

Multi-Projector Techniques for Real-Time Visualizations in

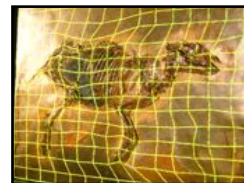
Outline

Outline

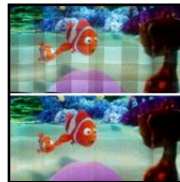
these slides:
www.uni-weimar.de/medien/AR



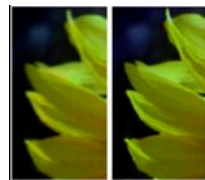
Introduction
Motivations and Applications



Geometric Correction
Planar, Non-Trivial, Complex Surfaces



Radiometric Compensation
Local and Global Light Effects



Advanced Techniques
View-Dependence, Multi-Focal Projection, Light Transport

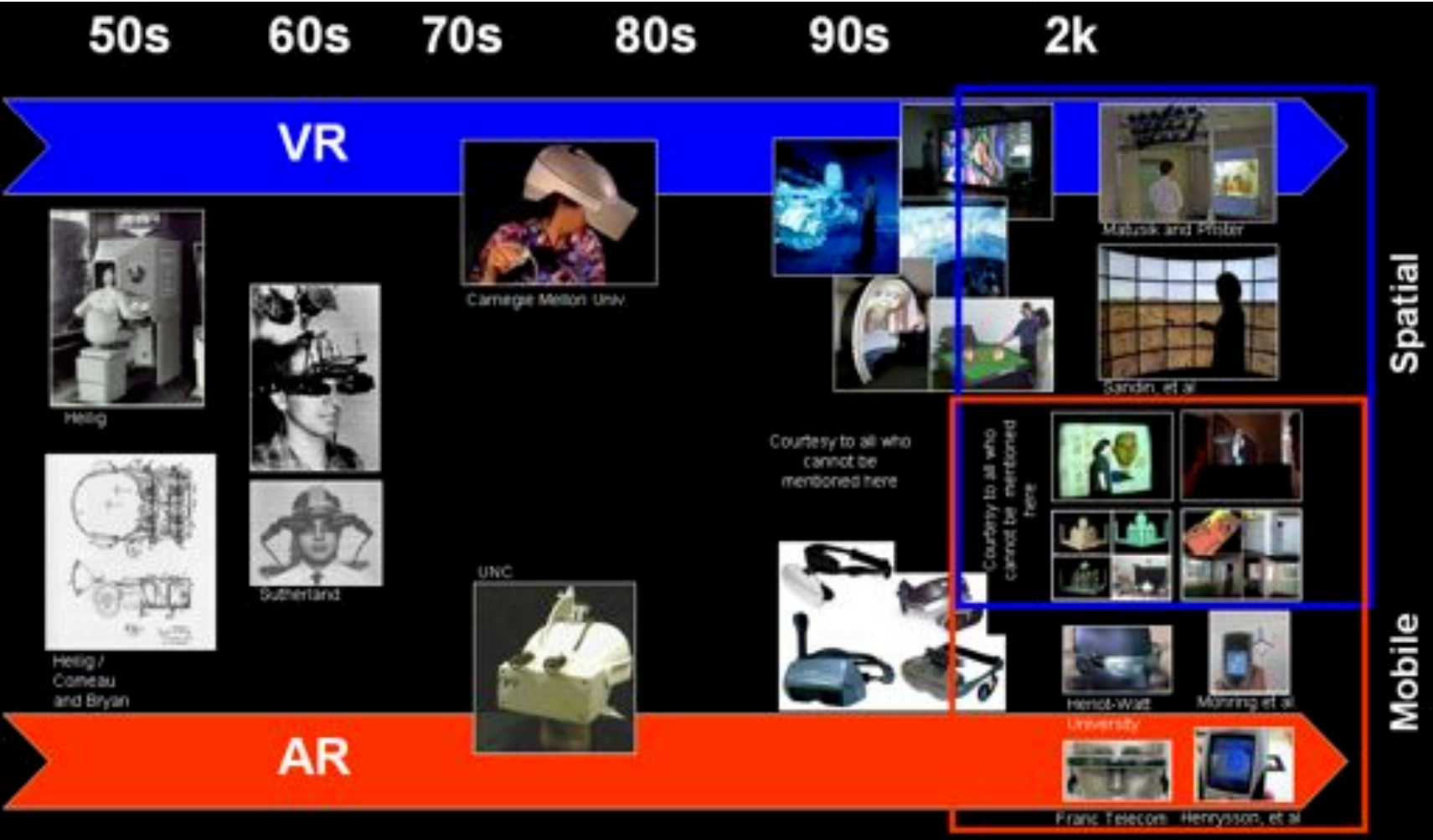


Outlook
Limitations and Future Work

Introduction

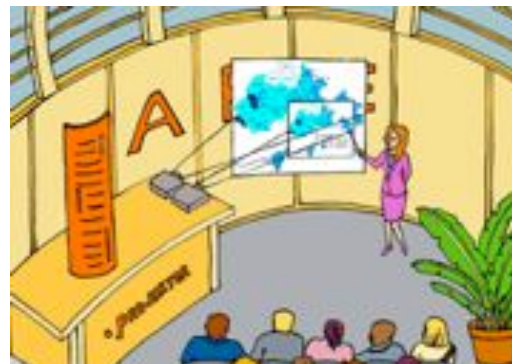
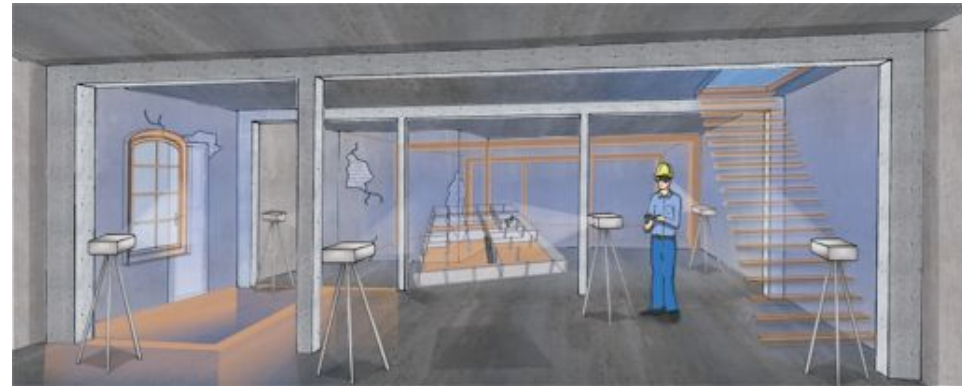
Evolving Evolution

Evolving Evolution



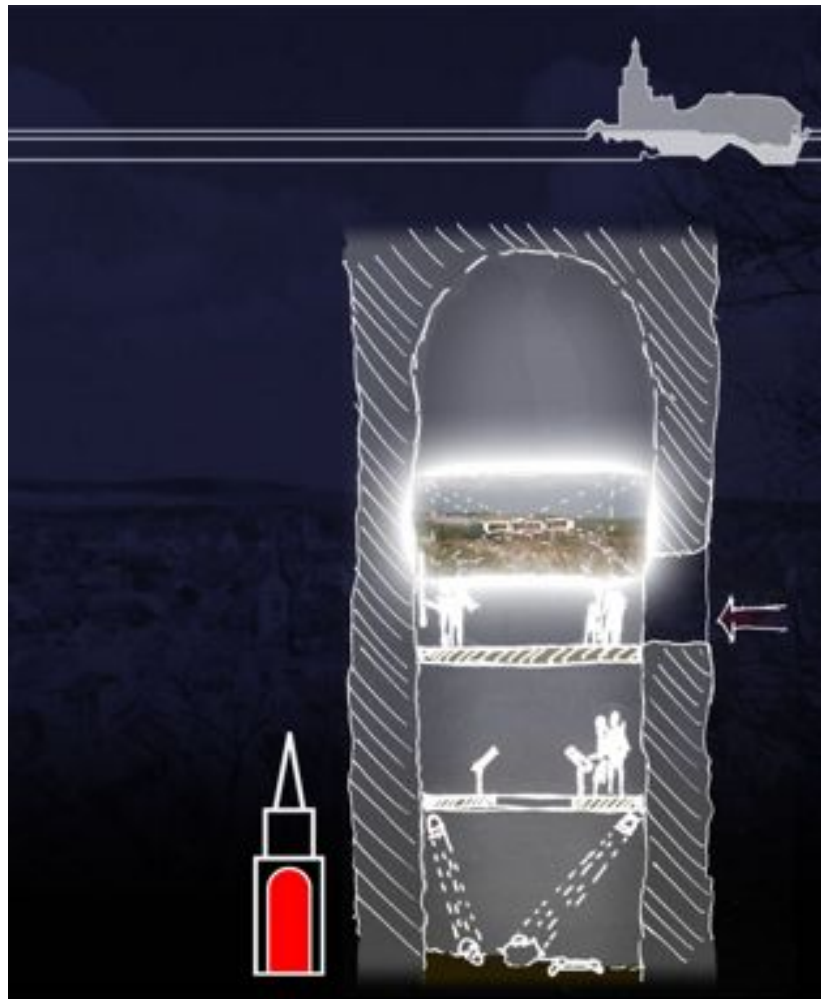
Motivation: Projection

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Application: Historic Sites and Museums

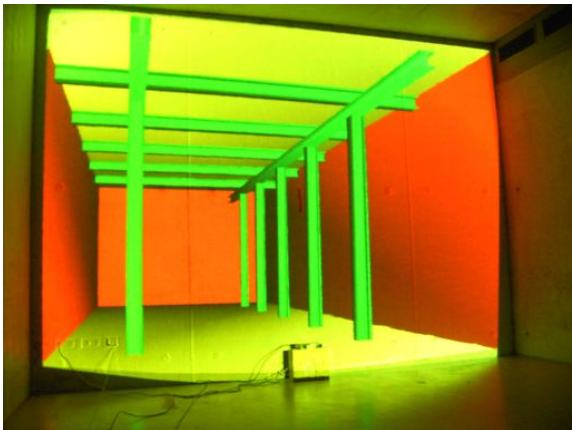
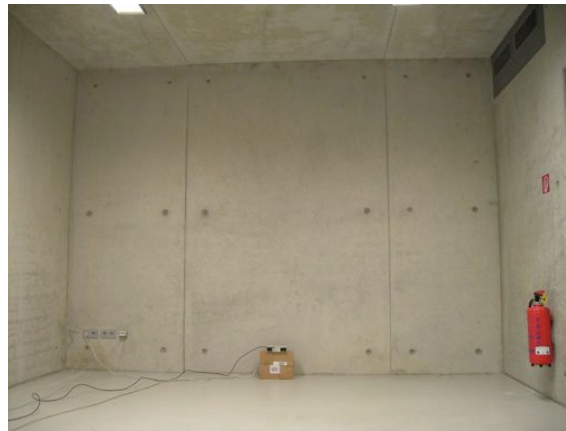
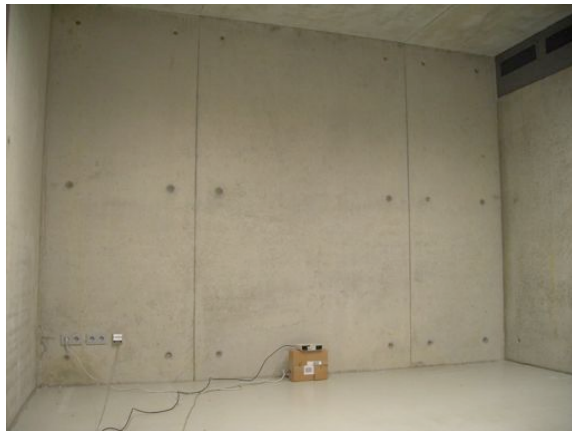
Application: Historic Sites and Museums



360° Surround
Projection in Castel
Tower
(Running project in
coop. with Bennert
Group)

Application: Architectural Visualization

Application: Architectural Visualization



Bimber et al, IEEE/ACM
ISMAR 2005

On-Site Architectural Visualizations
(Running project in coop. with Architecture Faculty, BUW)

Application: Pocket Projectors

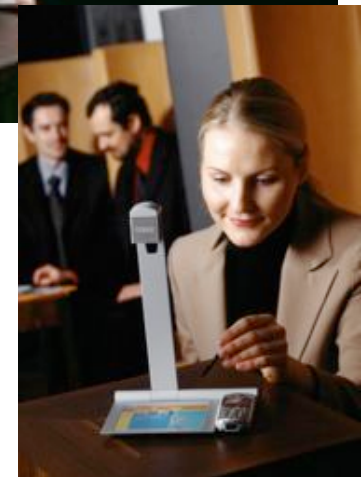
Application: Pocket Projectors



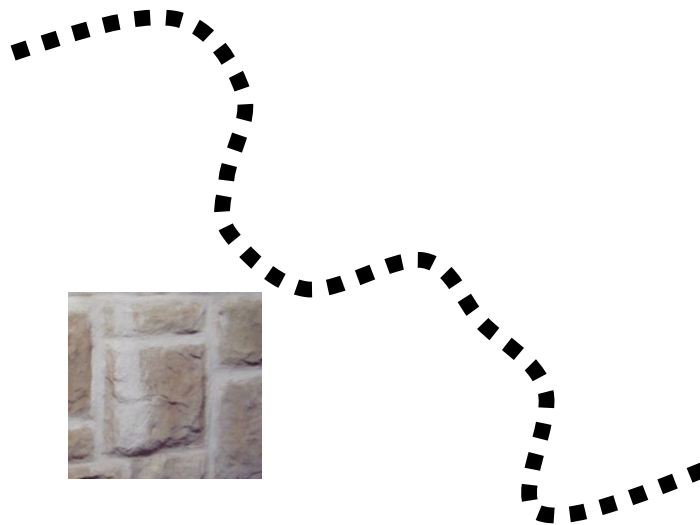
Courtesy: InFocus



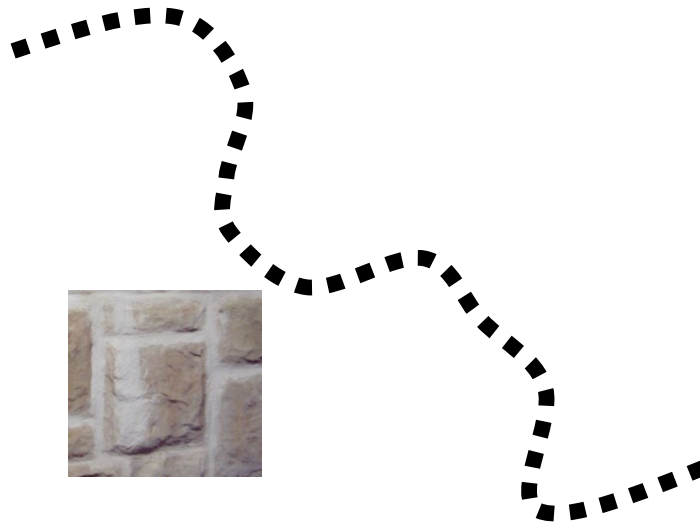
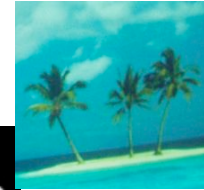
Courtesy: Siemens



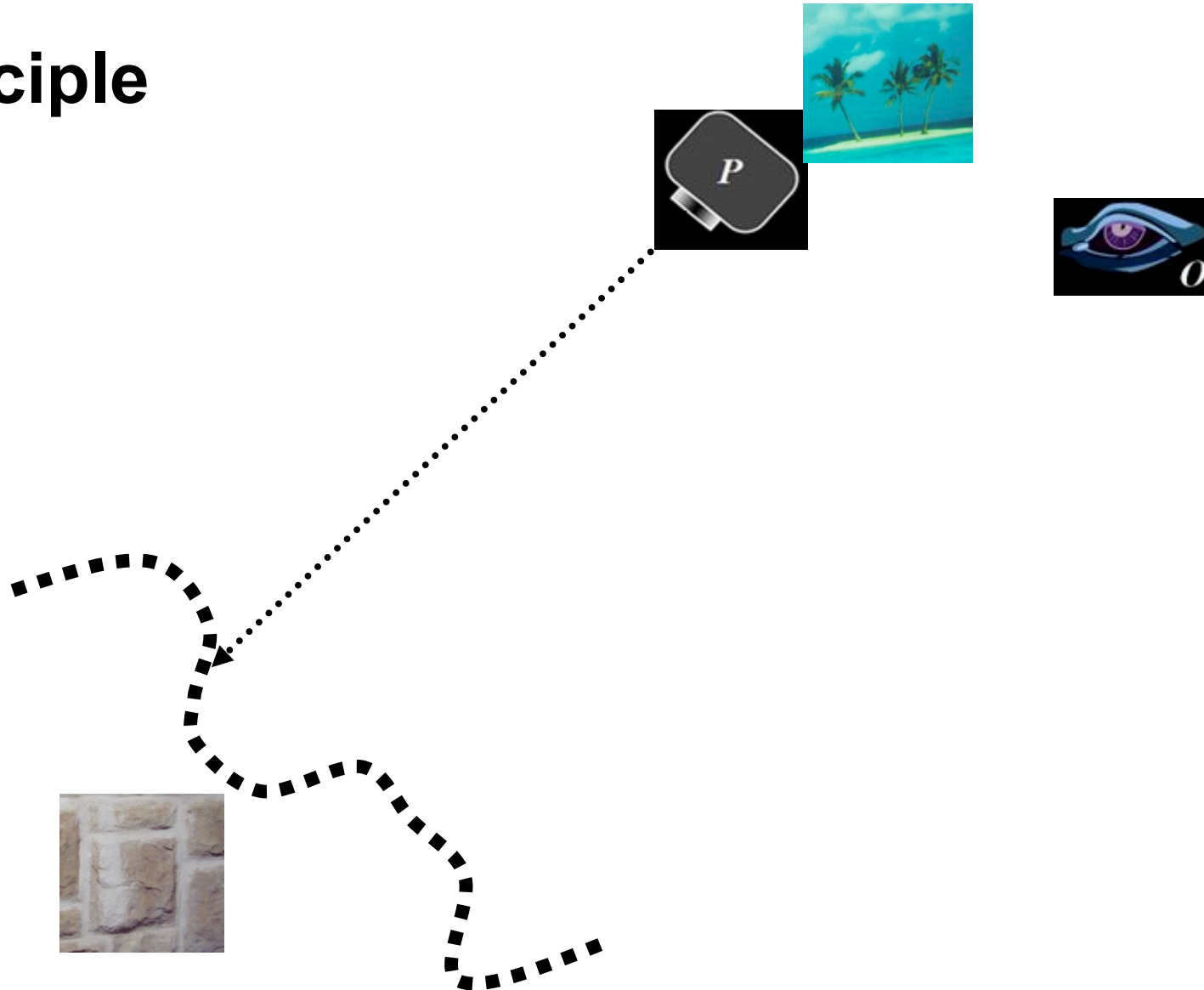
Principle



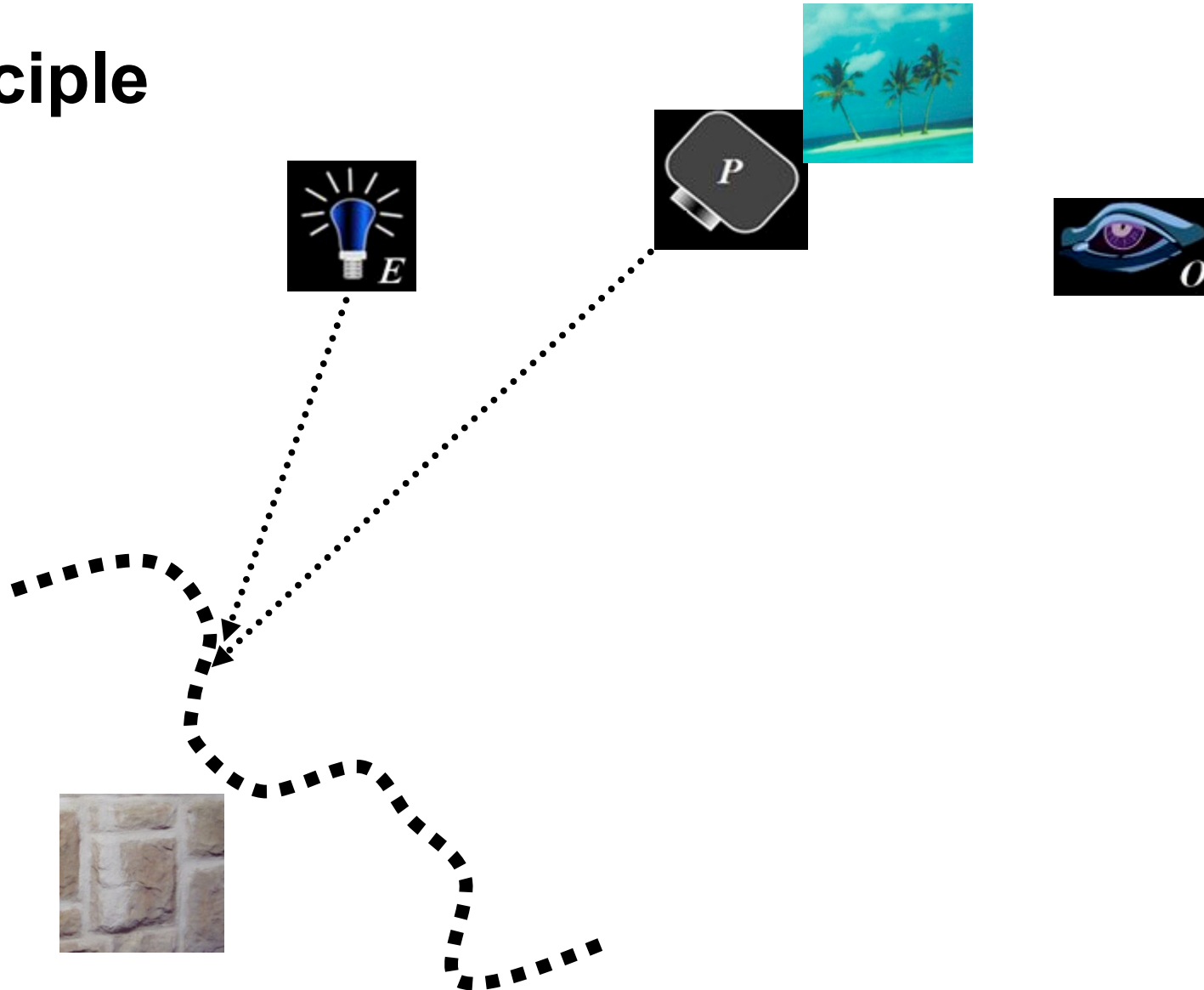
Principle



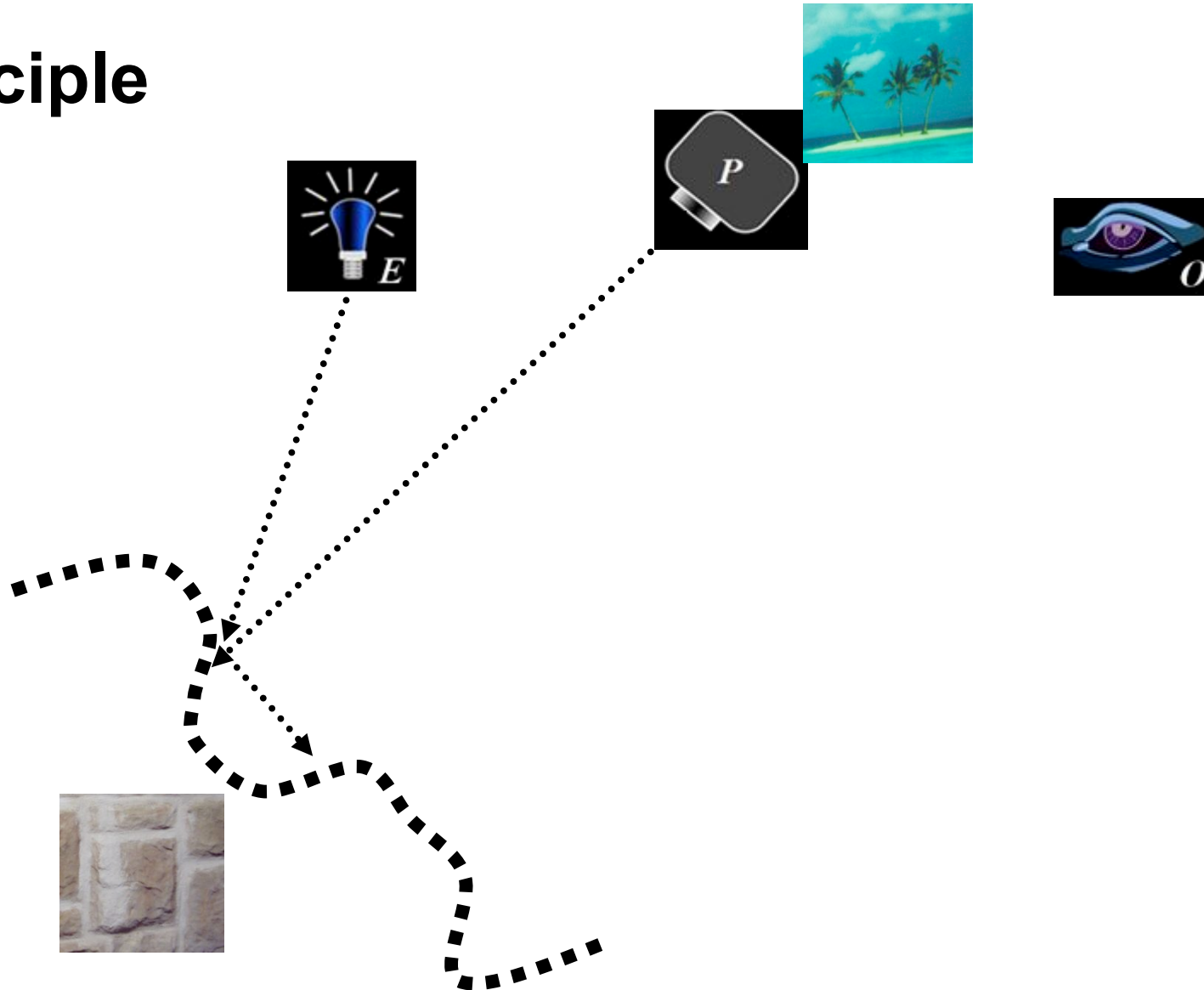
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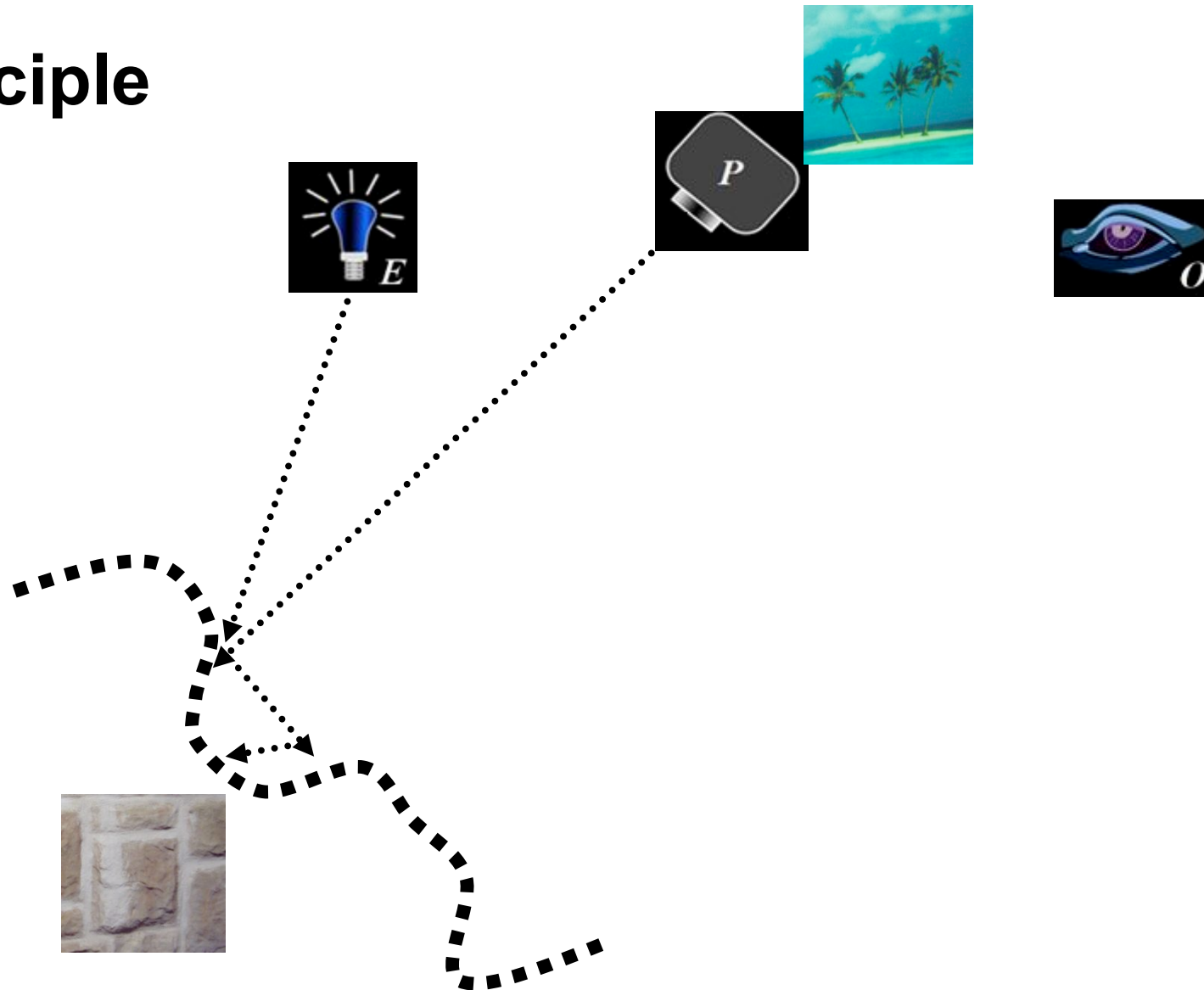
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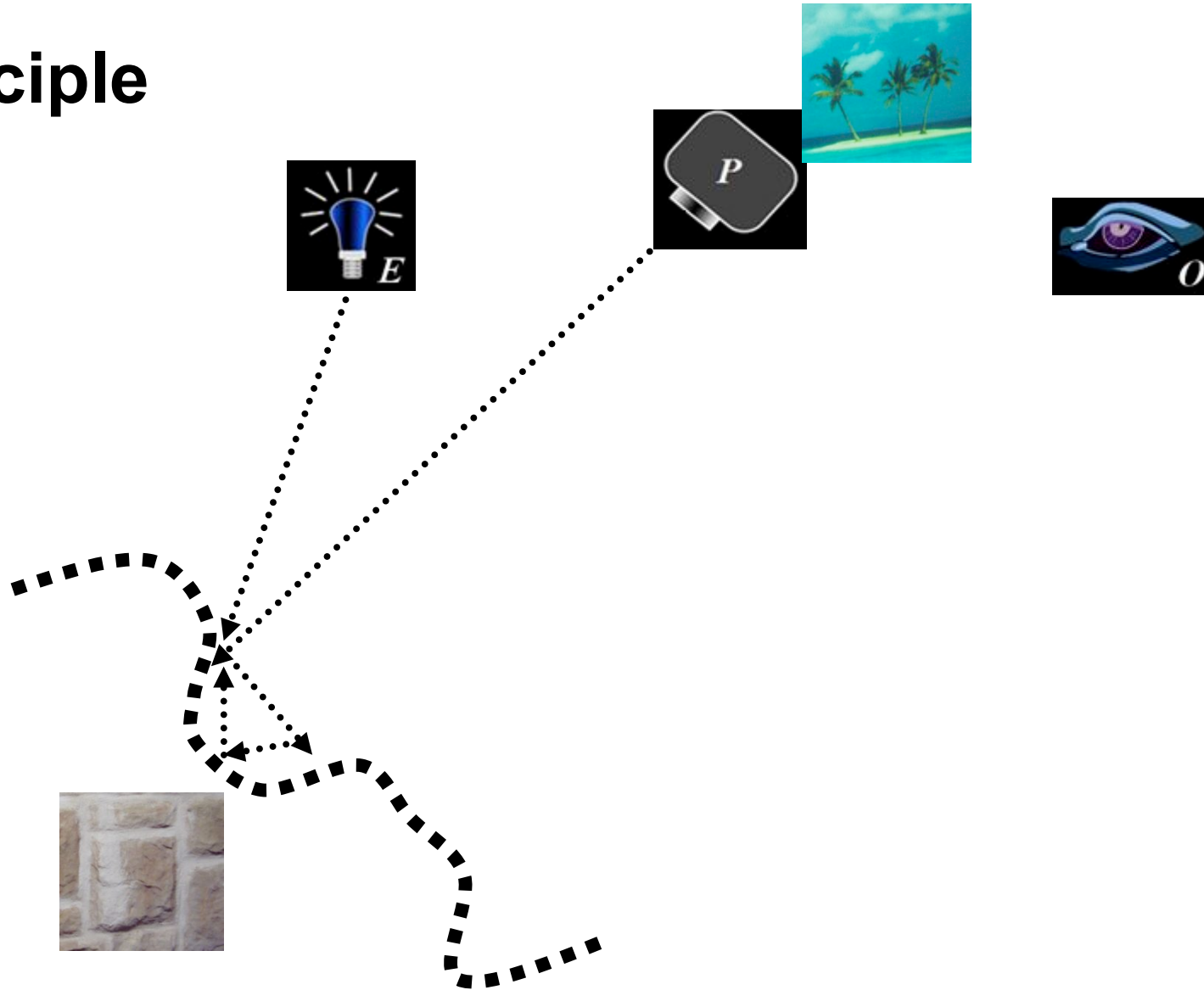
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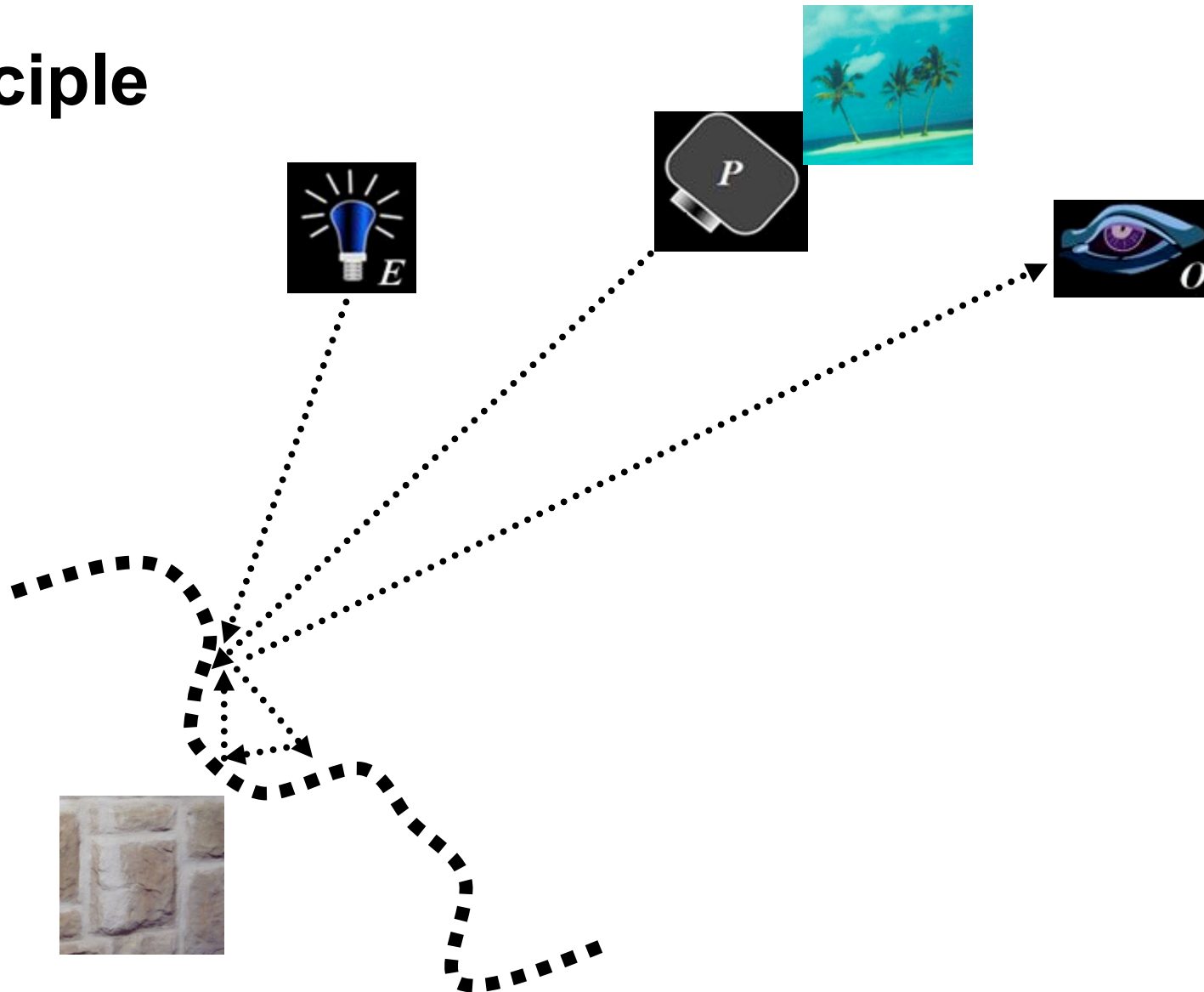
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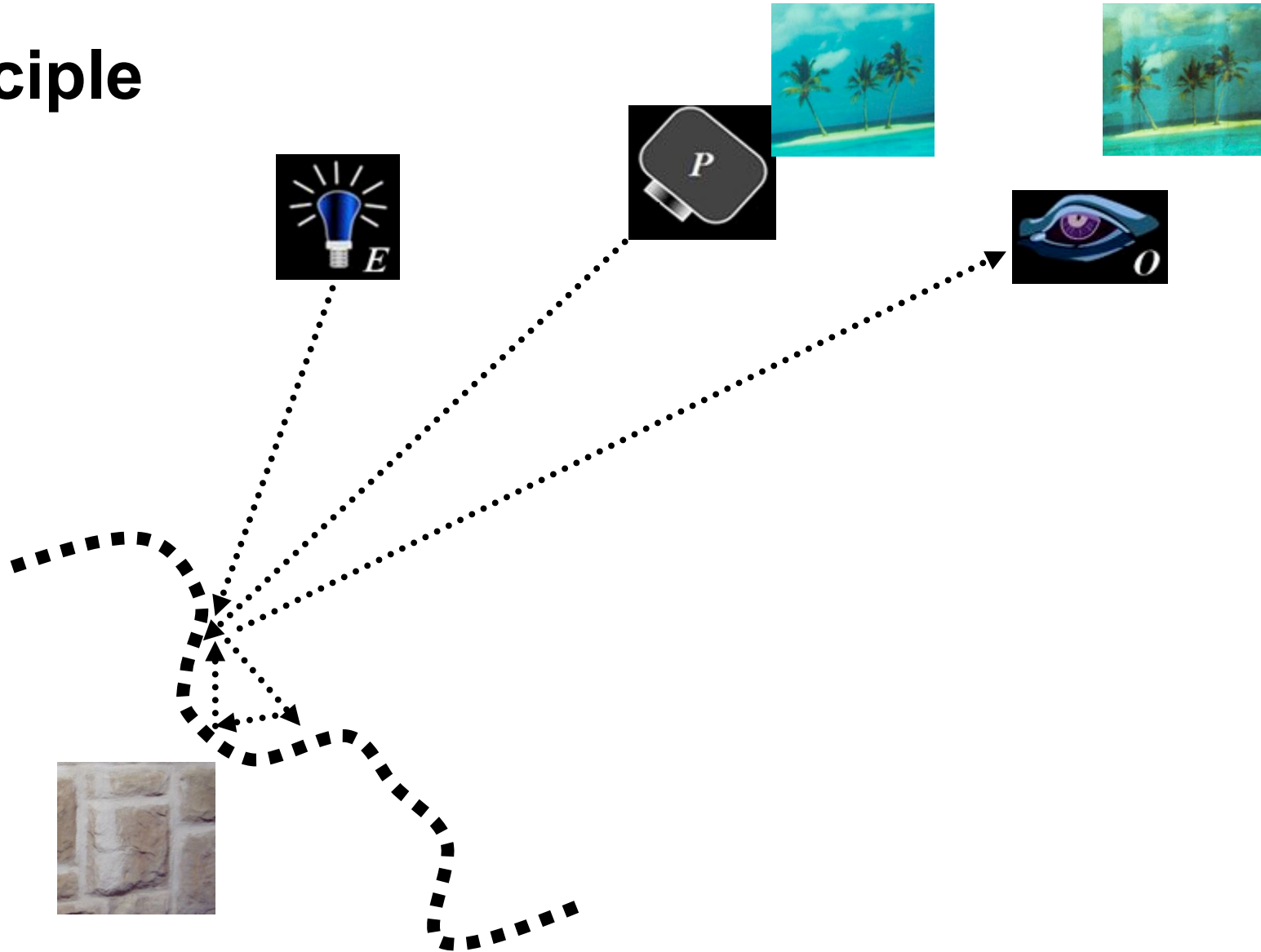
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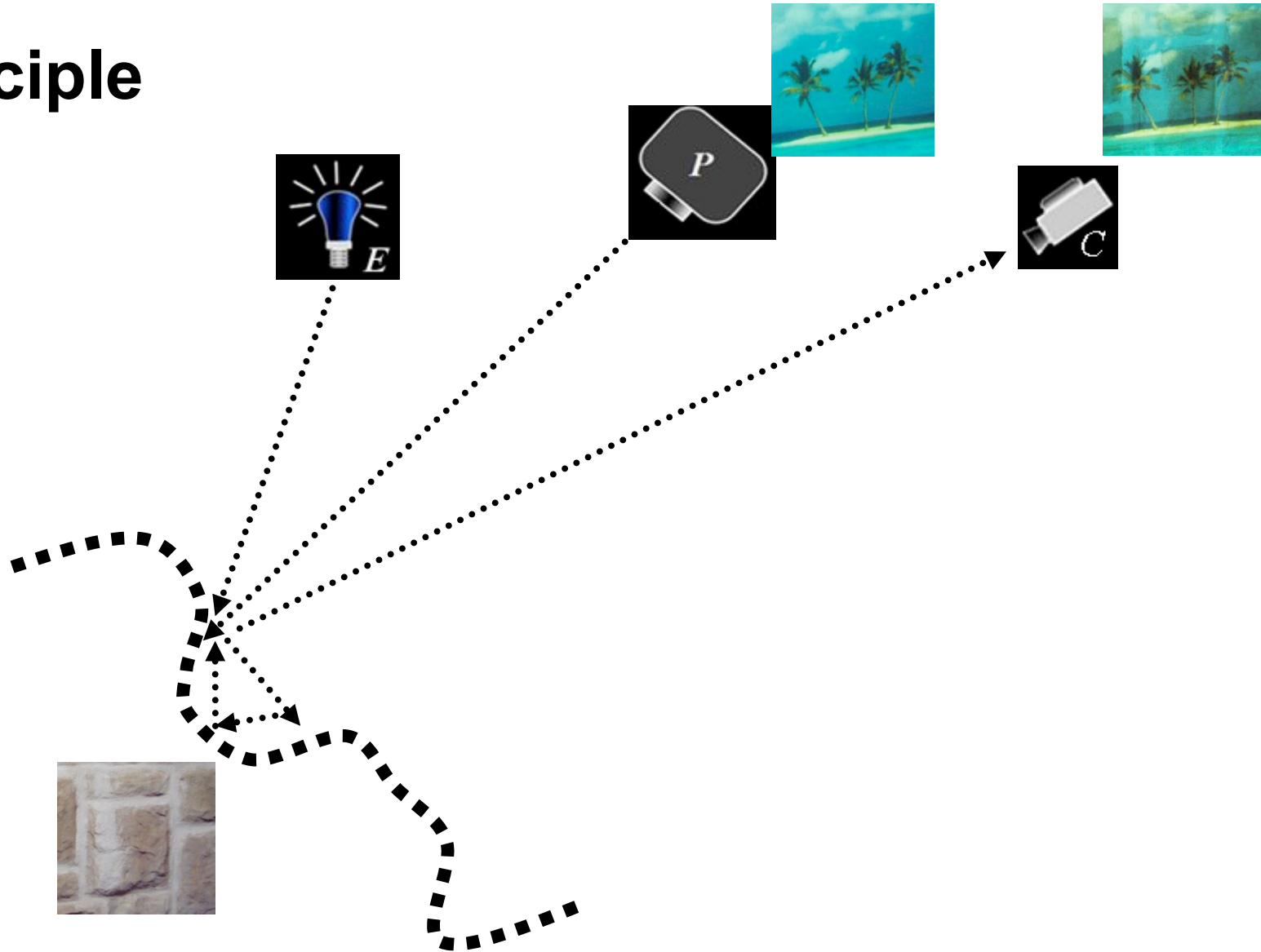
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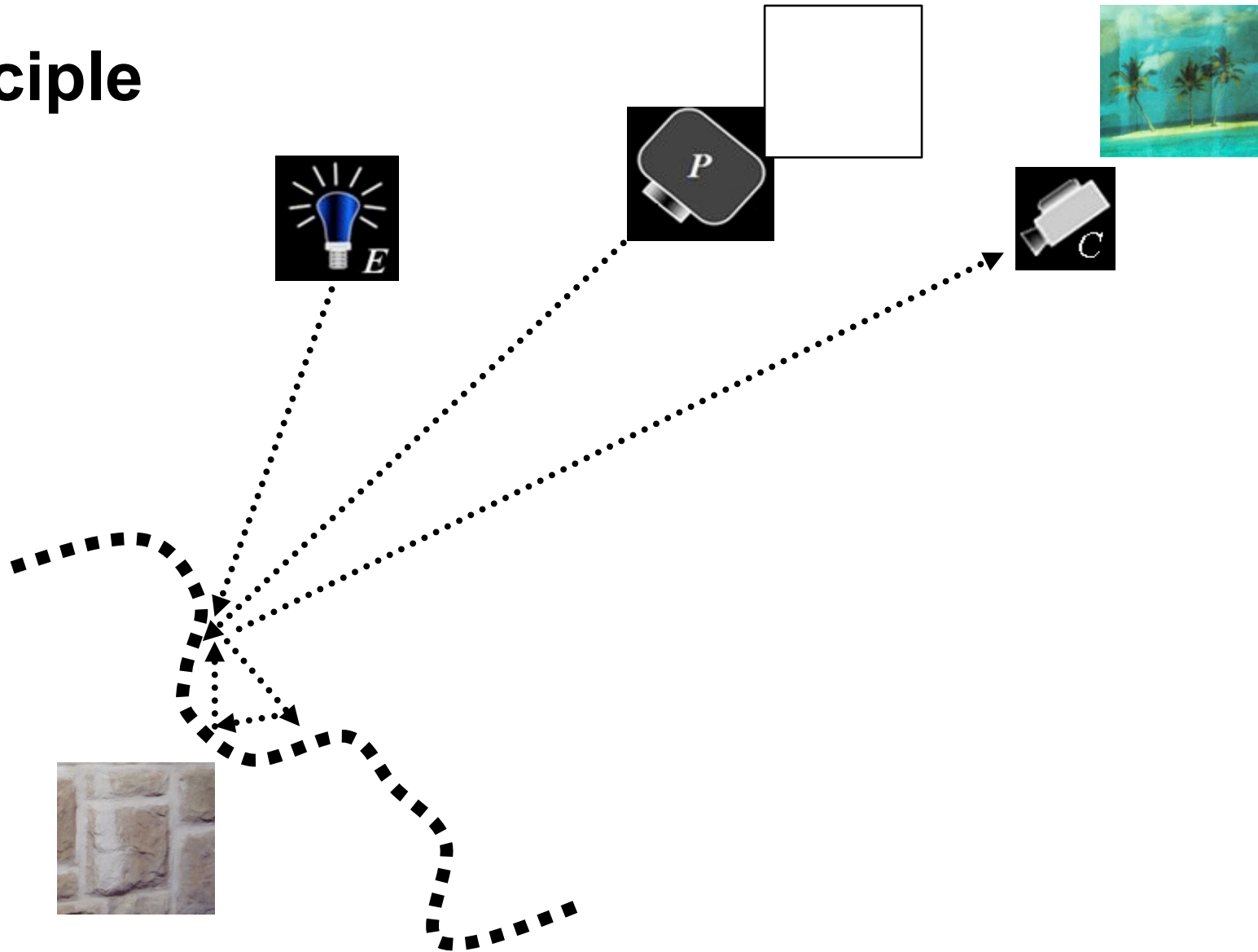
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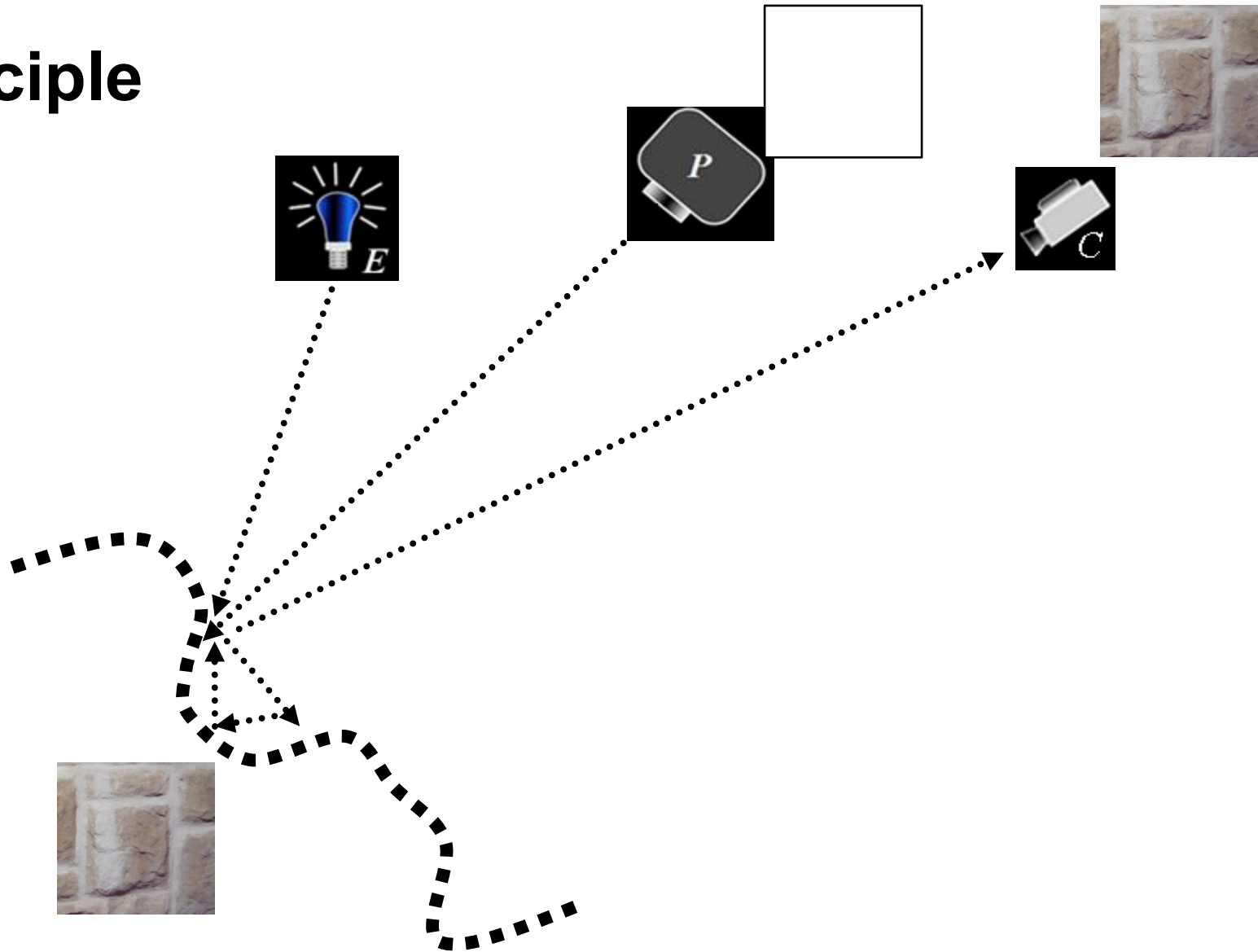
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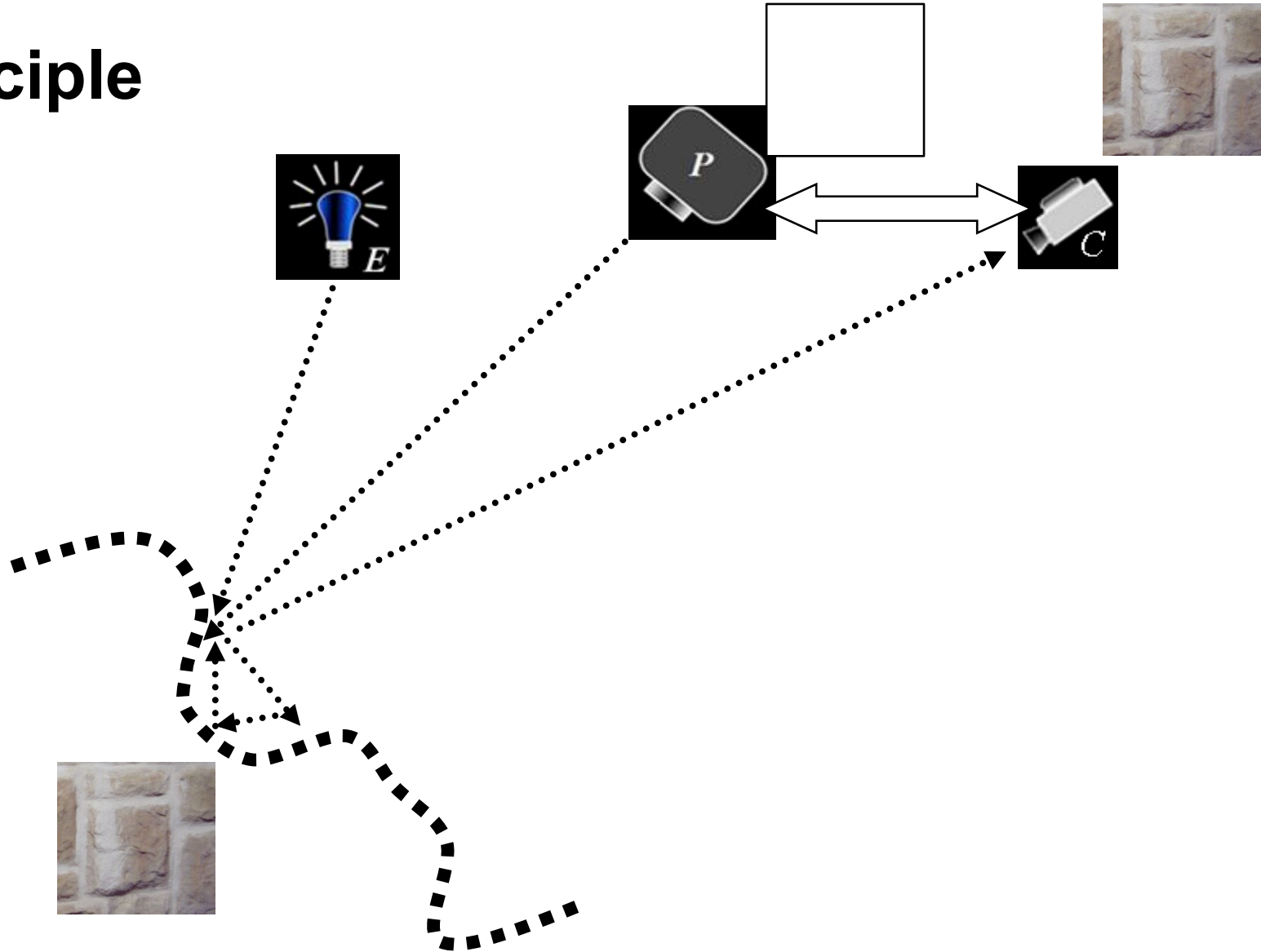
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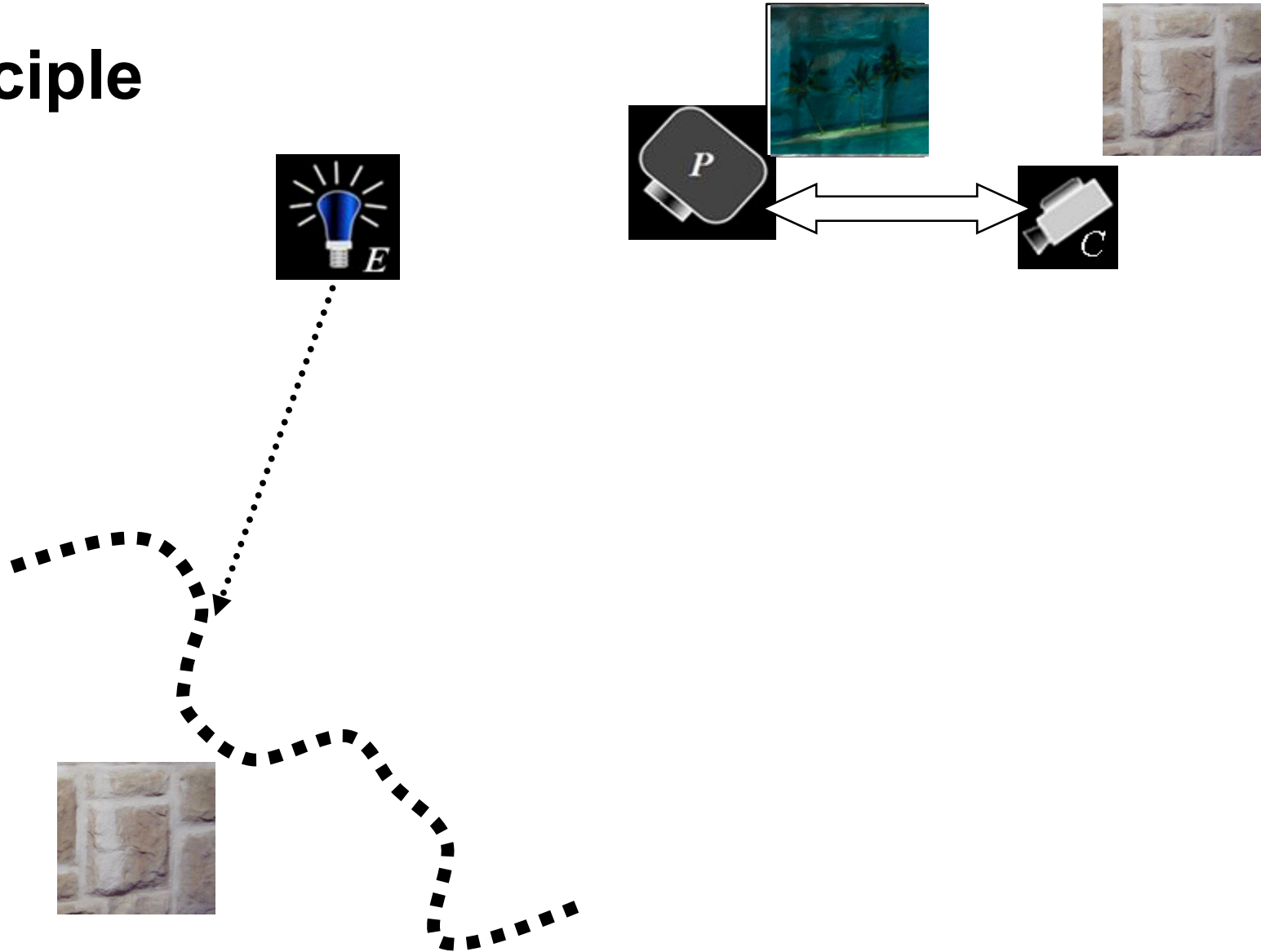
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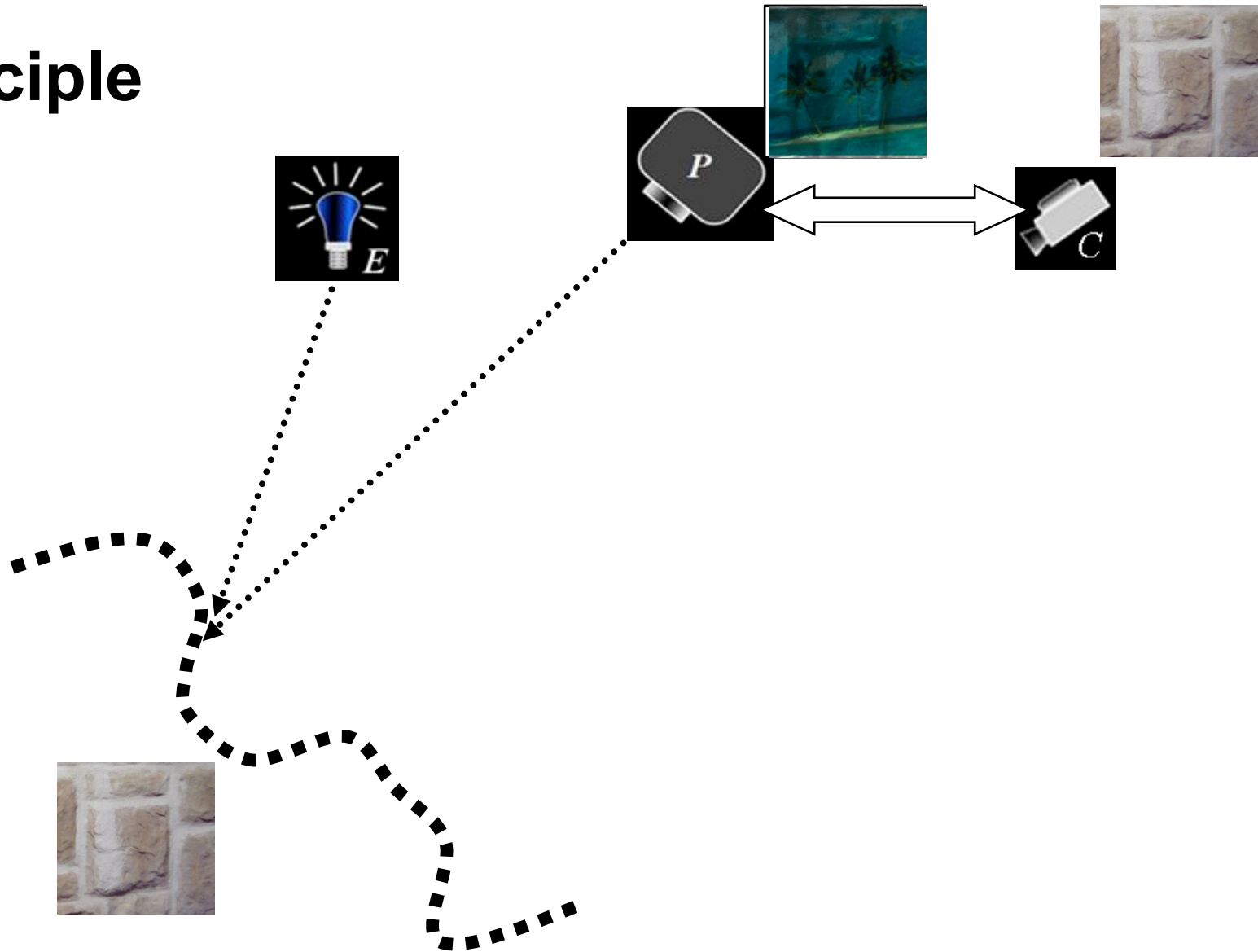
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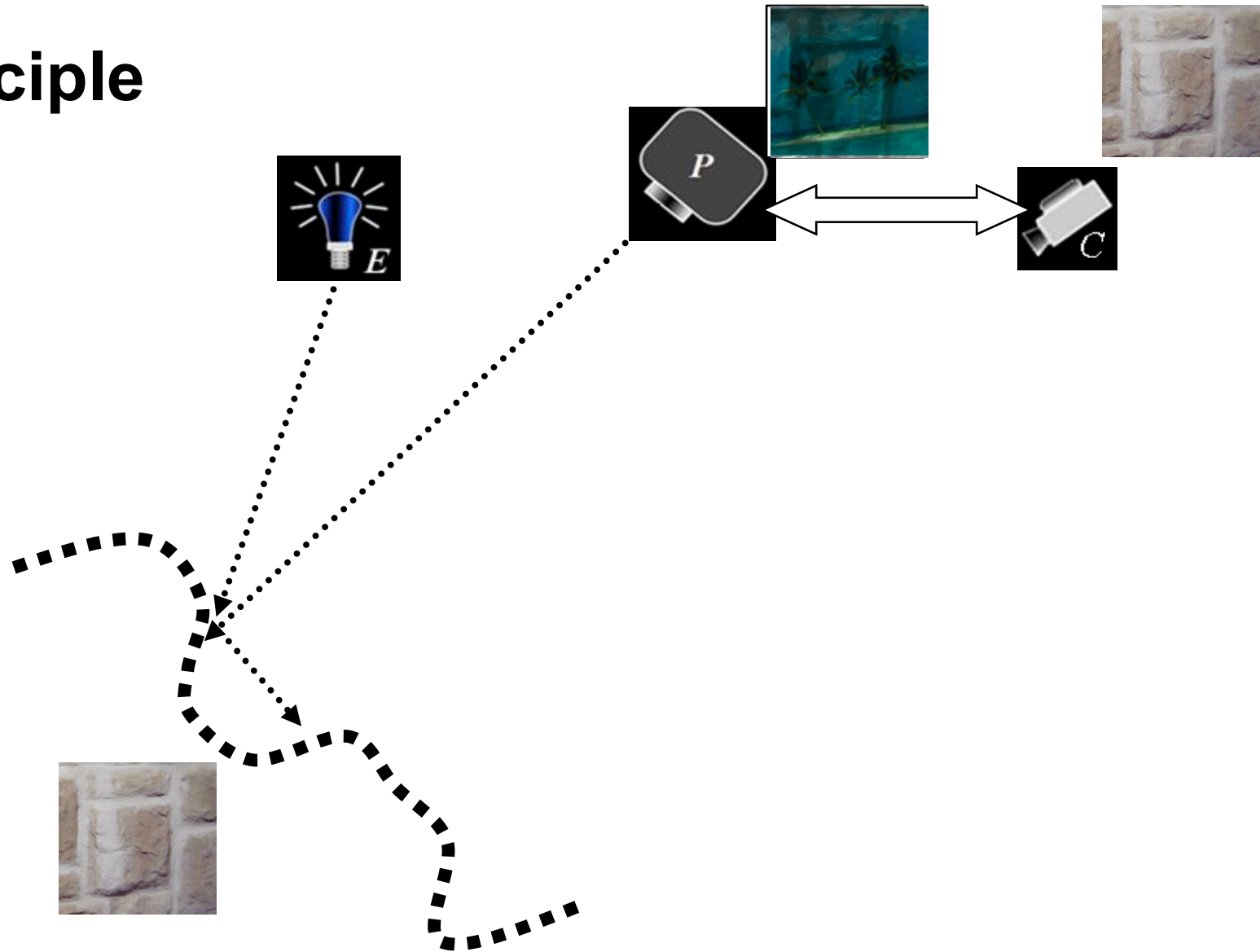
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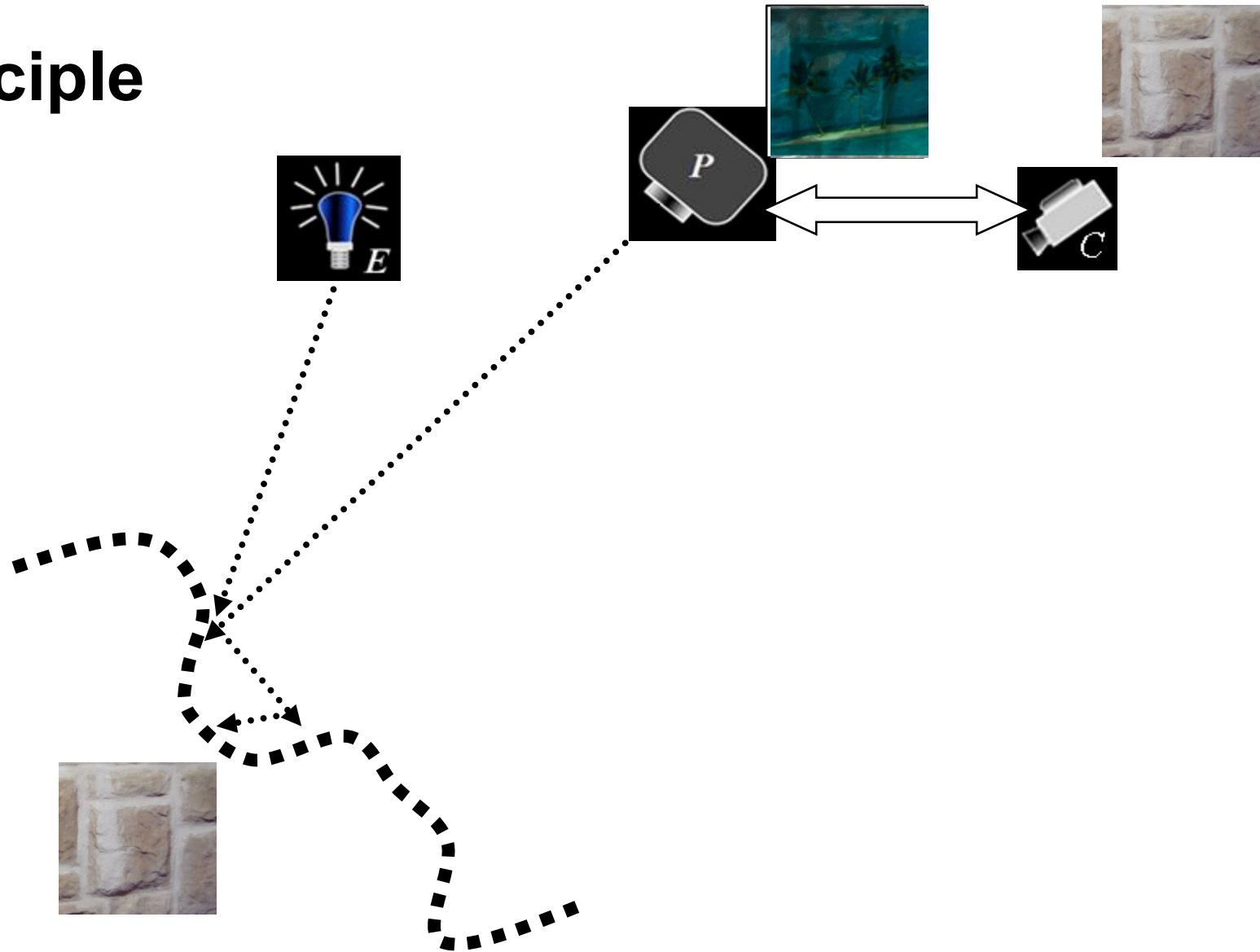
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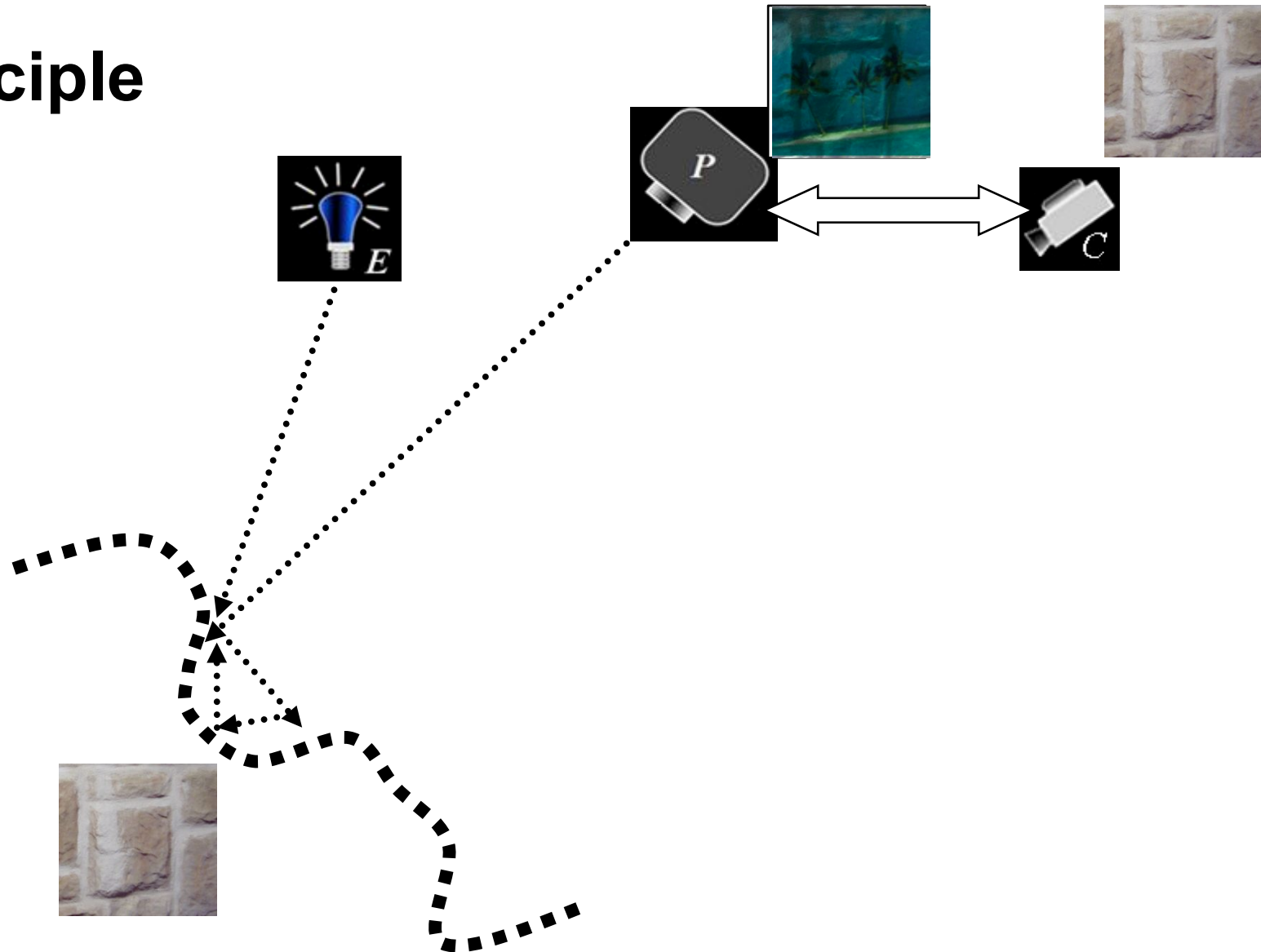
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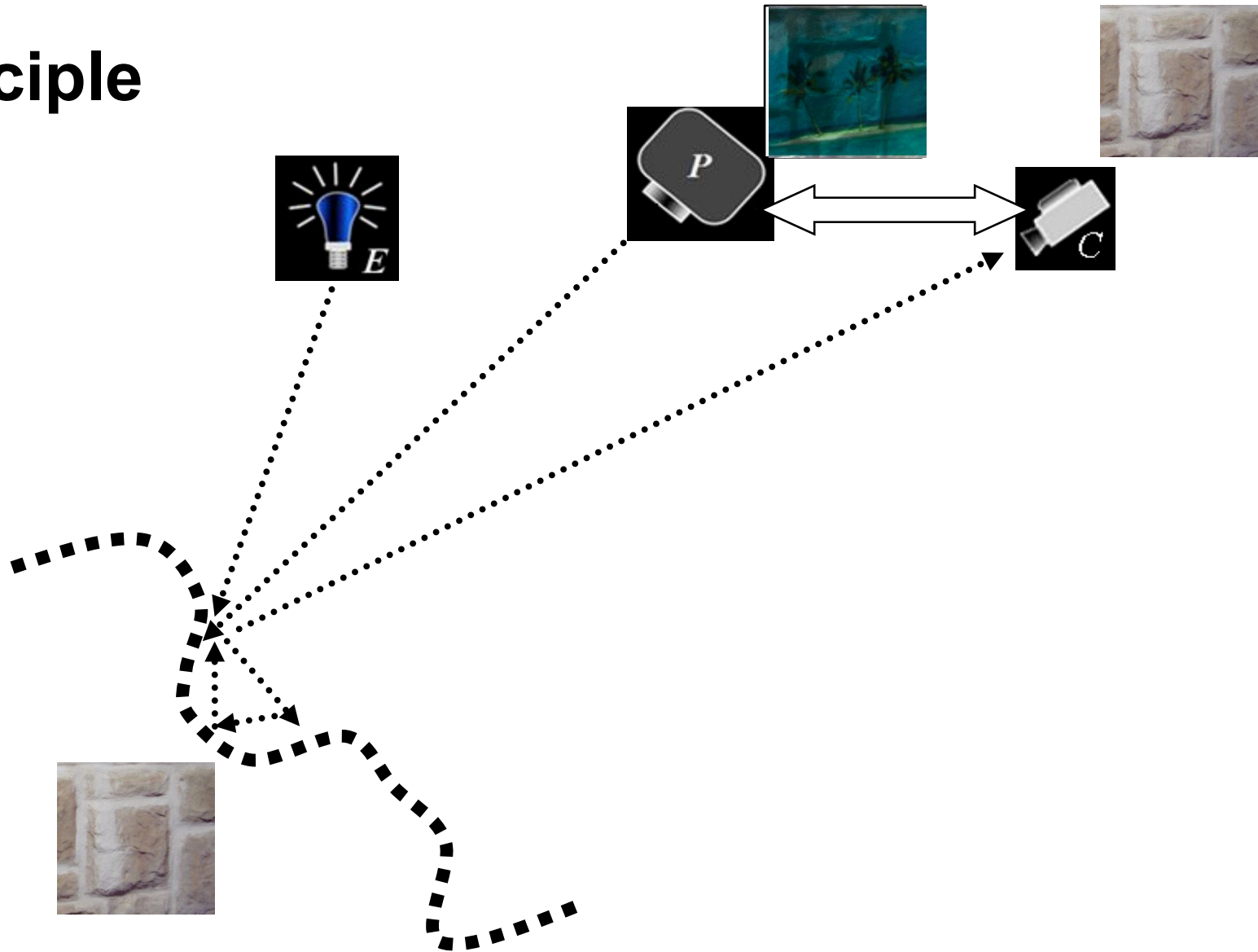
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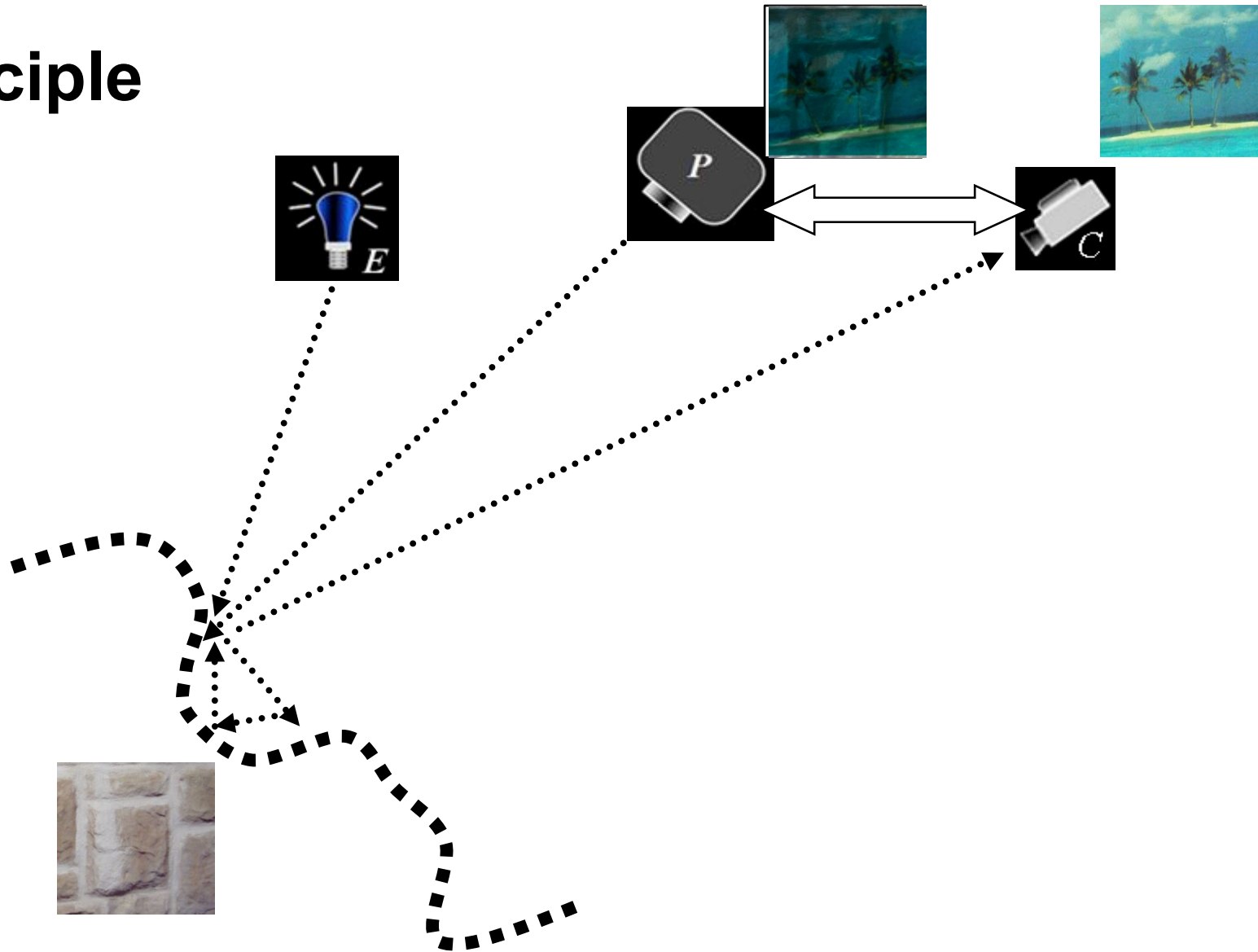
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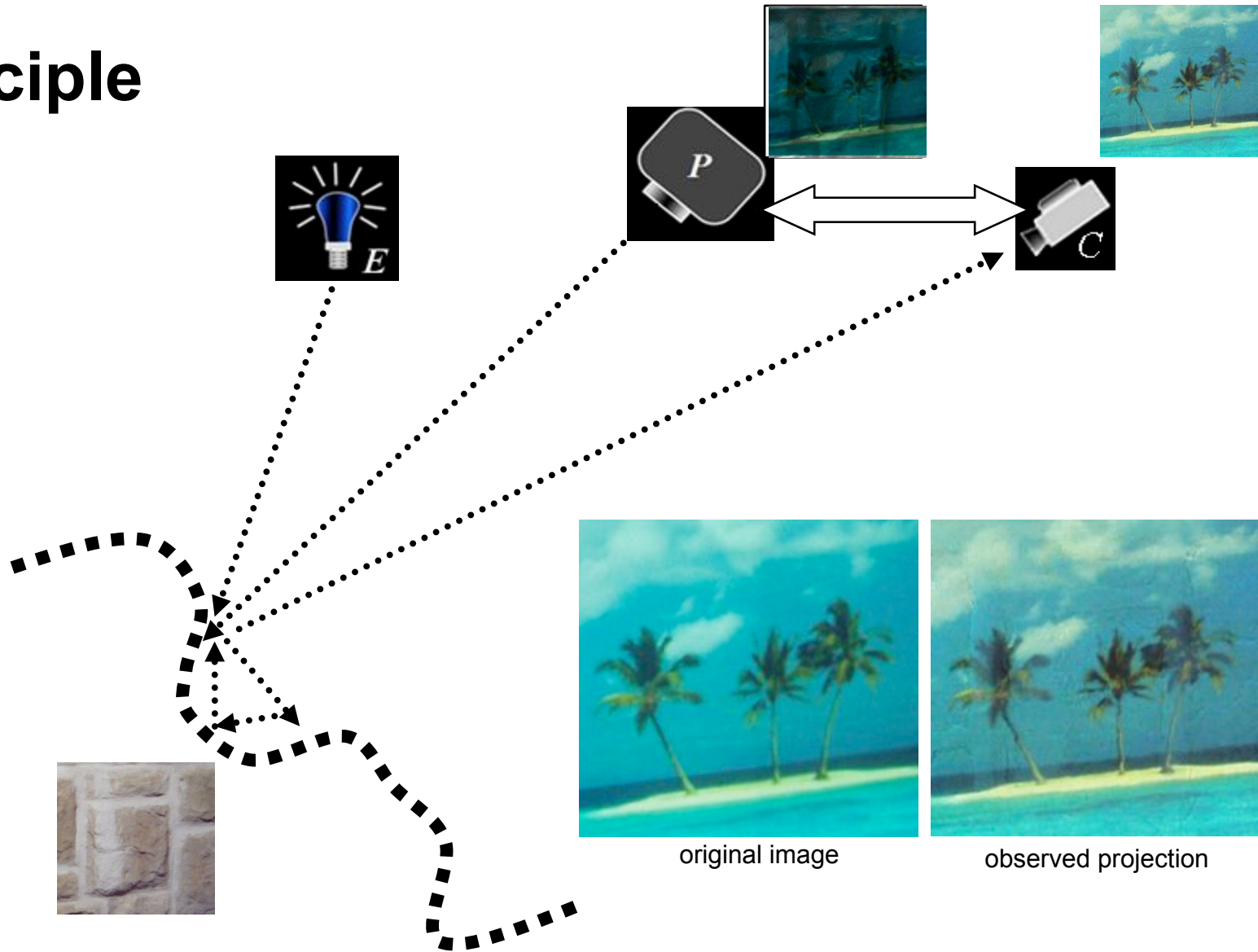
Principle



Principle



Principle



Some Challenges

Some Challenges



color blending

Some Challenges



color blending

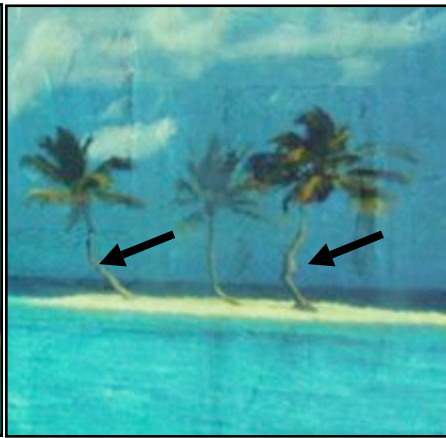


geometric warping

Some Challenges



color blending



geometric warping



misregistration

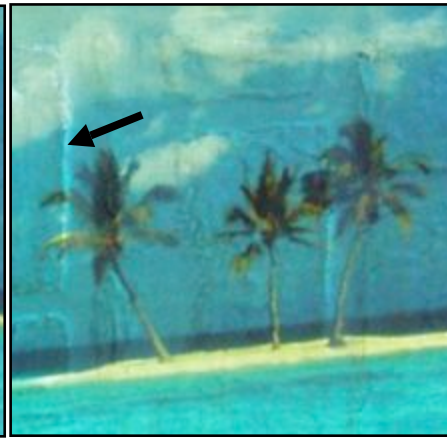
Some Challenges



color blending



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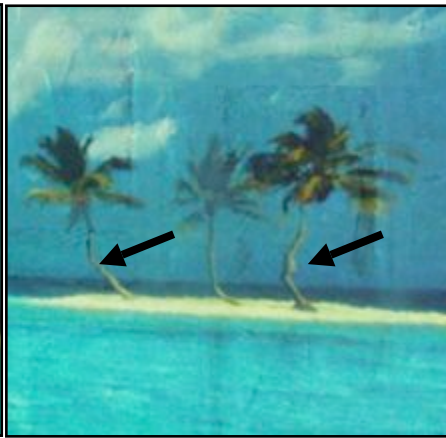


regional defocus

Some Challenges



color blending



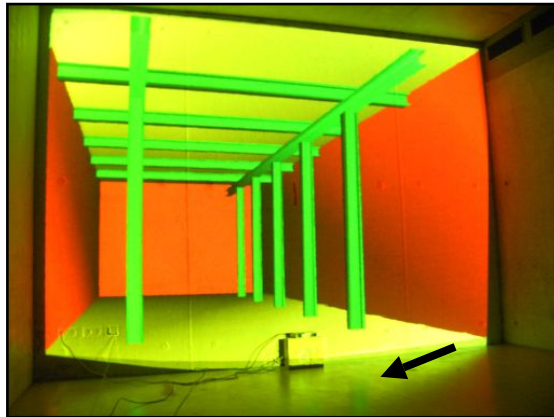
geometric warping



misregistration



regional defocus



scattering

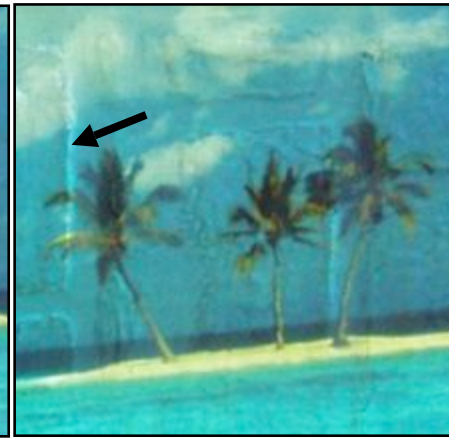
Some Challenges



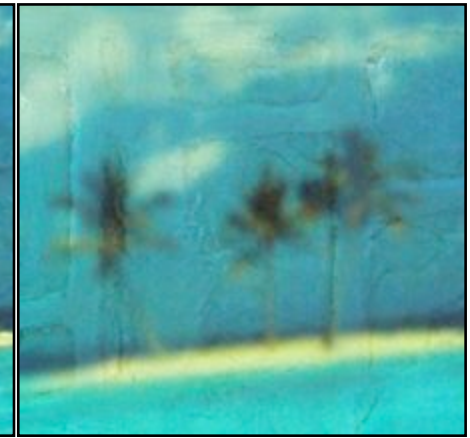
color blending



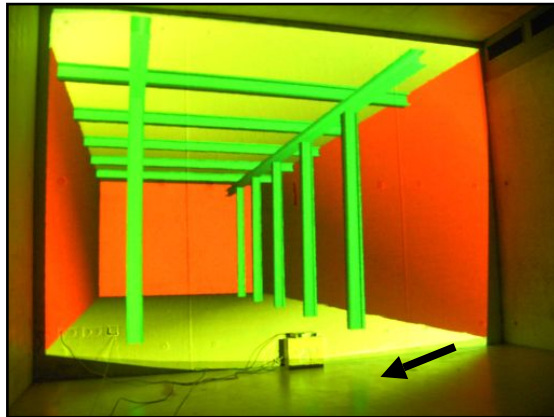
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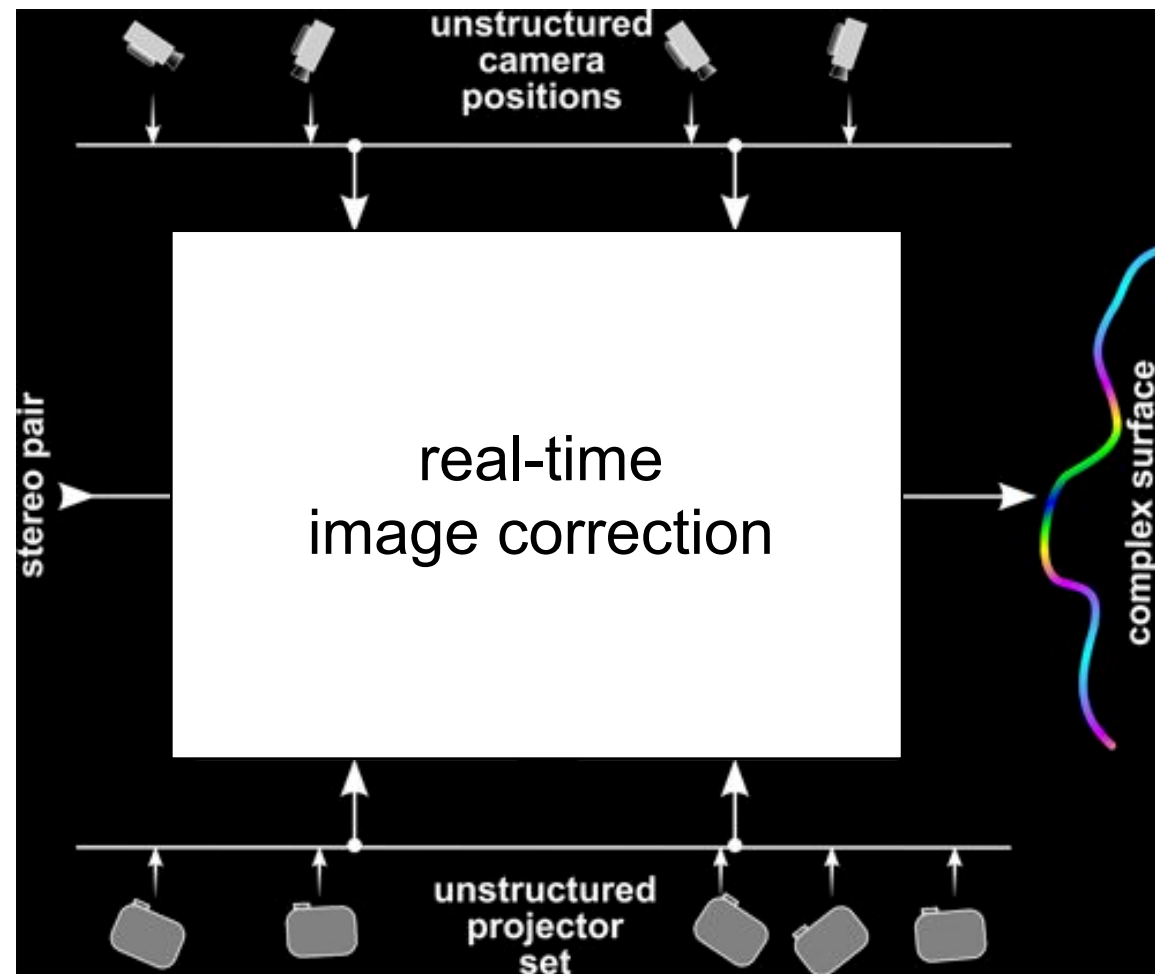


scattering

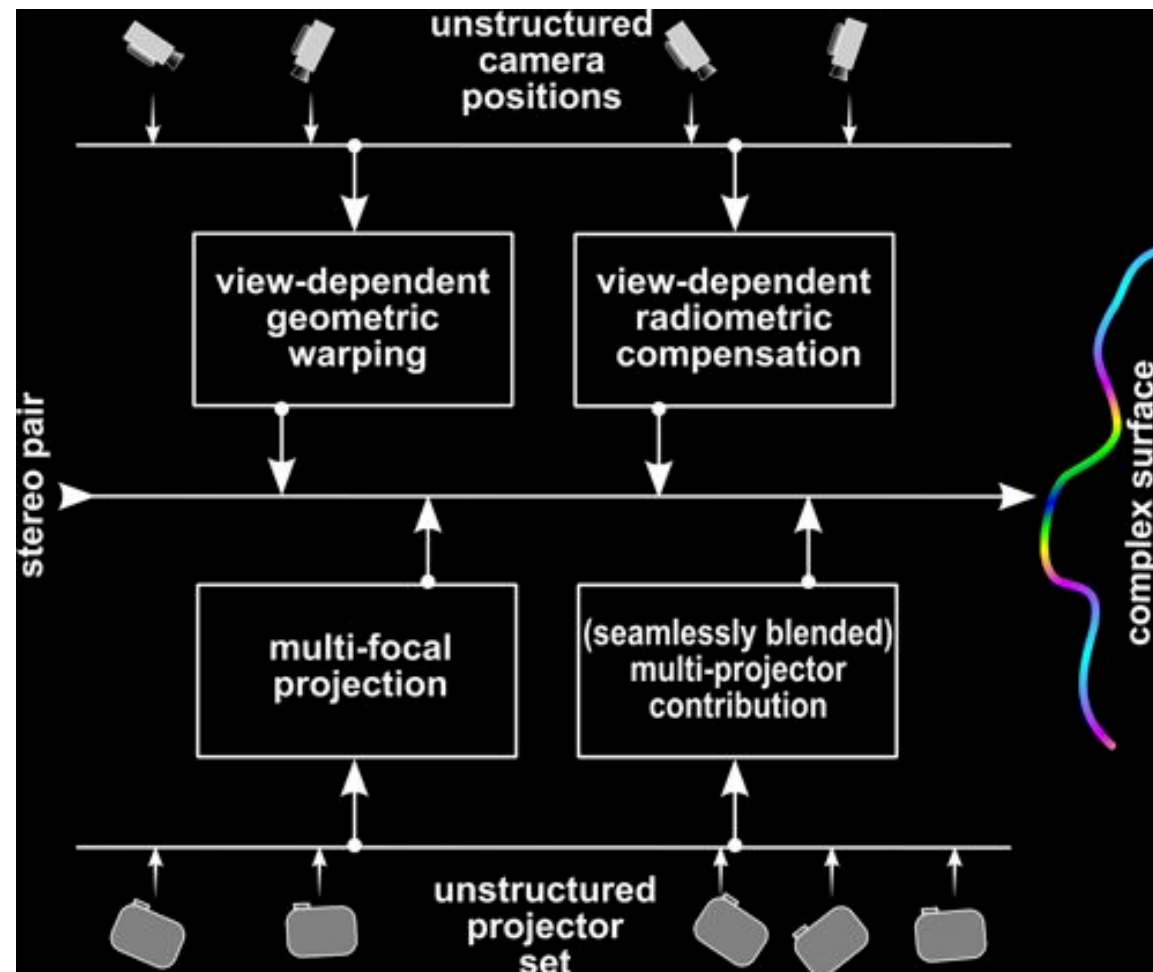


specular reflection, refraction, sub-surface scattering, inter-reflections, dispersion, diffraction, etc.

A Multi-Projector-Camera Approach

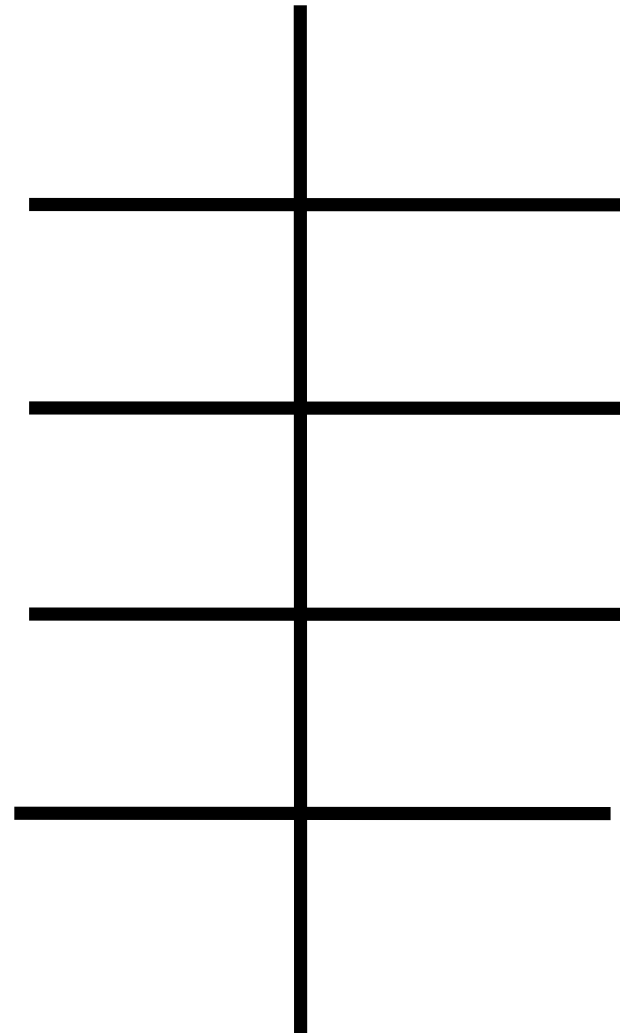


A Multi-Projector-Camera Approach

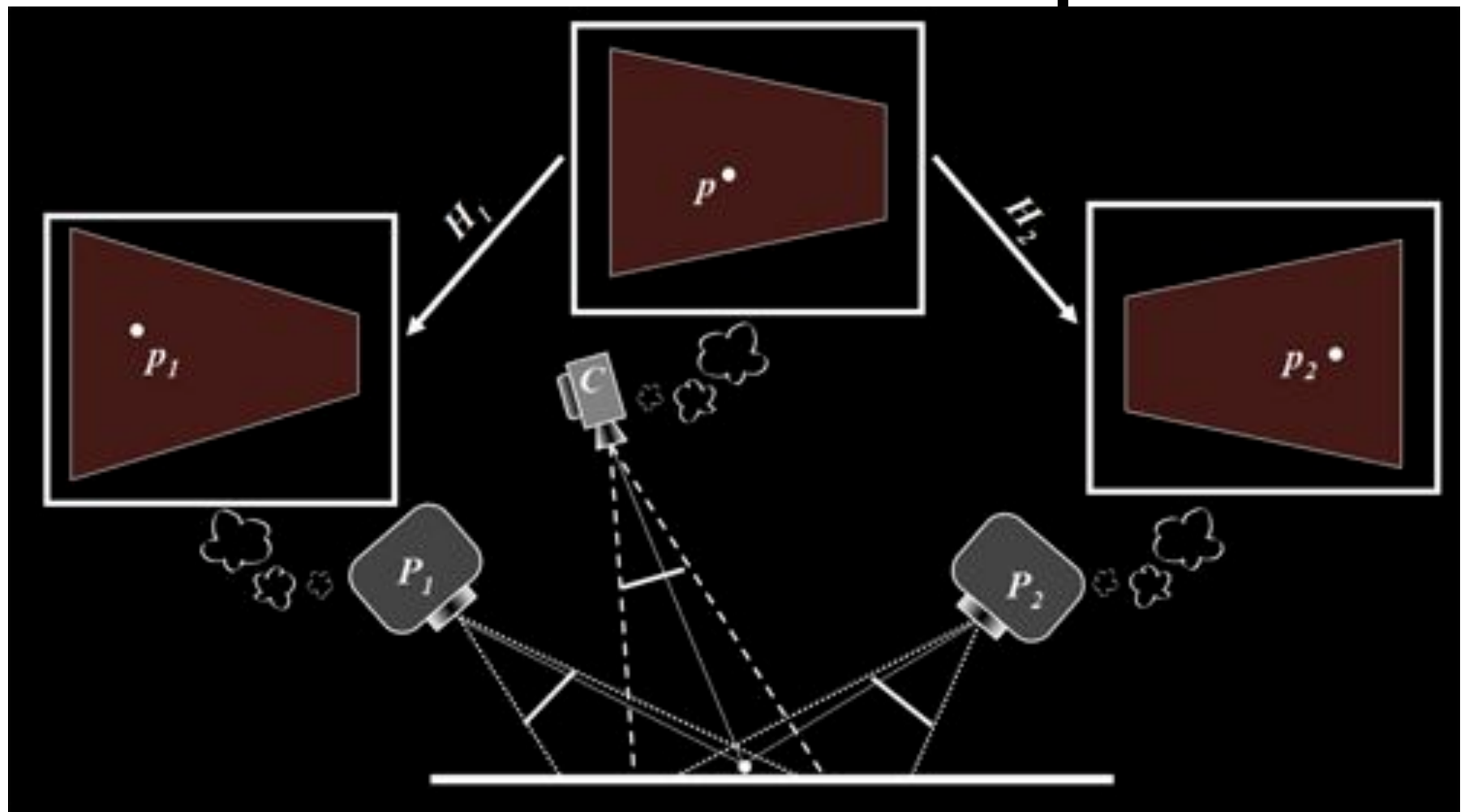


Geometric Correction

Planar Surfaces



Planar Surfaces



Homography

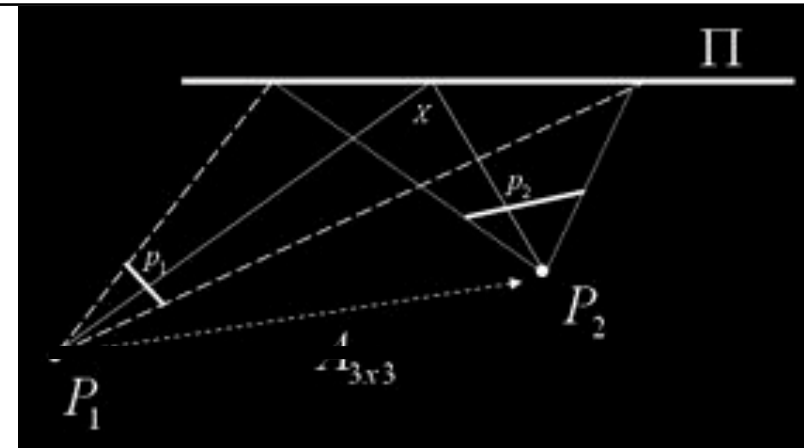


Homography

- homography is a mapping between two projections over a plane
- can map pixel coordinates from one perspective to another
- equation system has to be solved to determine 8 parameters of matrix A
- can be used directly in transformation pipeline by multiplying the following matrix after projection (without perspective division):

$$A_{4 \times 4} = \begin{bmatrix} a_{11} & a_{12} & 0 & a_{13} \\ a_{21} & a_{22} & 0 & a_{23} \\ 0 & 0 & 1 & 0 \\ a_{31} & a_{32} & 0 & 1 \end{bmatrix}$$

- ensure intact depth values with (approximately)



$$p_2 \cong A_{3 \times 3} p_1$$

$$\begin{bmatrix} p_{2x} \\ p_{2y} \\ 1 \end{bmatrix} \cong \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} p_{1x} \\ p_{1y} \\ 1 \end{bmatrix}$$

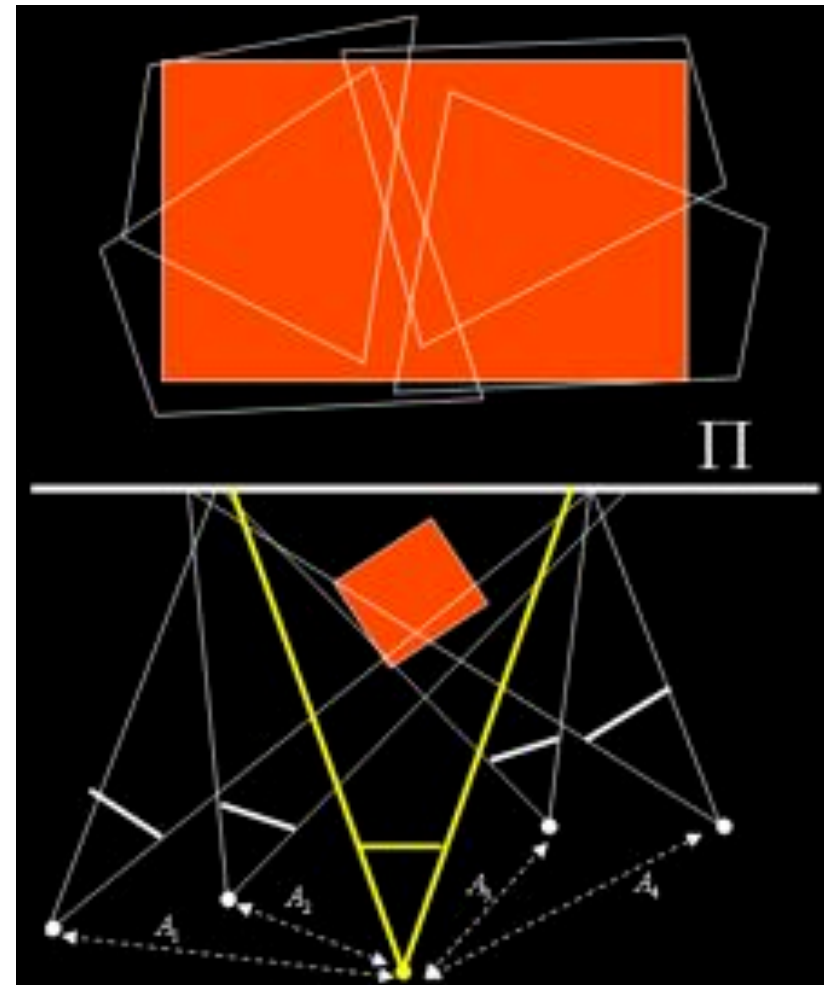
$$p_{2z} = \frac{p_{1z}}{(a_{31}p_{1x} + a_{32}p_{1y} + p_{1z})} \in [-1, 1]$$

$$A_{4 \times 4} = \begin{bmatrix} a_{11} & a_{12} & 0 & a_{13} \\ a_{21} & a_{22} & 0 & a_{23} \\ 0 & 0 & 1 - |a_{31}| - |a_{32}| & 0 \\ a_{31} & a_{32} & 0 & 1 \end{bmatrix}$$

Multi-Projector Registration

Multi-Projector Registration

- registering multiple projectors onto a common planar surface
- map all perspective into a single target perspective via homographies
- target perspective can be camera perspective
 - automatic determination of matrix parameters via structured light
- rendering
 - render image for target perspective (if target perspective is **orthogonal** to plane, then it can be done with an off-axis projection of an observer!)
 - map pixels into individual projector views (i.e., multiply 4x4 version of homography matrix onto matrix stack [after projection] and ensure that depth values remain intact!)



Example: Tiled Projection Screens

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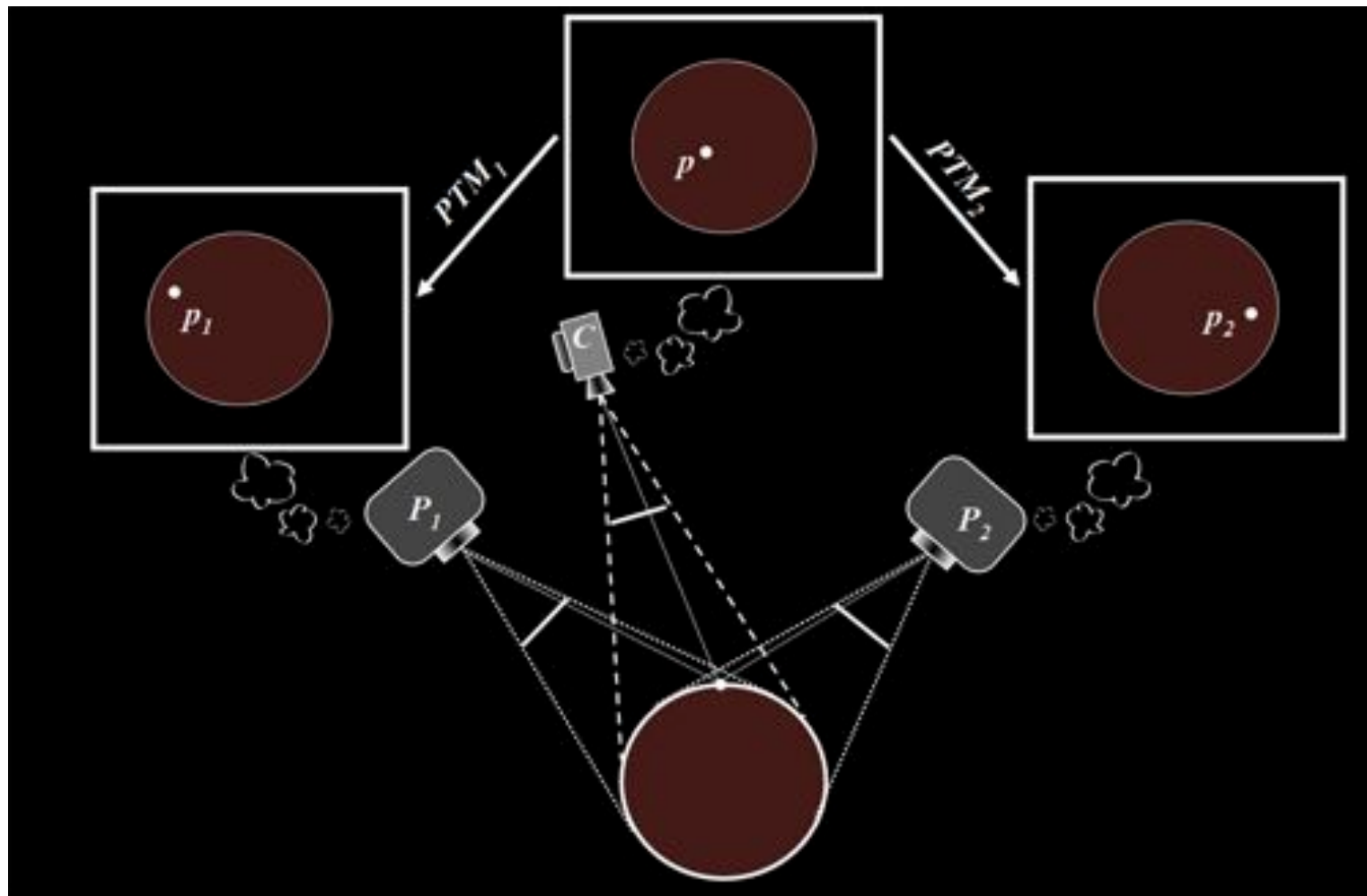


Courtesy: Brown, et al.,
IEEE TVCG, 2005

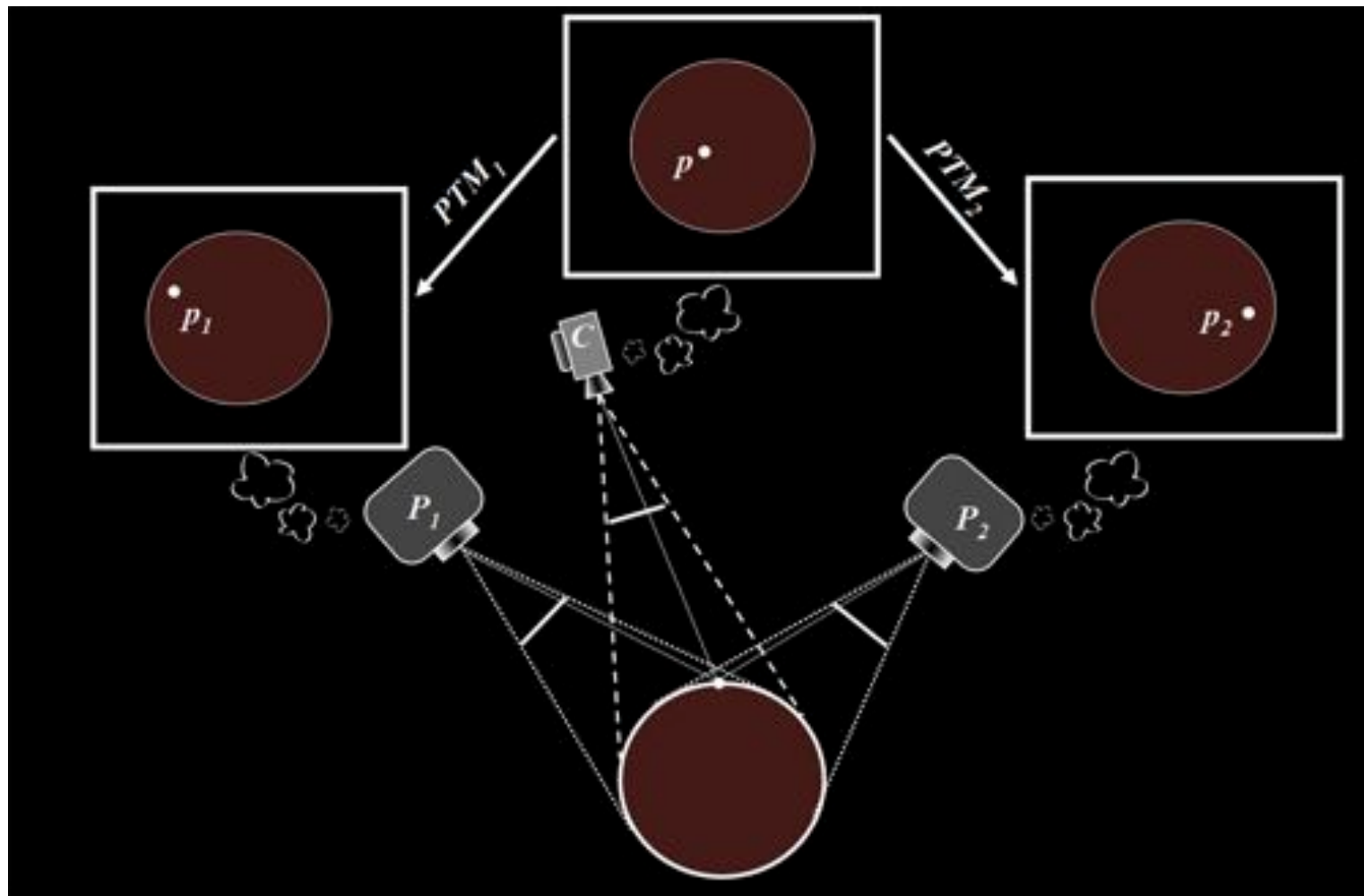


Non-Trivial Surfaces

Non-Trivial Surfaces



Non-Trivial Surfaces

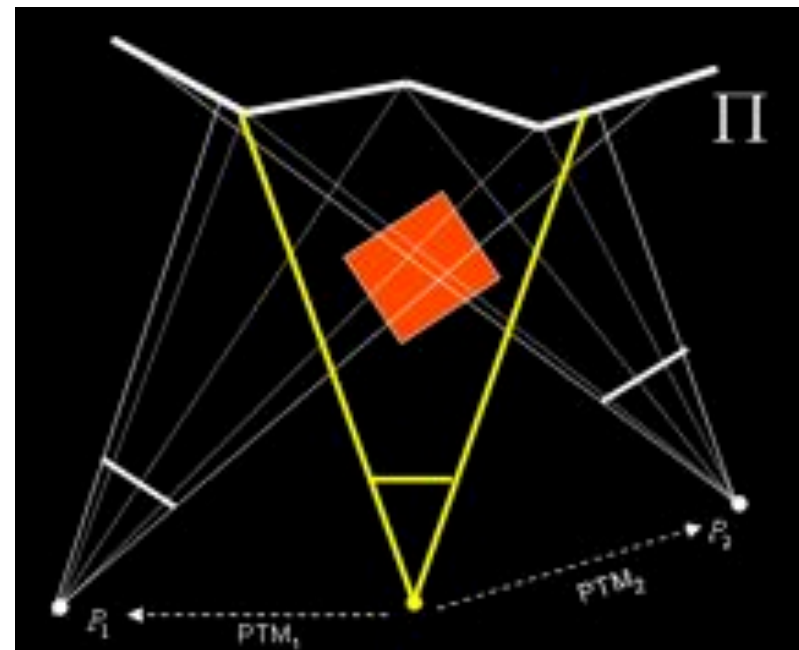


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Projective Texture Mapping

Projective Texture Mapping

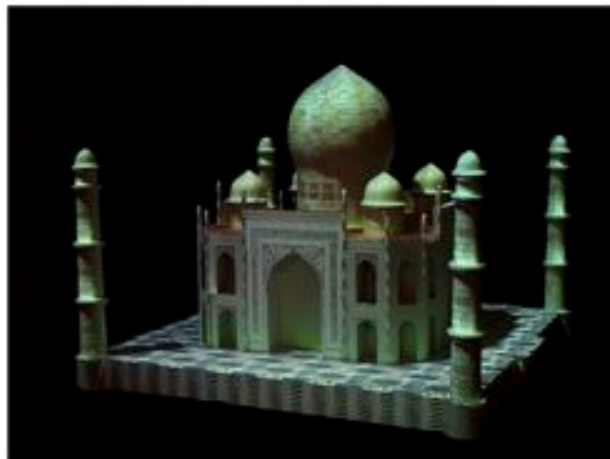
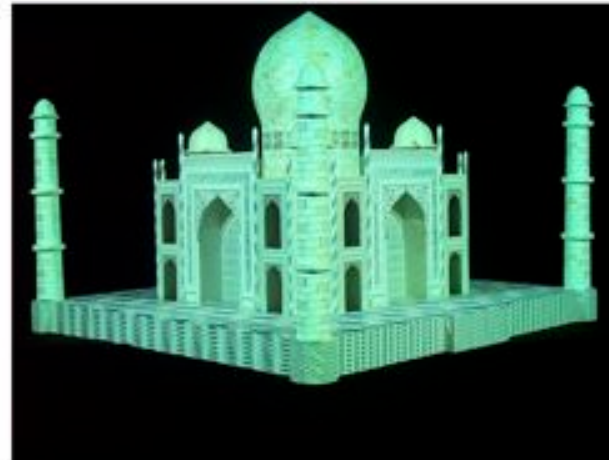
- given a geometric definition of the surface
 - scan or model
- determine intrinsic and extrinsic of projectors with respect to surface
 - measure projections of known 3D surface points on image plane of projector and solve equation system to determine parameters of matrix
- define virtual camera with same parameter for each projector
- render 3D model of surface, textured with images, from perspective of projectors/virtual cameras
- texture coordinates can be automatically generated from target perspective via projective texture mapping



$$\begin{pmatrix} wX \\ wY \\ wZ \\ w \end{pmatrix} = \begin{bmatrix} f & \cdot & \cdot & \cdot \\ \cdot & f & \cdot & \cdot \\ \cdot & \cdot & \cdot & 1 \\ \cdot & \cdot & 1 & \cdot \end{bmatrix} \begin{bmatrix} R_{11} & R_{12} & R_{13} & t_x \\ R_{21} & R_{22} & R_{23} & t_y \\ R_{31} & R_{32} & R_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$

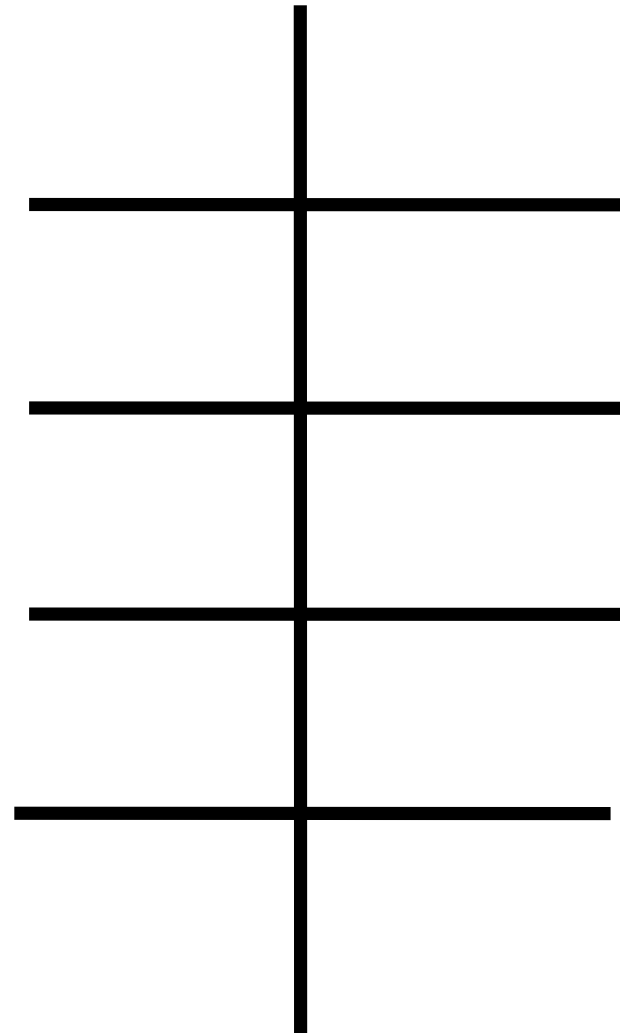
Example: Shader Lamps

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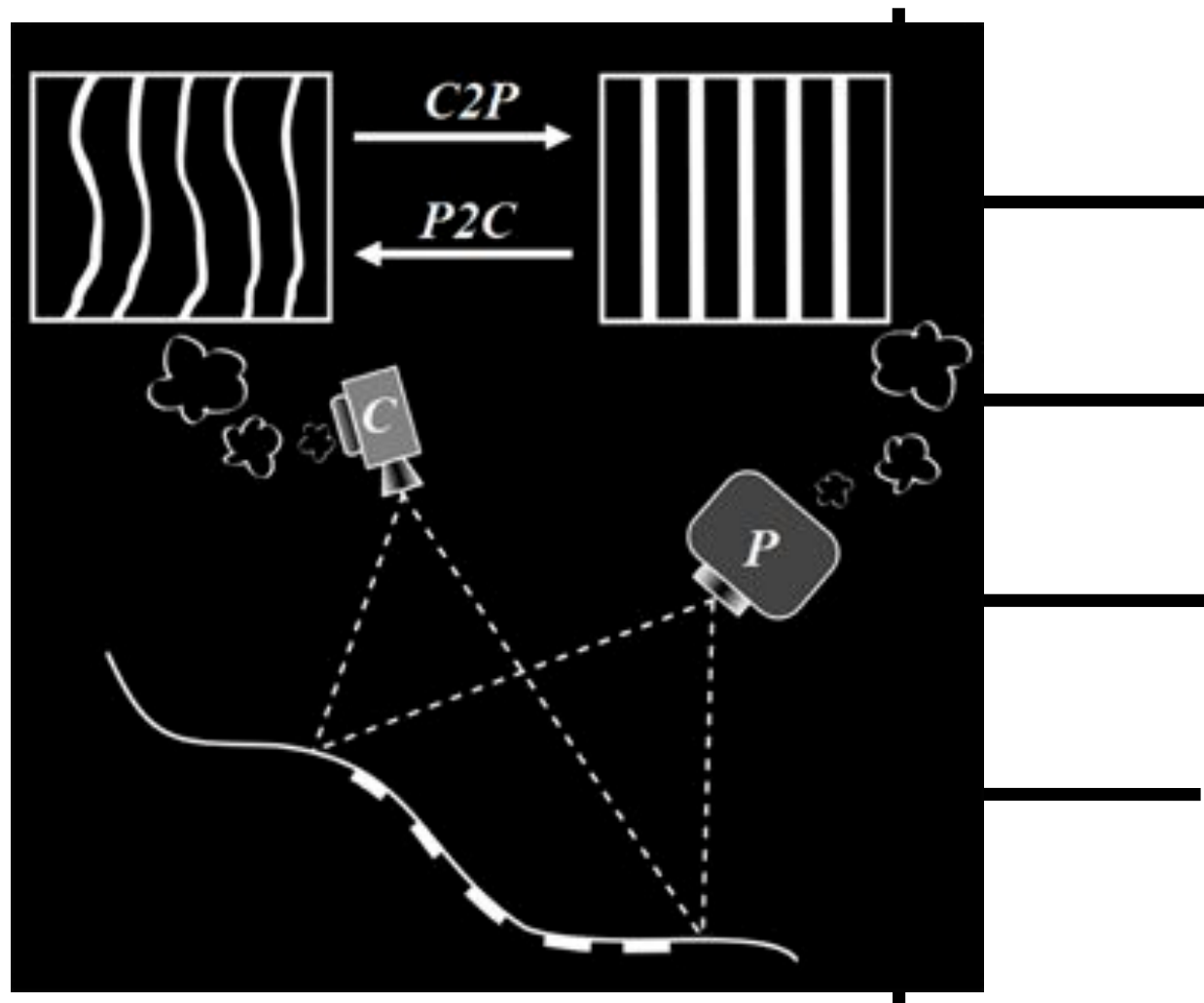


Courtesy: Raskar, et al., EGRW 2001

Complex Surfaces



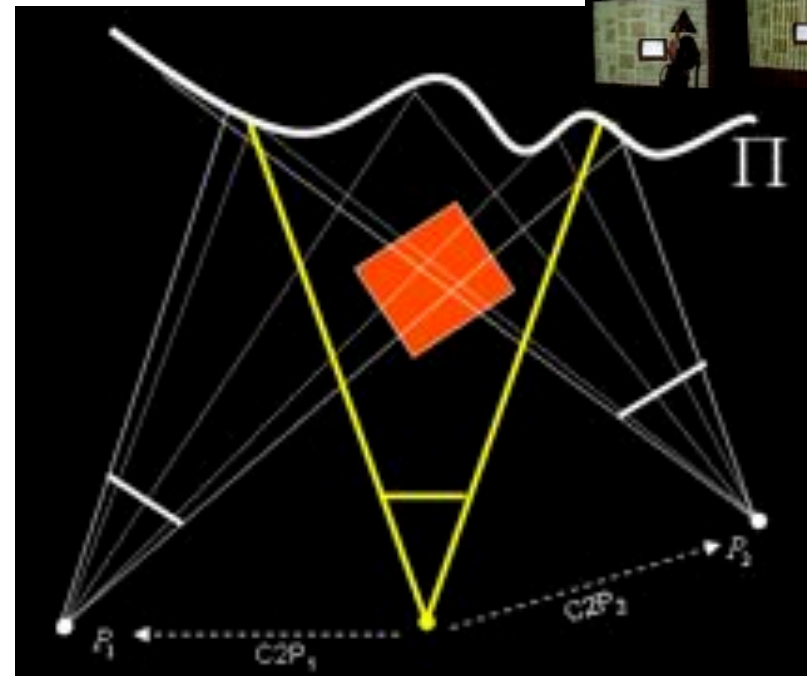
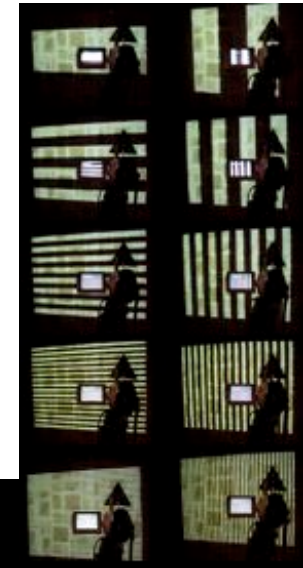
Complex Surfaces



Pixel Displacement Mapping

Pixel Displacement Mapping

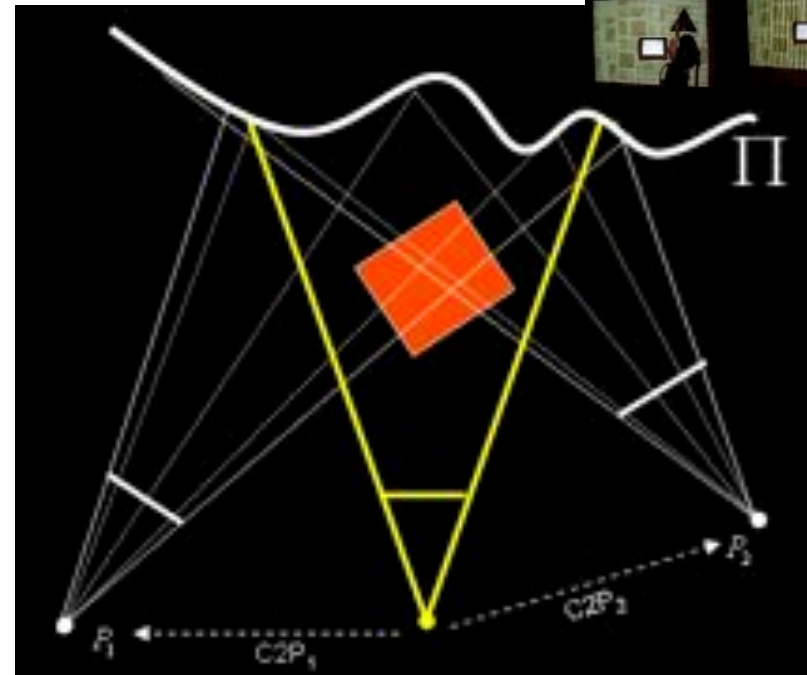
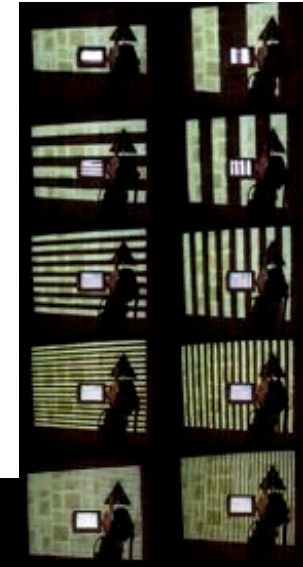
- registering projections to such a surface by determining their intrinsic and extrinsic is too imprecise
 - non-linear lens distortion
 - errors in measuring fiducials
- rendering of 3D surface representation from perspective of projector might be too slow
 - high geometric complexity of model
 - many triangles to render
 - project, raster, texture
- measure per-pixel mapping between projector perspectives and target perspective (e.g., camera)
- render image from target perspective and map it (look-up) into perspective of projectors (e.g., pixel-shading)



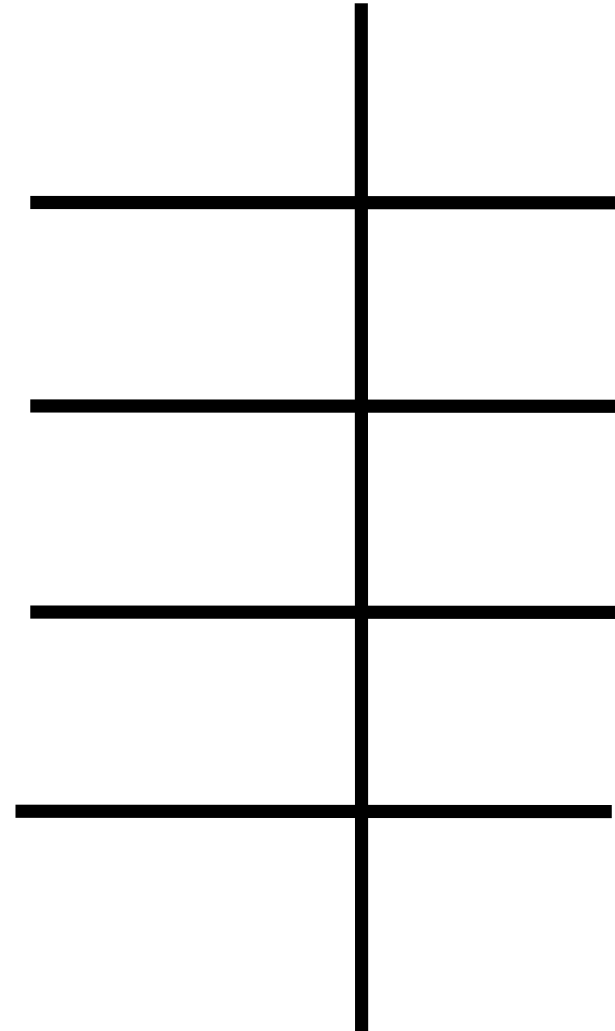
Pixel Displacement Mapping

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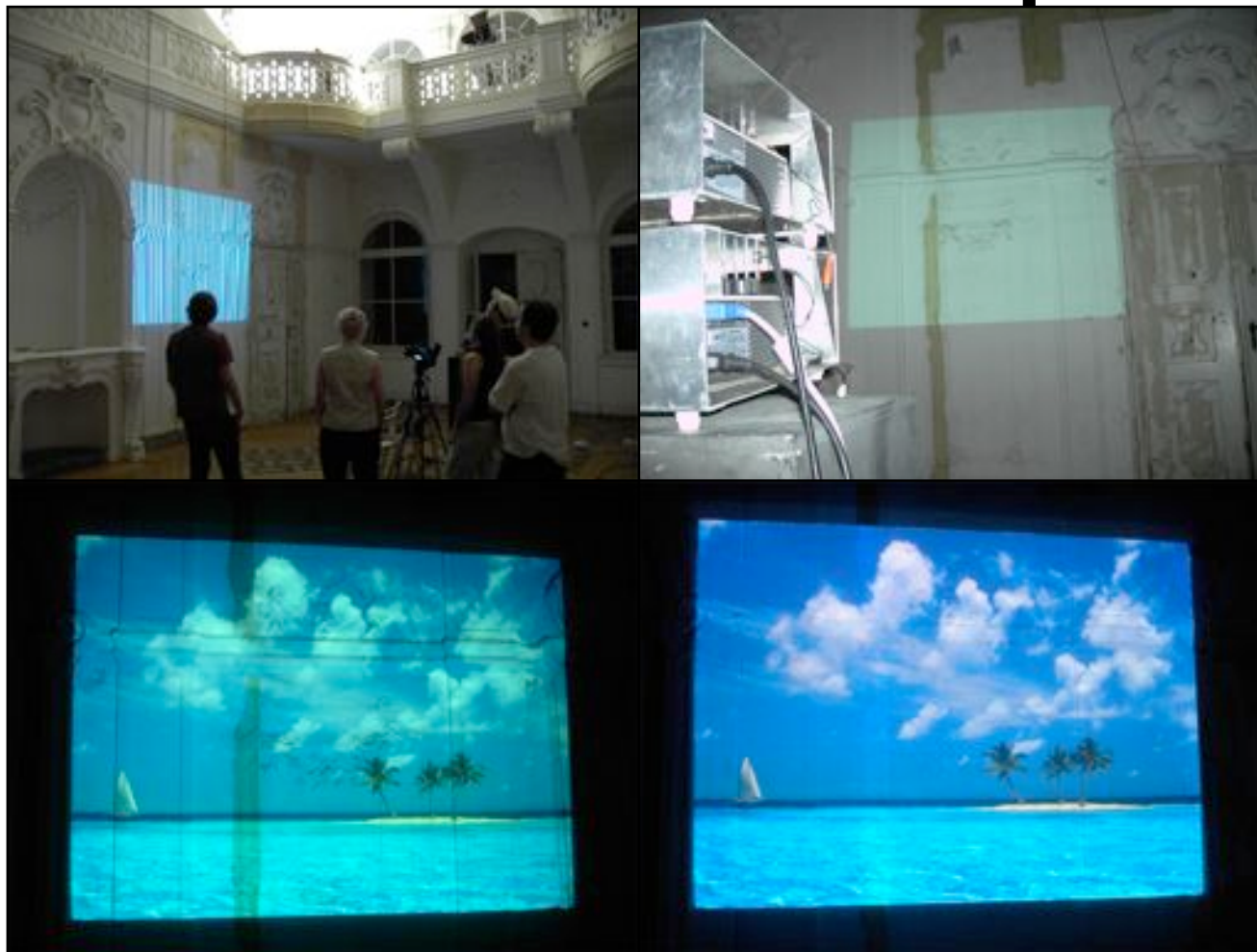
problem:
works only for static target perspective!
(but image-based rendering approaches exist)



Example: Stucco Wall

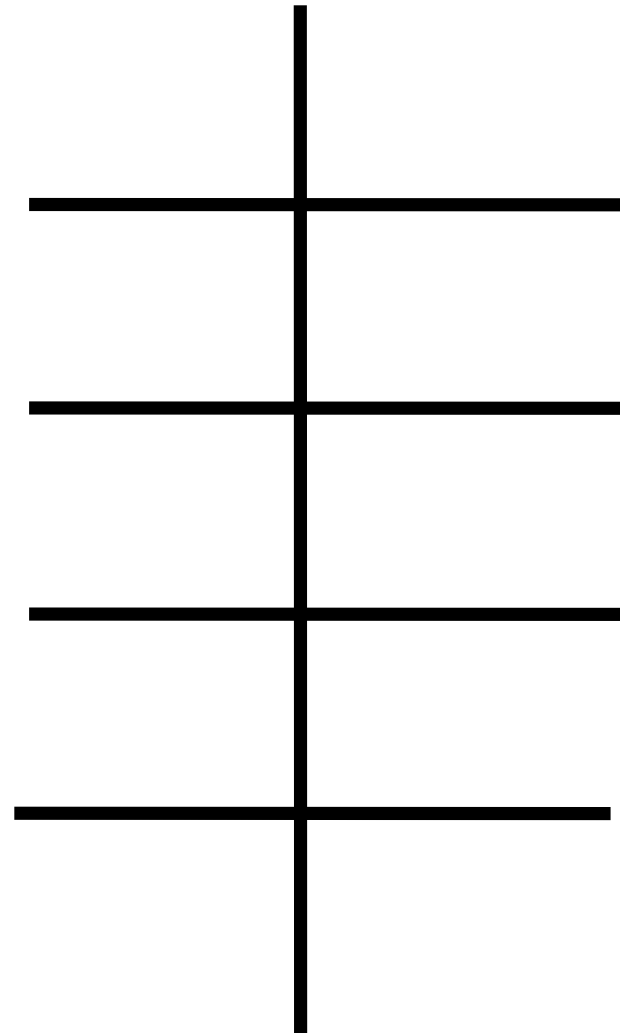


Example: Stucco Wall



In coop. with
castle Etters-
burg

Example: Fossil Cast

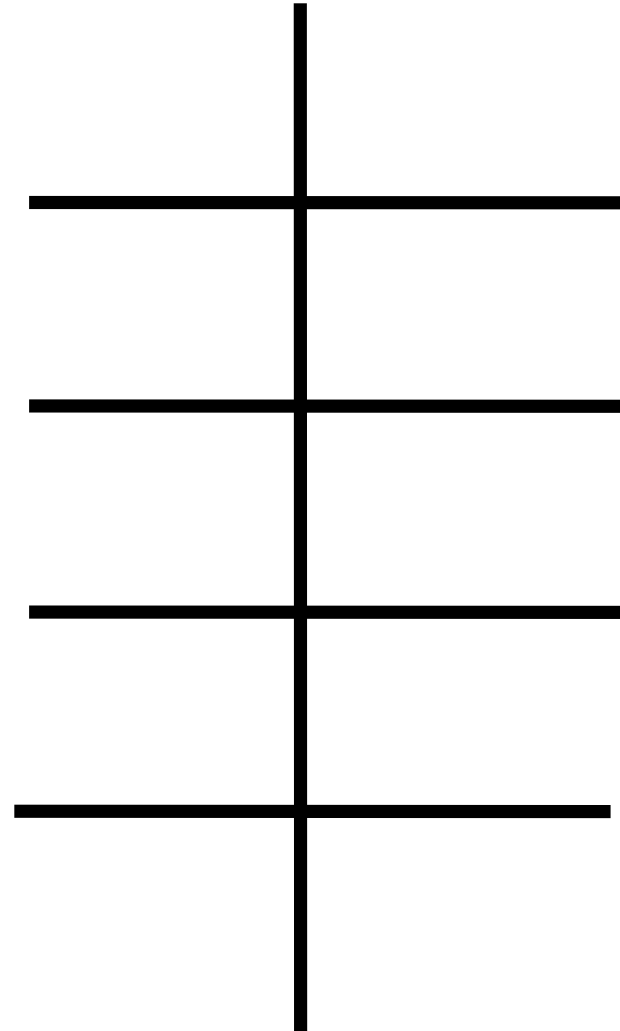


Example: Fossil Cast

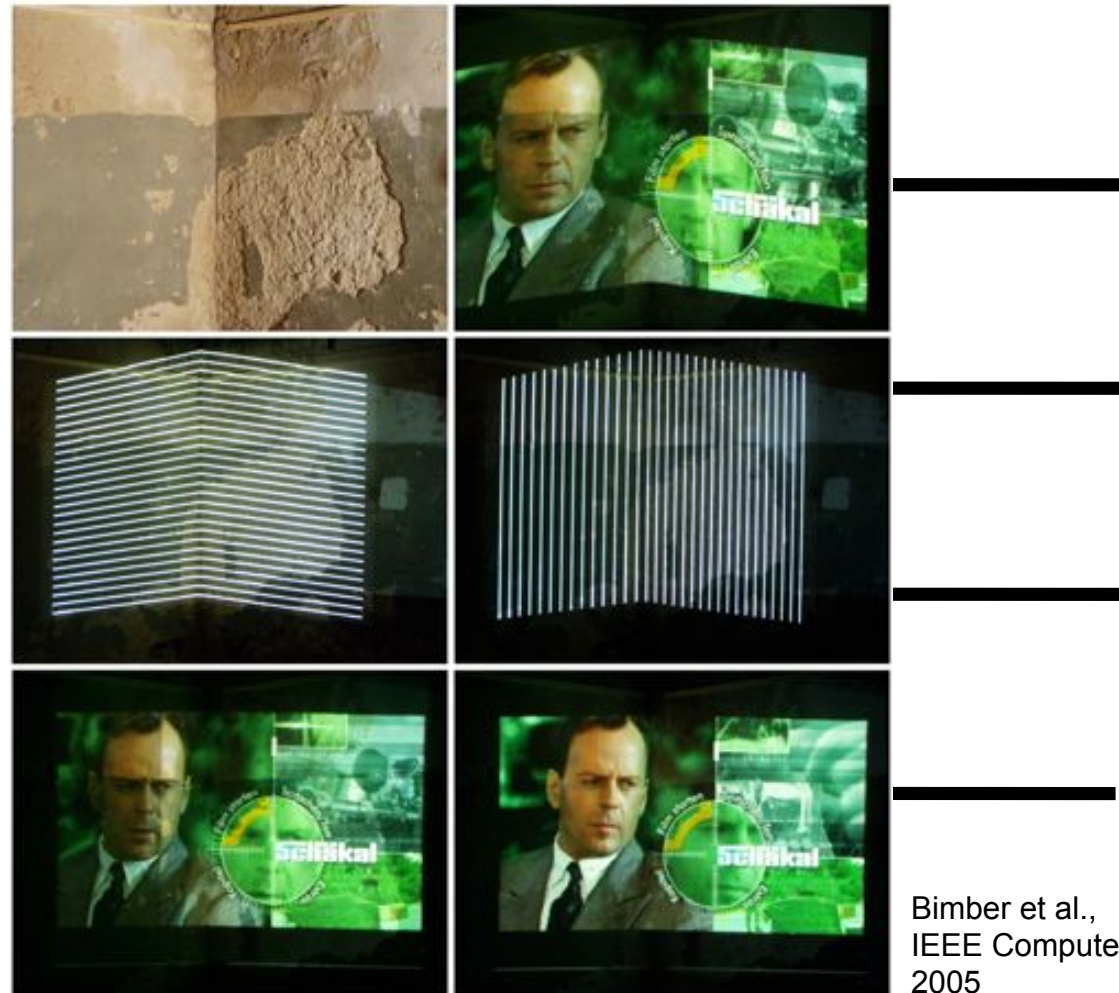


In coop. with Senckenberg Museum

Example: Scruffy Room Corner

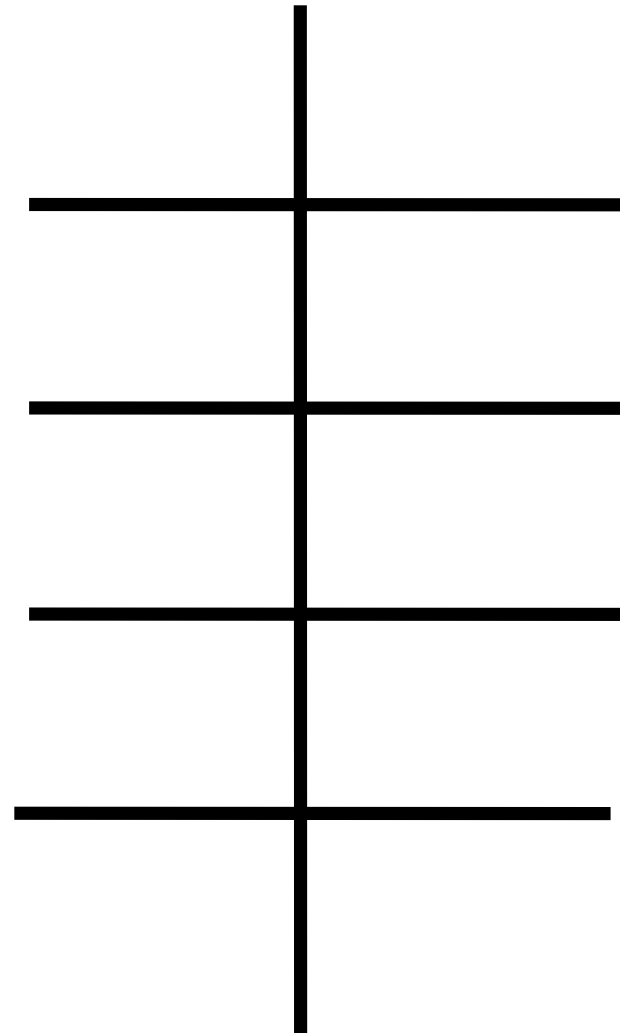


Example: Scruffy Room Corner



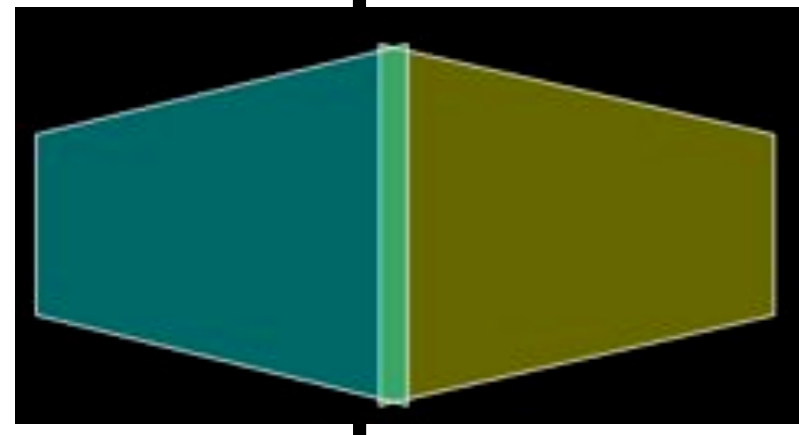
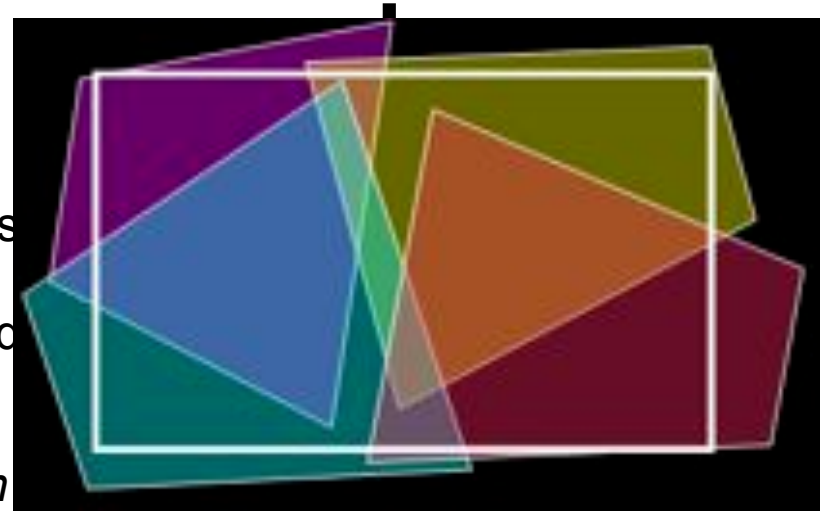
Radiometric Compensation

Photometric Calibration

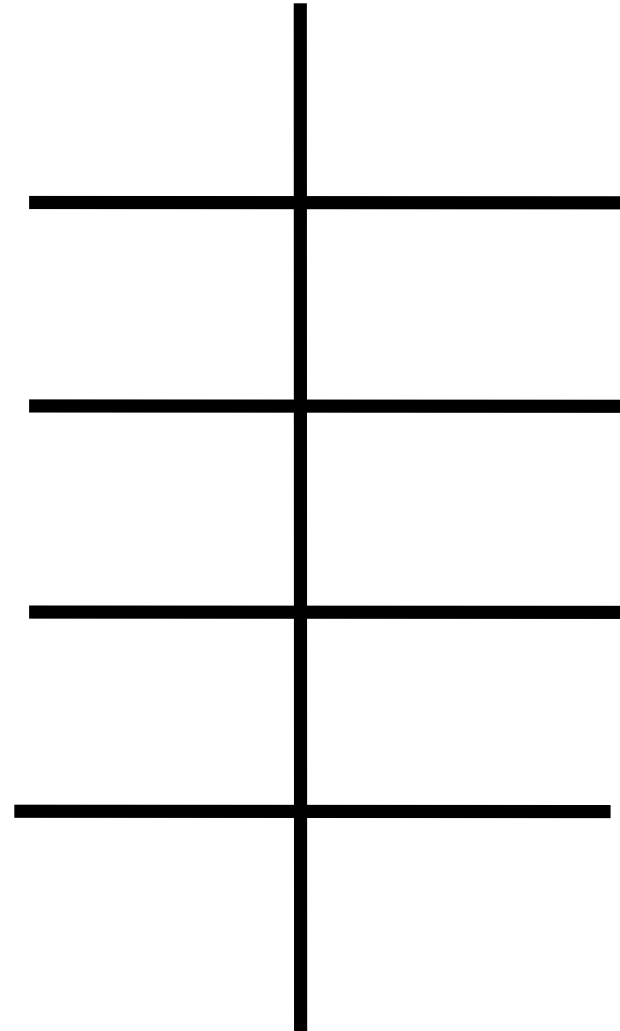


Photometric Calibration

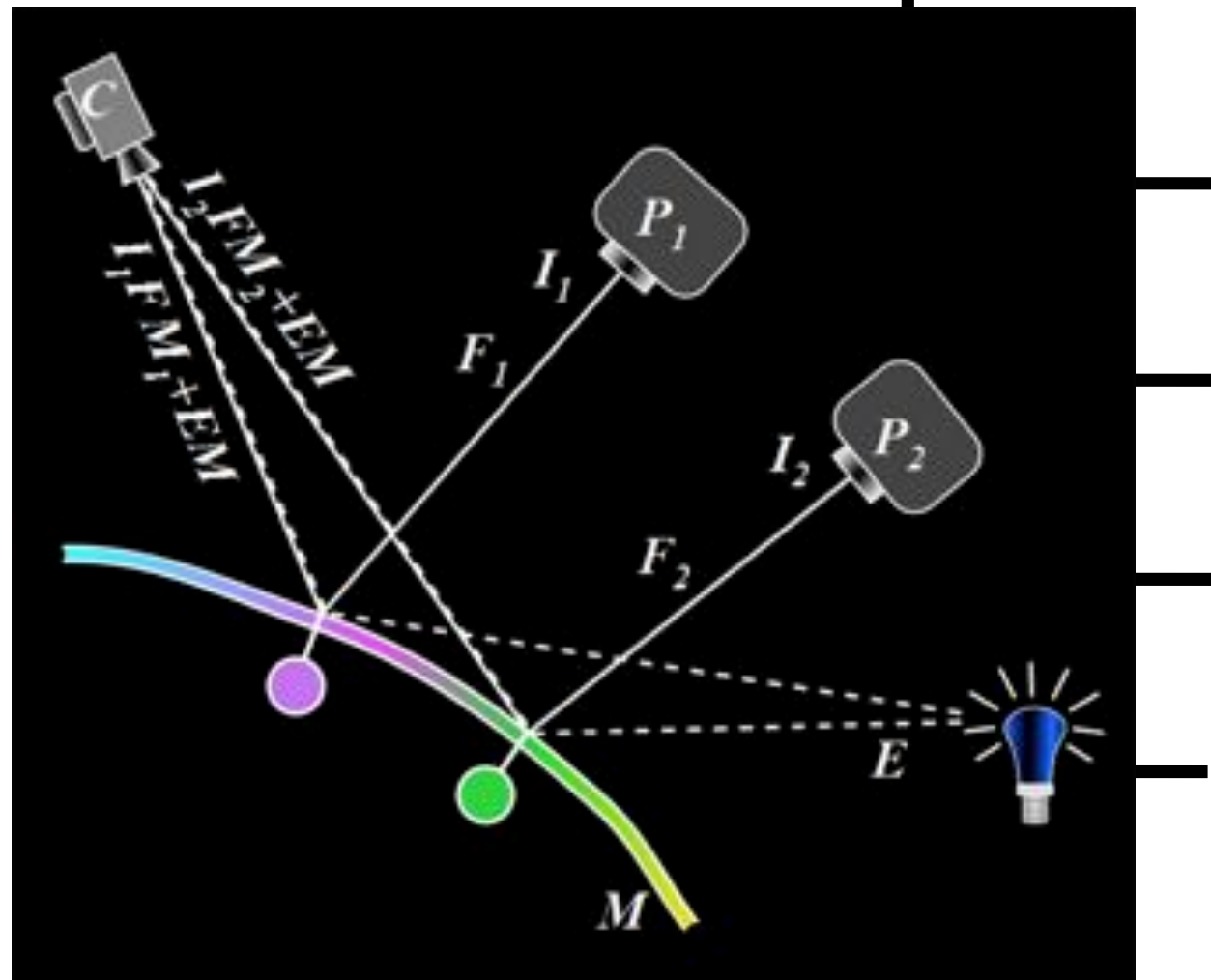
- regions of display surfaces that are illuminated by multiple projectors simultaneously appear brighter
- projectors can have different brightness and can cover a different color space
- result: inconsistent image (intensity and color)
- humans can perceive 2% difference in brightness and a color variation of $2nm$
- variations in brightness is more critical than variation in color
- solutions: intensity blending and color space mapping
- **these techniques are not explained here!**
- **we assume that projectors and cameras are linearized and color mapped**



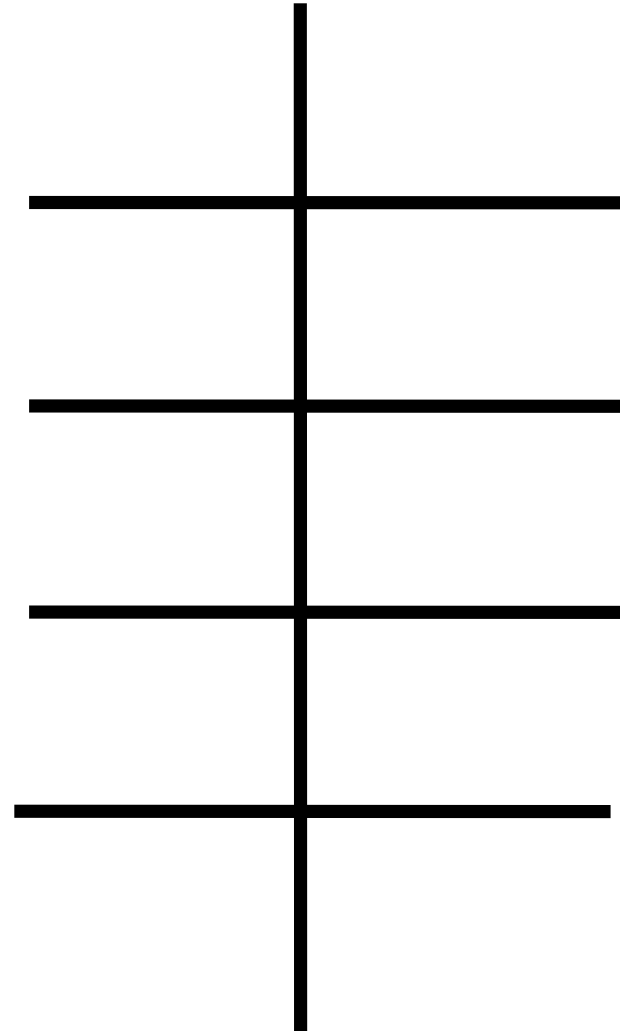
Compensating Local Light Effects



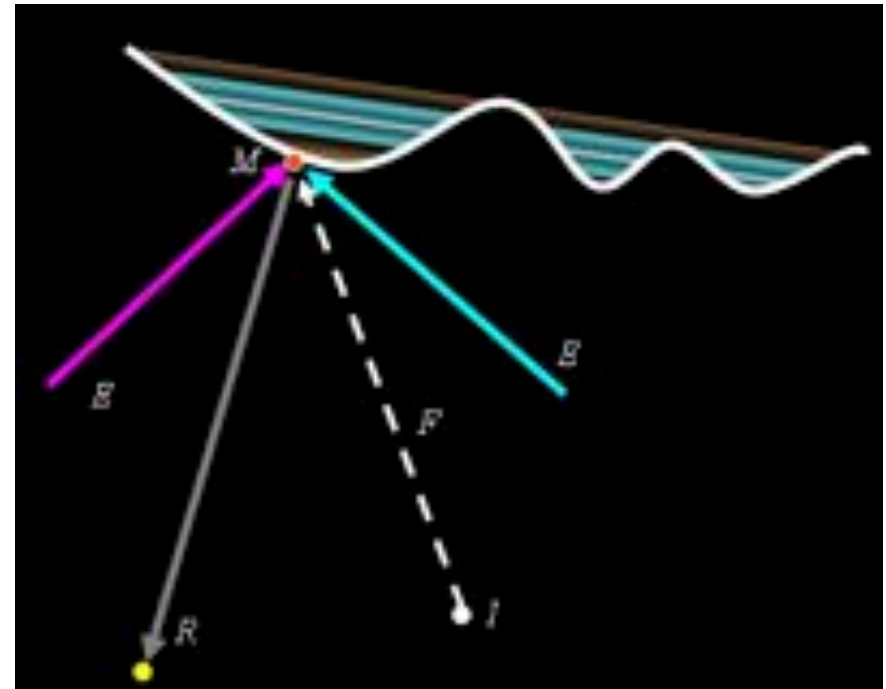
Compensating Local Light Effects



Single Projector



Single Projector



$$R = IFM + EM$$

I → projected image

B → black-level

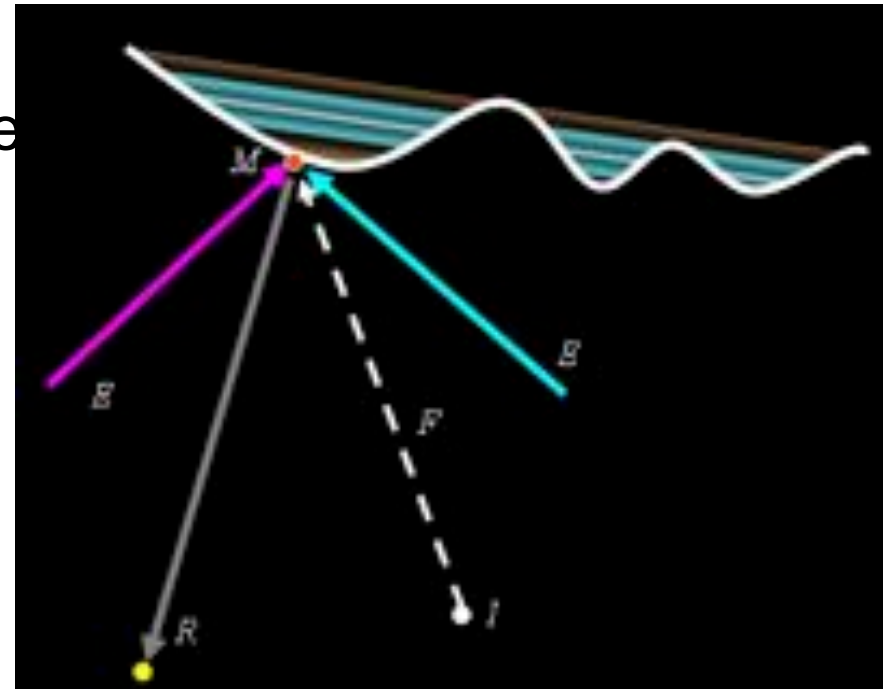
F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture



$$R = IFM + EM$$

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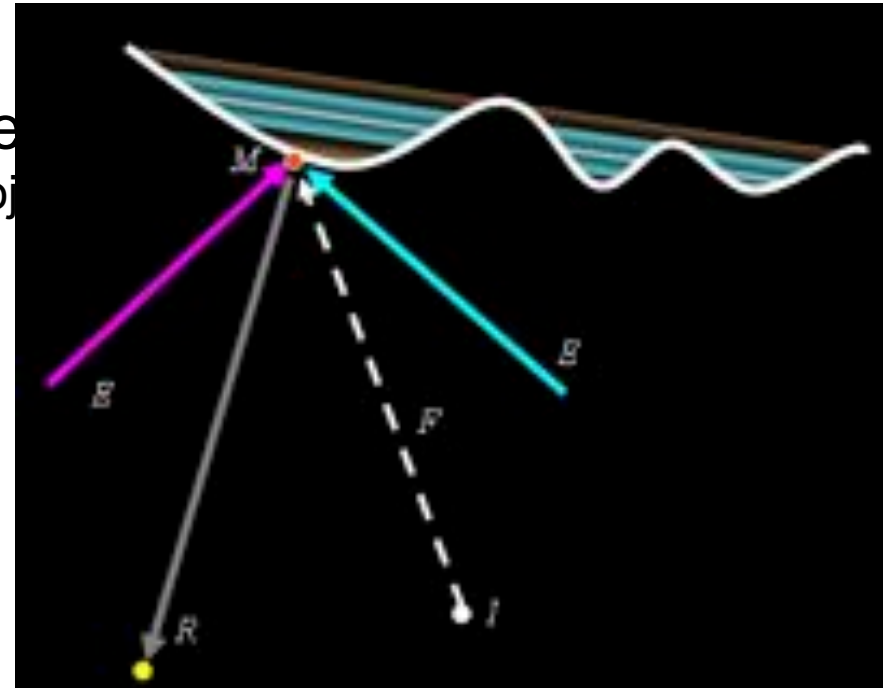
E → environment light

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Single Projector

determining parameters (texture

- (1) turn off environment light and project black flood image



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

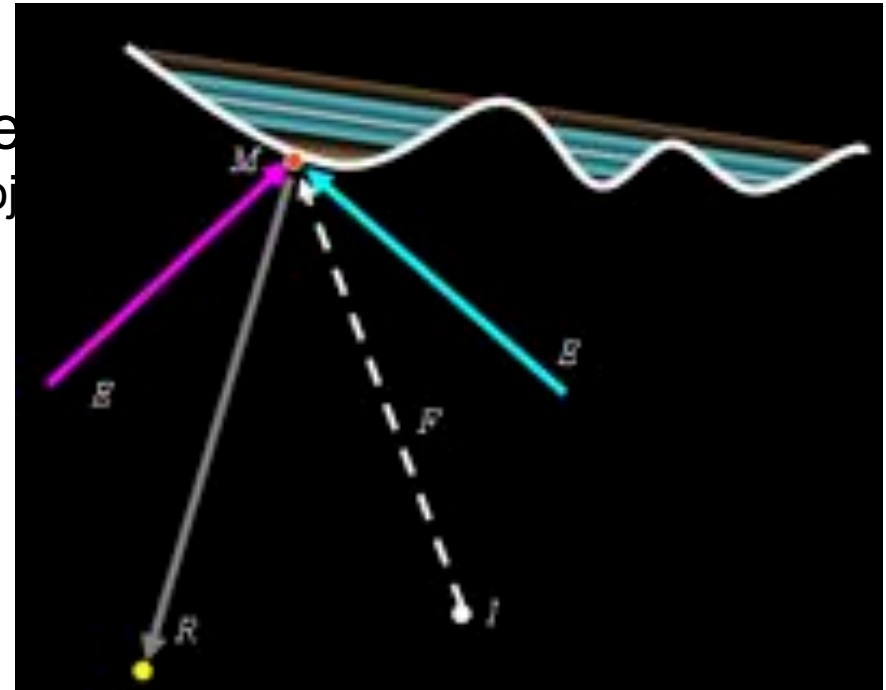
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Single Projector

determining parameters (texture

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow BFM$$



$$R=IFM+EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

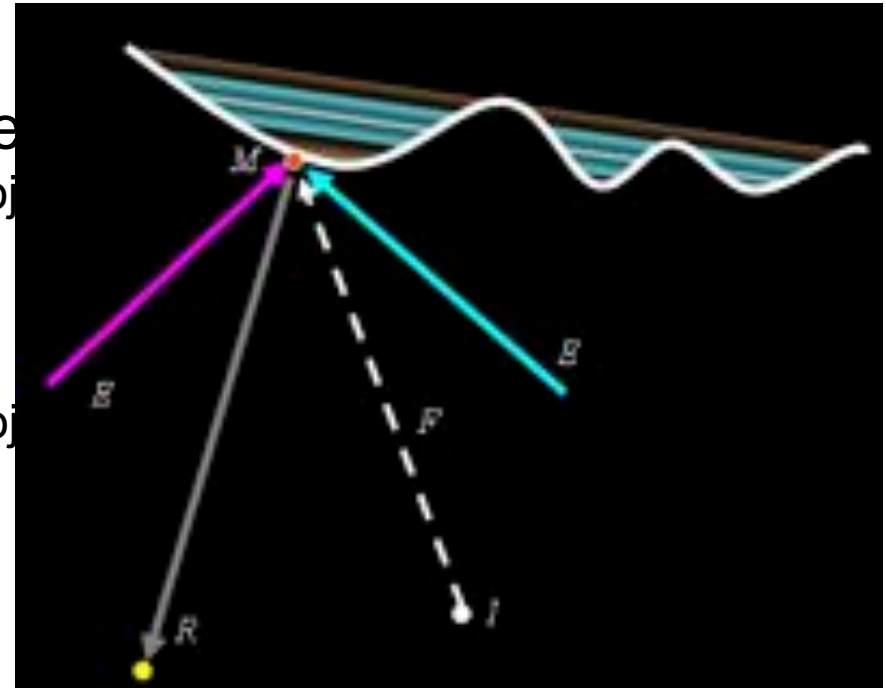
Single Projector

determining parameters (texture

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow BFM$$

- (2) turn on environment light and project black flood image



$$R=IFM+EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

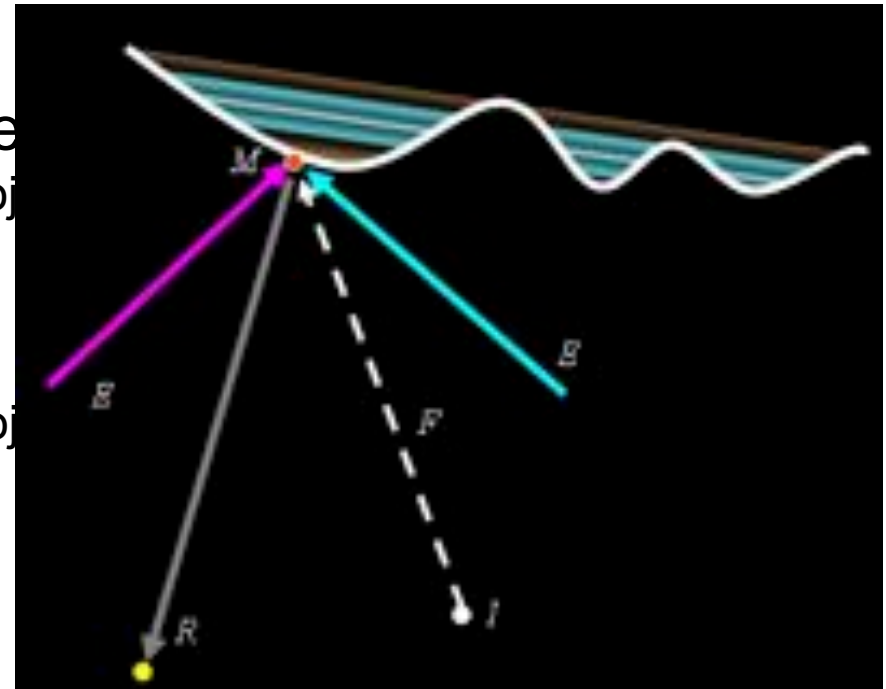
determining parameters (texture)

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture

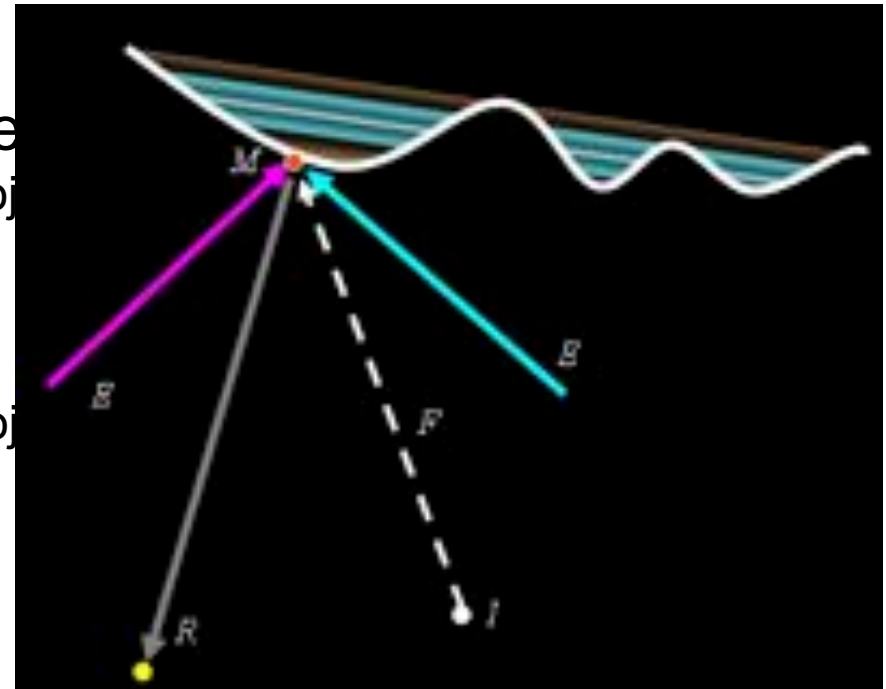
- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

- (3) turn off environment light and



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture)

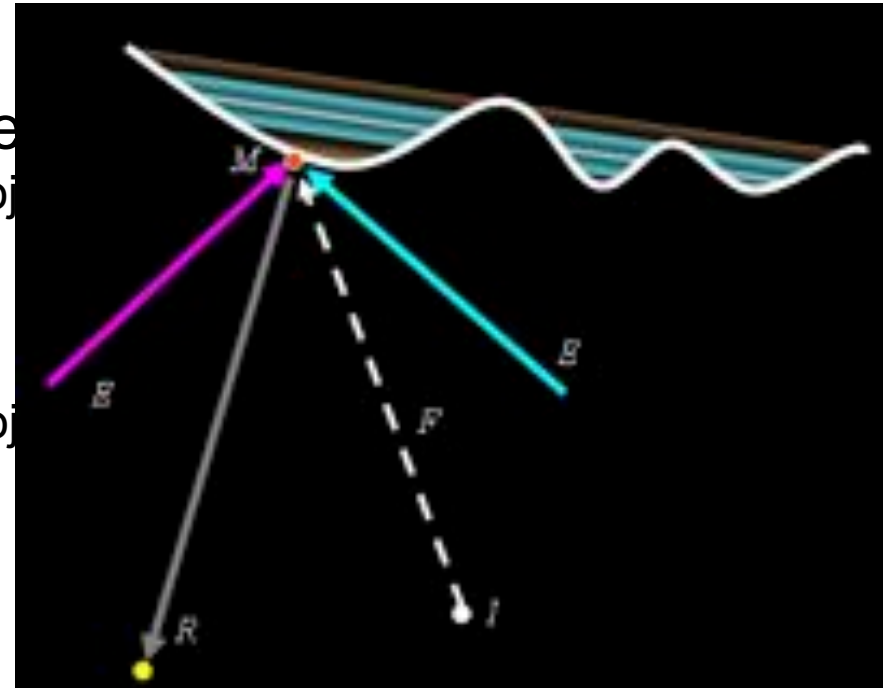
- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

- (3) turn off environment light and project white flood image



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture)

- (1) turn off environment light and project black flood image

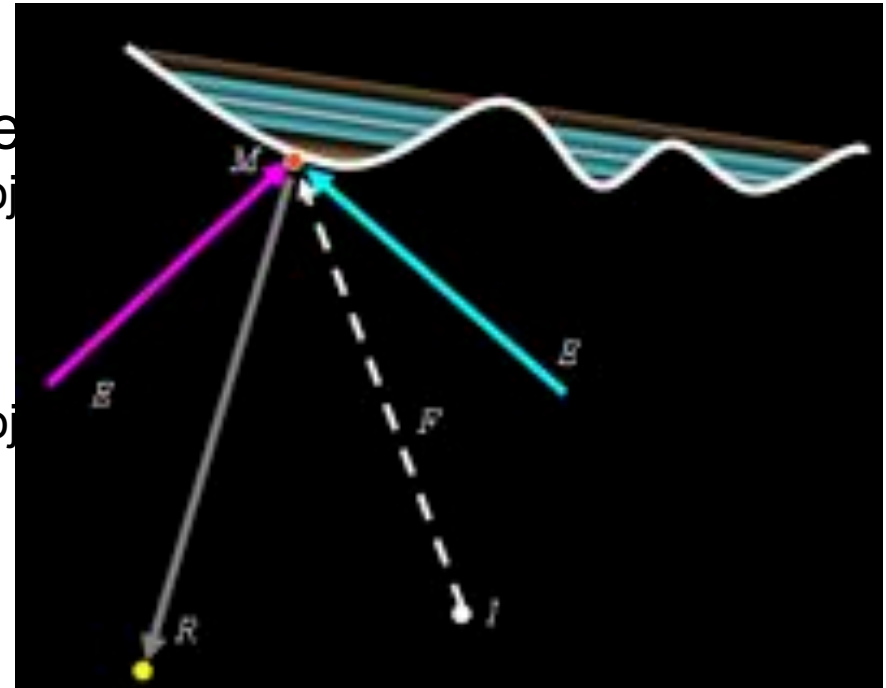
$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

- (3) turn off environment light and project white flood image

$$I=1, E=0 \rightarrow \text{FM (incl. BFM !)}$$



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture)

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

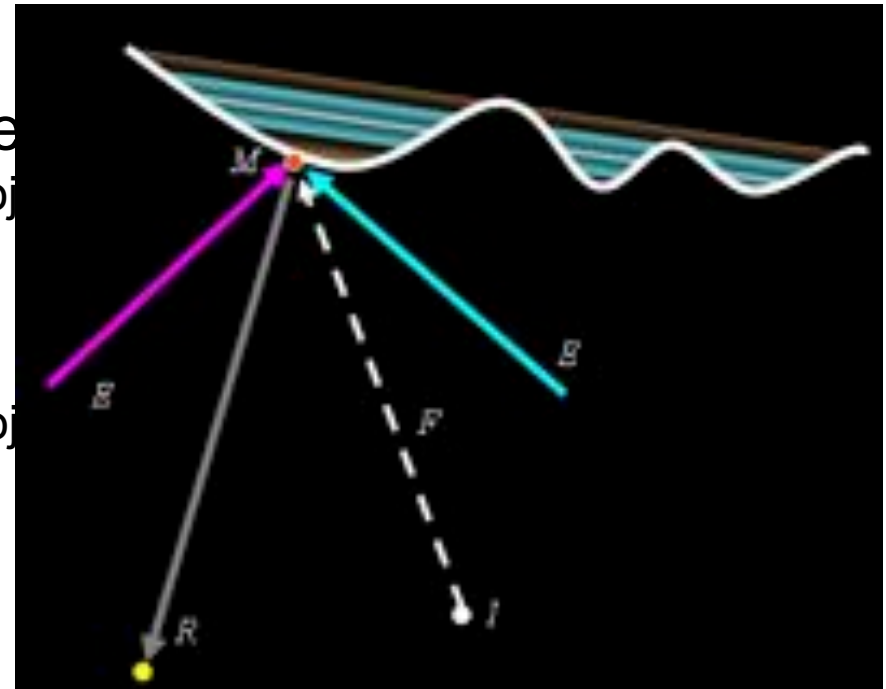
- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

- (3) turn off environment light and project white flood image

$$I=1, E=0 \rightarrow \text{FM (incl. BFM !)}$$

$$\rightarrow \text{FM} = \text{FM} - \text{BFM}$$



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

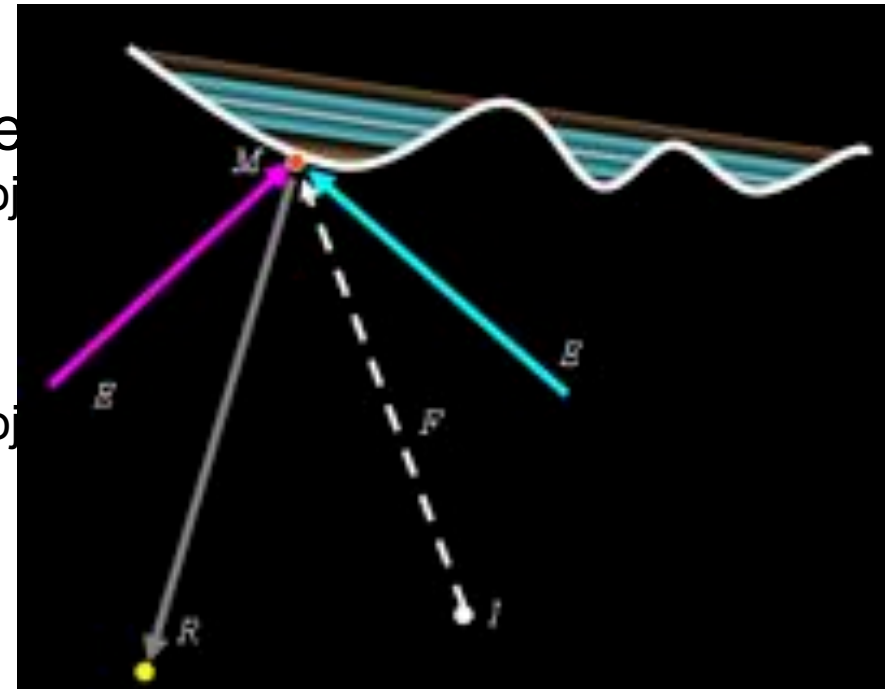
$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

- (3) turn off environment light and project white flood image

$$I=1, E=0 \rightarrow \text{FM (incl. BFM !)}$$

$$\rightarrow \text{FM} = \text{FM} - \text{BFM}$$

compensation (per pixel):



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Single Projector

determining parameters (texture

- (1) turn off environment light and project black flood image

$$I=0, E=0 \rightarrow \text{BFM}$$

- (2) turn on environment light and project black flood image

$$I=0, E=1 \rightarrow \text{EM (incl. BFM !)}$$

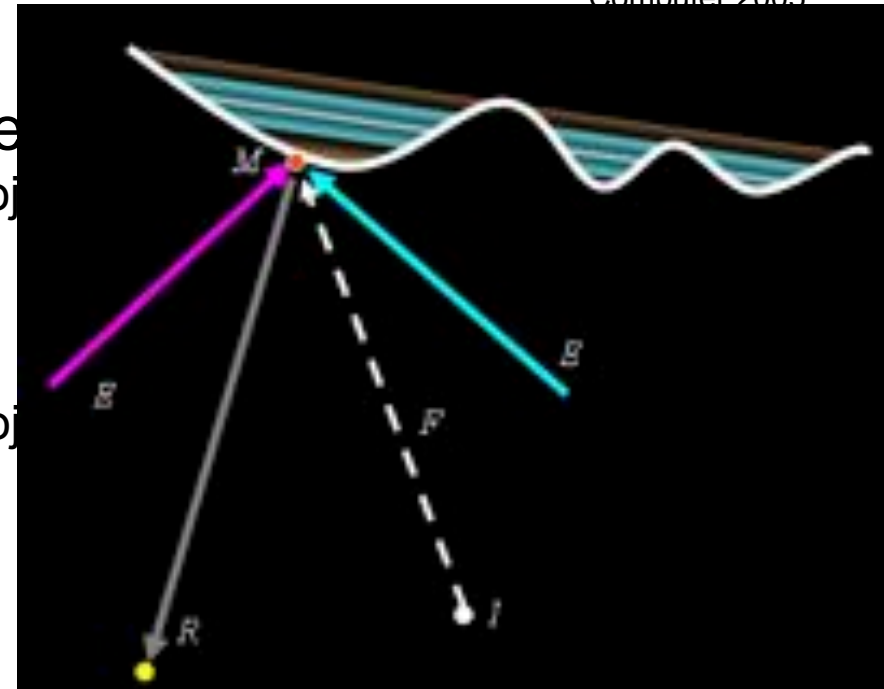
- (3) turn off environment light and project white flood image

$$I=1, E=0 \rightarrow \text{FM (incl. BFM !)}$$

$$\rightarrow \text{FM} = \text{FM} - \text{BFM}$$

compensation (per pixel):

$$I = (R - EM) / (FM)$$



$$R = IFM + EM$$

I → projected image

B → black-level

F → projector-2-surface form factor

E → environment light

M → surface reflectance (diffuse)

Color Mixing

Color Mixing

$$\begin{array}{c}
 \text{red in red} \quad \text{green in red} \quad \text{blue in red} \\
 \downarrow \quad \quad \downarrow \quad \quad \downarrow \\
 V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix} \\
 \text{(per)}
 \end{array}$$

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

$$\begin{array}{c}
 \text{red in red} \quad \text{green in red} \quad \text{blue in red} \\
 \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \\
 V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix} \\
 \text{(per)} \quad \quad \quad \downarrow \\
 \rightarrow \text{FM (in un-normalized matrix)}
 \end{array}$$

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

red in red
green in red
blue in red

(per) → FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

red in red
green in red
blue in red

(per) → FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

red in red
green in red
blue in red

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

red in red
green in red
blue in red

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(pe)

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

red in red
green in red
blue in red

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1, \Delta I_i = \Delta C_i$)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

red in red
green in red
blue in red

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1, \Delta I_i = \Delta C_i$)

capture 6 images C (2 per color channel)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1, \Delta I_i = \Delta C_i$)

capture 6 images \mathbf{C} (2 per color channel to determine deltas)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

\rightarrow FM (in un-normalized matrix)

$$\mathbf{R} = \mathbf{V} * \mathbf{I}$$

$\mathbf{I} \rightarrow$ projected image

$\mathbf{V} \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1$, $\Delta I_i = \Delta C_i$)

capture 6 images \mathbf{C} (2 per color channel to determine deltas)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

red in red
green in red
blue in red

\rightarrow FM (in un-normalized matrix)

$$\mathbf{R} = \mathbf{V} * \mathbf{I}$$

$\mathbf{I} \rightarrow$ projected image

$\mathbf{V} \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1, \Delta I_i = \Delta C_i$)

capture 6 images \mathbf{C} (2 per color channel to determine deltas)

compensation (per pixel):

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

\rightarrow FM (in un-normalized matrix)

$$\mathbf{R} = \mathbf{V} * \mathbf{I}$$

$\mathbf{I} \rightarrow$ projected image

$\mathbf{V} \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1$, $\Delta I_i = \Delta C_i$)

capture 6 images \mathbf{C} (2 per color channel to determine deltas)

compensation (per pixel):

$I = V^{-1} * R$ (does not consider

red in red green in red blue in red

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel) \rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Color Mixing

determining color mixing matrix V :

for un-normalized matrix: (camera and projector response must be known and linearized):

capture 9+ images \rightarrow least squares

for normalized matrix (camera response must be known, projector response can be unknown):

diagonals are 1 (unknown scaling)

off-diagonals are $V_{ij} = \Delta C_j / \Delta I_i = \Delta C_j / \Delta R_i$
(since $V_{ii} = 1$, $\Delta I_i = \Delta C_i$)

capture 6 images \mathbf{C} (2 per color channel to determine deltas)

compensation (per pixel):

$I = V^{-1} * R$ (does not consider environment light!)

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$

(per pixel)

\rightarrow FM (in un-normalized matrix)

$$R = V * I$$

$I \rightarrow$ projected image

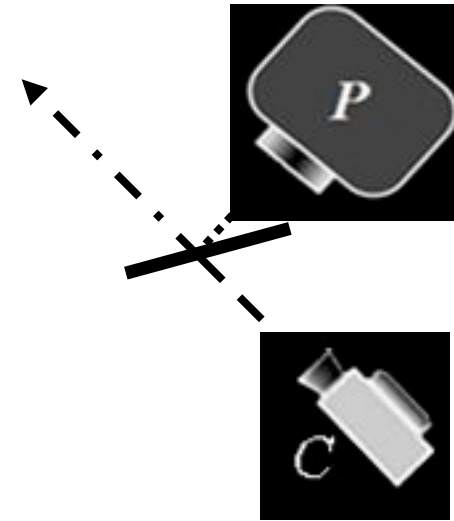
$V \rightarrow$ color mixing matrix

(projector/camera/reflectance)

Dynamic Adaptation

Fujii et al, CVPR
2005

Dynamic Adaptation



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

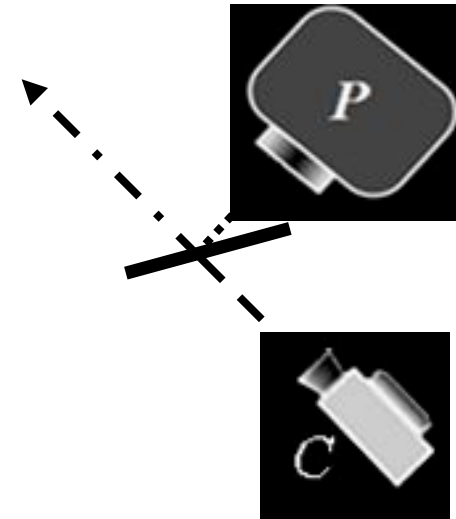
M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing matrix at $t=0$ (const.)

M_t → material at t

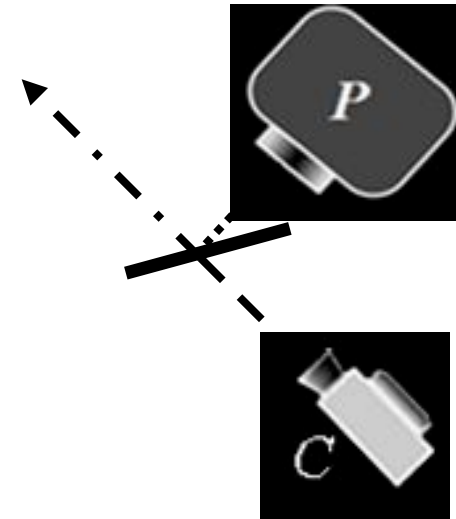
M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :
similar as before: $V_{ij} = \Delta C_j / \Delta I_i$



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

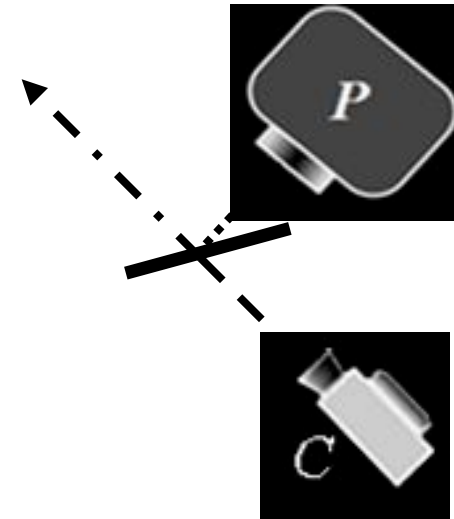
M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :
similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

M_0 → material at $t=0$

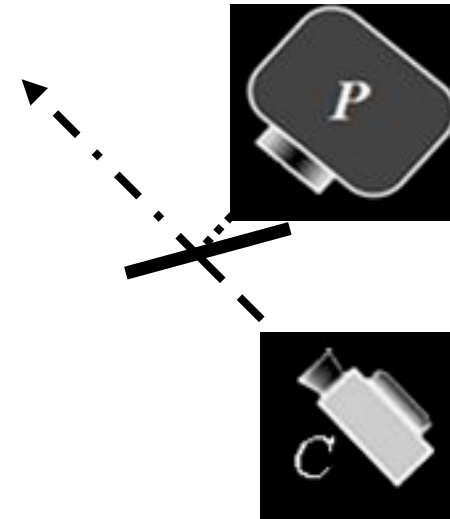
E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :
similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

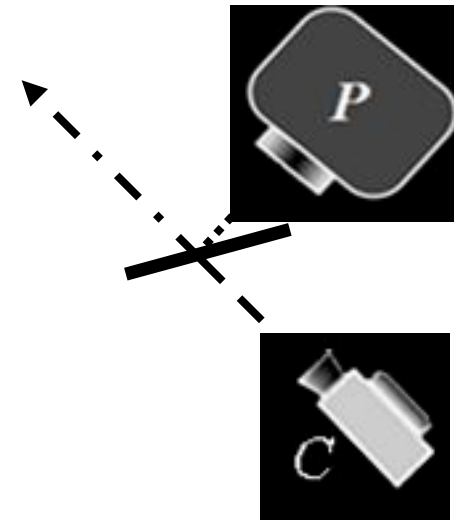
Dynamic Adaptation

determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment

light $E_0 * M_0$ at $t=0$:



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

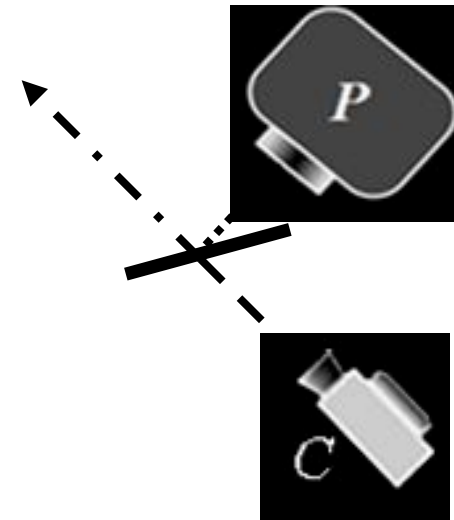
determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment

light $E_0 * M_0$ at $t=0$:

$E_0 * M_0 = C - V_0 * I$ (project



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

$t \rightarrow$ time index

$I_t \rightarrow$ projected image at t

$V_0 \rightarrow$ un-normalized color mixing
matrix at $t=0$ (const.)

$M_t \rightarrow$ material at t

$M_0 \rightarrow$ material at $t=0$

$E_t \rightarrow$ environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

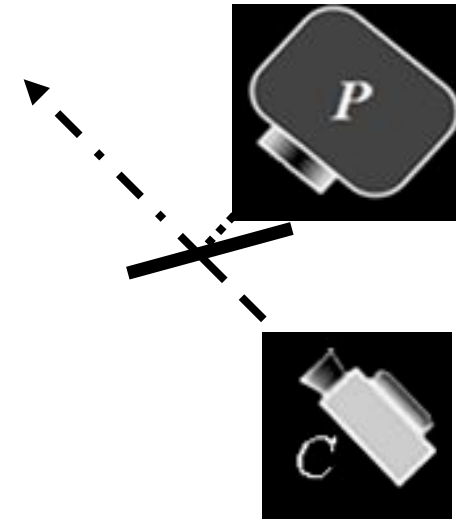
determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment

light $E_0 * M_0$ at $t=0$:

$E_0 * M_0 = C - V_0 * I$ (project
arbitrary I and capture C)



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

$t \rightarrow$ time index

$I_t \rightarrow$ projected image at t

$V_0 \rightarrow$ un-normalized color mixing
matrix at $t=0$ (const.)

$M_t \rightarrow$ material at t

$M_0 \rightarrow$ material at $t=0$

$E_t \rightarrow$ environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment

light $E_0 * M_0$ at $t=0$:

$E_0 * M_0 = C - V_0 * I$ (project
arbitrary I and capture C)

compensation (per pixel at t):

$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

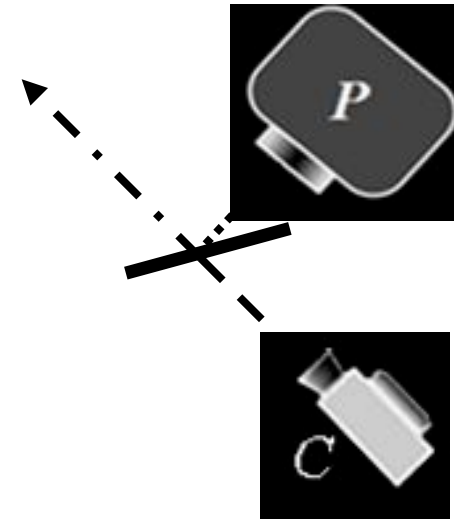
I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

M_0 → material at $t=0$

E_t → environment light at $t=0$



Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

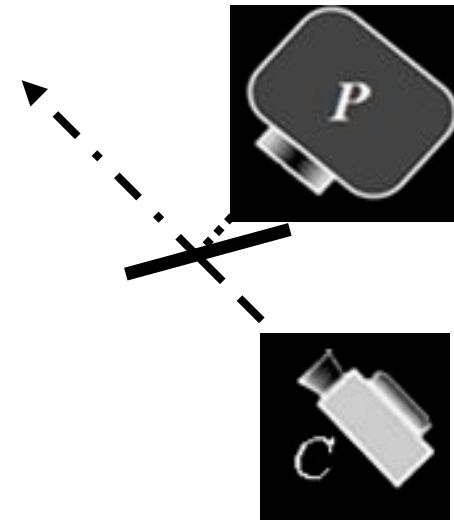
determine reflected environment

light $E_0 * M_0$ at $t=0$:

$E_0 * M_0 = C - V_0 * I$ (project
arbitrary I and capture C)

compensation (per pixel at t):

$$I_t = V_0^{-1} * (R * M_0 / M_{t-1} - E_{t-1} * M_0)$$



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

M_t → material at t

M_0 → material at $t=0$

E_t → environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

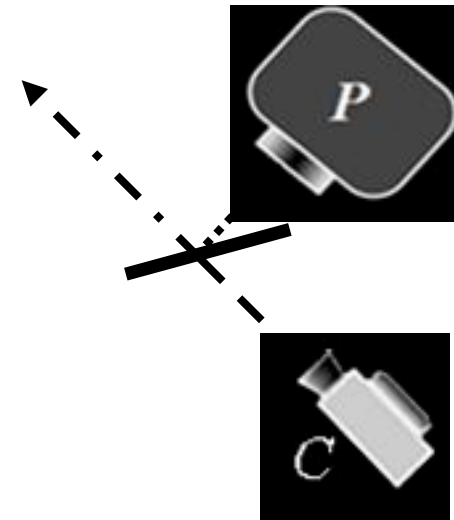
determine reflected environment

light $E_0 * M_0$ at $t=0$:

$E_0 * M_0 = C - V_0 * I$ (project
arbitrary I and capture C)

compensation (per pixel at t):

$I_t = V_0^{-1} * (R * M_0 / M_{t-1} - E_{t-1} * M_0)$
 $\rightarrow E_{t-1} * M_0$ approx. $E_0 * M_0$



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

$t \rightarrow$ time index

$I_t \rightarrow$ projected image at t

$V_0 \rightarrow$ un-normalized color mixing
matrix at $t=0$ (const.)

$M_t \rightarrow$ material at t

$M_0 \rightarrow$ material at $t=0$

$E_t \rightarrow$ environment light at $t=0$

Fujii et al, CVPR
2005

Dynamic Adaptation

determining color mixing matrix V_0 :

similar as before: $V_{ij} = \Delta C_j / \Delta I_i$
(un-normalized!)

determine reflected environment

light $E_0 * M_0$ at $t=0$:

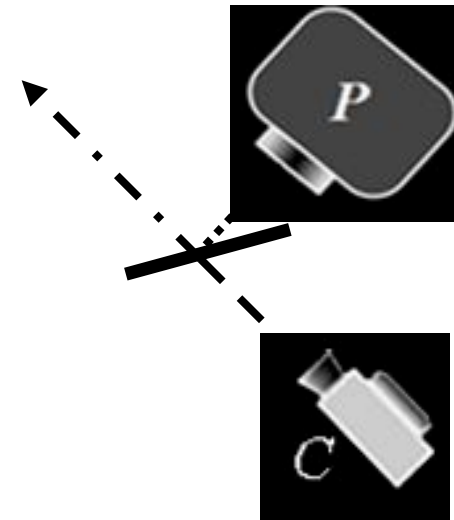
$E_0 * M_0 = C - V_0 * I$ (project
arbitrary I and capture C)

compensation (per pixel at t):

$$I_t = V_0^{-1} * (R * M_0 / M_{t-1} - E_{t-1} * M_0)$$

$$\rightarrow E_{t-1} * M_0 \text{ approx. } E_0 * M_0$$

$$\rightarrow M_0 / M_{t-1} = C_0 / C_{t-1}$$



$$R_t = M_t / M_0 * (E_t * M_0 + V_0 * I_t)$$

t → time index

I_t → projected image at t

V_0 → un-normalized color mixing
matrix at $t=0$ (const.)

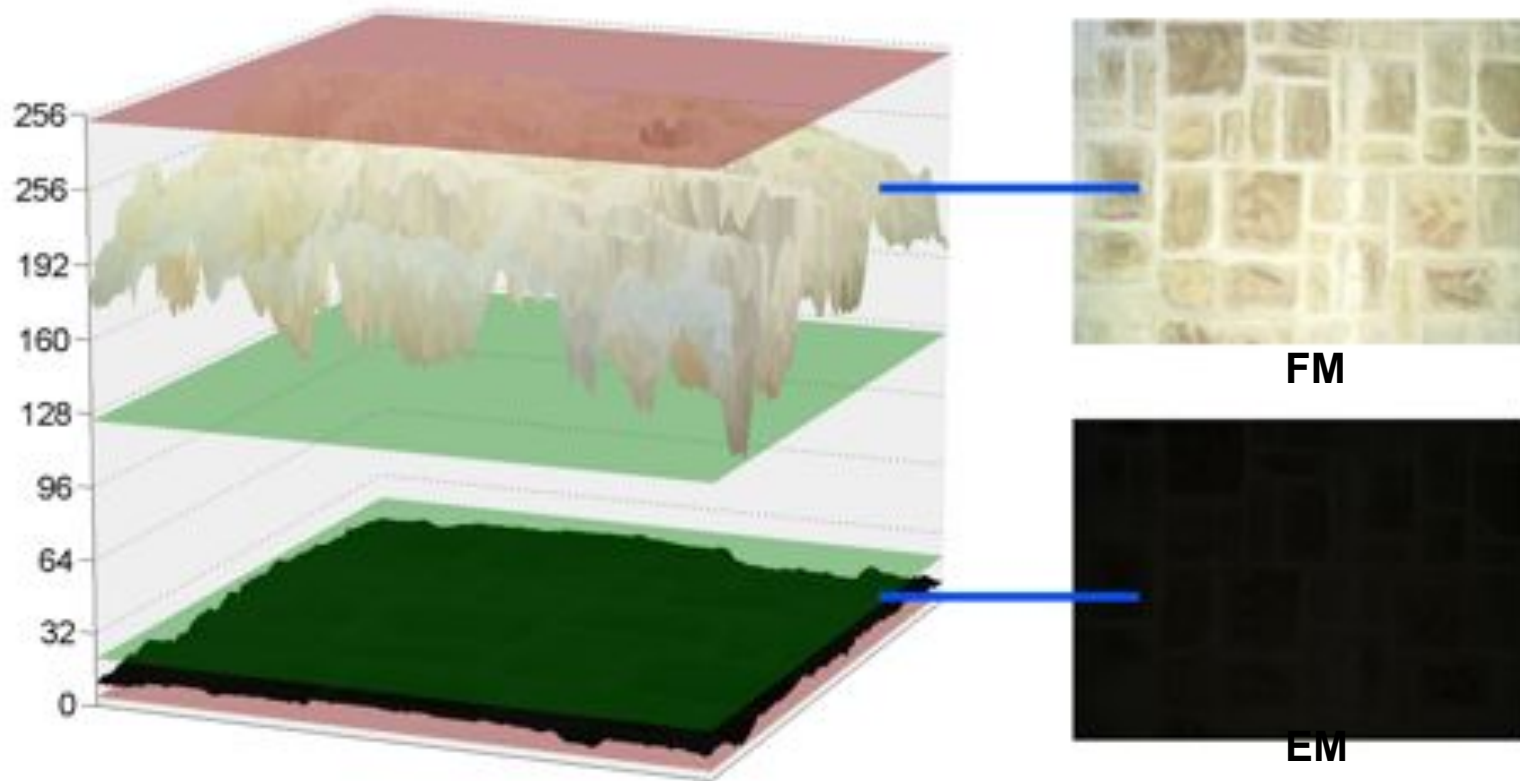
M_t → material at t

M_0 → material at $t=0$

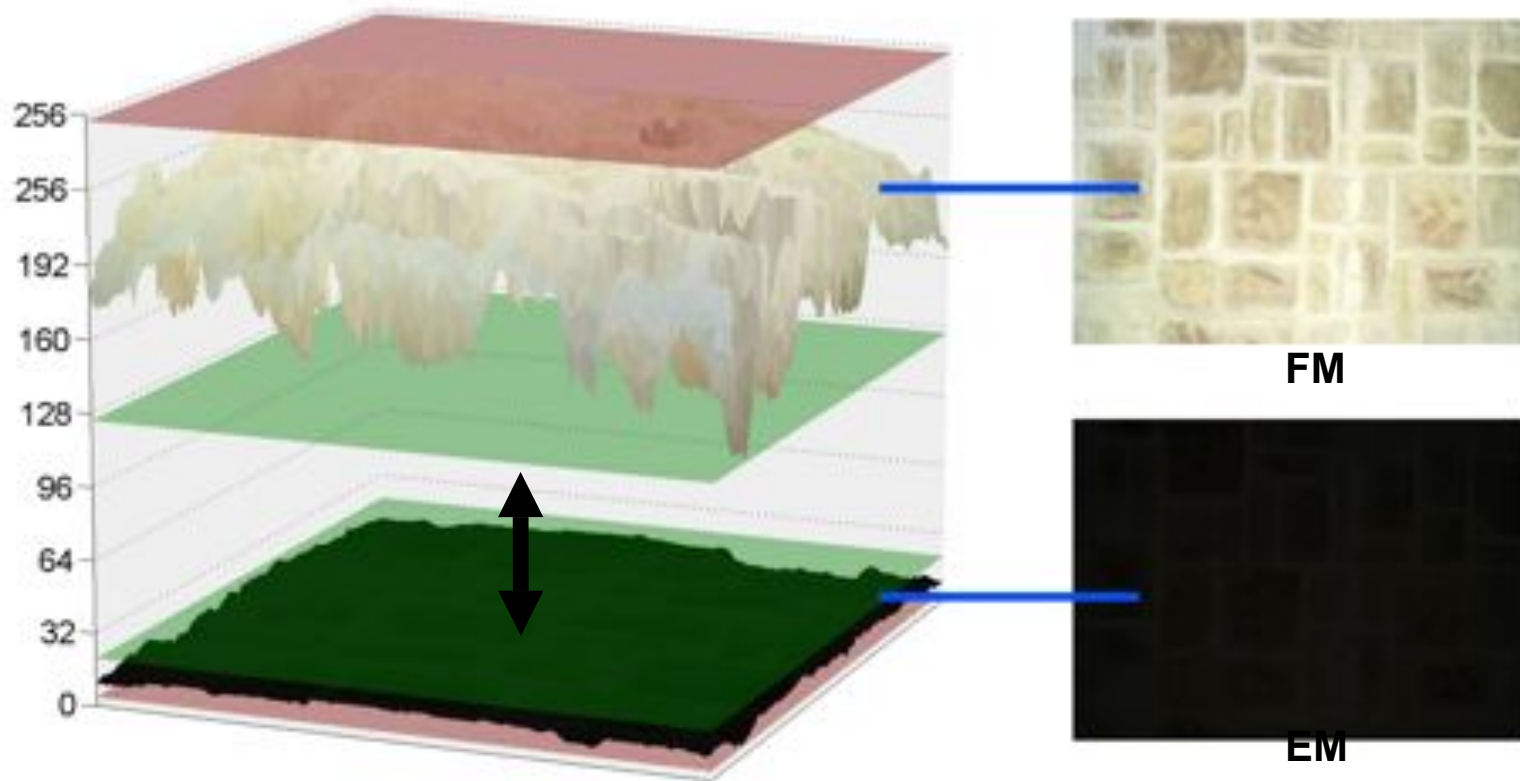
E_t → environment light at $t=0$

Limited Dynamic Range and Brightness

Limited Dynamic Range and Brightness



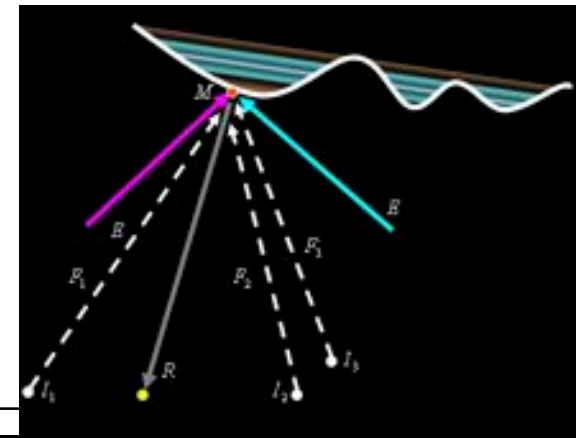
Limited Dynamic Range and Brightness



Multiple Projectors



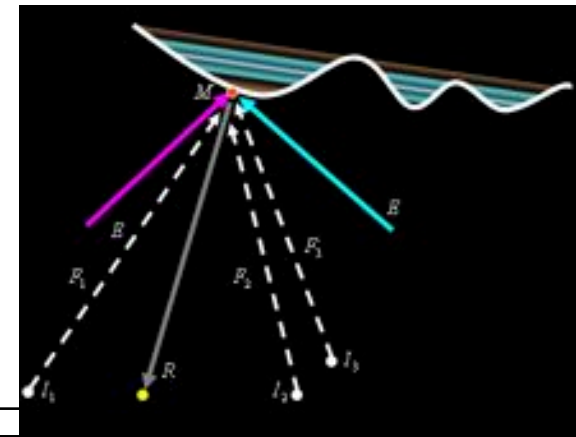
Multiple Projectors



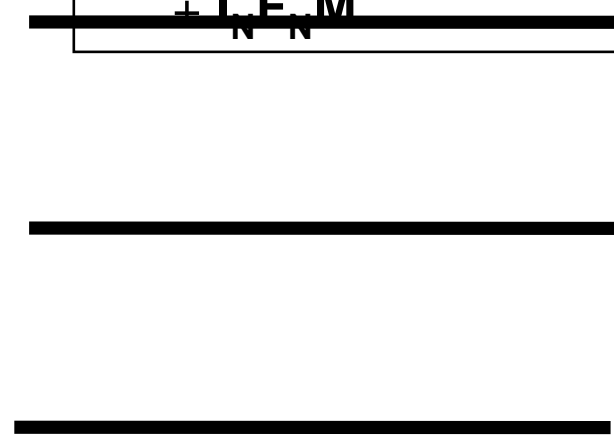
$$R = E_1 M + I_1 + I_2 + I_3 + I_N + I_M$$

Multiple Projectors

strategy: balance intensity load



$$R = \frac{L_1 M + I_1 M + I_2 M + \dots + I_N M}{N}$$

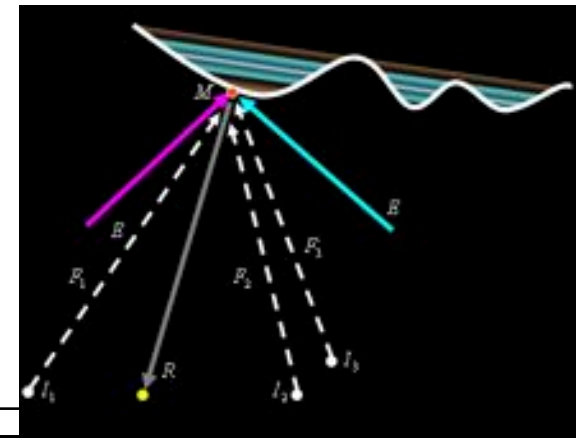


Multiple Projectors

strategy: balance intensity load

- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$



$$R = \frac{I_1}{N} + \frac{I_2}{N} + \dots + \frac{I_N}{N}$$

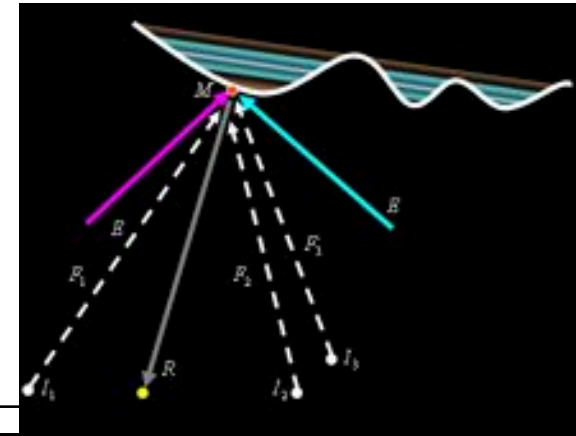


Multiple Projectors

strategy: balance intensity load

- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$



$$R = EM + I_1(F_1M + I_2(F_2M + \dots + I_N(F_NM + IEM))$$

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM)$$

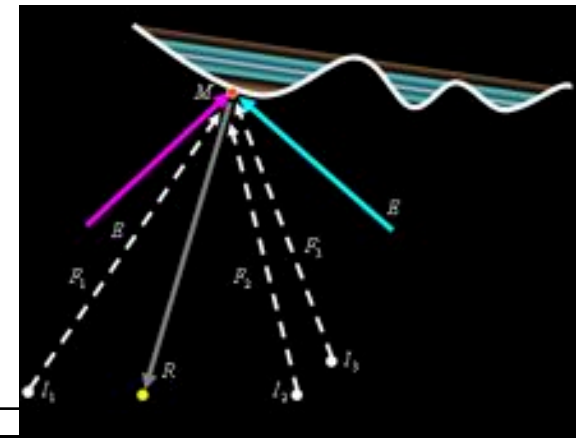
$$\rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$

Multiple Projectors

strategy: balance intensity load

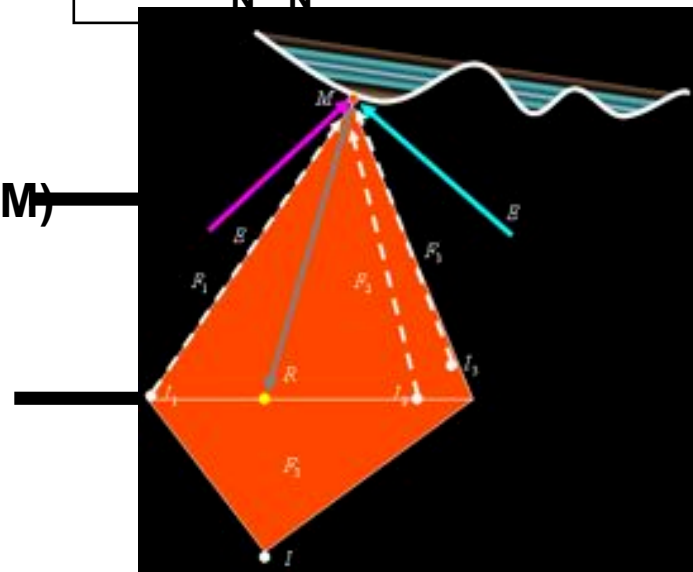
- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$



$$R = EM + I_1(F_1M + F_2M + \dots + F_NM) + IEFM$$

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM) \rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$



Multiple Projectors

strategy: balance intensity load

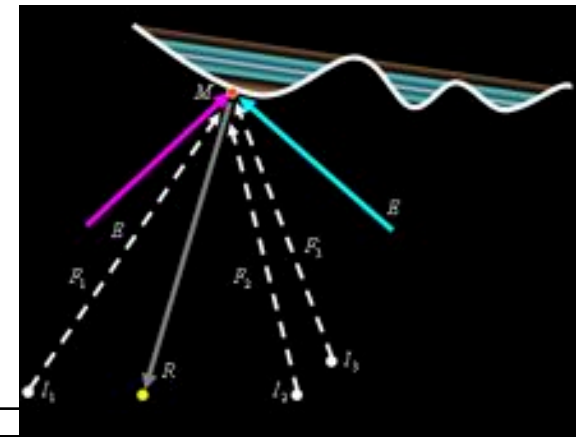
- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$

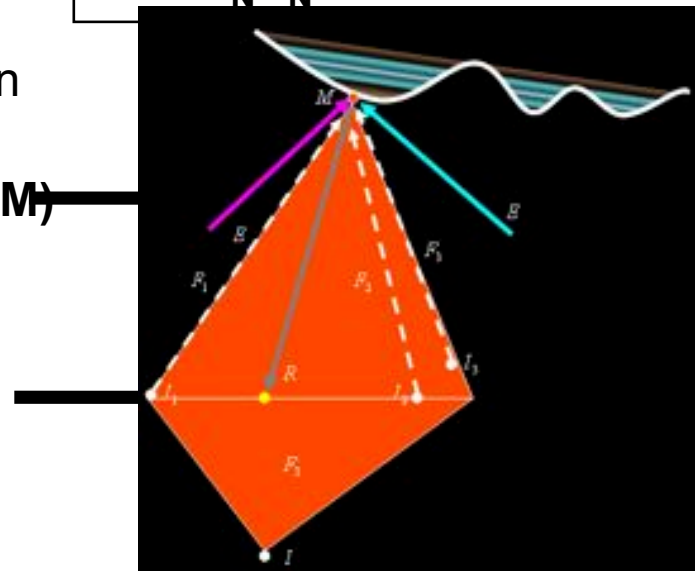
- this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM)$$

$$\rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$



$$R = EM + I_1(F_1M + F_2M + \dots + F_NM)$$



Multiple Projectors

strategy: balance intensity load

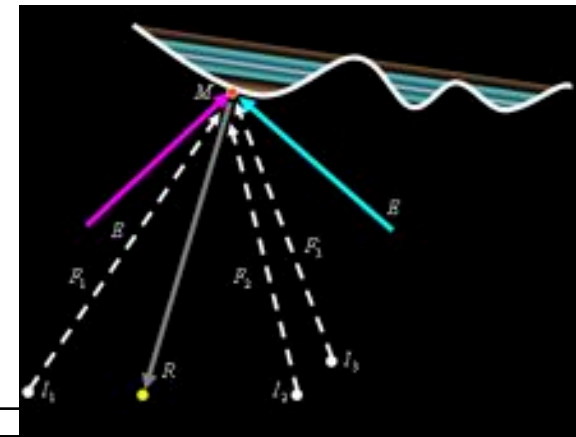
- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$

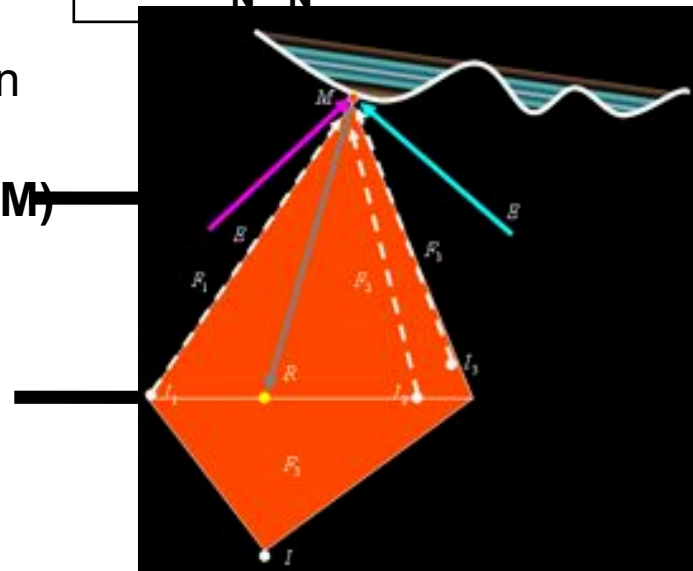
- this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM)$$

$$\rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$



$$R = EM + I_1(F_1M + F_2M + \dots + F_NM)$$



Multiple Projectors

strategy: balance intensity load

- assume: total intensity is equally balanced among multiple low-capacity units

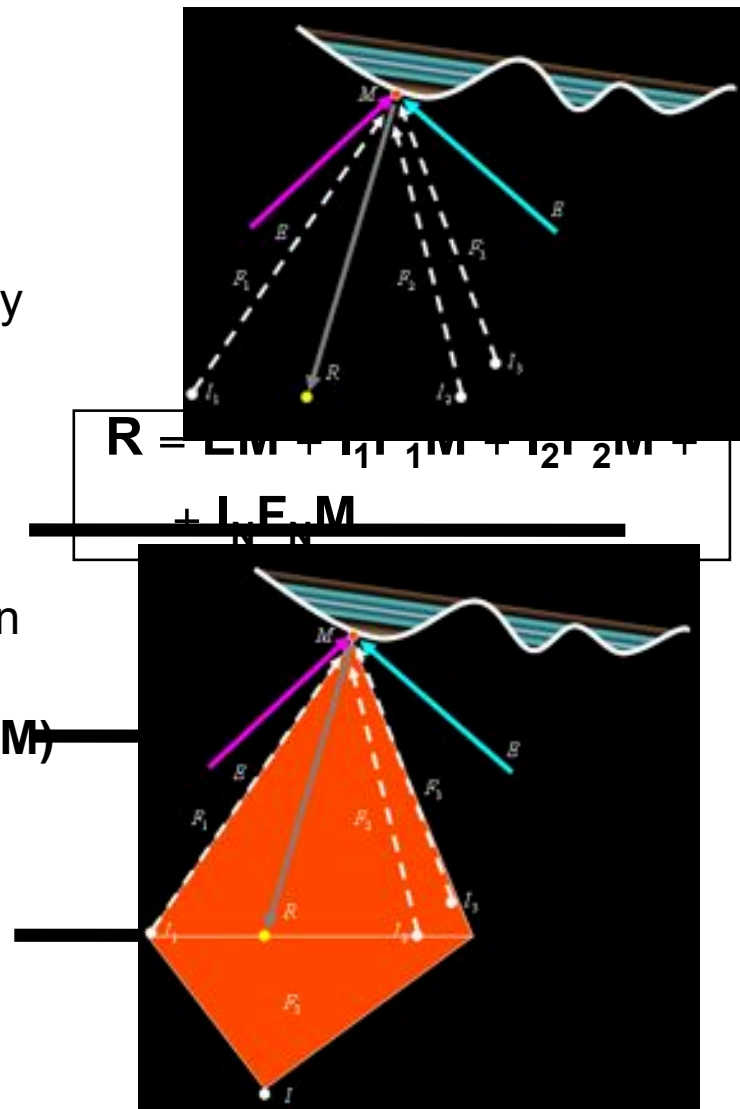
$$I_i = I_1 = I_2 = \dots = I_N$$

- this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM)$$

$$\rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$

compensation (per pixel):



Multiple Projectors

strategy: balance intensity load

- assume: total intensity is equally balanced among multiple low-capacity units

$$I_i = I_1 = I_2 = \dots = I_N$$

- this is equivalent to the assumption that a single high capacity projector produces the total intensity arriving on the surface virtually

$$R = EM + I_i(F_1M + F_2M + \dots + F_NM)$$

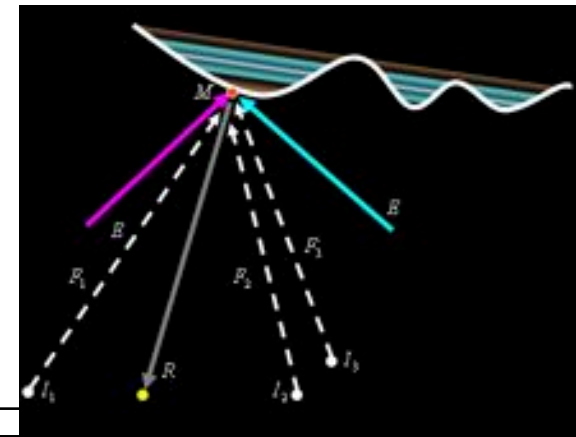
$$\rightarrow EM + I(F_1 + F_2 + \dots + F_N)M$$

compensation (per pixel):

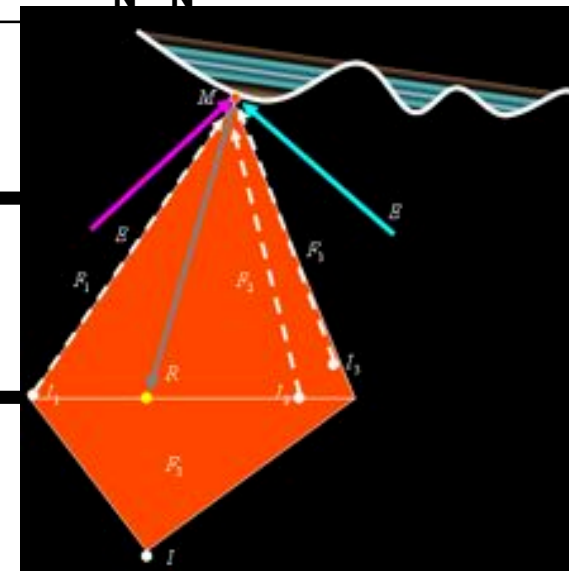
$$I_i = (R - EM) / (F_1M + F_2M + \dots + F_NM)$$

remember: $F_iM = F_iM - B_iF_iM$!

or $BFM = B_1F_1M + \dots + B_iF_iM$



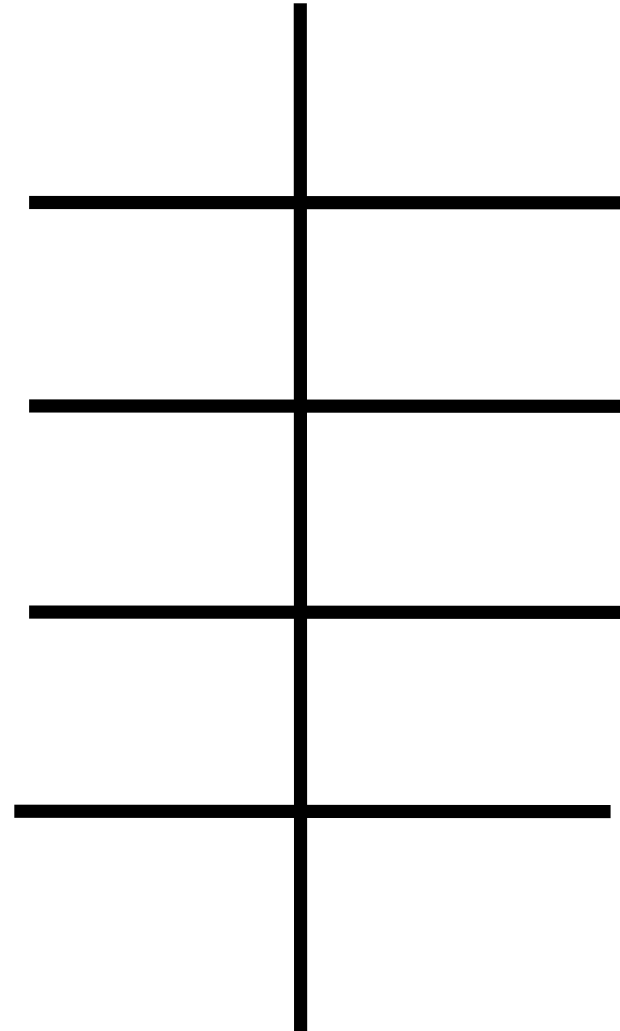
$$R = EM + I_1(F_1M + F_2M + \dots + F_NM)$$



IEEE

Computer 2005

Considering Human Visual Perception



Considering Human Visual Perception

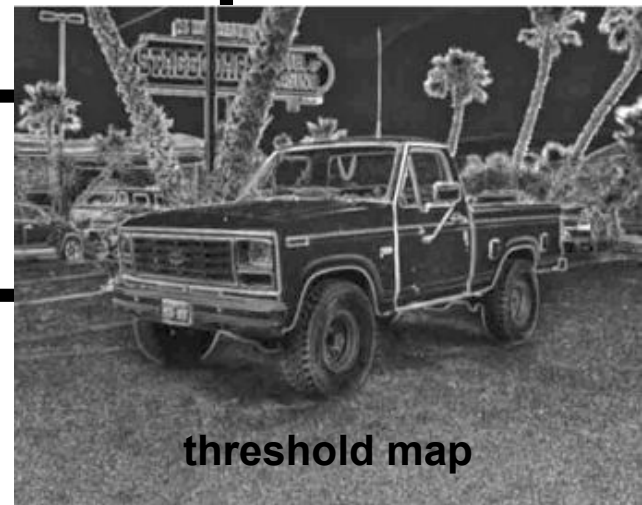
threshold map (Ramasubramanian et al. Siggraph'99)

- computes for every pixel of an image R the amount of luminance difference that is imperceptible
- considers *contrast*, *luminance* and *spatial frequency* in local neighborhood

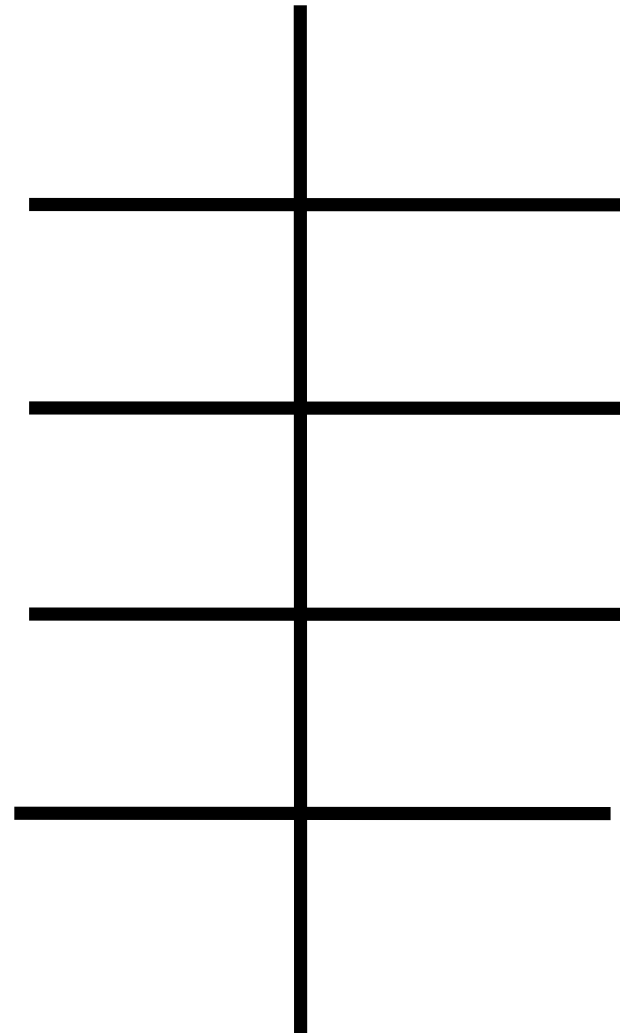


adaptation of un-compensated (original) image R :

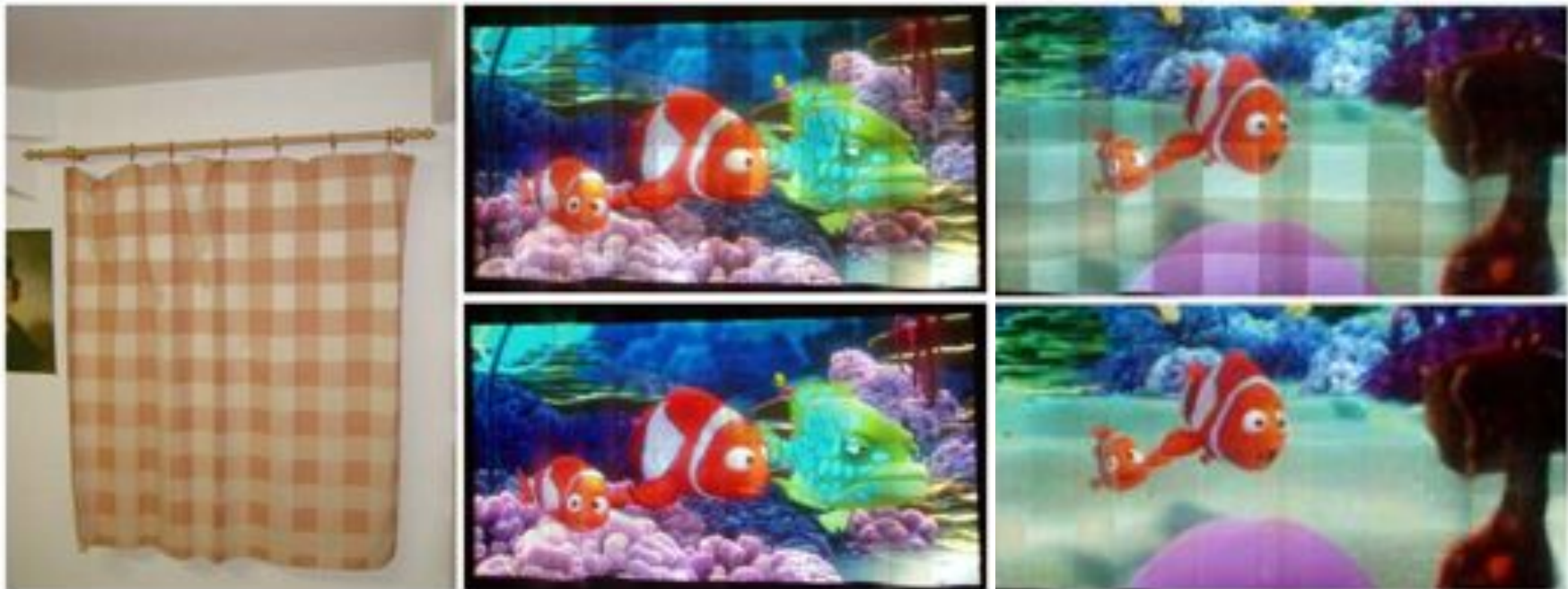
- compute and apply a single (global) scaling factor $R' = R * \alpha$ that minimizes the perceived error (Wang, et al. 2005, only monochrome, not real-time, single projector)
- coming soon: color, real-time, global and local adaptation, potentially multiple projectors



Example: Curtain



Example: Curtain

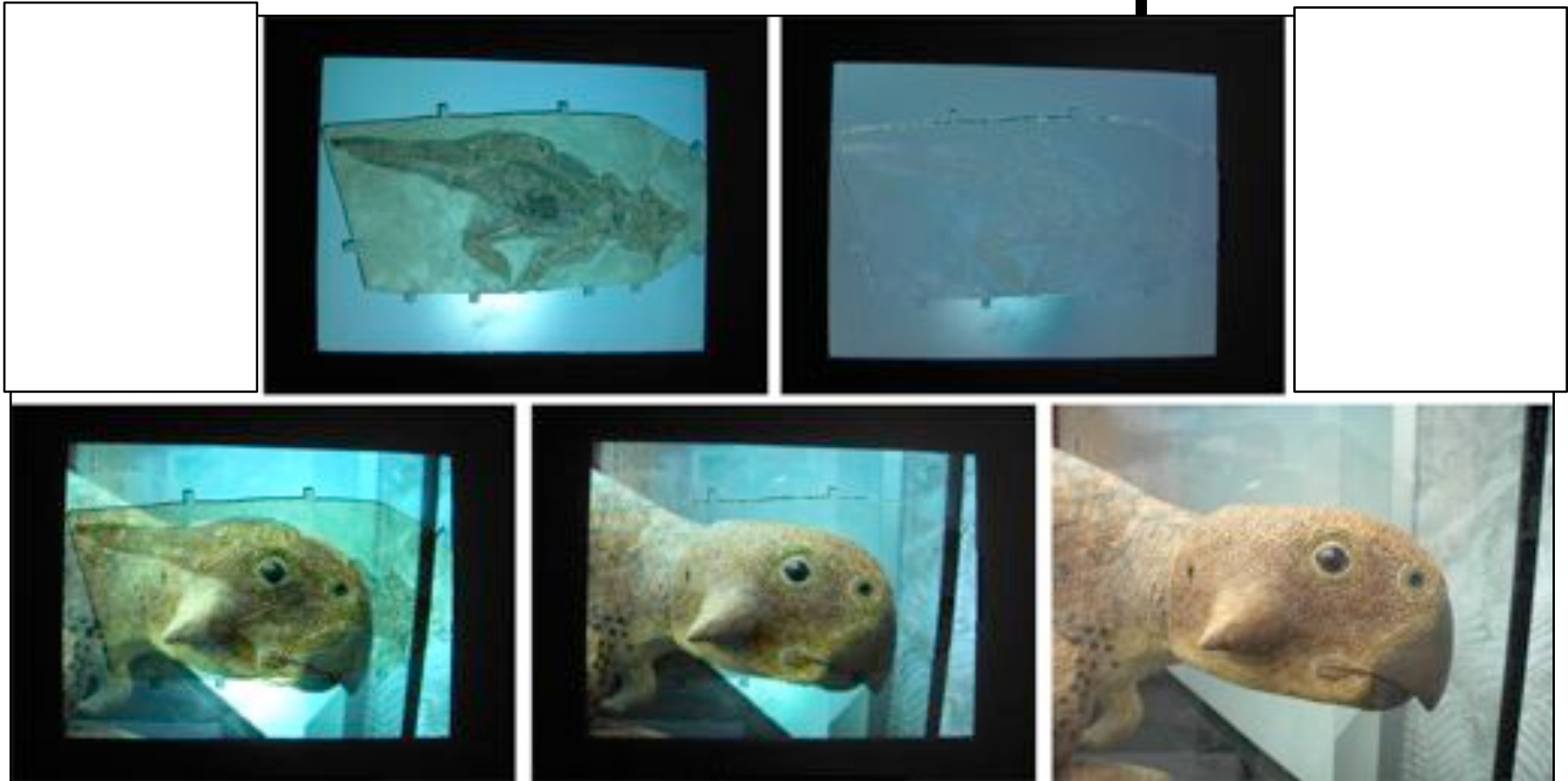


Bimber et al, IEEE
Computer 2005

Example: Fossil

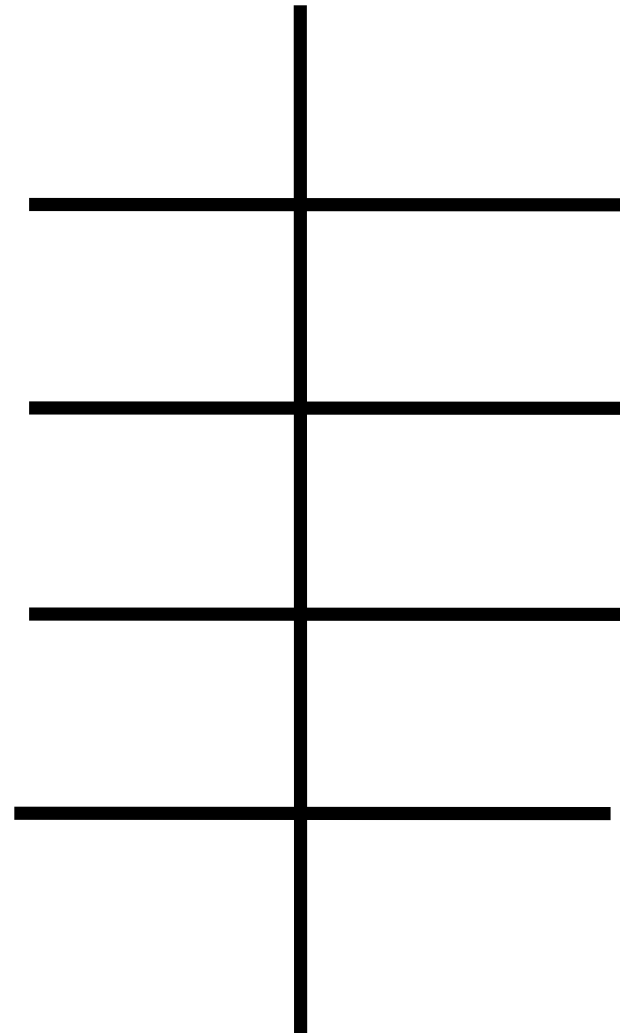


Example: Fossil

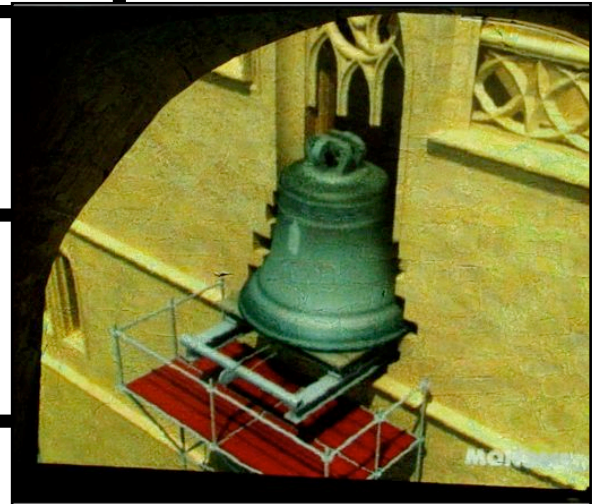


In coop. with Senckenberg Museum

Example: Natural Stone Wall

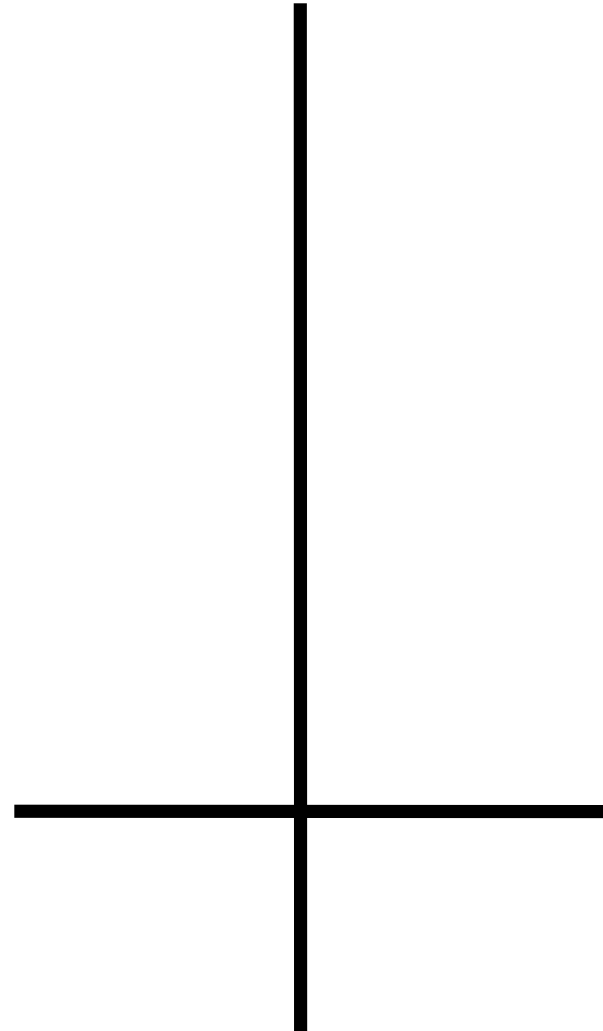


Example: Natural Stone Wall



Bimber et al, IEEE Computer 2005
In coop. with Bennert Group

Example: Wallpaper

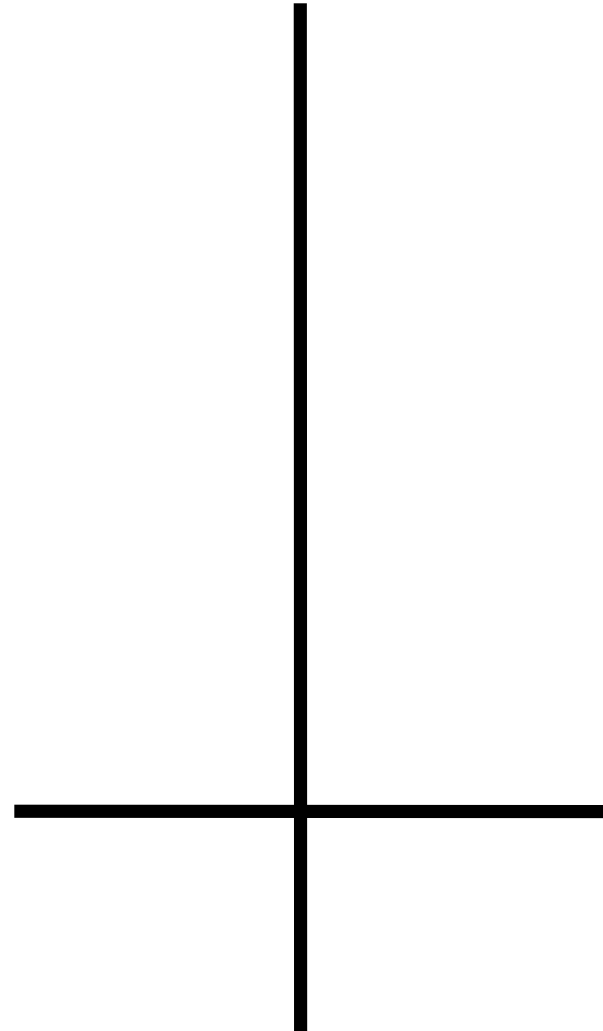


Example: Wallpaper

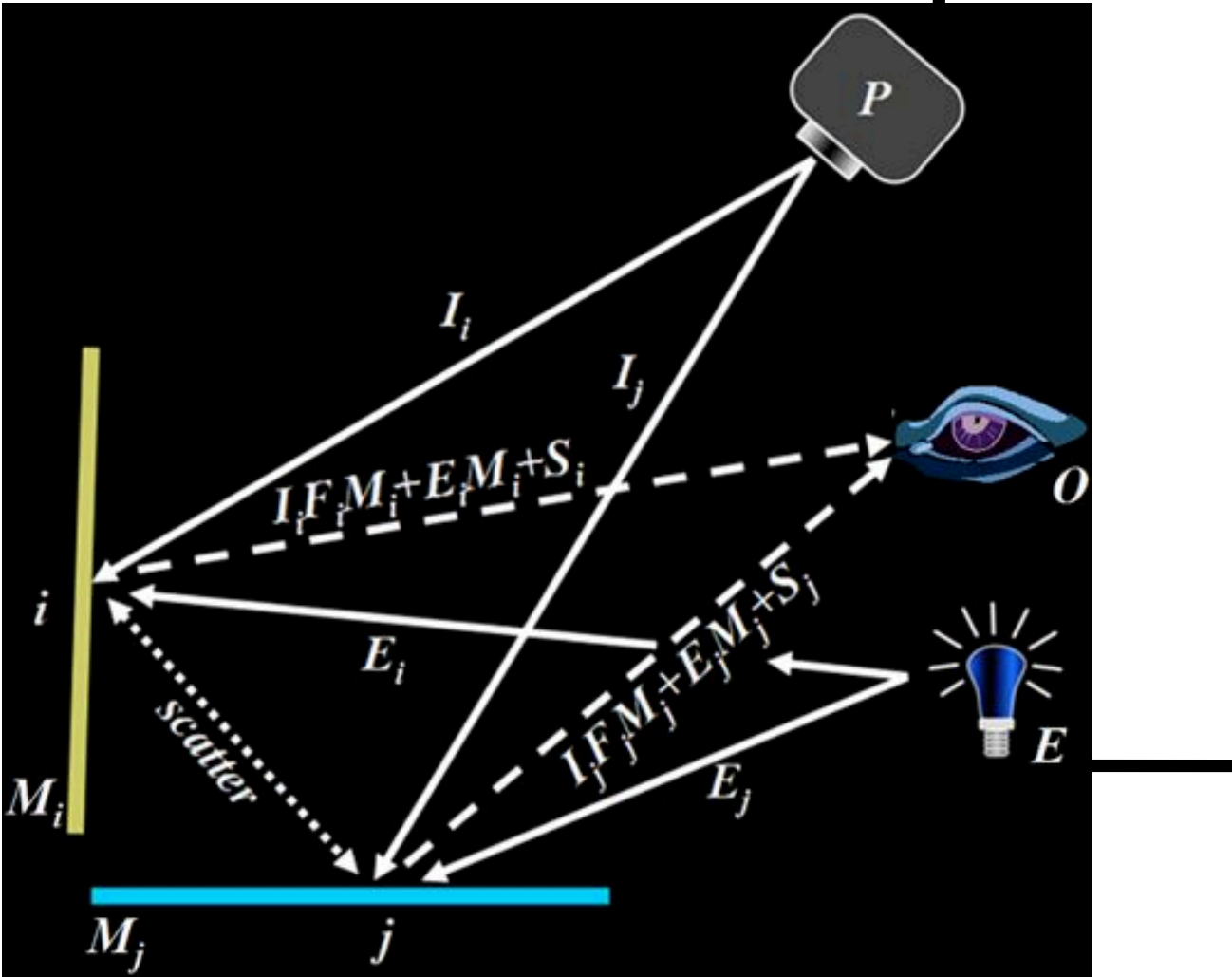


Bimber et al,
IEEE Computer
2005

Compensating Global Light Effects



Compensating Global Light Effects

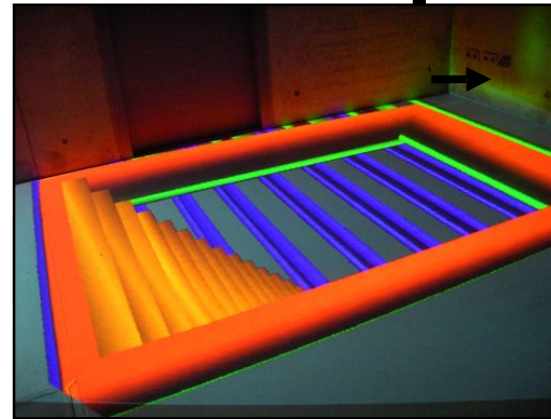
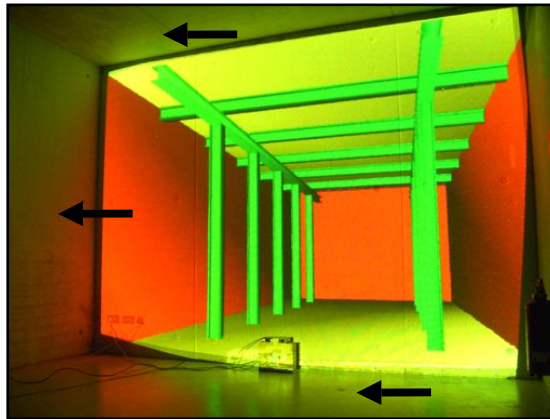


Compensating Diffuse Scattering



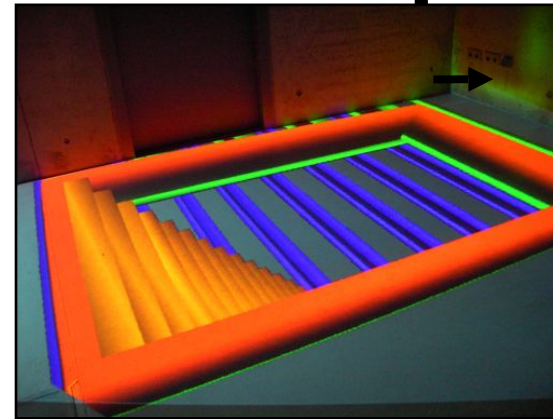
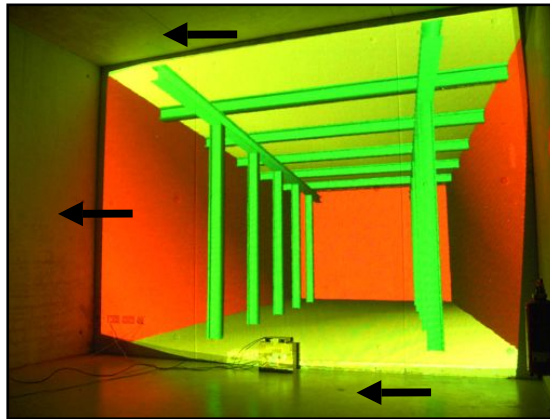
Compensating Diffuse Scattering

Bimber et al,
IEEE/ACM
ISMAR 2005

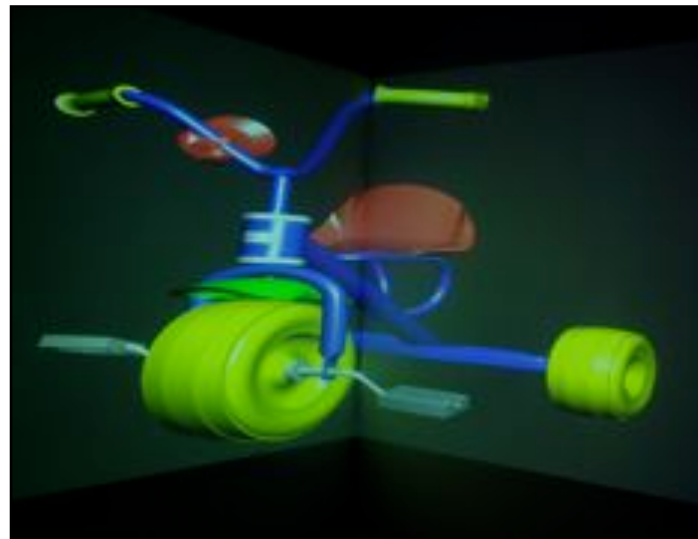


Compensating Diffuse Scattering

Bimber et al,
IEEE/ACM
ISMAR 2005

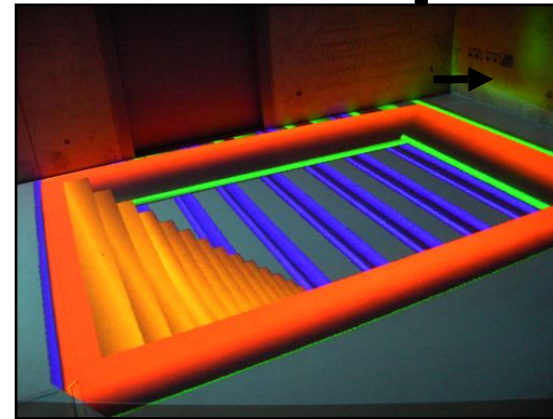
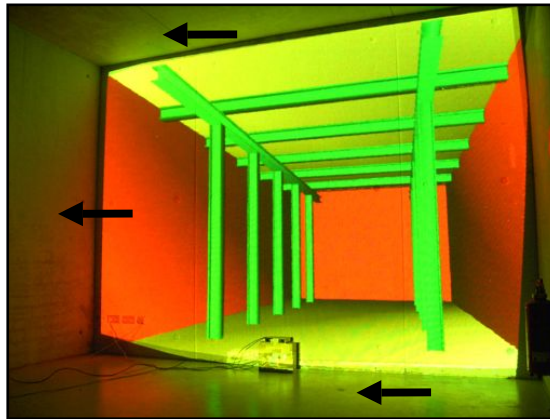


Bimber et al,
IEEE VR, 2006

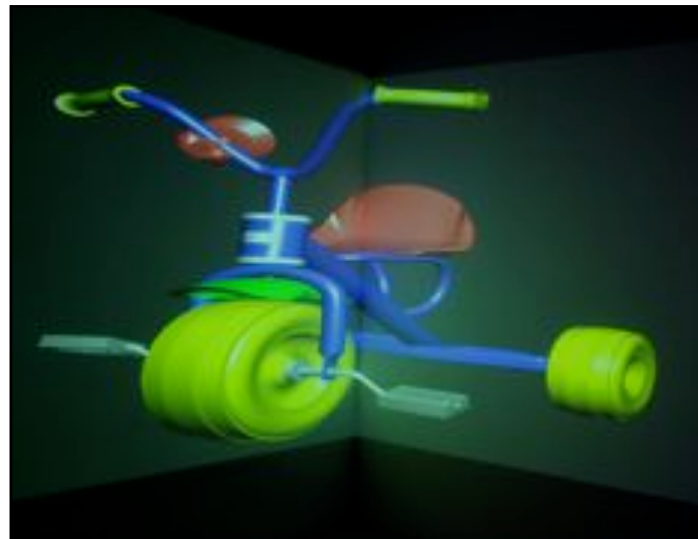


Compensating Diffuse Scattering

Bimber et al,
IEEE/ACM
ISMAR 2005

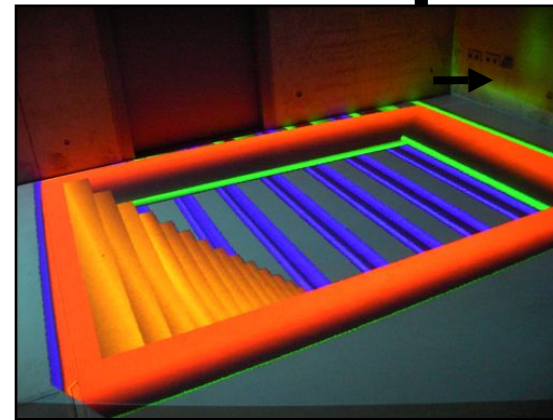
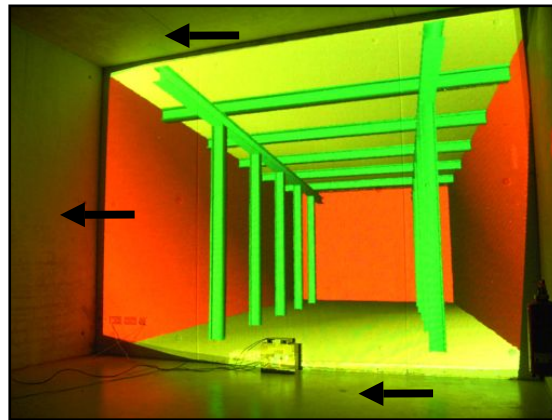


Bimber et al,
IEEE VR, 2006

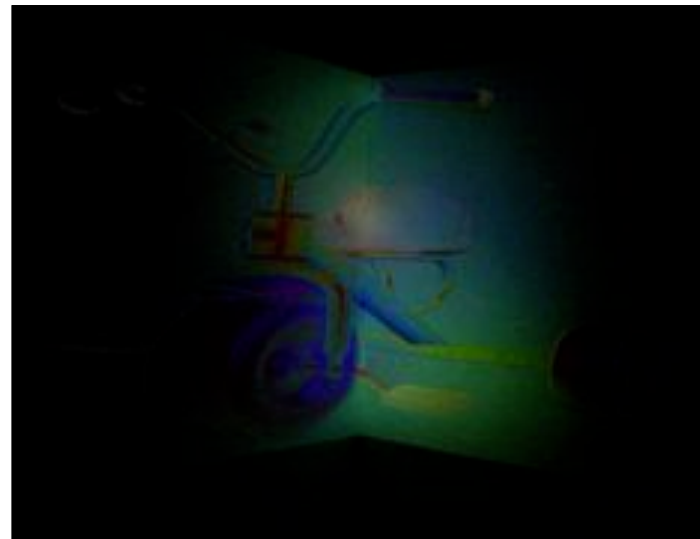


Compensating Diffuse Scattering

Bimber et al,
IEEE/ACM
ISMAR 2005



Bimber et al,
IEEE VR, 2006



details:
IEEE VR talk on
Wednesday morning
(8:30am), session on
tracking and projection
displays

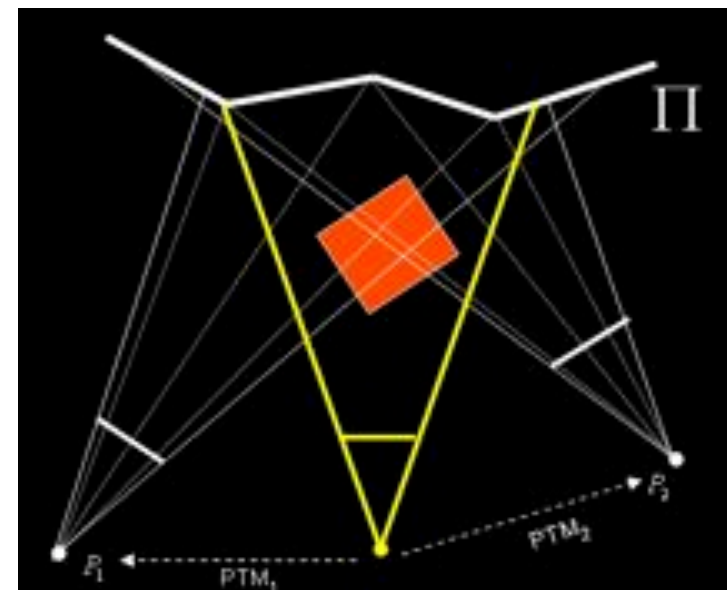
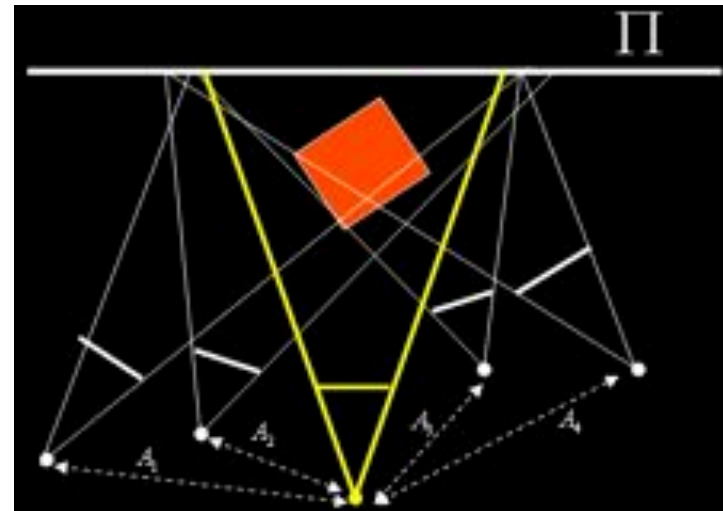
see demo!

Advanced Techniques View-Dependence

Non-Complex Surfaces

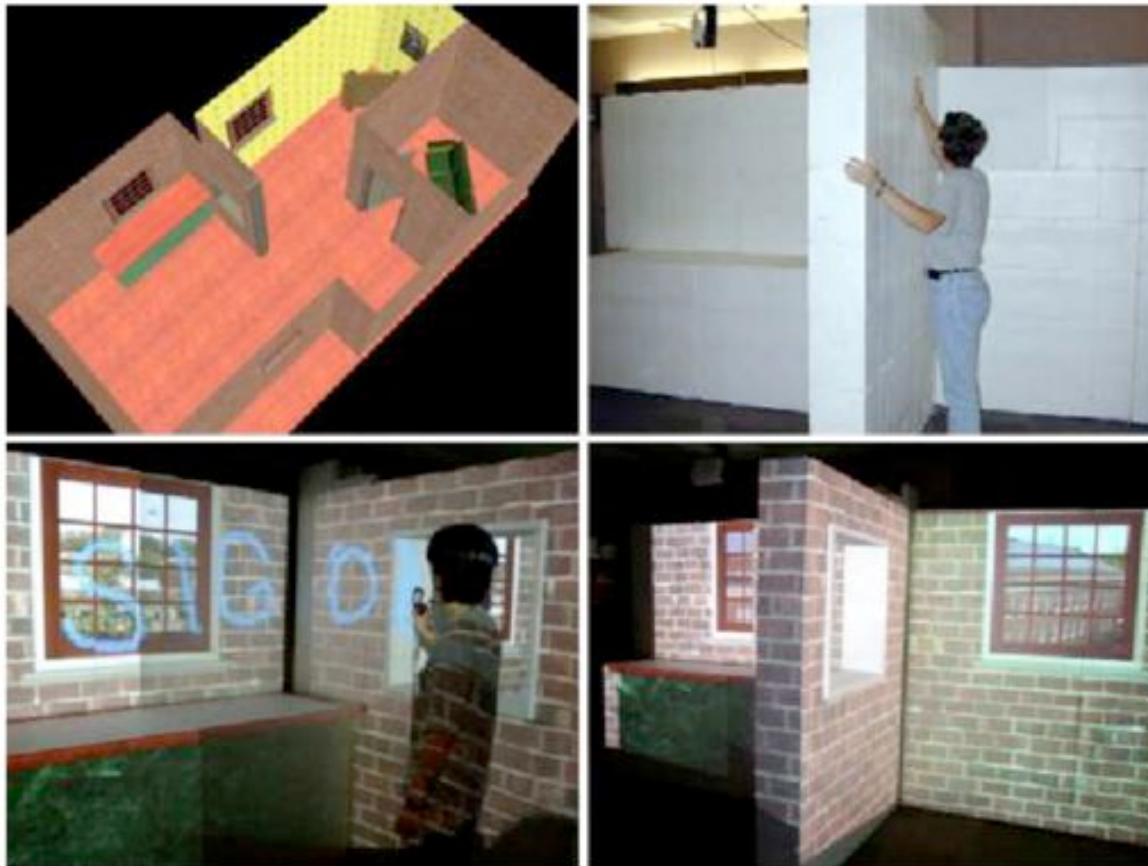
Non-Complex Surfaces

- view-dependent geometry correction can be compute if geometry is known
- for example:
 - **planar/multi-plane:** off-axis projection
 - **parametric:** warping via parametric description
 - **scanned/modelled:** projective texture mapping



Example: Life-Sized Projector-Based Dioramas

Example: Life-Sized Projector-Based Dioramas



Courtesy: Low, et al., 2001

Complex Surfaces

Complex Surfaces

- if geometry is unknown image-based rendering helps
- sample geometric and radiometric parameters from multiple (source) camera (perspective)
- for novel (destination) camera
 - compute weighted penalties:

$$p_j = \alpha a_j + (1 - \alpha) b_j$$

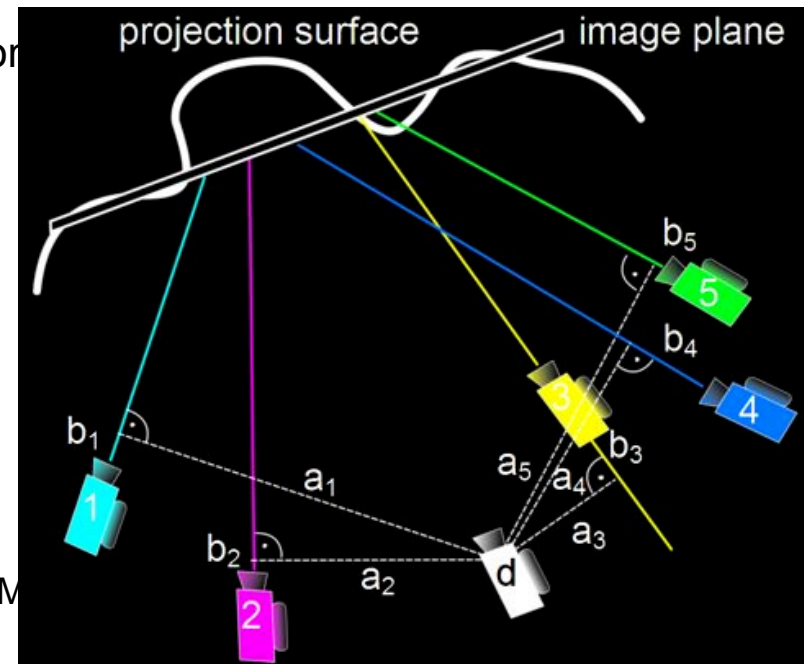
- select k best perspectives (lowest penalties) and normalize them:

$$w_j = \left(1 - \frac{p_j}{\max_{pk} p_k} \right) \frac{1}{p_j}$$

- interpolate n $(F_{ij}M, E_{ij}M, P_i2C_j, F_{ij}M, E_{ij}M)$ and direction vector for destination perspective to render new IP:

$$t_d = \sum_j^k w_j t_j$$

- lookups in $F_{ij}M, E_{ij}M$ with non-interpolated P_i2C_j
- lookups in IP with interpolated P_i2C_j



Example: Tracking and Stereo

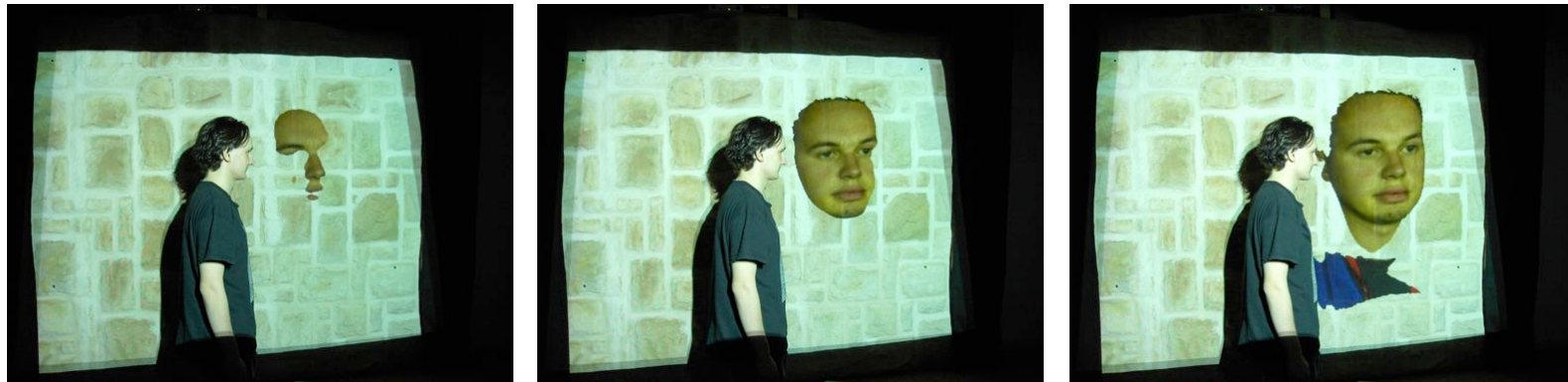
Example: Tracking and Stereo



Bimber et al, IEEE/ACM ISMAR 2005

Depth and Occlusion

Depth and Occlusion

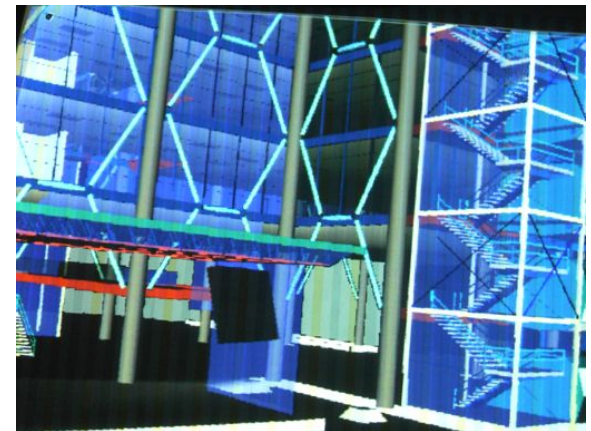
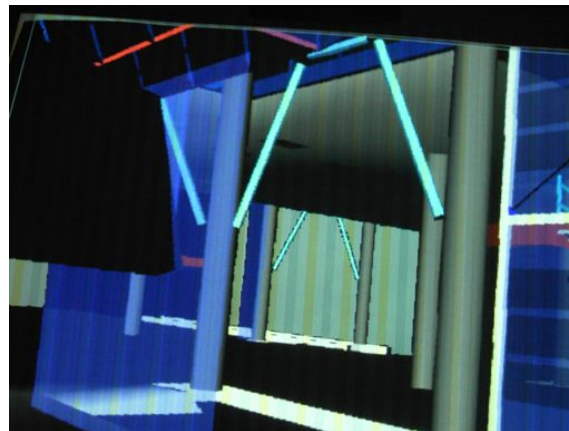
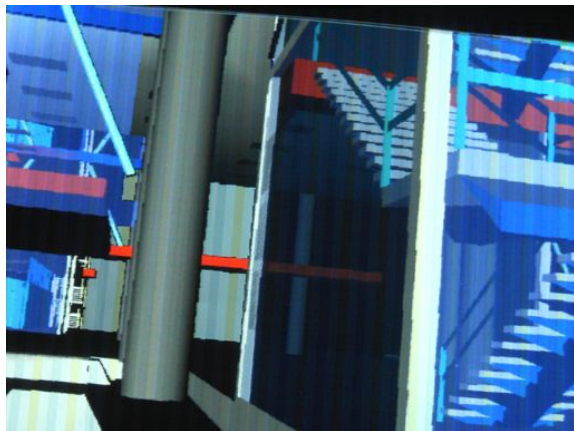
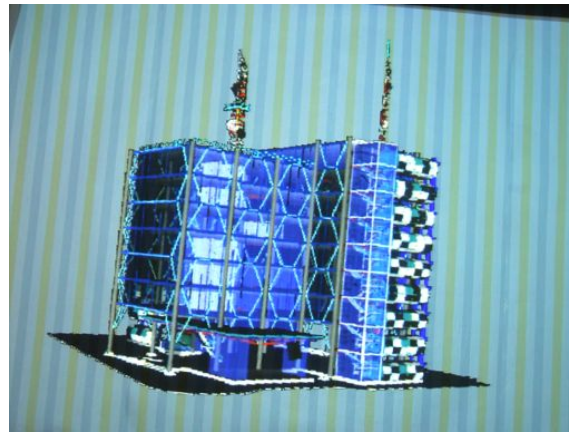


Bimber et al,
IEEE/ACM
ISMAR 2005



Example: Stereo on Wallpaper

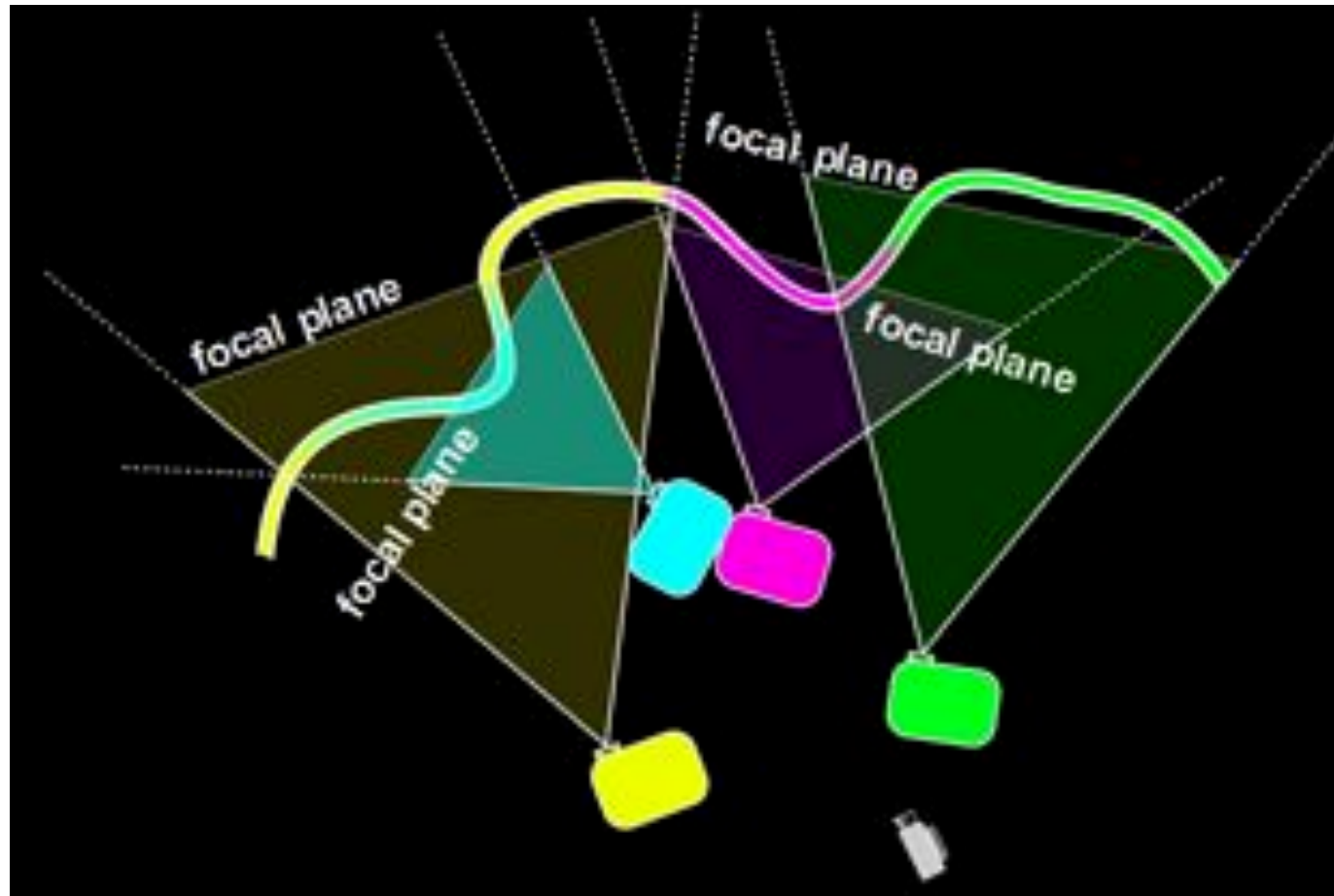
Example: Stereo on Wallpaper



Bimber et al, IEEE/ACM
ISMAR 2005

Advanced Techniques Multi-Focal Projection

Multi-Projector-Camera Technique that Increases Focal Depth



Determining Defocus



Determining Defocus

- structured light projection of grid point samples (2- dimensional phase shift)
 - pre-correction:** geometric and radiometric correction (corrected grid points must be observed in camera)

$$I_{x,y} = (R_{x,y} - EM_{x,y}) / FM_{x,y}$$

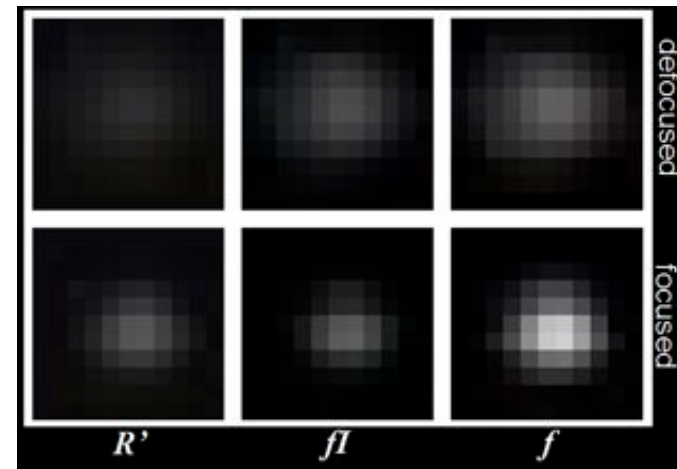
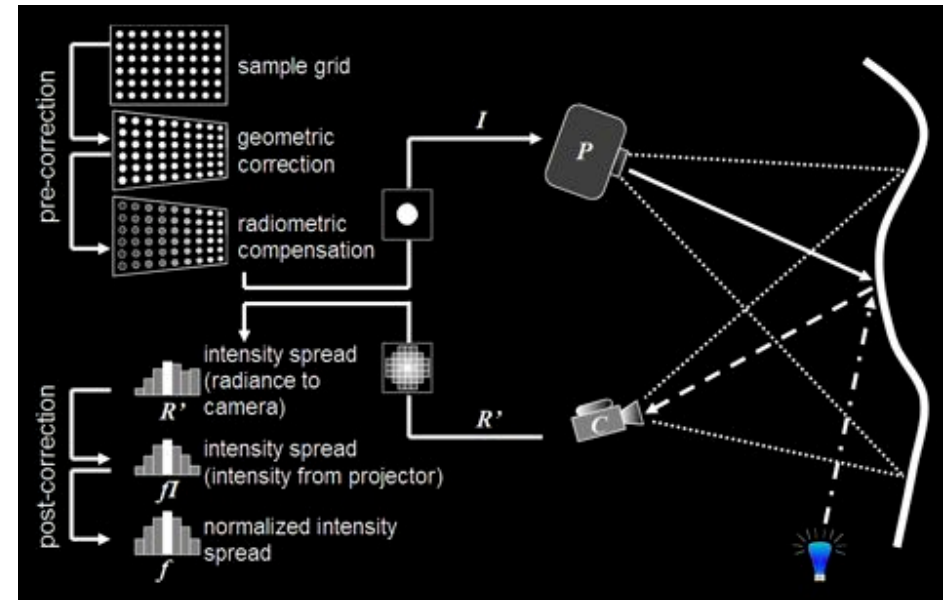
- post-correction:**

$$R'_{x',y'} = fI_{x,y} FM_{x',y'} + EM_{x',y'}$$

$$fI_{x,y} = \frac{(R'_{x',y'} - EM_{x',y'})}{FM_{x',y'}}$$

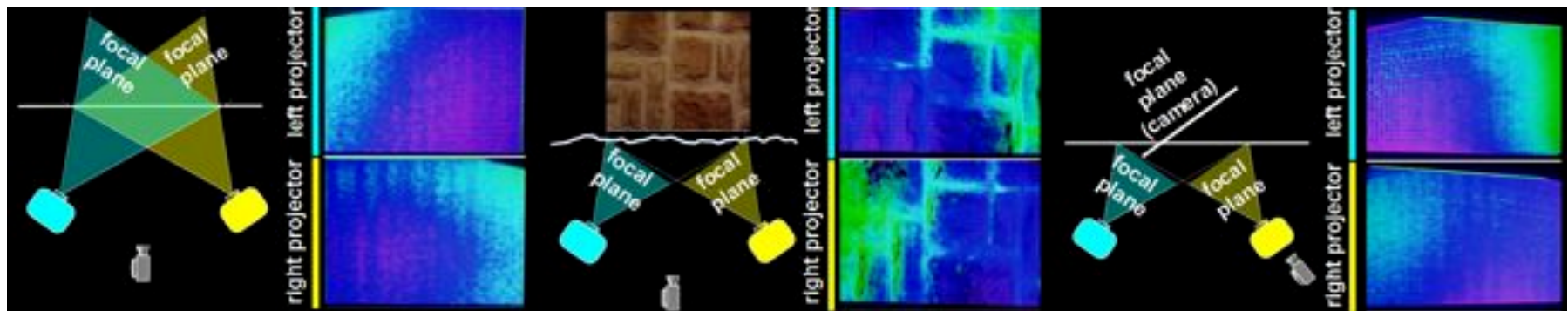
$$f = \frac{fI_{x,y}}{I_{x,y}}$$

- the texture f serves as basis to estimate focus measures (e.g., via FFT/DCT, intensity loss, point spread, etc.)



Example: Different Configurations

Example: Different Configurations

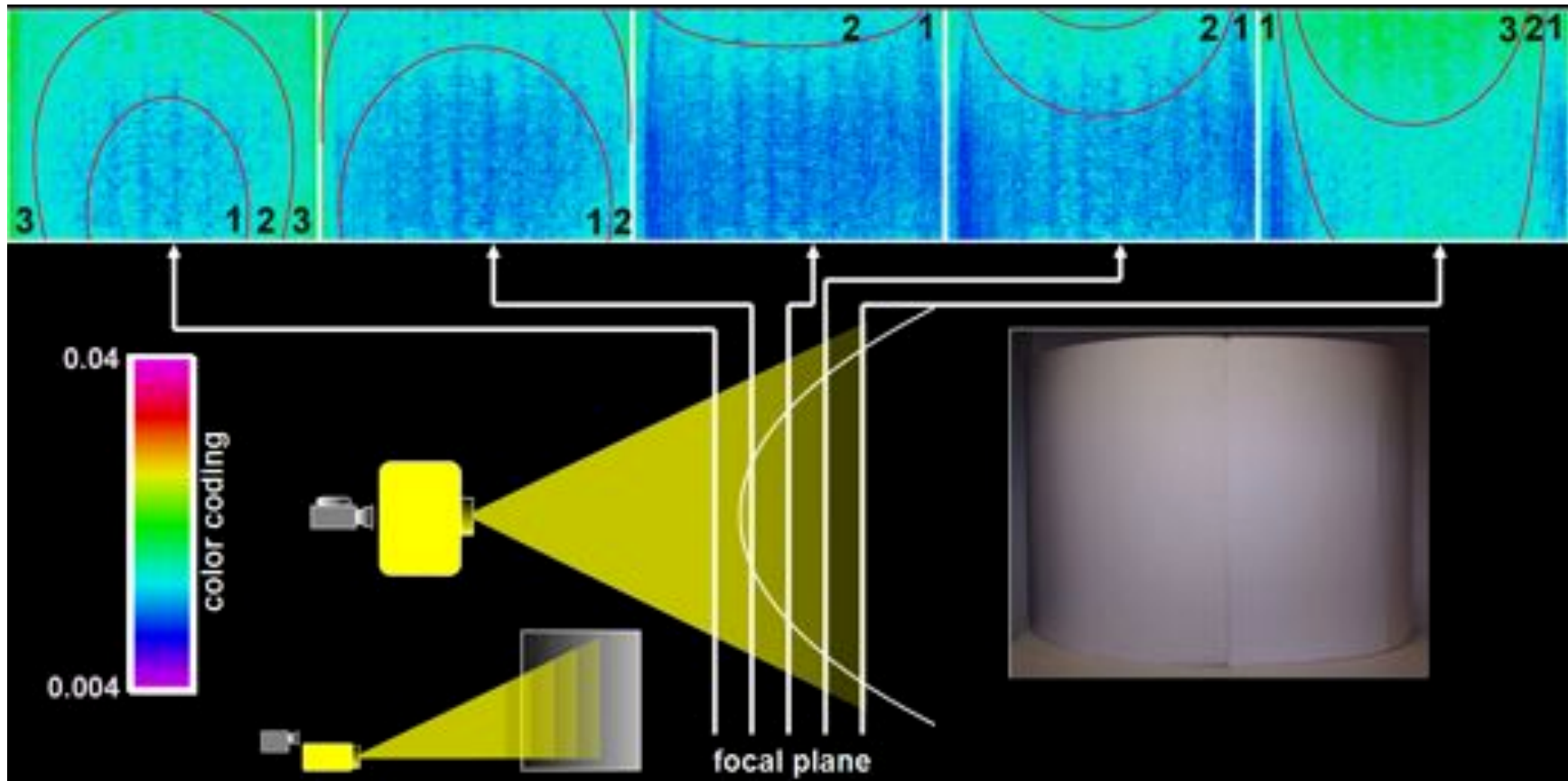


Bimber et al, IEEE TVCG 2006

Example: Shifting Focal Plane



Example: Shifting Focal Plane

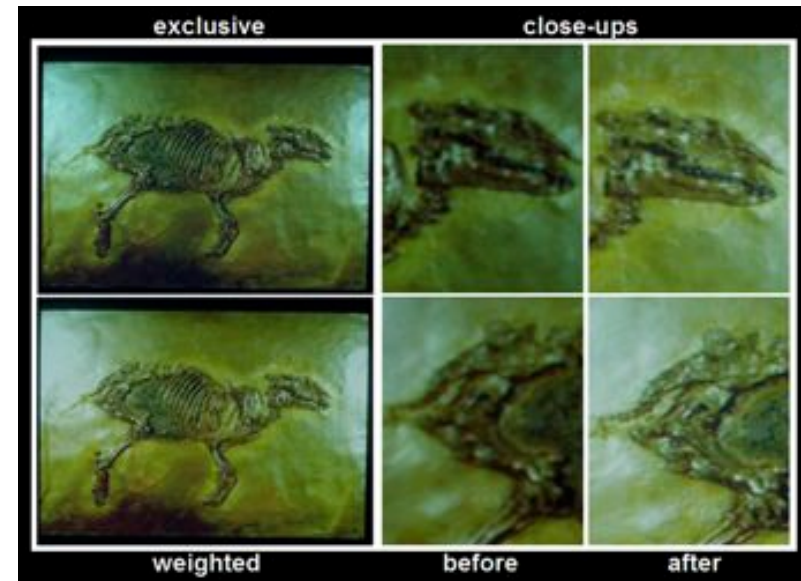


Bimber et al, IEEE TVCG 2006

Image Composition

Image Composition

- using the focus values of each projector's pixels $\Phi_{i,x,y}$, compose an image with minimal total defocus
 - exclusive composition:** surface point is covered by a single projector pixel (the one with highest $\Phi_{i,x,y}$)



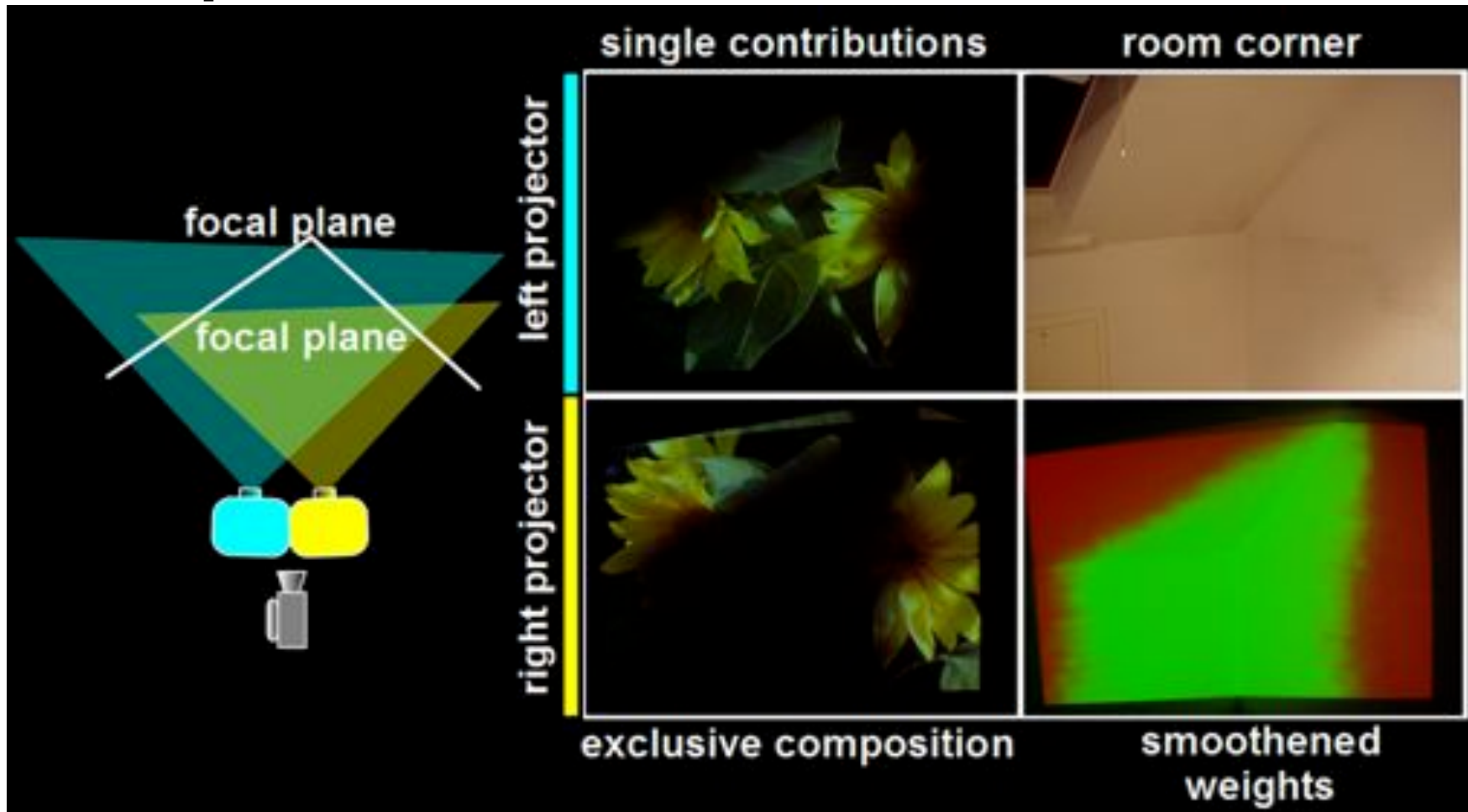
$$I_i = \frac{w_i(R - EM)}{\sum_j^N w_j FM_j} \quad w_{i,x,y} = \frac{\Phi_{i,x,y}}{\sum_j^N \Phi_{j,x,y}}$$

- weighted composition:** compute normalized weight and multiply it with FM and I

$$I_i = w_i(R - EM) / FM_i, \quad w_i = \begin{cases} 1 & \Phi_{i,x,y} \geq \Phi_{j,x,y} \\ 0 & \text{else} \end{cases}$$

Example: Room Corner

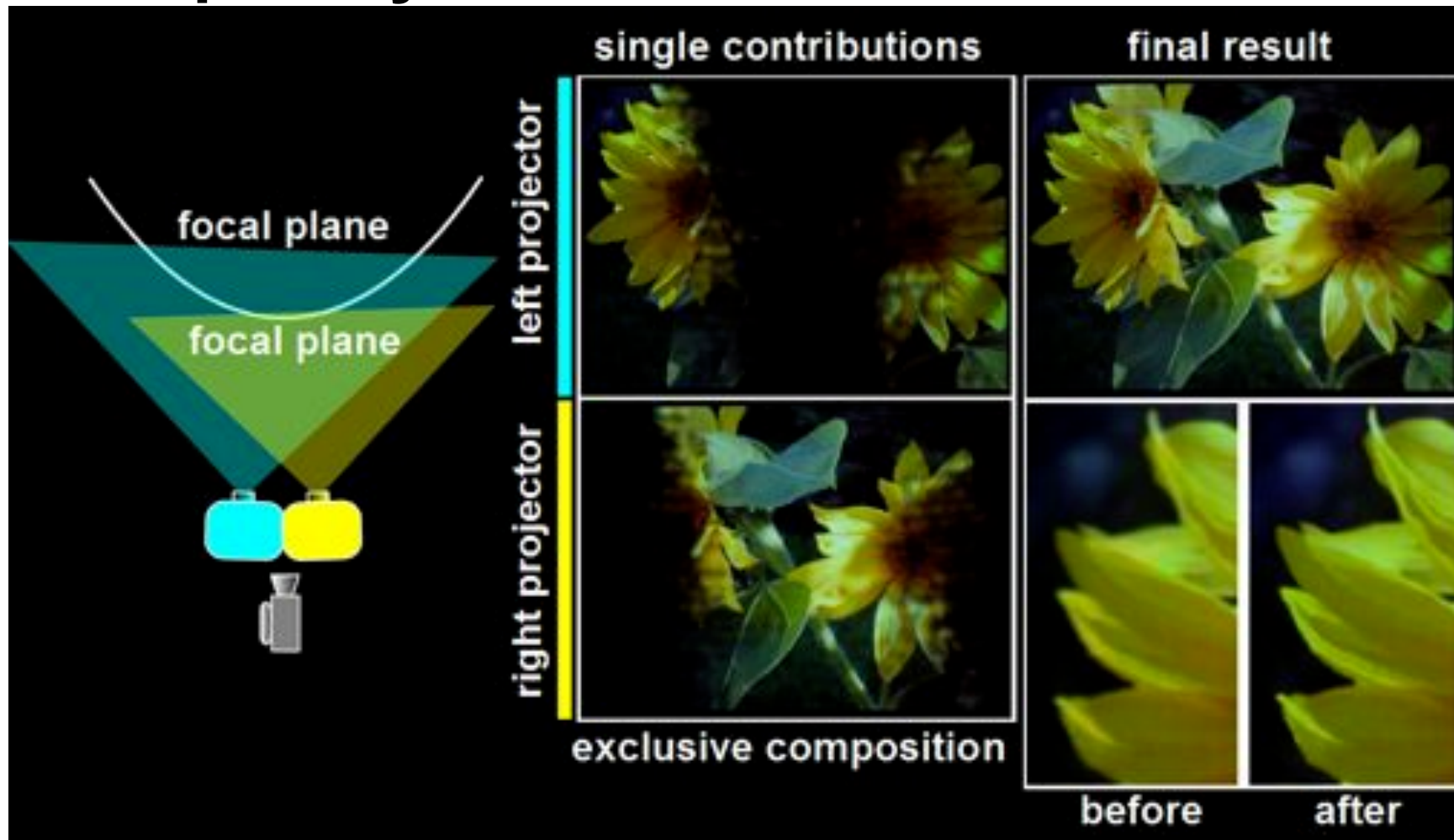
Example: Room Corner



Bimber et al, IEEE TVCG 2006

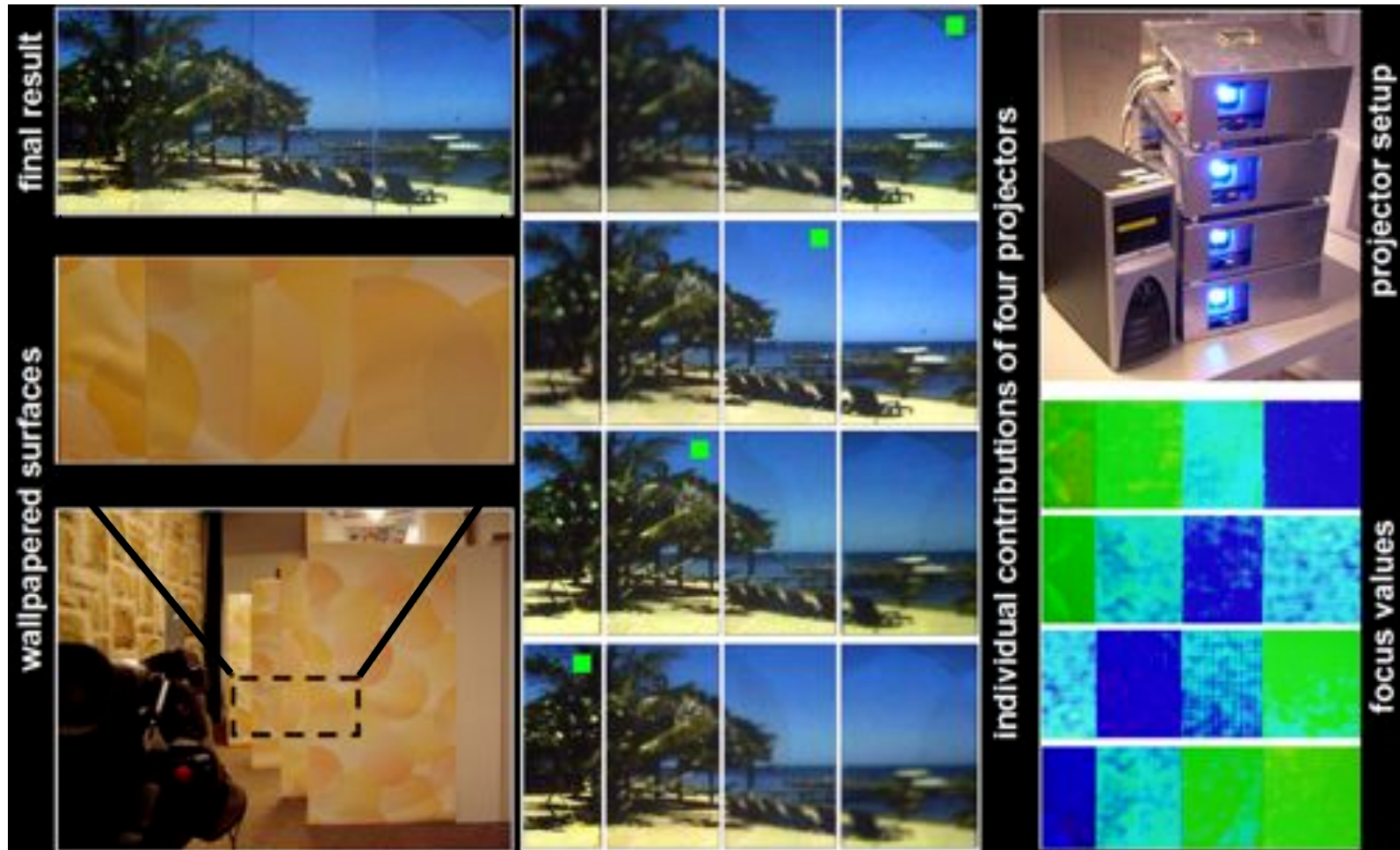
Example: Cylindrical Surface

Example: Cylindrical Surface



Example: Large Focal Depth

Example: Large Focal Depth



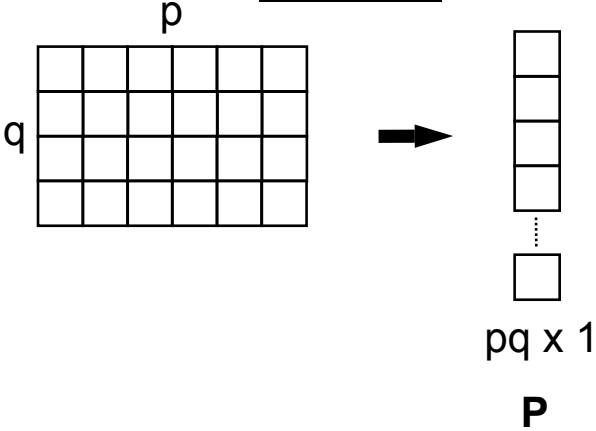
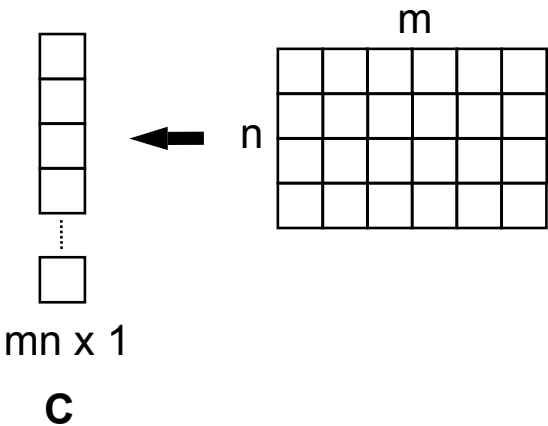
Bimber et al, IEEE TVCG 2006

Advanced Techniques Light Transport

Acquisition

Acquisition

single camera & projector capture 4D slice of 8D reflectance field



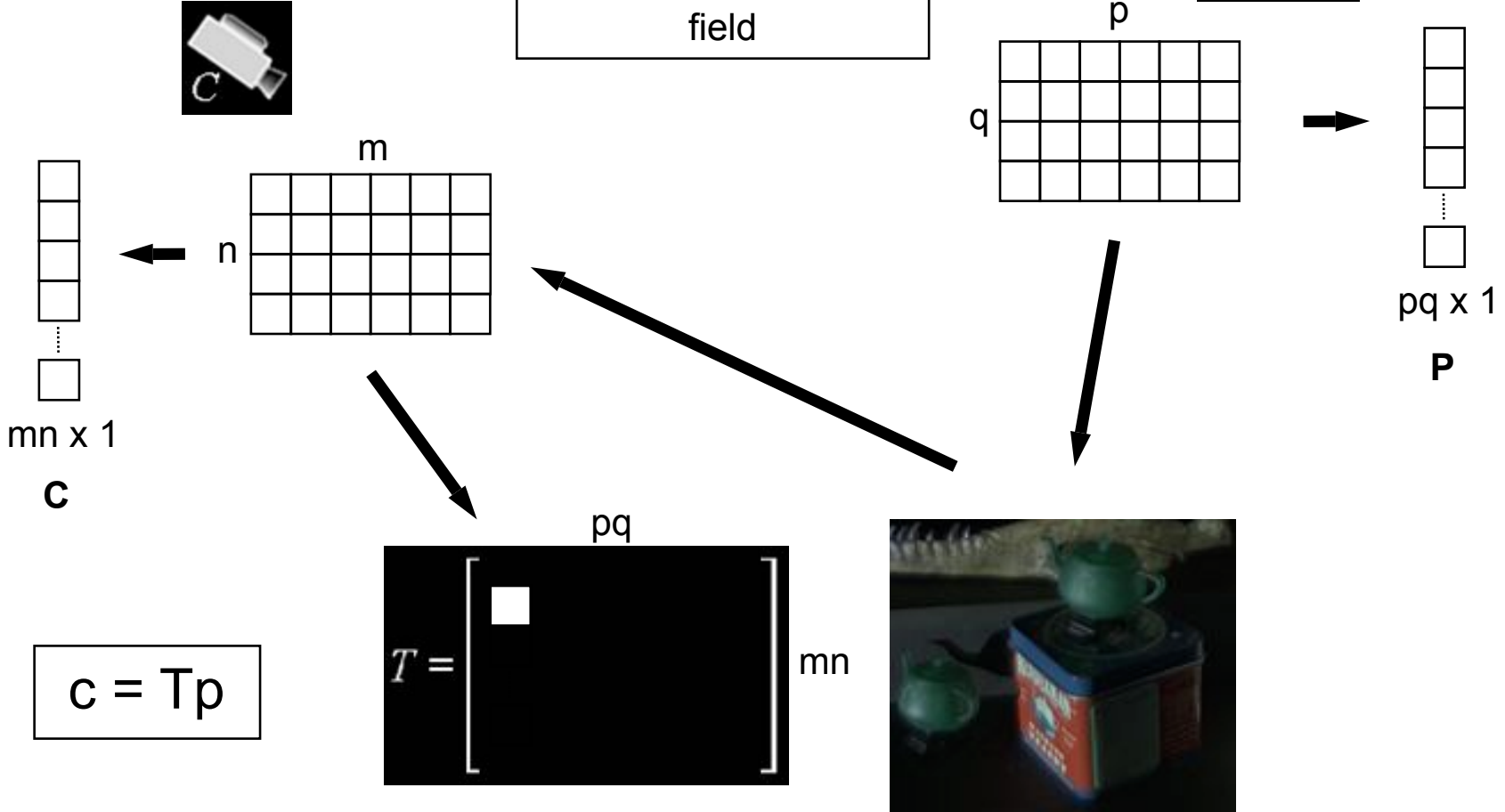
$$T = \begin{bmatrix} & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \end{bmatrix} \begin{matrix} pq \\ \\ \\ \\ mn \end{matrix}$$

$c = Tp$



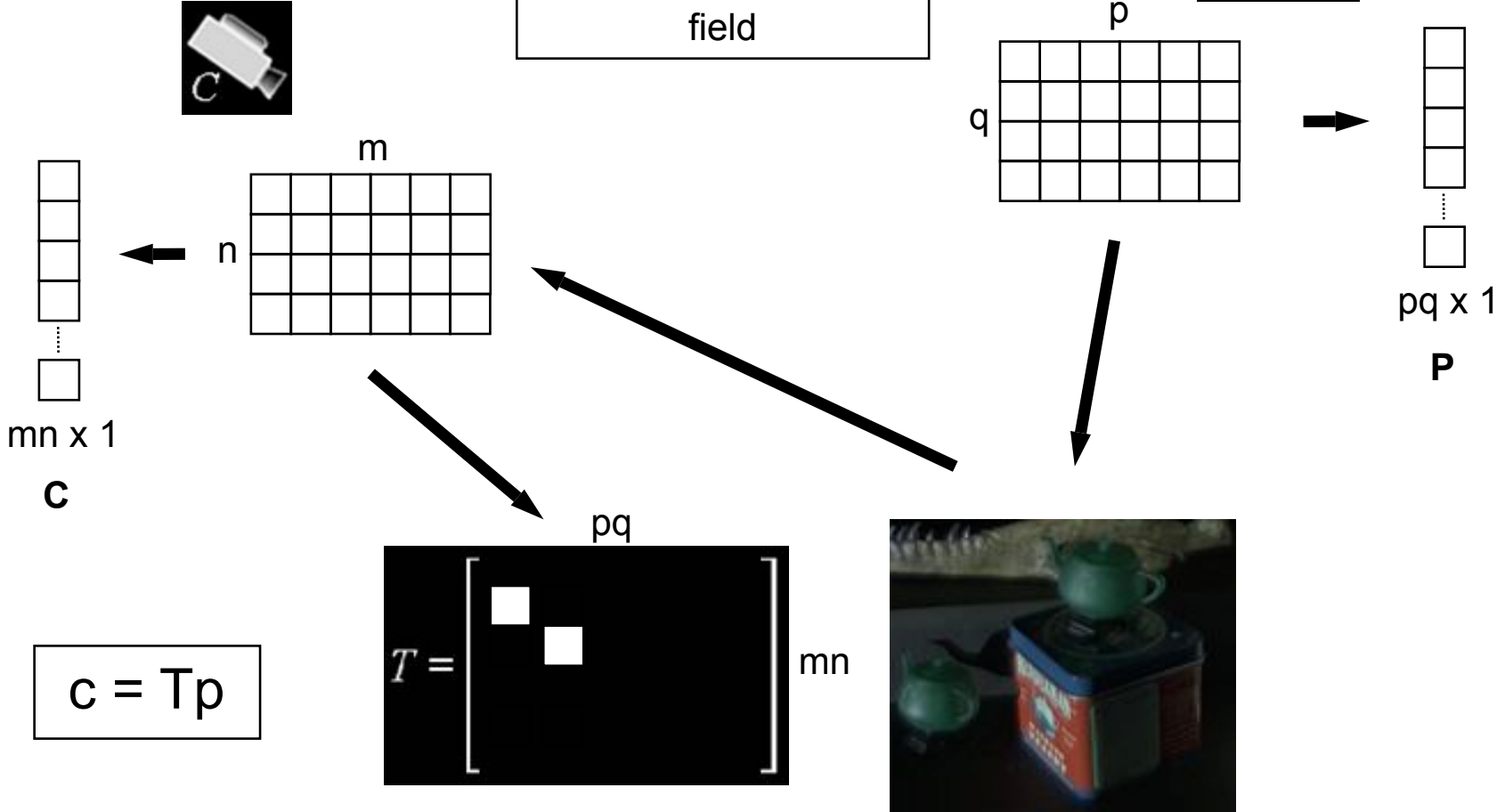
Acquisition

single camera & projector capture 4D slice of 8D reflectance field

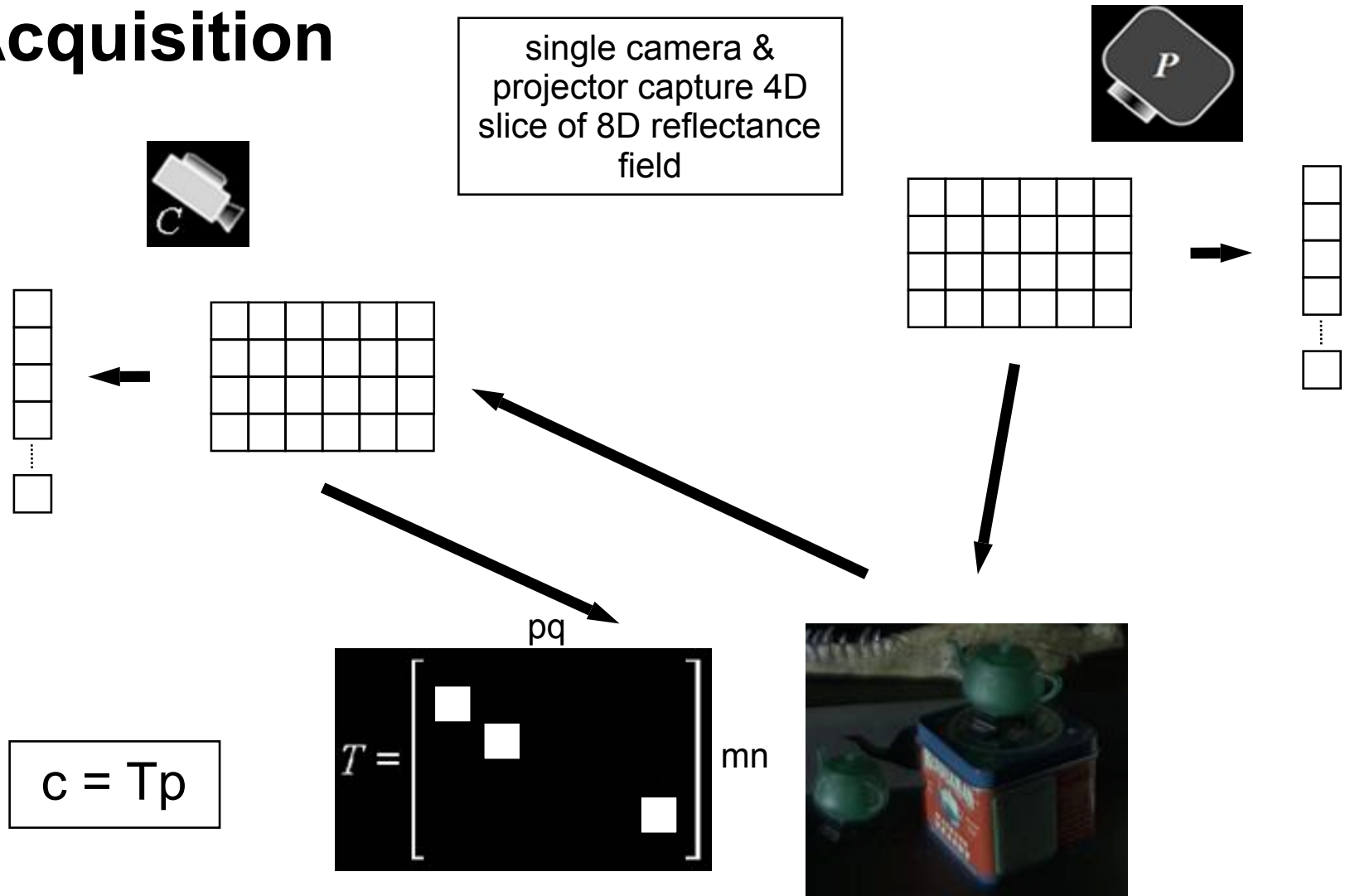


Acquisition

single camera & projector capture 4D slice of 8D reflectance field

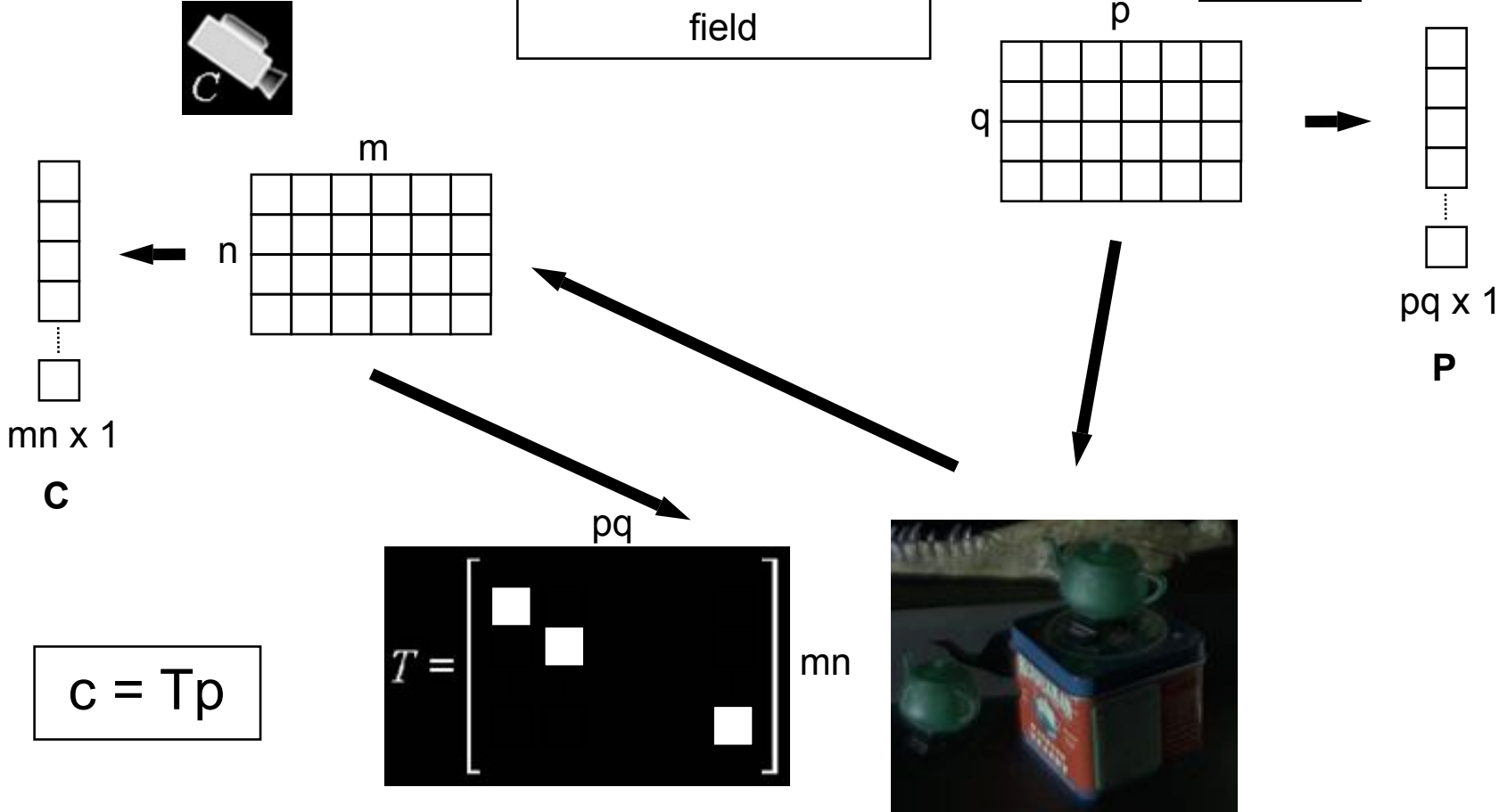


Acquisition



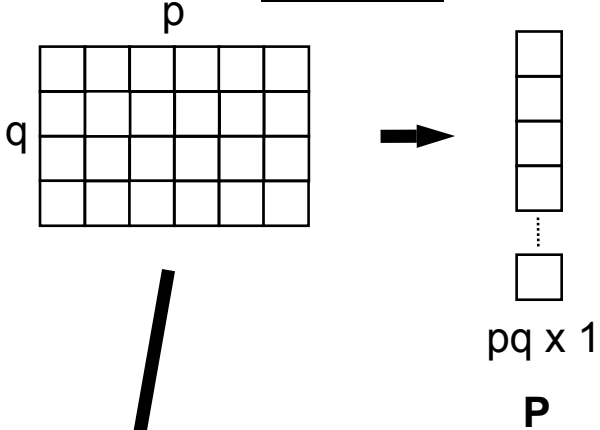
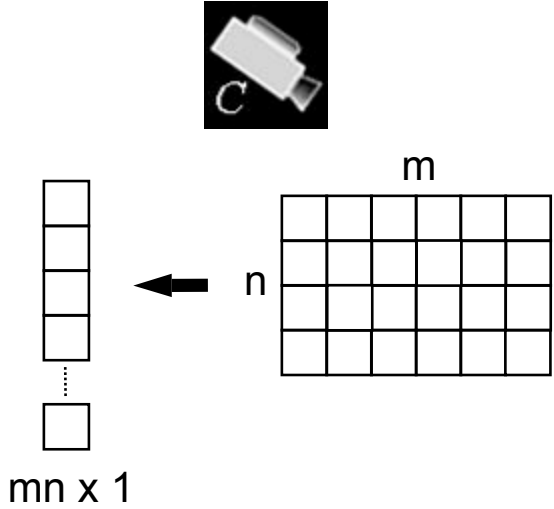
Acquisition

single camera & projector capture 4D slice of 8D reflectance field



Acquisition

single camera & projector capture 4D slice of 8D reflectance field



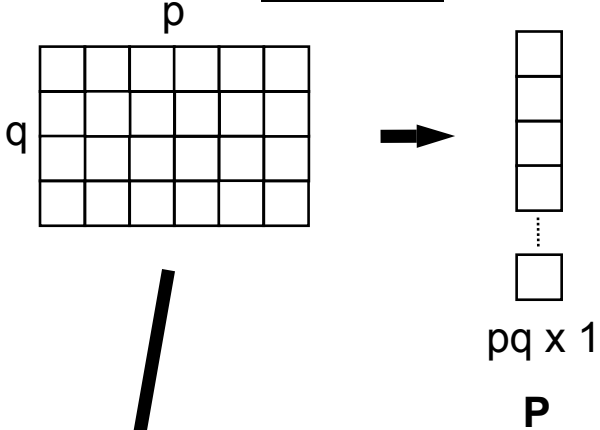
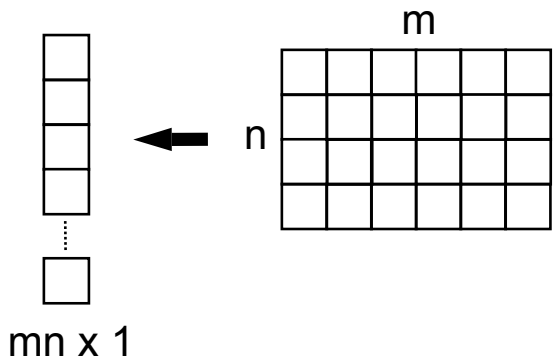
$c = T p$

$$T = \begin{bmatrix} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \end{bmatrix} \begin{matrix} pq \\ mn \end{matrix}$$

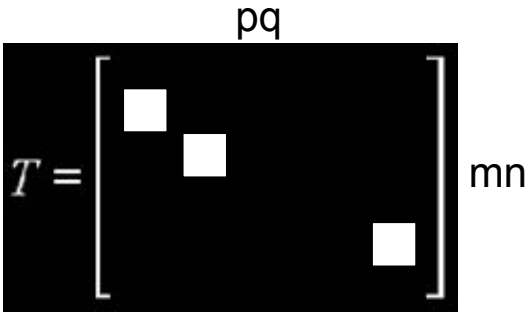


Acquisition

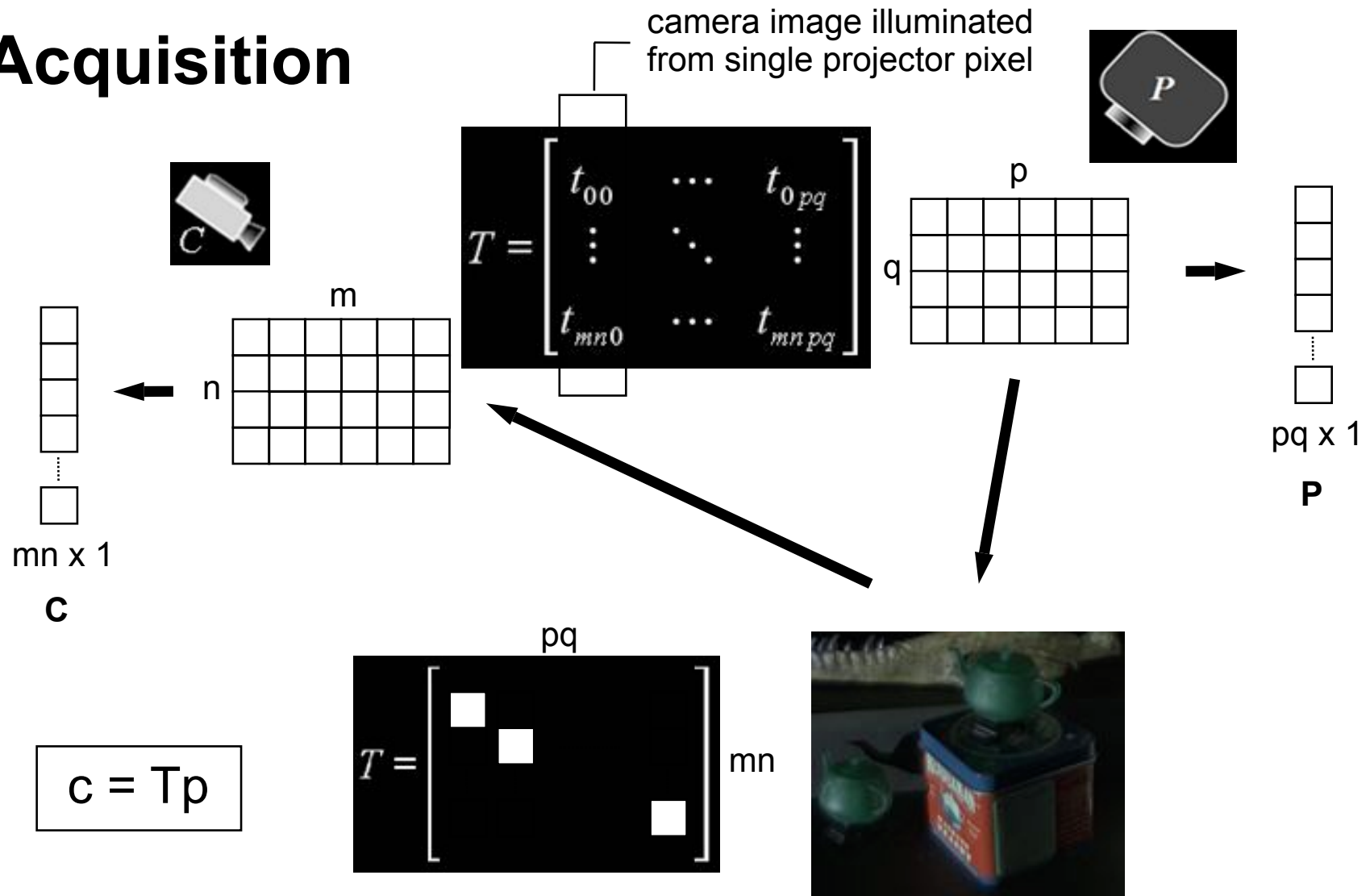
single camera & projector capture 4D slice of 8D reflectance field



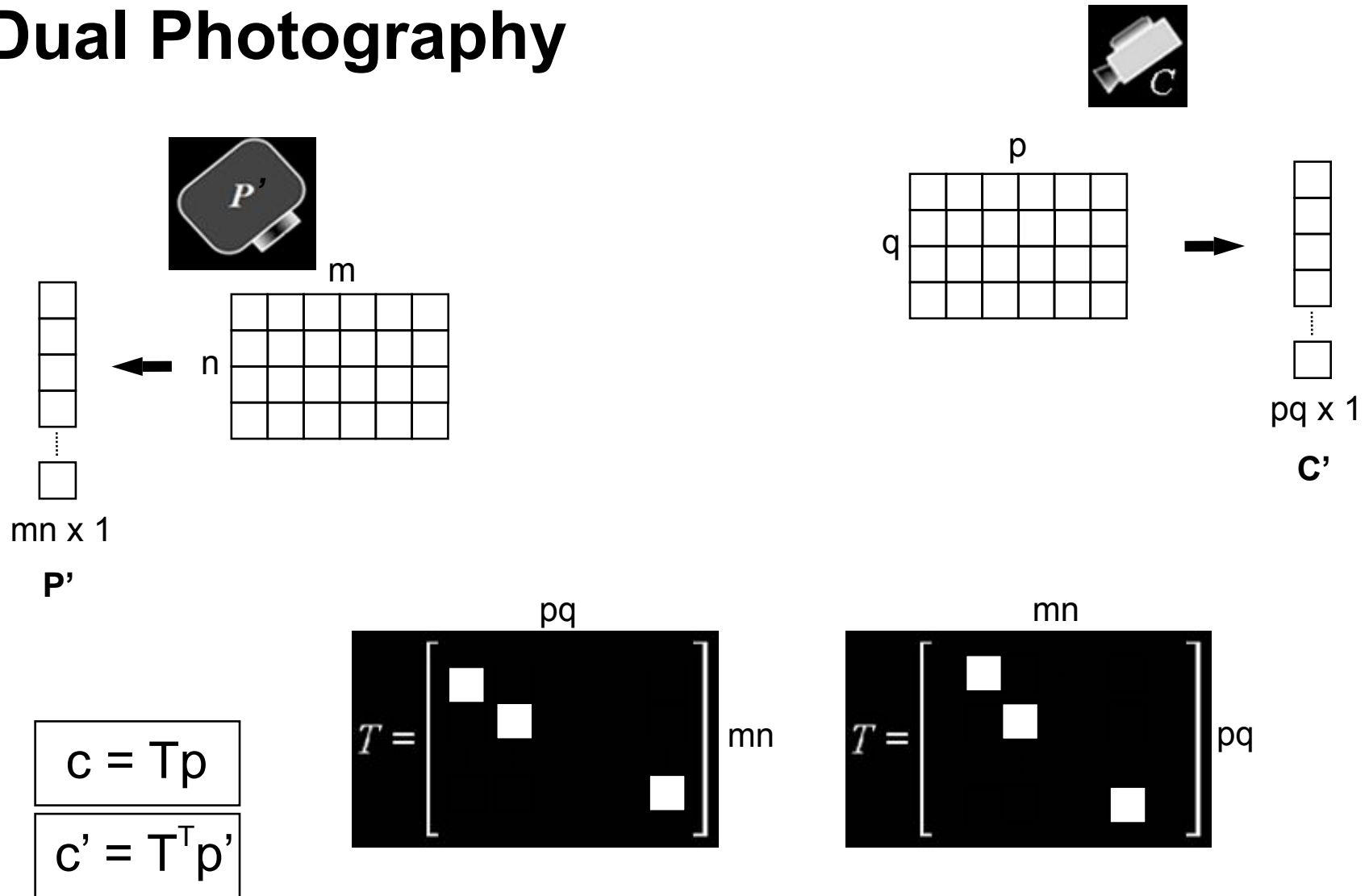
$c = T p$



Acquisition



Dual Photography

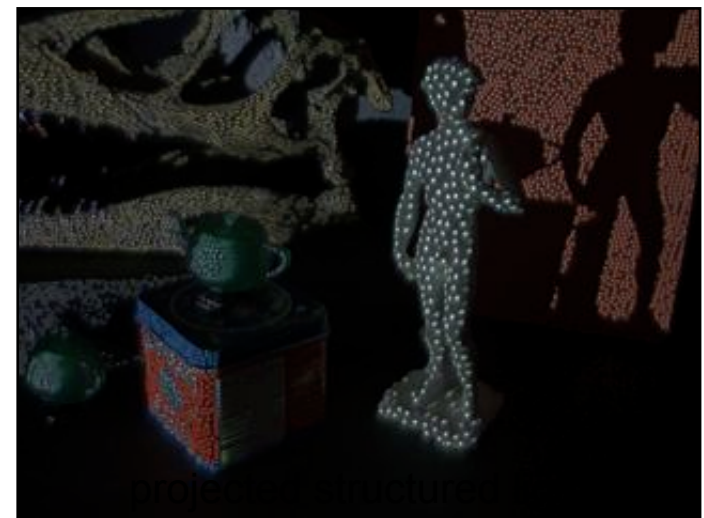


Dual Photography

Dual Photography



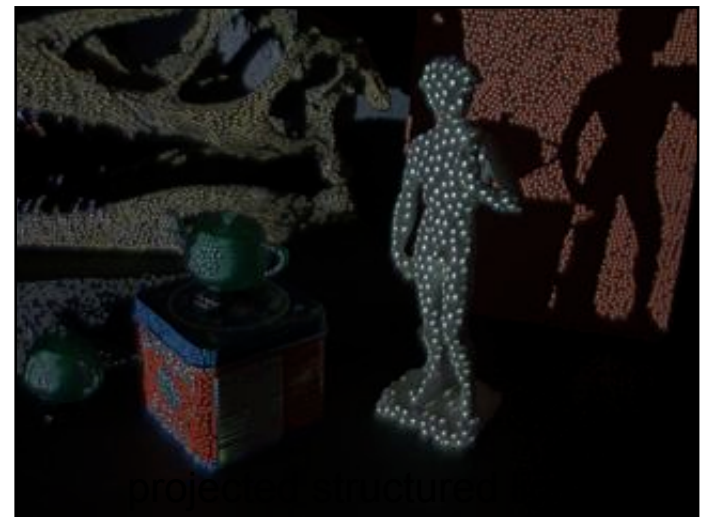
Dual Photography



Dual Photography



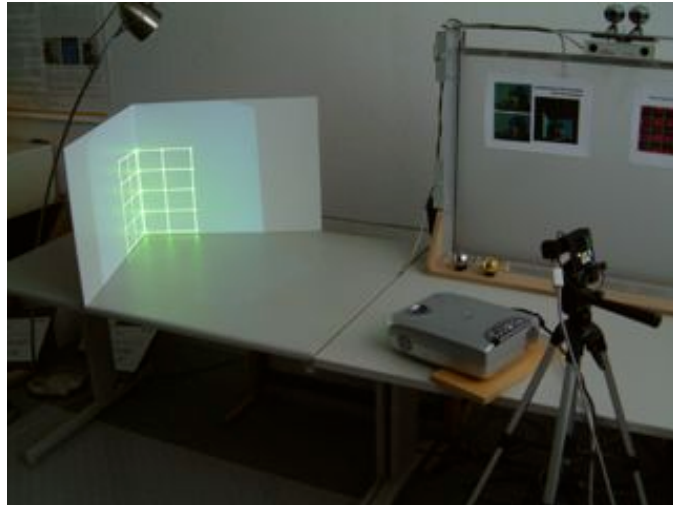
floodlight camera image



more information on
dual photography:
Sen, et al.,
Siggraph'05

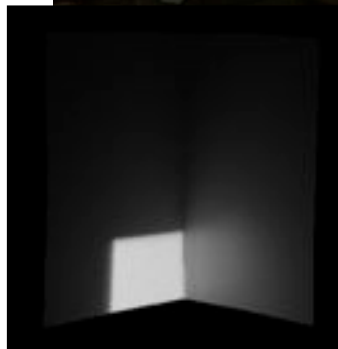
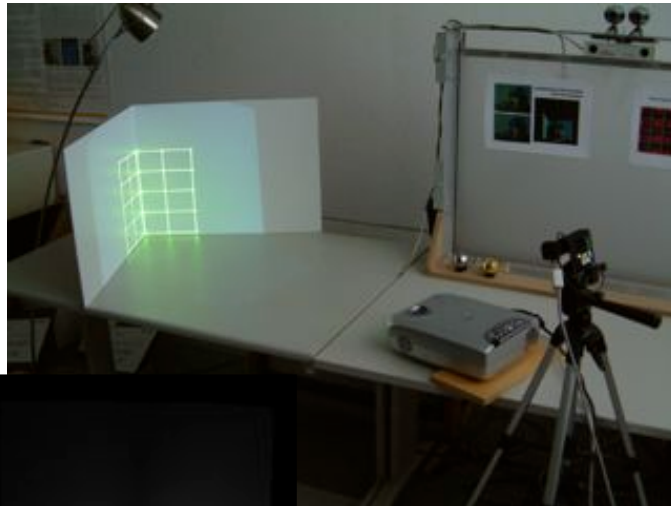
Form-Factors from Light Transport Matrix

Form-Factors from Light Transport Matrix

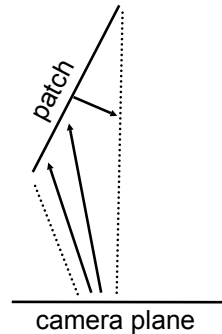


experimental setup

Form-Factors from Light Transport Matrix

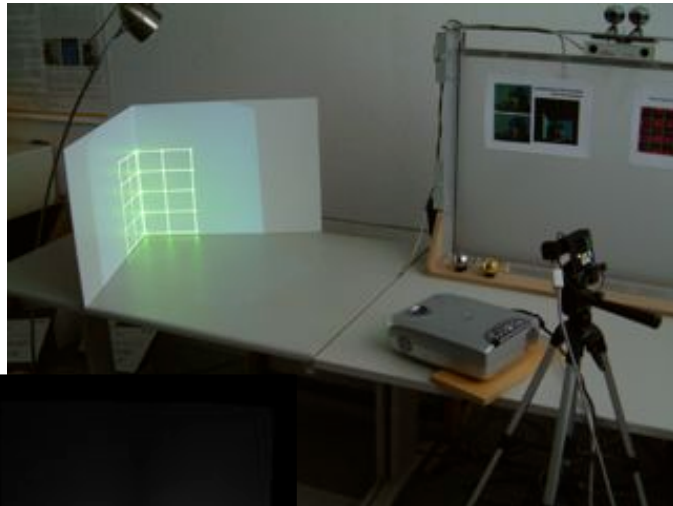


experimental setup

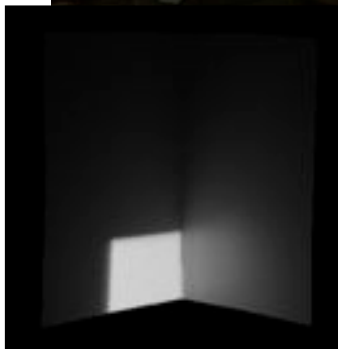


$$M_e = \frac{d^2}{\cos \alpha} L_e$$

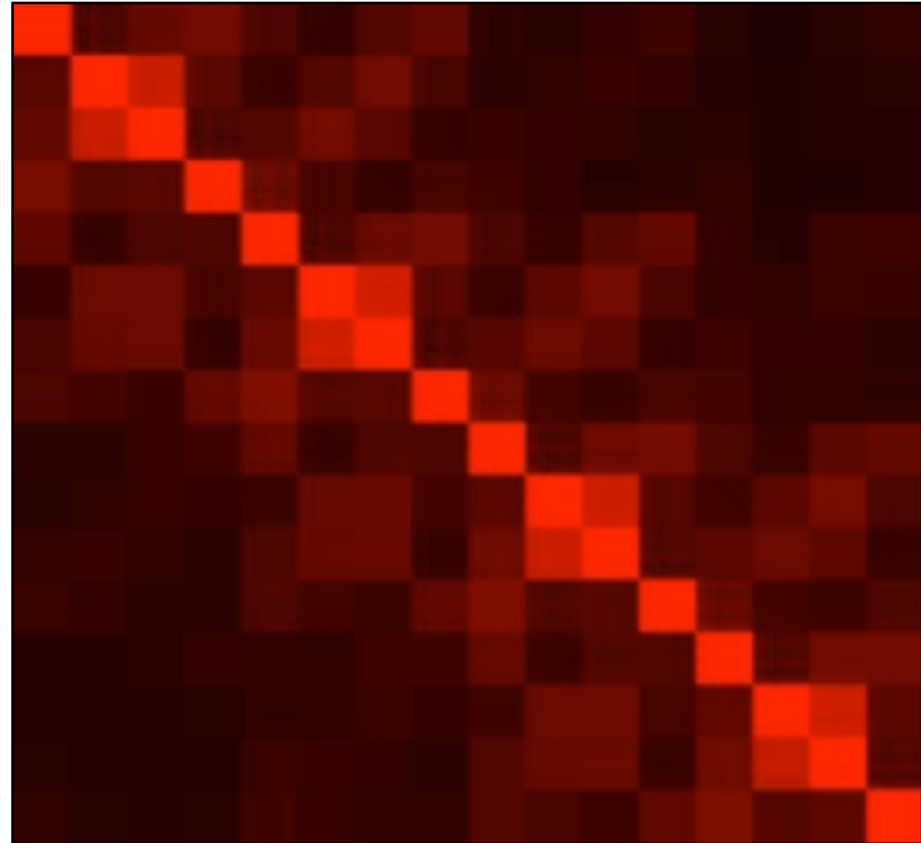
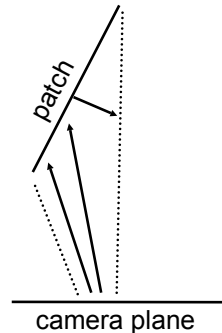
Form-Factors from Light Transport Matrix



experimental setup



$$M_e = \frac{d^2}{\cos \alpha} L_e$$

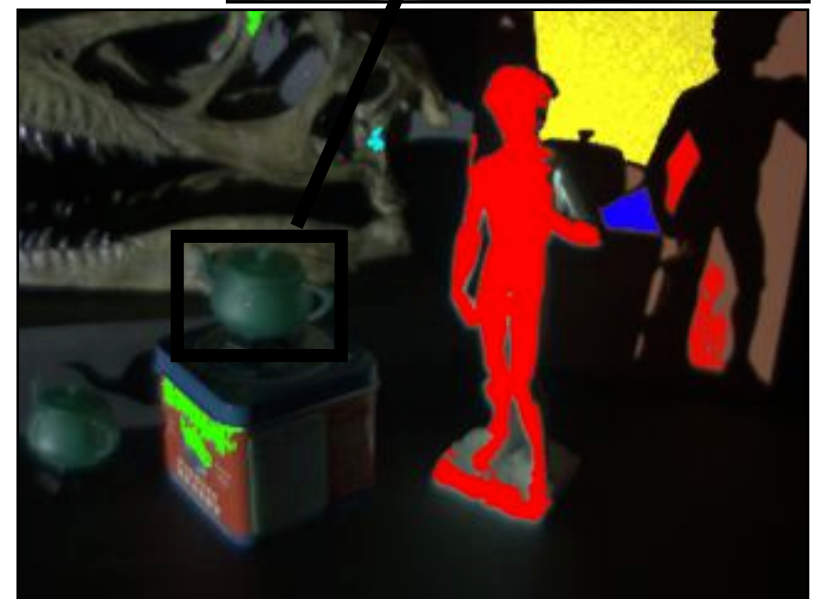


measured 16x16 form-factor matrix
(computed from light transport matrix)

Global Radiometric Compensation

Global Radiometric Compensation

- traditional radiometric compensation requires direct projector-camera pixel correspondence
- include arbitrary global illumination effects using T
- apply inverse light transport $T^{-1}C=P$
- since T is huge, decompose it into clusters and solve in real-time on GPU



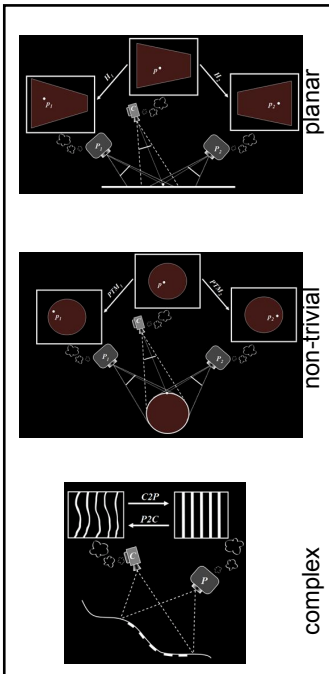
$$C = T P \quad T^{-1} \quad C = P$$

$$\begin{bmatrix} c_{10} \\ c_{11} \\ c_{12} \\ c_{13} \\ c_{14} \end{bmatrix} = \begin{bmatrix} t_{10}^4 & t_{10}^3 \\ t_{11}^4 & t_{11}^3 \\ t_{12}^4 & t_{12}^3 \\ t_{13}^4 & t_{13}^3 \\ t_{14}^4 & t_{14}^3 \end{bmatrix} \begin{bmatrix} p_4 \\ p_3 \end{bmatrix}$$

$$\begin{bmatrix} t_{10}^4 & t_{11}^4 & t_{12}^4 & t_{13}^4 & t_{14}^4 \\ t_{10}^3 & t_{11}^3 & t_{12}^3 & t_{13}^3 & t_{14}^3 \end{bmatrix}^{-1} \begin{bmatrix} c_{10} \\ c_{11} \\ c_{12} \\ c_{13} \\ c_{14} \end{bmatrix} = \begin{bmatrix} p_4 \\ p_3 \end{bmatrix}$$

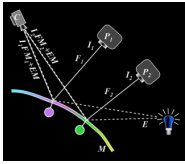
Outlook





geometric warping

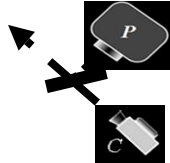




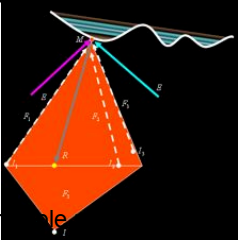
single projector

$$V = \begin{bmatrix} V_{RR} & V_{RG} & V_{RB} \\ V_{GR} & V_{GG} & V_{GB} \\ V_{BR} & V_{BG} & V_{BB} \end{bmatrix}$$


color mixing



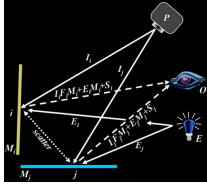
dynamic adaptation



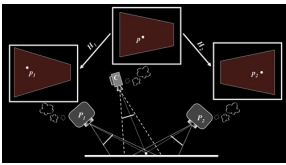
radiometric compensation



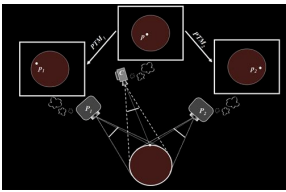
perception



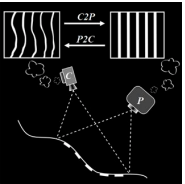
global effects



planar



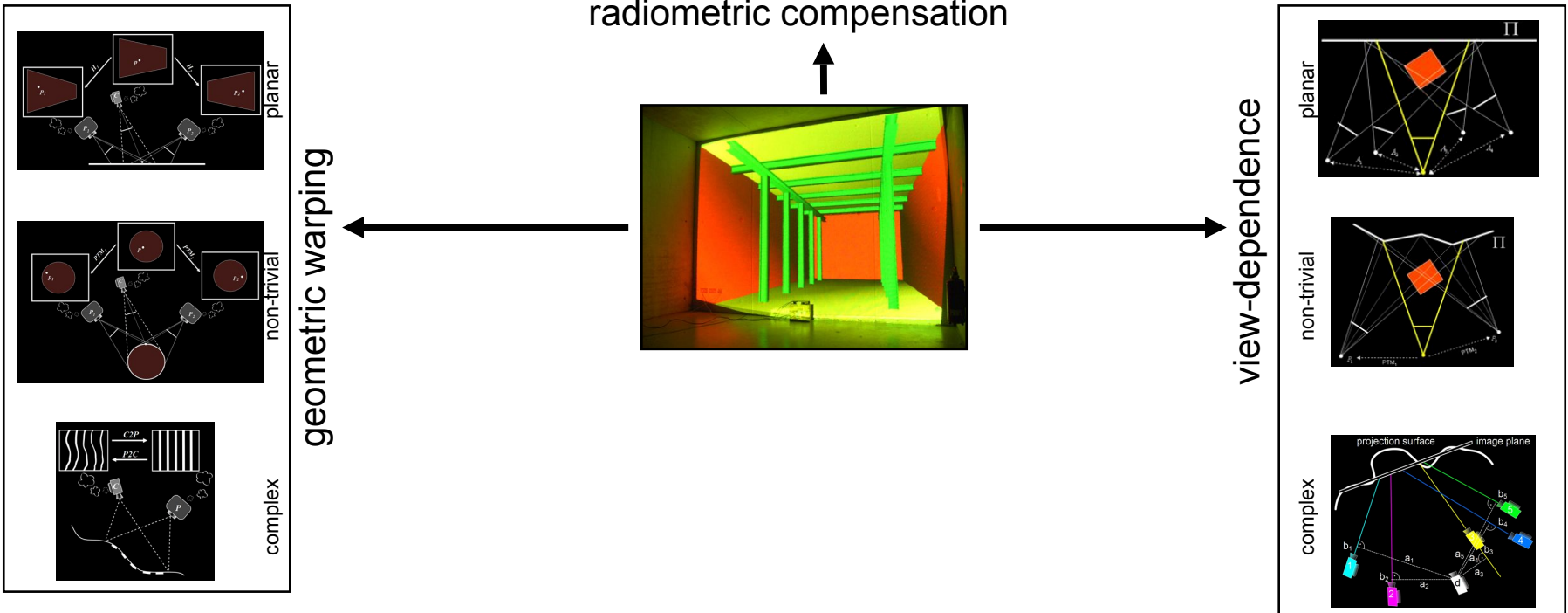
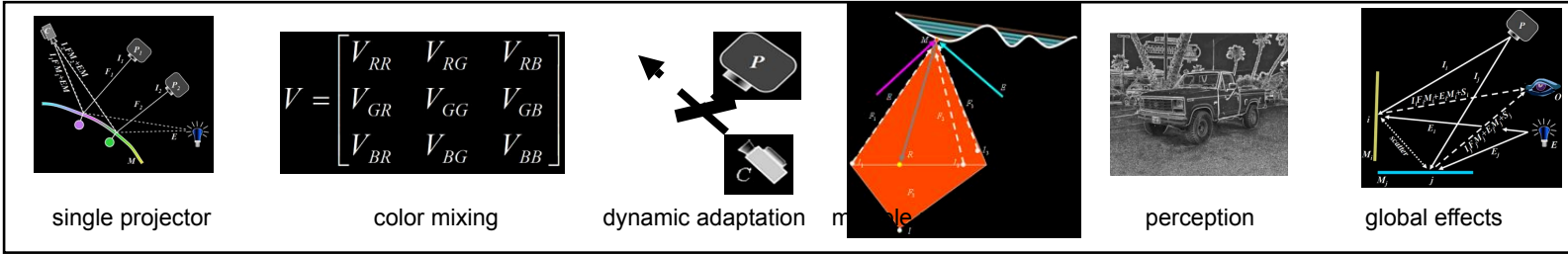
non-trivial

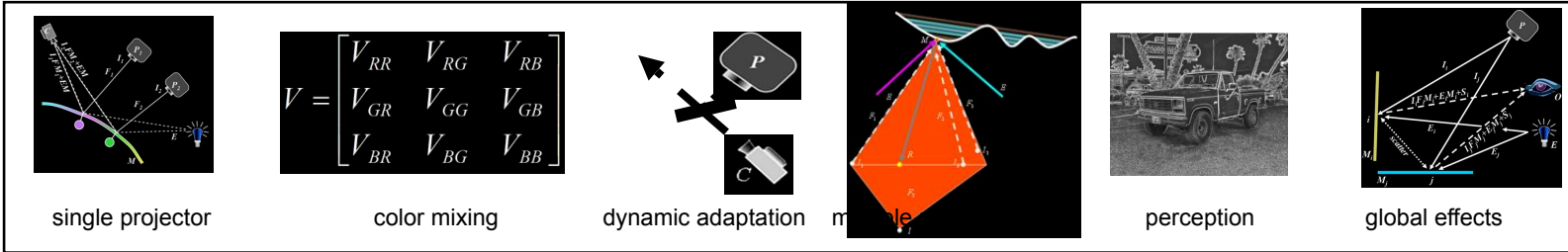


complex

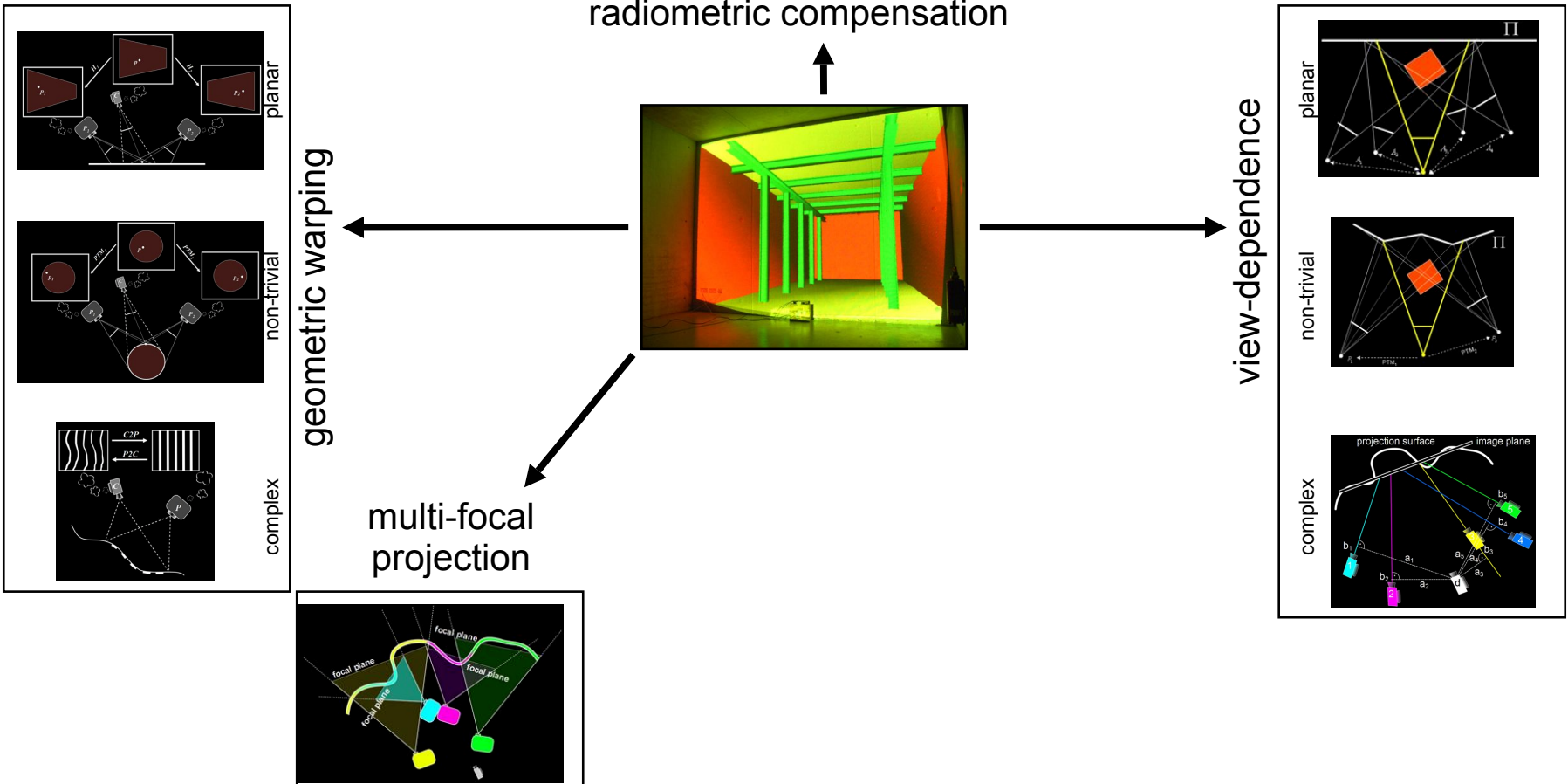
geometric warping

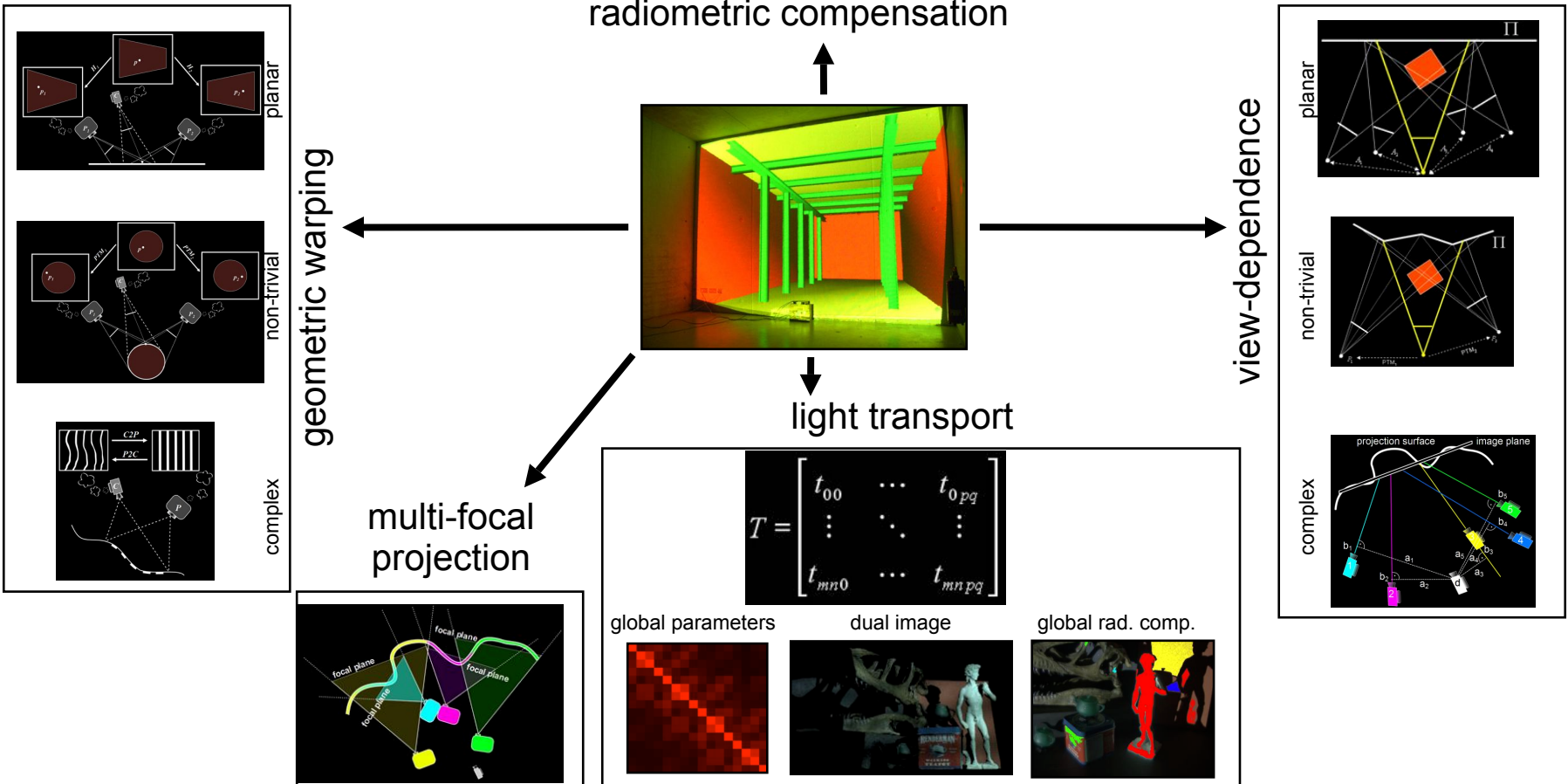
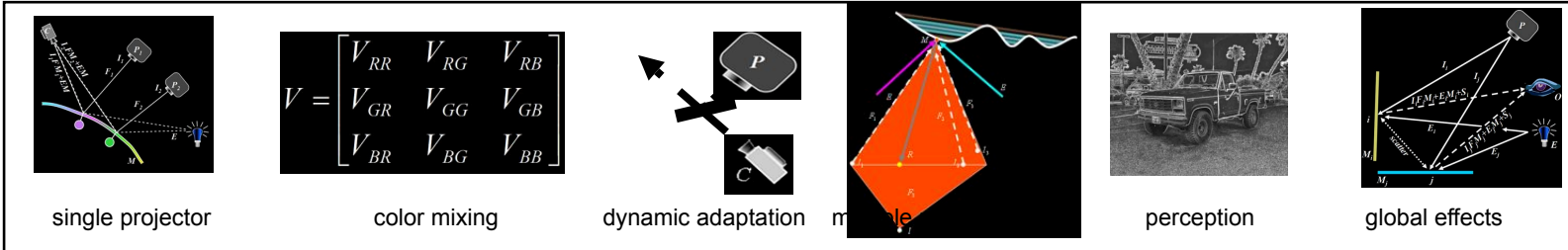




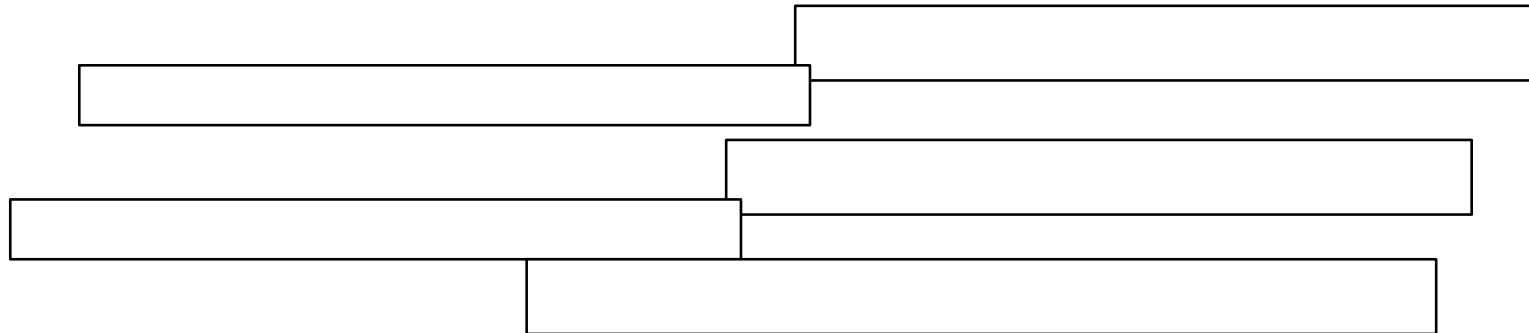


radiometric compensation





Limitations



Limitations

- technological limitations of projectors:
 - brightness, resolution, focal depth

[Redacted text]

[Redacted text]

[Redacted text]

Limitations

- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range

Limitations

- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range → wait for HDR light-valve or laser projectors
 - size, cost, portability

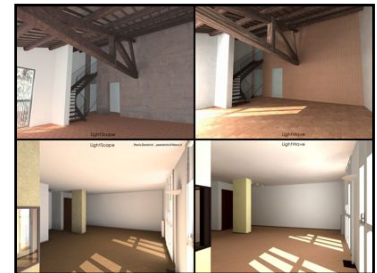
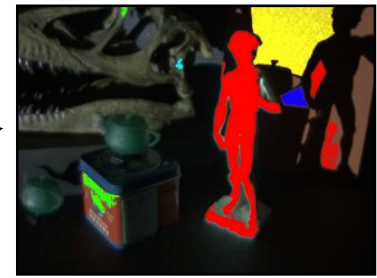
Limitations

- technological limitations of projectors:
 - brightness, resolution, focal depth → can be solved by using multiple projectors (or wait for better ones)
 - black-level and dynamic range → wait for HDR light-valve or laser projectors
 - size, cost, portability → wait for (good enough) pocket projectors
- technological limitations of cameras:

Future Work

Future Work

- new techniques:
 - consider human visual perception
 - spent computational power only on overcoming limitations that can actually be perceived
 - consider global effects
 - inter-reflections, scattering, etc.



Selected Papers on Geometric Correction

Selected Papers on Geometric Correction

Bimber, O., Wetzstein, G., Emmerling, A., & Nitschke, C. (2005). Enabling View-Dependent Stereoscopic Projection in Real Environments. *Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'05)*, 14-23.

Low, K-L., Welch, G., Lastra, A., & Fuchs, H. (2001). Life-Sized Projector-Based Dioramas, *Proc. Symp. Virtual Reality Software and Technology (VRST'01)*, 93-101.

Raskar, R. (1999). Oblique Projector Rendering on Planar Surfaces for a Tracked User. *Proc. of ACM Siggraph '99*, sketch.

Raskar, R., Brown, M.S., Yang, R., Chen, W., Welch, G., Towles, H., Seales, B., & Fuchs, H. (1999b). Multi-projector displays using camera-based registration, *Proc. of IEEE Visualization (IEEE Viz'99)*, 161-168.

Raskar, R., Welch, G., Low, K.L. & Bandyopadhyay, D. (2001). Shader Lamps: Animating real objects with image-based illumination. *Proc. of Eurographics Rendering Workshop*, 89-102.

Selected Papers on Radiometric Compensation

Selected Papers on Radiometric Compensation

Bell, I.E. (2003). Neutralizing Paintings with a Projector. *Proc. of SPIE/IS&T*, 5008, 560-568.

Bimber, O., Coriand, F., Kleppe, A., Bruns, E., Zollmann, S., & Langlotz, T. (2005). Superimposing Pictorial Artwork with Projected Imagery. *IEEE MultiMedia*. 12(1), 16-26.

Bimber, O., Grundhöfer, A., Zeidler, T., Danch, D., & Kapakos, P. (2006). Compensating Indirect Scattering for Immersive and Semi-Immersive Projection Displays. *Proc. of IEEE Virtual Reality (IEEE VR'06)*.

Fujii, K., Grossberg, M.D., & Nayar, S.K. (2005). A projector-camera system with real-time photometric adaptation for dynamic environments. *Proc. of Computer Vision and Pattern Recognition (CVPR'05)*, 2, 20-25.

Grossberg, M.D., Peri, H., Nayar, S.K., & Bulhumeur, P. (2004). Making One Object Look Like Another: Controlling Appearance Using a Projector-Camera System. *Proc. of IEEE Conference on Computer Vision and Pattern Recognition (CVPR'04)*, 1, 452-459.

Nayar, S.K., Peri, H., Grossberg, M.D., & Belhumeur, P.N. (2003). A Projection System with Radiometric Compensation for Screen Imperfections. *Proc. of International Workshop on Projector-Camera Systems (ProCams'03)*.

Wang, D., Sato, I., Okabe, T., & Sato, Y. (2005). Radiometric Compensation in a Projector-Camera System Based on the Properties of Human Vision System. *In Proc. of IEEE International Workshop on Projector-Camera Systems (ProCams'05)*.

O. Bimber

**Multi-Projector Techniques for Real-Time
Visualizations in Everyday Environments**

04/01/06

Yoshida, T., Horii, C. & Sato, K. (2003). A Virtual Color reconstruction System for Real Heritage with Light Projection. *Proc. of Virtual Systems and Multimedia*. 158-164

Selected Papers Other and Related Techniques

Selected Papers Other and Related Techniques

Bimber, O. & Emmerling, A. (2006). Multi-Focal Projection: A Multi-Projector Technique for Increasing Focal Depth. *IEEE Transactions on Visualization and Computer Graphics (TVCG)*.

Brown, M., Majumder, A., and Yang, R. (2005). Camera-Based Calibration Techniques for Seamless Multi-Projector Displays. *IEEE Transactions on Visualization and Computer Graphics (TVCG)*, 11(2), 193-206.

Cotting, D., Naef, M., Gross, M., & Fuchs, H. (2004). Embedding Imperceptible Patterns into Projected Images for Simultaneous Acquisition and Display. *Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'04)*, 100-109.

Ehnes, J., Hirota, K., & Hirose, M. (2004). Projected Augmentation – Augmented Reality using Rotatable Video Projectors. *Proc. of IEEE/ACM International Symposium on Mixed and Augmented Reality (ISMAR'04)*, 26-35.

Underkoffler, J., Ullmer, B. & Ishii, H. (1999). Emancipated pixels: real-world graphics in the luminous room. *Proc. of ACM Siggraph*, 385-392.

Levoy, M., Chen, B., Vaish, V., Horowitz, M., McDowall, I., and Bolas, M. (2004) Synthetic Aperture Confocal Imaging, *Proc. of ACM Siggraph'04*, pp. 825-834.

Sen, P., Chen, B., Garg, G., Marschner, S.R., Horowitz, M., Levoy, M., and Lensch, H.P.A (2005)., Dual Photography, *Proc. of ACM*

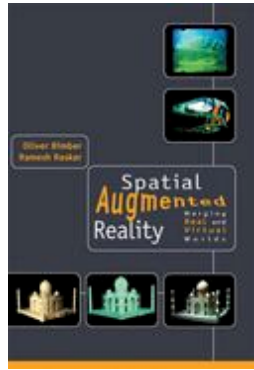
Siggraph, pp. 745-755

O. Bimber

Multi-Projector Techniques for Real-Time
Visualizations in Everyday Environments

04/01/06

Thank you!
www.uni.weimar.de/medien/AR



Bimber, O. & Raskar, R.
*Spatial Augmented Reality: Merging
Real and Virtual Worlds*. A K Peters
LTD (publisher), ISBN:
1-56881-230-2.

Thank you!
www.uni.weimar.de/medien/AR



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Forschungsgemeinschaft (DFG) under contract number
PE 1183/1-1.