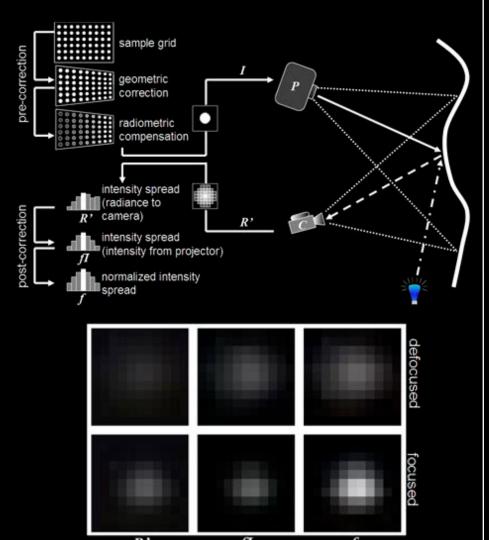
$$I_{\rm x,y} = (R_{\rm x,y} - EM_{\rm x,y})/FM_{\rm x,y}$$

post-correction:

$$R'_{x',y'} = fI_{x,y}FM_{x',y'} + EM_{x',y'}$$

$$fI_{x,y} = \frac{(R'_{x',y'} - EM_{x',y'})}{FM_{x',y'}}$$
 $f = \frac{fI_{x,y}}{FM_{x',y'}}$

 the normalized intensity appeared texture f serves as basis to estimate focus measures (e.g., via FFT/DCT, intensity loss, point spread, etc.)

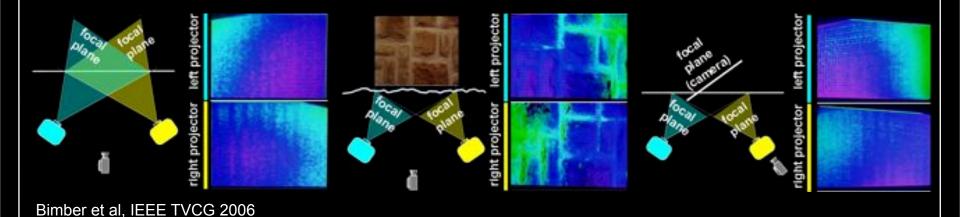




Example: Different Configurations



Example: Different Configurations





Example: Shifting Focal Plane



Example: Shifting Focal Plane

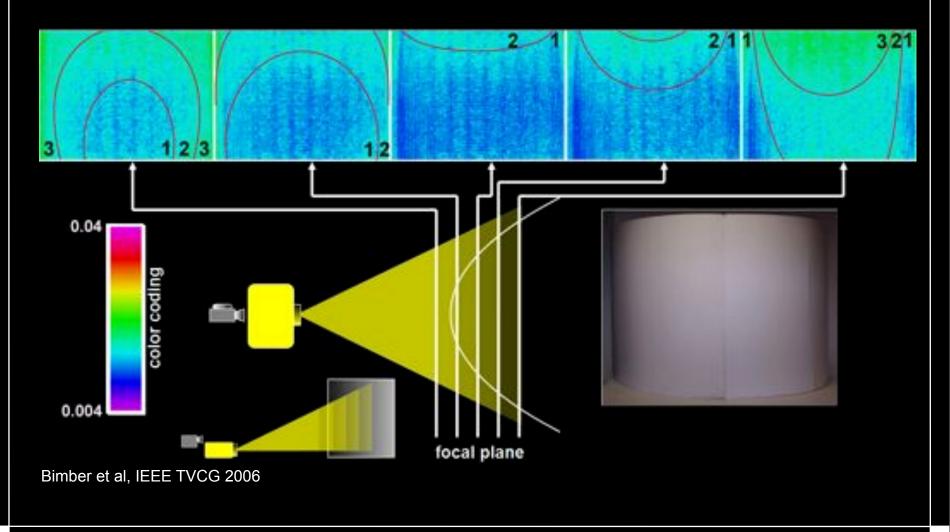




Image Composition



Image Composition

- using the focus values of each projector's pixels $(\Phi_{i,x,y})$, compose an image with minimal total defocus

$$I_i = \frac{w_i (R - EM)}{\sum_{j=1}^{N} w_j FM_j} \quad w_{i,x,y} = \frac{\Phi_{i,x,y}}{\sum_{j=1}^{N} \Phi_{j,x,y}}$$

 weighted composition: compute normalized weight and multiply it with FM and I

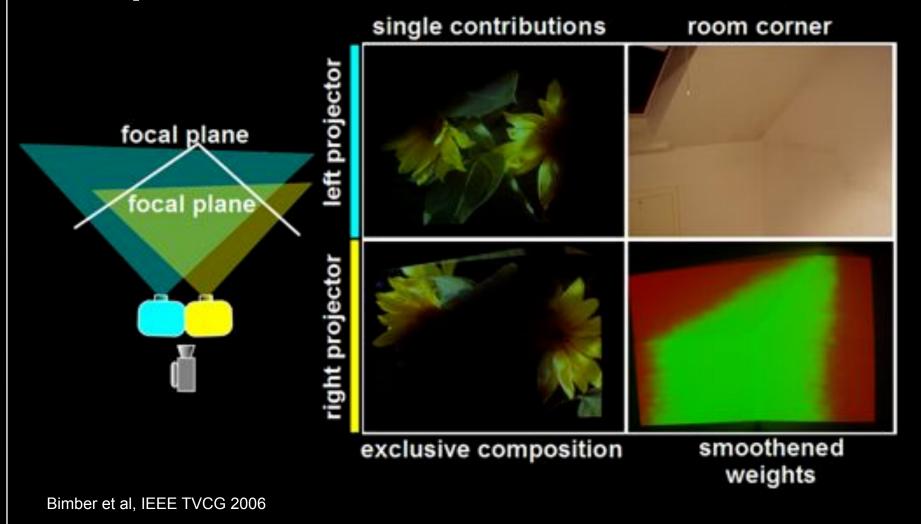
$$I_{i} = w_{i}(R-EM)/FM_{i}, \quad w_{i} = \begin{cases} 1 & \Phi_{i,x,y} \geq \Phi_{j,x,y} \\ 0 & else \end{cases}$$



Example: Room Corner



Example: Room Corner

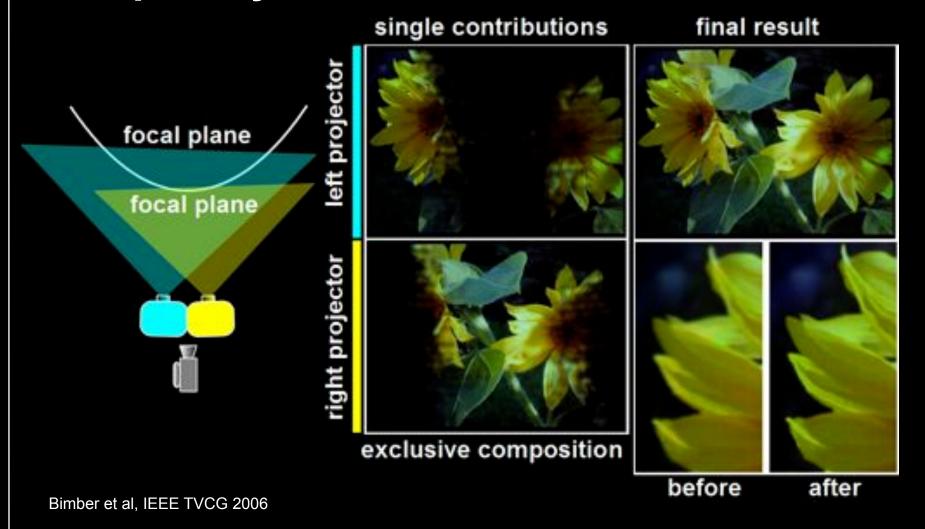




Example: Cylindrical Surface



Example: Cylindrical Surface

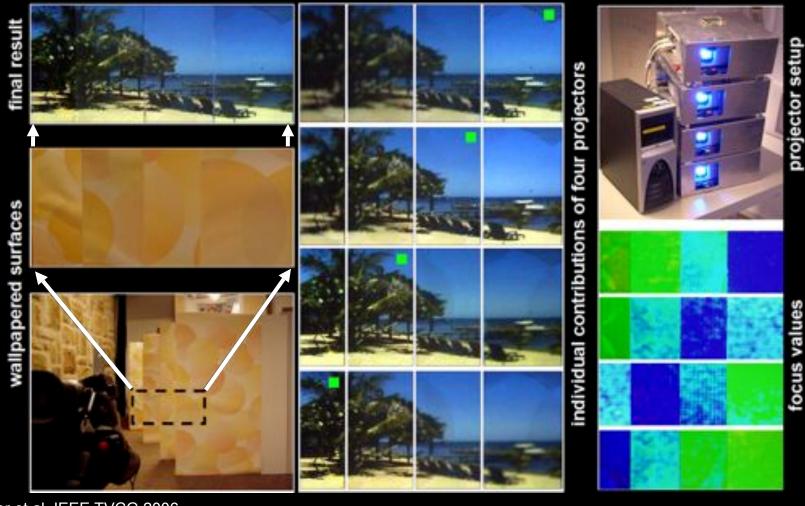




Example: Large Focal Depth



Example: Large Focal Depth



Bimber et al, IEEE TVCG 2006

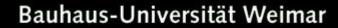


Advanced Techniques Light Transport



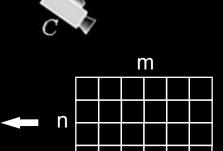
Acquisition

O. Bimber

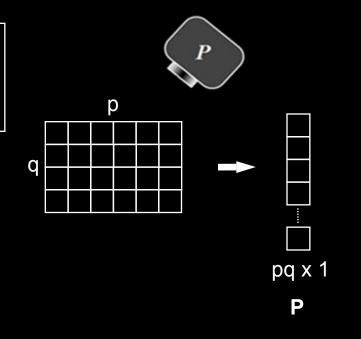




Acquisition



single camera & projector capture 4D slice of 8D reflectance field



mn x 1

C

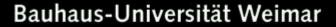
$$c = Tp$$

T =

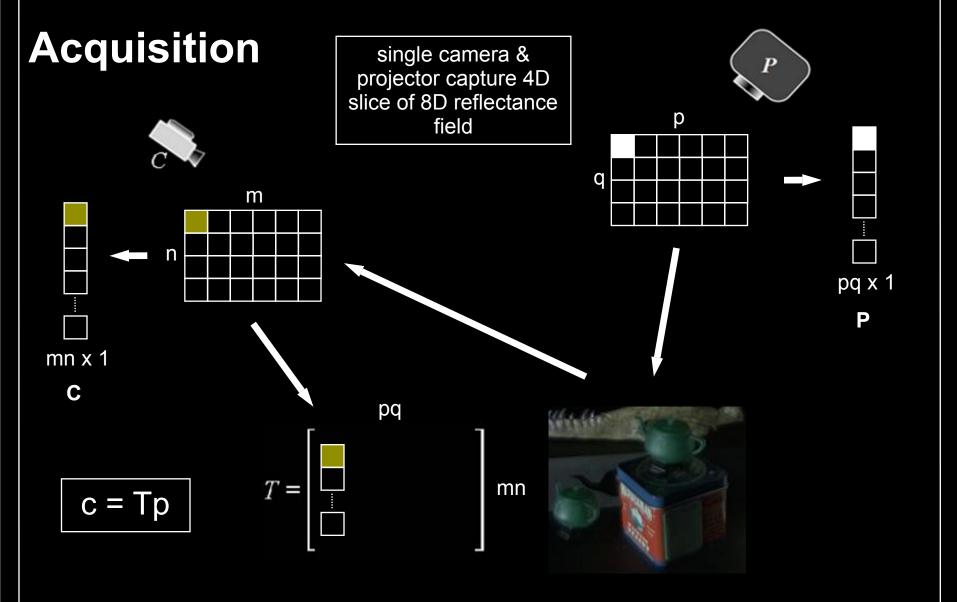
pq

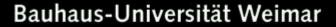
mn



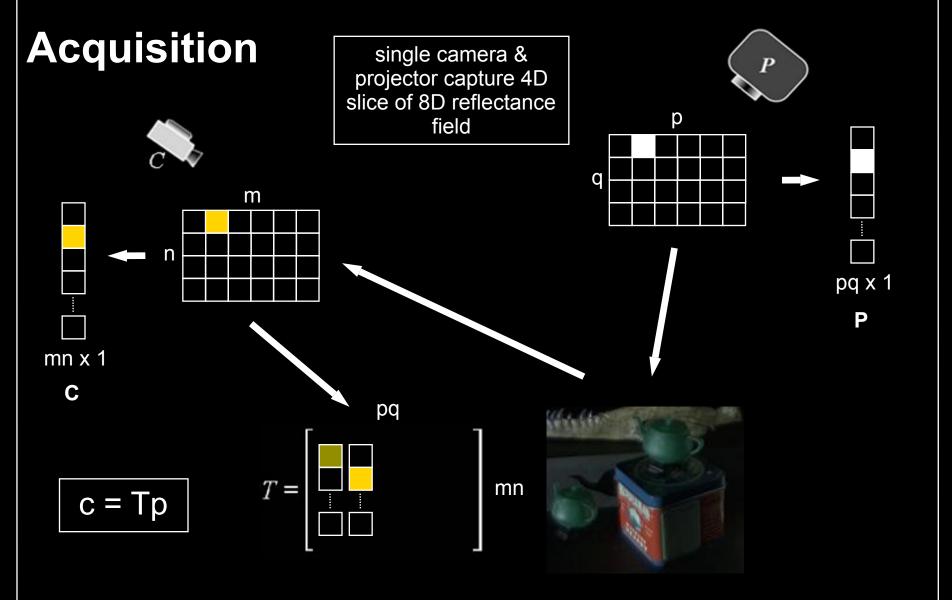


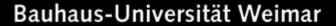




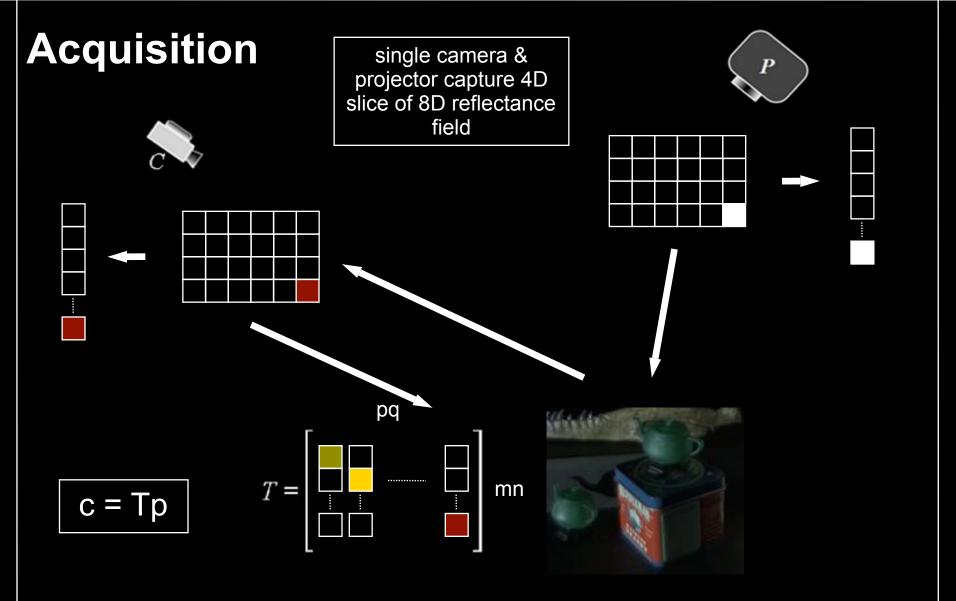


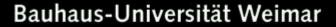




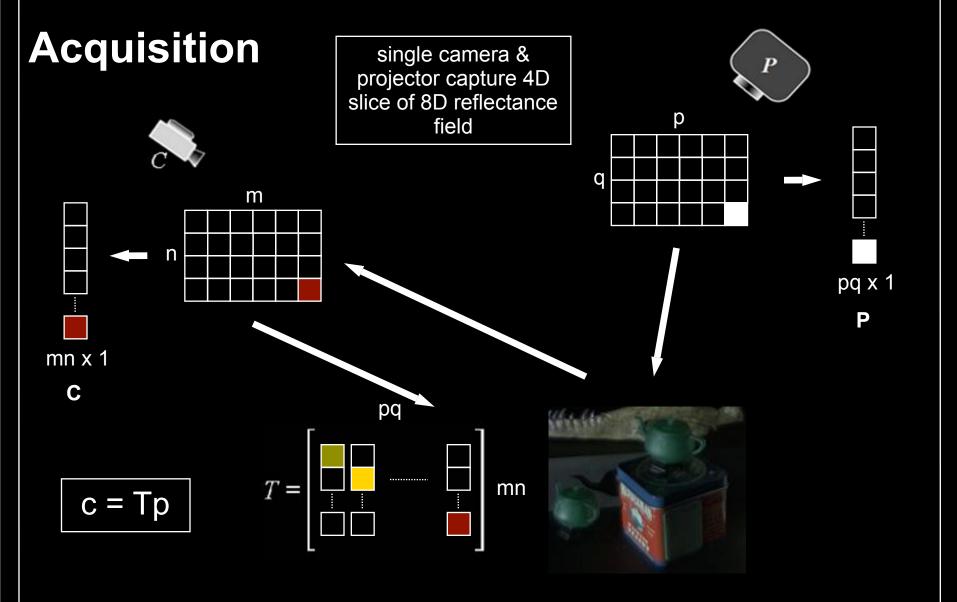


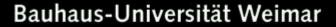




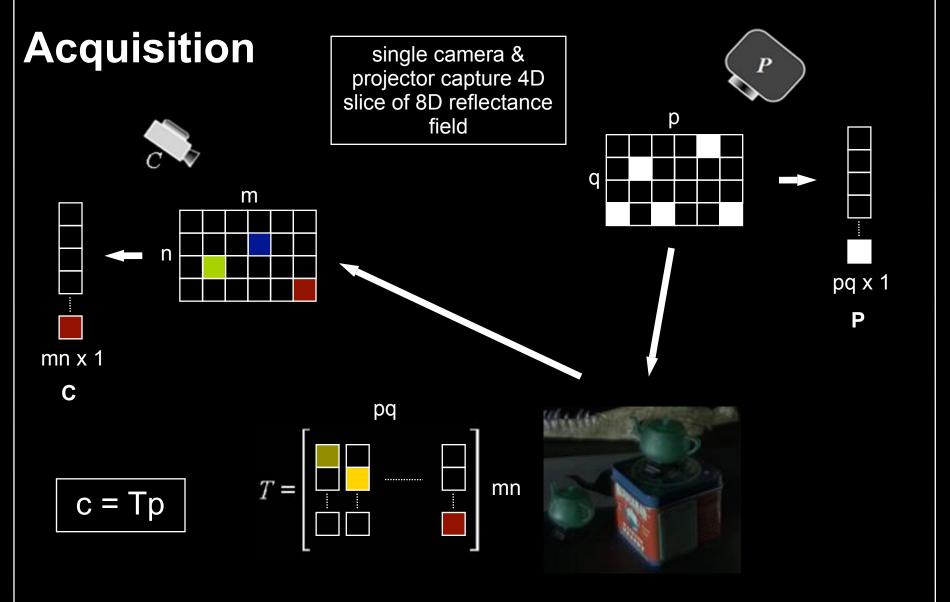


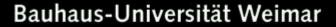




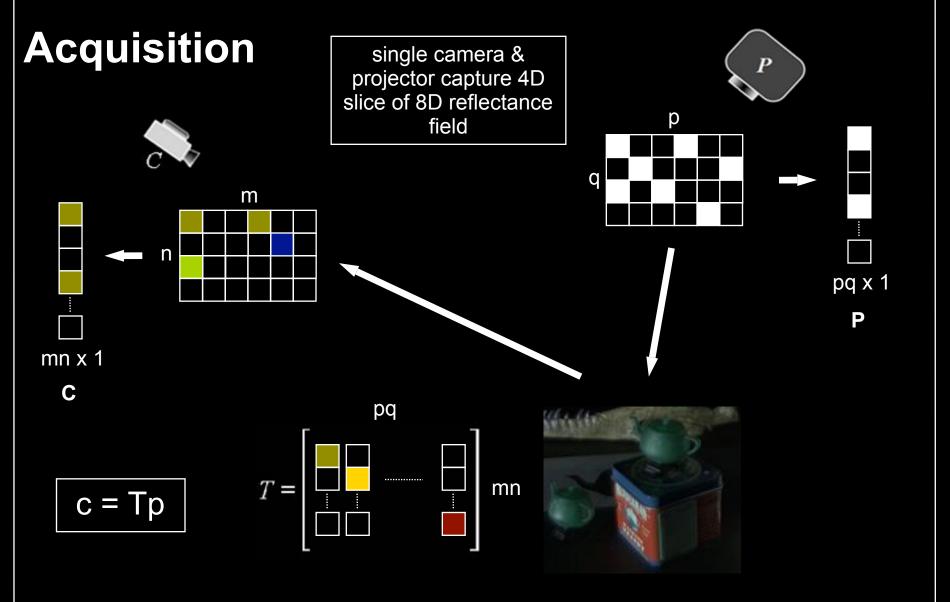


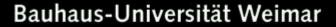




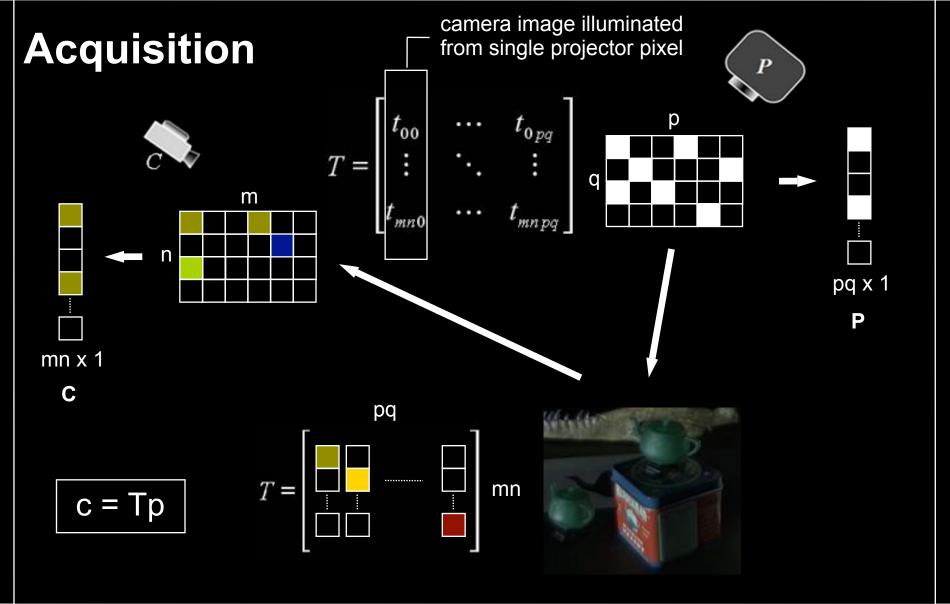




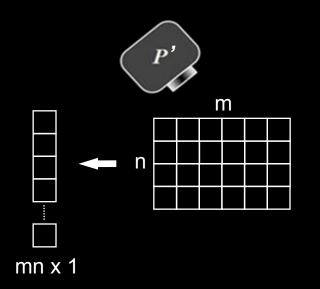




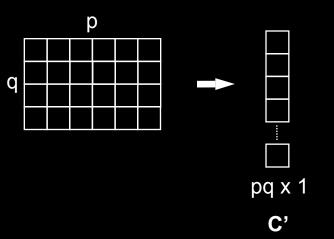


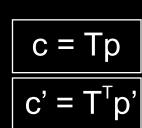










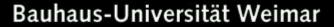


$$T = \begin{bmatrix} & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \end{bmatrix} mn$$

mn

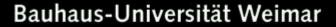
P'







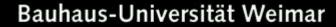
















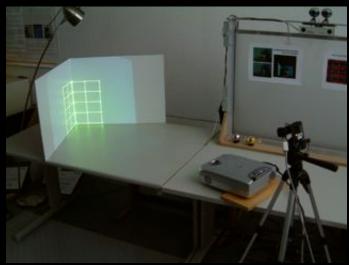
more information on dual photography: Sen,et al., Siggraph'05





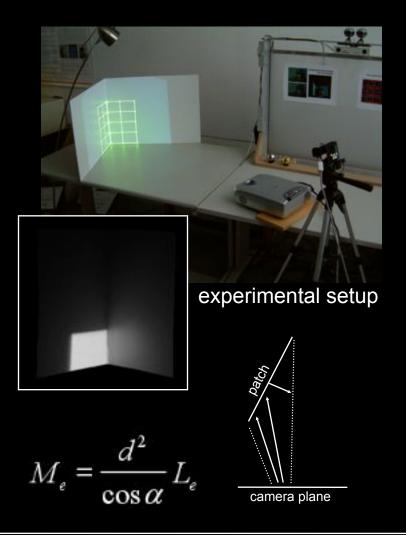




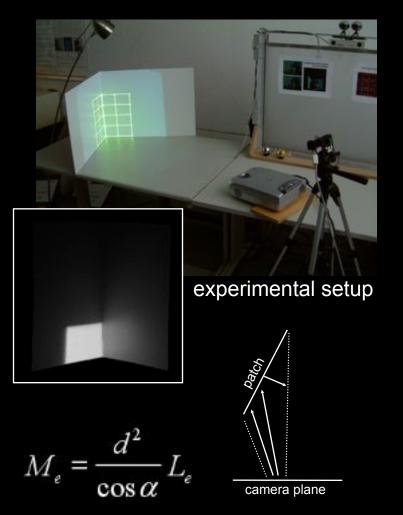


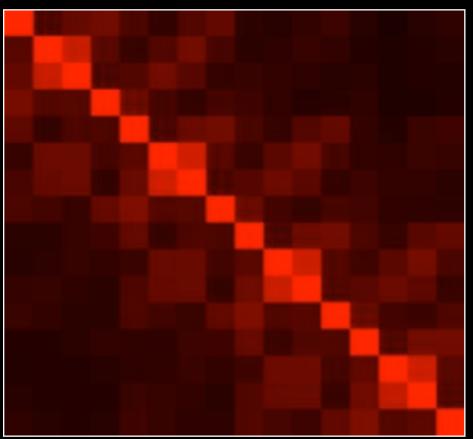
experimental setup











measured 16x16 form-factor matrix (computed from light transport matrix)

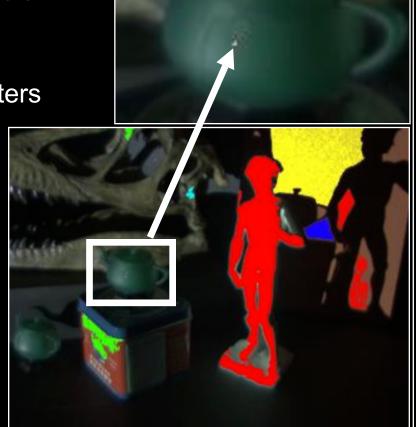


Global Radiometric Compensation



Global Radiometric Compensation

- traditional radiometric compensation requires direct projector-camera pixel correspondence
- include arbitrary global illumination effects using T
- apply inverse light transport T⁻¹C=P
- since T is huge, decompose it into clusters and solve in real-time on GPU

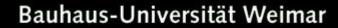




Outlook

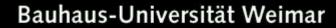


Multi-Projector Techniques for Real-Time Visualizations in Everyday Environments

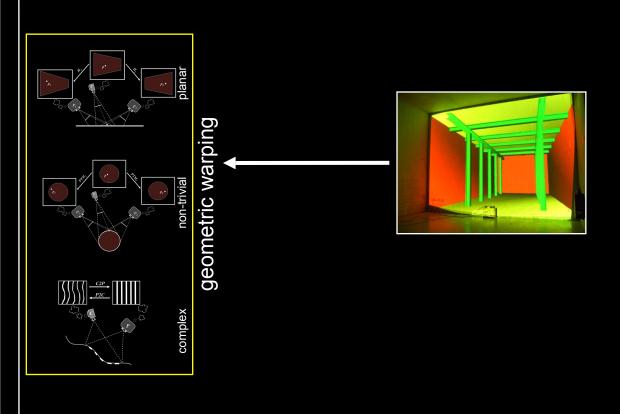






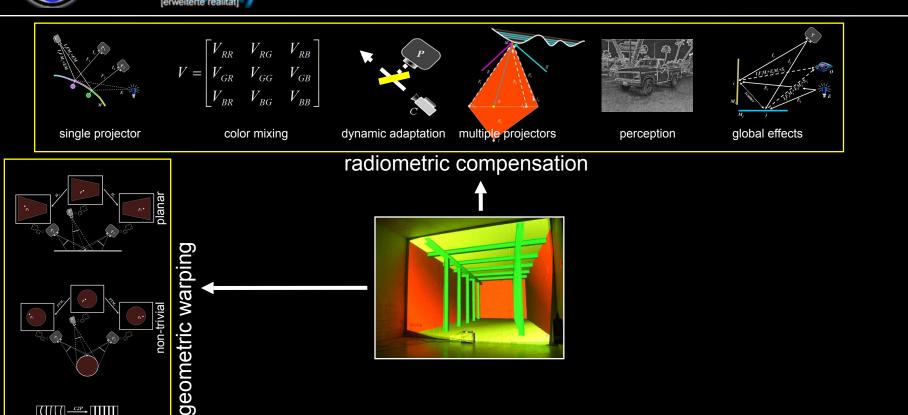




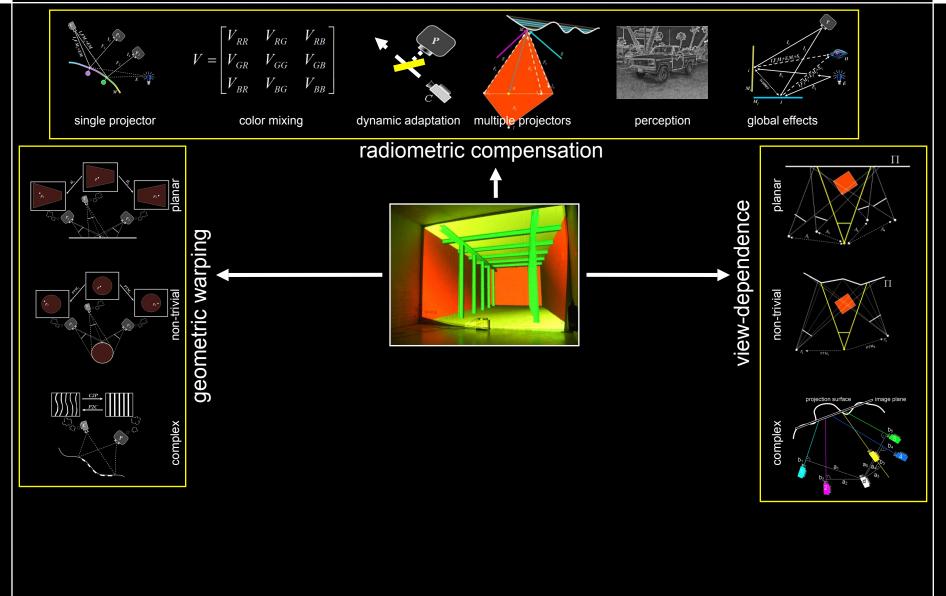




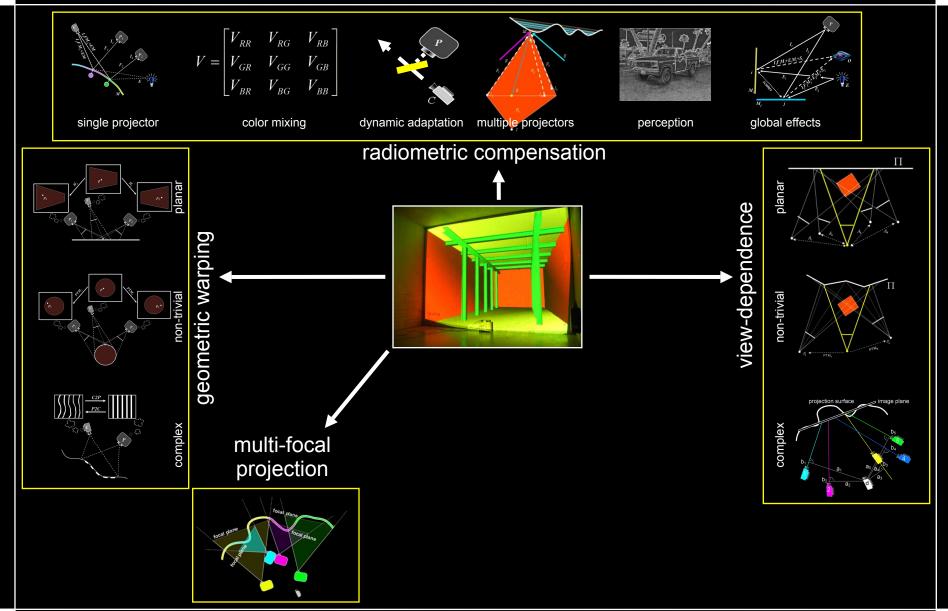
complex



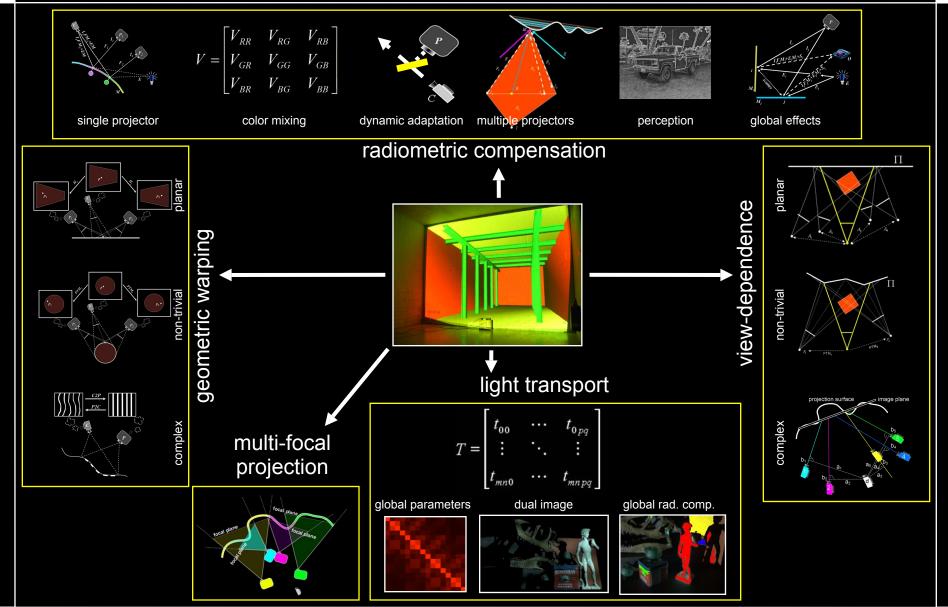














O. Bimber



- technological limitations of projectors:
 - brightness, resolution, focal depth



- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range



- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range → wait for HDR light-valve or laser projectors
 - size, cost, portability ·

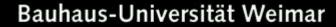


- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range → wait for HDR light-valve or laser projectors
 - size, cost, portability → wait for (good enough) pocket projectors
- technological limitations of cameras:



Future Work

O. Bimber

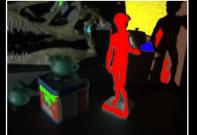




Future Work

- new techniques:
 - consider human visual perception
 - spent computational power only on overcoming limitations that can actually be perceived
 - consider global effects
 - inter-reflections, scattering, etc.











Selected Papers on Geometric Correction



Selected Papers on Geometric Correction

Bimber, O., Wetzstein, G., Emmerling, A., & Nitschke, C. (2005). Enabling View-Dependent Stereoscopic Projection in Real Environments. *Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'05)*, 14-23.

Low, K-L., Welch, G., Lastra, A., & Fuchs, H. (2001). Life-Sized Projector-Based Dioramas, *Proc. Symp. Virtual Reality Software and Technology (VRST'01)*, 93-101.

Raskar, R. (1999). Oblique Projector Rendering on Planar Surfaces for a Tracked User. Proc. of ACM Siggraph'99, sketch.

Raskar, R., Brown, M.S., Yang, R., Chen, W., Welch, G., Towles, H., Seales, B., & Fuchs, H. (1999b). Multi-projector displays using camera-based registration, *Proc. of IEEE Visualization* (IEEE Viz'99), 161-168.

Raskar, R., Welch, G., Low, K.L. & Bandyopadhyay, D. (2001). Shader Lamps: Animating real objects with image-based illumination. *Proc. of Eurographics Rendering Workshop*, 89-102.



Selected Papers on Radiometric Compensation



Selected Papers on Radiometric Compensation

Bell, I.E. (2003). Neutralizing Paintings with a Projector. *Proc. of SPIE/IS&T*, 5008, 560-568.

Bimber, O., Coriand, F., Kleppe, A., Bruns, E., Zollmann, S., & Langlotz, T. (2005). Superimposing Pictorial Artwork with Projected Imagery. *IEEE MultiMedia*. 12(1), 16-26.

Bimber, O., Grundhöfer, A., Zeidler, T., Danch, D., & Kapakos, P. (2006). Compensating Indirect Scattering for Immersive and Semi-Immersive Projection Displays. *Proc. of IEEE Virtual Reality (IEEE VR'06)*.

Fujii, K., Grossberg, M.D., & Nayar, S.K. (2005). A projector-camera system with real-time photometric adaptation for dynamic environments. *Proc. of Computer Vision and Pattern Recognition (CVPR'05)*, 2, 20-25.

Grossberg, M.D., Peri, H., Nayar, S.K., & Bulhumeur, P. (2004). Making One Object Look Like Another: Controlling Appearance Using a Projector-Camera System. *Proc. of IEEE Conference on Computer Vision and Pattern Recognition (CVPR'04)*, 1, 452-459.

Nayar, S.K., Peri, H., Grossberg, M.D., & Belhumeur, P.N. (2003). A Projection System with Radiometric Compensation for Screen Imperfections. *Proc. of International Workshop on Projector-Camera Systems (ProCams'03)*.

Wang, D., Sato, I., Okabe, T., & Sato, Y. (2005). Radiometric Compensation in a Projector-Camera System Based on the Properties of Human Vision System. *In Proc. of IEEE International Workshop on Projector-Camera Systems (ProCams'05)*.



Selected Papers Other and Related Techniques



Selected Papers Other and Related Techniques

Bimber, O. & Emmerling, A. (2006). Multi-Focal Projection: A Multi-Projector Technique for Increasing Focal Depth. *IEEE Transactions on Visualization and Computer Graphics (TVCG)*.

Brown, M., Majumder, A., and Yang, R. (2005). Camera-Based Calibration Techniques for Seamless Multi-Projector Displays. *IEEE Transactions on Visualization and Computer Graphics (TVCG)*, 11(2), 193-206.

Acquisition and Display. Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'04), 100-109.

Cotting, D., Naef, M., Gross, M., & Fuchs, H. (2004). Embedding Imperceptible Patterns into Projected Images for Simultaneous

Ehnes, J., Hirota, K., & Hirose, M. (2004). Projected Augmentation – Augmented Reality using Rotatable Video Projectors. *Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'04)*, 26-35.

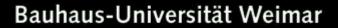
Underkoffler, J., Ullmer, B. & Ishii, H. (1999). Emancipated pixels: real-world graphics in the luminous room. *Proc. of ACM Siggraph*, 385-392.

Levoy, M., Chen, B., Vaish, V., Horowitz, M., McDowall, I., and Bolas, M. (2004) Synthetic Aperture Confocal Imagining, Proc. of ACM Siggraph'04, pp. 825-834.

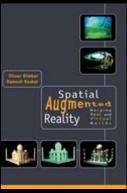
Sen, P., Chen, B., Garg, G., Marschner, S.R., Horowitz, M., Levoy, M., and Lensch, H.P.A (2005)., Dual Photography, *Proc. of ACM*



Thank you! www.uni.weimar.de/medien/AR







Bimber, O. & Raskar, R. Spatial Augmented Reality: Merging Real and Virtual Worlds. A K Peters LTD (publisher), ISBN: 1-56881-230-2.

Thank you! www.uni.weimar.de/medien/AR



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