

Efficient Object Sharing in Quantum-Based Real-Time Systems*

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Abstract

We consider the problem of implementing shared objects in uniprocessor and multiprocessor real-time systems in which tasks are executed using a scheduling quantum. In most quantum-based systems, the size of the quantum is quite large in comparison to the length of an object call. As a result, most object calls can be expected to execute without preemption. A good object-sharing scheme should optimize for this expected case, while achieving low overhead when preemptions do occur. Our approach is to use an optimistic retry scheme coupled with the assumption that each task can be preempted at most once across two object calls. Given this preemption assumption, each object call can be retried at most once. Experimental evidence is cited that suggests that for most quantum-based systems, our preemption assumption is reasonable. Major contributions of this paper include several new retry-based shared-object algorithms for uniprocessors and multiprocessors, and scheduling analysis results that can be used in conjunction with these algorithms. We consider both conventional periodic real-time task systems implemented using a scheduling quantum, and also proportional-share systems. The retry mechanism used in our multiprocessor implementation is based on a preemptable queue-lock algorithm. Our queue-lock is much simpler than preemptable queue locks proposed previously. Experimental results are presented that show that the performance of our lock is up to 25% better than one presented at last year's RTSS, when applied in quantum-based systems.

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1 Introduction

In many real-time systems, tasks are scheduled for execution using a scheduling quantum. Under quantum-based scheduling, processor time is allocated to tasks in discrete time units called *quanta*. When a processor is allocated to some task, that task is guaranteed to execute without preemption for Q time units, where Q is the length of the quantum, or until it terminates, whichever comes first. Many real-time applications are designed based on scheduling disciplines such as proportional-share [24] and round-robin scheduling that are expressly quantum-based. Under proportional-share scheduling, each task is assigned a *share* of the processor, which represents the fraction of processing time that that task should receive. Quanta are allocated in a manner that ensures that the amount of processor time each task receives is commensurate with its share. Round-robin scheduling is a simpler scheme in which each task has an identical share.

Quantum-based execution also arises when conventional priority-based scheduling disciplines, such as rate-monotonic (RM) and earliest-deadline-first (EDF) scheduling, are implemented on top of a timer-driven real-time kernel [16]. In such an implementation, interrupts are scheduled to occur at regular intervals, and scheduling decisions are made when these interrupts occur. The length of time between interrupts defines the scheduling quantum. Timer-driven systems can be seen as a compromise between nonpreemptive and completely preemptive systems. In fact, nonpreemptive and preemptive systems abstractly can be viewed as the extreme endpoints in a continuum of quantum-based systems: a nonpreemptive system results when $Q = \infty$ and a fully preemptive system results when $Q = 0$. Nonpreemptive systems have several advantages over preemptive systems, including lower scheduling overheads (if preemptions are frequent) and simpler object-sharing protocols [8, 14]. In addition, timing analysis is simplified because cache behavior is easier to predict. However, these advantages come at the potential expense of longer response times for higher-priority tasks. Quantum-based systems can be seen as a compromise between these two extremes.

In this paper, we consider the problem of efficiently implementing shared objects in quantum-based real-time systems. We consider both uniprocessor and multiprocessor systems. The basis for our results is the observation that, in most quantum-based systems, the size of the quantum is quite large compared to the length of an object call. Indeed, processors are becoming ever faster, decreasing object-access times, while quantum sizes are not changing. Even with the technology of several years ago, one could make the case that object calls are typically short compared to a quantum. As evidence of this, we cite results from experiments conducted by Ramamurthy to compute access times for several common objects [21]. These experiments were performed on a 25 MHz 68030 machine and involved objects ranging from queues to linked lists to medium-sized balanced trees. Both lock-based and lock-free (see below) object implementations were evaluated. Ramamurthy found that, even on a slow 25 MHz machine, all object calls completed within about 100 microseconds, with most taking much less. In contrast, a quantum in the range 1-100 milliseconds is used in most quantum-based systems.

These numbers suggest that, in a quantum-based system, most object calls are likely to execute without preemption. A good object-sharing scheme should optimize for this expected case, while achieving low overhead when preemptions do occur. Clearly, an optimistic object-sharing scheme is called for here, because pessimisti-

```

type Qtype = record data: valtype; next: pointer to Qtype end
shared variable Head, Tail: pointer to Qtype
private variable old, new: pointer to Qtype; addr: pointer to pointer to Qtype
procedure Enqueue(input: valtype)
  *new := (input, NULL);
  repeat old := Tail;
    if old ≠ NULL then addr := &(old->next) else addr := &Head fi
  until CAS2(&Tail, addr, old, NULL, new, new)

```

Figure 1: Lock-free enqueue implementation.

cally defending against interferences on every object call by acquiring a lock will lead to wasted overhead most of time. In an optimistic scheme, objects are accessed in a manner that does not preclude interferences due to concurrent accesses. If an operation on an object *is* interfered with before it is completed, then it has no effect on the object. Any operation that is interfered with must be retried in order to complete. Optimistic schemes perform well when retries are rare, which is precisely the situation in quantum-based systems.

In this paper, we show that it is possible to significantly optimize retry-based shared-object algorithms by directly exploiting the relative infrequency of preemptions in quantum-based systems. The specific assumption we make throughout this paper regarding preemptions is as follows.

Preemption Axiom: *The quantum is large enough to ensure that each task can be preempted at most once across two consecutive object calls.* □

Given the Preemption Axiom, each object call can be retried at most once, i.e., there is a bound on overall object-sharing costs. The Preemption Axiom is quite liberal: not only are object calls of short to medium duration allowed (the case we most expect and optimize for), but also calls that are quite long, approaching the length of an entire quantum.

Our work has been heavily influenced by recent research by us and others on using lock-free and wait-free shared-object algorithms in real-time systems [2, 3, 4, 5, 6, 15, 17, 22]. Operations on lock-free objects are optimistically performed using a user-level retry loop. Such an operation is atomically validated and committed by invoking a synchronization primitive such as *compare-and-swap* (CAS). Figure 1 depicts a lock-free enqueue operation that is implemented in this way. An item is enqueued in this implementation by using a two-word compare-and-swap (CAS2) instruction¹ to atomically update a tail pointer and either the “next” pointer of the last item in the queue or a head pointer, depending on whether the queue is empty. This loop is executed repeatedly until the CAS2 instruction succeeds. As with any optimistic synchronization scheme, concurrent operations may interfere with each other. This happens when a successful CAS2 by one task results in failed CAS2 by another task. Wait-free shared objects are required to satisfy an extreme form of lock-freedom that precludes all waiting dependencies among tasks, including potentially unbounded operation retries.

¹The first two parameters of CAS2 specify addresses of two shared variables, the next two parameters are values to which these variables are compared, and the last two parameters are new values to assign to the variables if both comparisons succeed.

Major Contributions. In the first part of the paper, we consider the problem of implementing shared objects in quantum-based uniprocessor systems. Our approach is to develop lock-free algorithms that are optimized in accordance with the Preemption Axiom. The Preemption Axiom ensures that each lock-free operation is retried at most once. Thus, if an operation is interfered with due to a preemption, then the retry code can be purely sequential code in which shared data is read and written without using synchronization primitives. In short, the Preemption Axiom automatically converts a lock-free implementation into a wait-free one. In addition to discussing algorithmic techniques for implementing objects, we also show how to account for object-sharing costs in scheduling analysis. In previous work, Anderson and Ramamurthy showed that when using lock-free shared objects under RM or EDF scheduling, retry costs can be bounded by solving a linear programming problem [3]. We show that a slightly different linear programming must be solved to bound retries when the proposed object implementations are used in a quantum-based uniprocessor system. We also show that, when analyzing such a system, the techniques we present result in better retry-cost estimates and a much faster schedulability test than when using the results of [3]. In addition to RM and EDF scheduling, we also consider proportional-share (PS) scheduling. Under PS scheduling, lag-bound calculations are an important concern. We show how object-sharing overheads affect such calculations when using either our algorithms or lock-based schemes.

In the second part of the paper, we consider the problem of implementing shared objects in quantum-based multiprocessor systems. In a multiprocessor, a retry mechanism by itself clearly is not sufficient, because a task on one processor may be repeatedly interfered with due to object invocations by tasks on other processors. Our approach is to use a retry mechanism in conjunction with a preemptable queue lock. A *queue lock* is a spin lock in which waiting tasks form a queue [19]. In our approach, a task performs an operation on an object by first acquiring a lock; if a task is preempted before its operation is completed, then its operation is retried.

With any (non-preemption-safe) locking algorithm, if a task holding a lock is preempted, then no task waiting for that lock can make progress. In a queue lock, preemptions are even more costly, because if a task waiting in the queue is preempted, then tasks waiting behind it cannot make progress. To overcome such problems, several researchers have proposed queue lock algorithms that use kernel support to ensure that preemptions do not adversely impact performance [25, 26]. Unfortunately, many of these previous algorithms are based on a kernel interface that is provided only on very few machines. Most previous algorithms that do not rely on such an interface are quite complicated. We show that for systems satisfying the Preemption Axiom, the job of designing a preemptable queue lock becomes much easier. The algorithm we present is very simple, consisting of only 17 lines of code. Our lock is designed to ensure that all spins are on locally-cached variables when used in a system with coherent caches. We present results from performance experiments that show that our lock is up to 25% faster than a preemptable queue lock presented by Takada and Sakamura at last year’s RTSS when applied in quantum-based systems.

The rest of this paper is organized as follows. In Section 2, we present our results for uniprocessor systems. Then, in Section 3, we consider multiprocessor systems. We end with concluding remarks in Section 4.

```

procedure RMW(Addr: pointer to valtype; f: function) returns valtype
private variable old, new: valtype
1:   old := *Addr;
2:   new := f(old);
3:   if CAS(Addr, old, new) = false then
4:     old := *Addr; /* statements 4 and 5 execute without preemption */
5:     *Addr := f(old)
   fi;
6:   return old

```

Figure 2: Uniprocessor read-modify-write implementation.

2 Uniprocessor Systems

In this section, we consider the implementation of shared objects in quantum-based uniprocessor systems. We first present algorithms for implementing several useful primitives and objects in Section 2.1. Then, in Section 2.2, we show how to account for object-sharing costs arising from these implementations in scheduling analysis.

2.1 Implementing Objects

As mentioned previously, the Preemption Axiom can be exploited to convert a lock-free object implementation into a wait-free one. In particular, the Preemption Axiom ensures that each lock-free operation is retried at most once. Thus, if an operation is interfered with due to a preemption, then the retry code can be purely sequential code in which shared data is read and written without using synchronization primitives.

Implementing read-modify-writes. As a first example of an implementation that is optimized in this way, consider Figure 2. This figure shows how to implement read-modify-write (RMW) operations using *CAS*. A RMW operation on a variable X is characterized by specifying a function f . Informally, such an operation has the effect of the following atomic code fragment: $\langle x := X; X := f(x); \mathbf{return} \ x \rangle$. Example RMW operations include fetch-and-increment, fetch-and-store, and test-and-set.

The implementation in Figure 2 is quite simple. If the *CAS* at line 3 succeeds, then the RMW operation atomically takes effect when the *CAS* is performed. If the *CAS* fails, then the invoking task must have been preempted between lines 1 and 3. In this case, the Preemption Axiom implies that lines 4 and 5 execute without preemption. Given this implementation, we can conclude that, in any quantum-based uniprocessor system that provides *CAS*, any object accessed only by means of reads, writes, and read-modify-writes can be implemented in constant time. It should be noted that virtually every modern processor (including the ubiquitous Pentium) either provides *CAS* or instructions that can be used to easily implement *CAS*.

Conditional compare-and-swap. Using similar principles, it is possible to efficiently implement *conditional compare-and-swap* (CCAS), which is a very useful primitive when implementing lock-free and wait-free objects. CCAS has the following semantics.

```

type wdtype = record val: valtype; task: 0..N end           /* all fields are stored in one word ... */
                                     /* ... task indices range over 1..N; the task field should be 0 initially */

procedure CCAS(V: pointer to vertype; ver: vertype;
                W: pointer to wdtype; old, new: wdtype; p: 1..N) returns boolean
private variable w: wdtype           /* p, the index of the invoking task, is an input parameter */

1:  w := *W;
2:  if w.val ≠ old.val then return false fi;
3:  if *V ≠ ver then return false fi;
4:  if CAS(W, w, (old.val, p)) then
5:    if *V ≠ ver then
6:      w := *W;                               /* lines 6-8 execute without preemption */
7:      *W := (w.val, 0);
8:      return false
    fi;
9:  if CAS(W, (old.val, p), (new.val, 0)) then return true fi
    fi;
10: if W→val ≠ old.val then return false fi;           /* lines 10-13 execute without preemption */
11: if *V ≠ ver then return false fi;
12: *W := (new.val, 0);
13: return true

procedure Read(W: pointer to wdtype) returns wdtype
private variable w: wdtype

14: w := *W;
15: if w.task = 0 then return w.val
    else
16:   CAS(W, w, (w.val, 0));                     /* lines 16-19 will almost never be executed */
17:   w := *W;
18:   CAS(W, w, (w.val, 0));
19:   return w.val
    fi

```

Figure 3: CCAS implementation. Code for reading a word accessed by CCAS is also shown.

```

procedure CCAS(V: pointer to vertype; ver: vertype; W: pointer to wdtype; old, new: wdtype) returns boolean
  ⟨ if *V ≠ ver then return false fi;
    if *W ≠ old then return false fi;
    *W := new;
    return true ⟩

```

The angle brackets above indicate that **CCAS** is atomic. As its definition shows, **CCAS** is a restriction of **CAS2** in which one word is a compare-only value. Lock-free and wait-free objects can be implemented by using a “version number” that is incremented by each object call [2, 13]. **CCAS** is useful because the version number can be used to ensure that a “late” **CCAS** operation performed by a task after having been preempted has no effect.

Figure 3 shows how to implement **CCAS** using **CAS** on a quantum-based uniprocessor. The implementation works by packing a task index into the words being accessed. The task index field is used to detect preemptions. It is clearly in accordance with the semantics of **CCAS** for a task T_i to return from line 2 or 3. To see that the rest of the algorithm is correct, observe that a task T_i can find $*V \neq ver$ at line 5 only if it was preempted

between lines 3 and 5. Similarly, the **CAS** operations at lines 4 and 9 can fail only if a preemption occurs. By the Preemption Axiom, this implies that lines 6-8 and 10-13 execute without preemption. It is thus easy to see that these lines are correct. The remaining possibility is that a task T_i returns from line 9. This line is reached only if the **CAS** operations performed by T_i at lines 4 and 9 both succeed. The first of these **CAS** operations only updates the task index field of W ; the second updates the value field. We claim that T_i 's **CAS** at line 9 is successful only if no task performs a **Read** operation on word W or assigns W within its **CCAS** procedure between the execution of lines 4 and 9 by T_i — note that this property implies that T_i 's **CCAS** can be linearized to its execution of line 5. To see that this property holds, observe that if some other task updates W in its **CCAS** procedure, then $W \rightarrow \text{task} \neq i$ is established, implying that T_i 's **CAS** at line 9 fails. Also, if some task T_j performs a **Read** operation on W when $W \rightarrow \text{task} = i$ holds, then it must establish $W \rightarrow \text{task} = 0$, causing T_i 's **CAS** at line 9 to fail. To see this, note that, by the Preemption Axiom, T_j 's execution of the **Read** procedure itself can be preempted at most once. By inspecting the code of this procedure, it can be seen that this implies that T_j must establish $W \rightarrow \text{task} = 0$ during the same quantum as when it reads the value of W .

It is important to stress that our objective here is to design object implementations that perform very well in the absence of preemptions and that are still correct when preemptions do occur. If the code in Figure 3 is never preempted when executed by any task, then lines 6-8, 10-13, and 16-19 are never executed. Thus, in the expected case, this object implementation should perform well.

Multi-word compare-and-swap. The last object implementation we consider in this subsection, that of a multi-word **CAS** (**MWCAS**) object, is shown in Figure 4. The semantics of **MWCAS** generalizes that of **CAS2** used in Figure 1. **MWCAS** is a useful primitive for two reasons. First, it simplifies the implementation of many lock-free objects; queues, for instance, are easy to implement with **MWCAS**, but harder to implement with single-word primitives (see Figure 1). Second, it can be used to implement multi-object operations. For example, an operation that dequeues an item off of one queue and enqueues it onto another could be implemented by using **MWCAS** to update both queues. The idea of using **MWCAS** to atomically access many objects can be generalized to implement arbitrary lock-free transactions on memory-resident data. Such an implementation was presented recently by Anderson, Ramamurthy, Moir, and Jeffay [6].

Our **MWCAS** implementation uses a rollback mechanisms. Before beginning a **MWCAS** operation, a task T_i first checks to see if there exists a partially-completed operation that was preempted (line 2). If such an operation exists, T_i marks it as having failed (line 3). This is done by updating the shared variable V , which contains a version counter as well as status information concerning any pending operation. T_i then rolls back the operation it has preempted by restoring all of the words already updated by that operation with their original values (lines 5-9). The arrays *Addr* and *Old* are consulted to determine which words to update and the values to use. If T_i is preempted while performing any of these steps, then it invokes the routine $NP()$. This routine is called only after a preemption is detected, and thus by the Preemption Axiom, it always executes without preemption. In $NP()$, a task performs steps that are similar to those performed in the **MWCAS** procedure. However, since these

```

type wdlist = array[1..B] of wdtype;                               /* list of old and new values for MWCAS */
addrlist = array[1..B] of pointer to wdtype;                   /* addresses to perform MWCAS on */
partype = record numwds: 1..B; addr: addrlist; old: wdlist end; /* parameter information */
vertype = record cnt: 0..C; task: 1..N; status: 0..2 end /* version number, current task, status ... */
/* ... these fields are packed in one word; status is 0 initially, 1 if preempted, 2 if done */

shared variable
V: vertype initially (0, 1, 2);
Numwds: array[1..N] of 1..B;
Addr: array[1..N, 1..B] of pointer to wdtype;
Old: array[1..N, 1..B] of wdtype

procedure MWCAS(numwds: 1..B; addr: addrlist; old, new: wdlist;
                p: 1..N) returns boolean
1: v := V;
2: if v.status ≠ 2 then
3:   if ¬CAS(&V, v, (v.cnt, v.task, 1)) then return(NP()) fi;
4:   n, v.status := Numwds[v.task], 1;
5:   for k := 1 to n do
6:     addr := Addr[v.task, k];
7:     old := Old[v.task, k];
8:     new := *addr;
9:     if ¬CCAS(&V, v, addr, new, old) then return(NP()) fi
   od
   fi;
10: for k := 1 to numwds do
11:   if *addr[k] ≠ old[k] then
12:     if V = v then return false else return(NP()) fi
   fi;
13:   Addr[p, k] := addr[k];
14:   Old[p, k] := old[k]
   od;
15: Numwds[p] := numwds;
16: v := (v.cnt + 1 mod C, p, 0);
17: if ¬CAS(&V, v, v) then return(NP()) fi;
18: for k := 1 to numwds do
19:   if ¬CCAS(&V, v, addr[k], old[k], new[k]) then return(NP()) fi
   od;
20: if ¬CAS(&V, v, (v.cnt, p, 2)) then return(NP()) fi;
21: return true

procedure NP() returns boolean
/* executes without preemption */
22: v := V;
23: if v.status ≠ 2 then
24:   V := (v.cnt, v.task, 1);
25:   n := Numwds[v.task];
26:   for k := 1 to n do
27:     old := Old[v.task, k];
28:     *Addr[v.task, k] := old
   od
   fi;
29: for k := 1 to numwds do
30:   if *addr[k] ≠ old[k] then return false fi
   od;
31: for k := 1 to numwds do
32:   *addr[k] := new[k]
   od;
33: V := (v.cnt + 1 mod C, p, 2);
34: return true

```

Figure 4: MWCAS implementation. Private variable declarations are omitted for brevity. MWCAS is usually used in conjunction with a Read operation that returns the current value of a word accessed by MWCAS. In most applications, Read can be implemented by means of a simple read, because words that are read are subsequently accessed by MWCAS, which ensures proper synchronization.

steps are performed in the absence of preemptions, the code is much simpler. After having rolled back any preempted operation, T_i checks to see if each word it wants to update has the desired old value (lines 10-14). If no mismatch is detected, the appropriate words are updated (lines 18-19).

If the number of words accessed is fixed (e.g., CAS2 is to be implemented), then the MWCAS procedure in Figure 4 can be simplified considerably. Also, it should be remembered that our standing assumption is that preemptions are relatively rare. Most of the code in Figure 4 is never executed in the absence of preemptions. All of the implementations presented in this subsection can be further simplified if tasks have the ability to

disable interrupts (which is not always the case). In this case, interrupts should be disabled only when executing short code fragments, or significant blocking terms and high interrupt latencies may result.

We have not attempted here to give an exhaustive list of algorithmic techniques that can be used, but rather have focused on a few example implementations that illustrate the power of the Preemption Axiom. Indeed, the development of algorithmic techniques that can be generally applied is an important topic for further research.

2.2 Scheduling Analysis

We now turn our attention to the issue of accounting for object-sharing costs in scheduling analysis when object implementations like those proposed in the previous subsection are used. We consider scheduling analysis under the rate-monotonic (RM), earliest-deadline-first (EDF), and proportional-share (PS) scheduling schemes.

RM and EDF scheduling. We begin by considering the RM and EDF schemes. In both of these schemes, a periodic task model is assumed. We call each task invocation a *job*. For brevity, we limit our attention to systems in which each task’s relative deadline equals its period (extending our results to deal with systems in which a task’s relative deadline may be less than its period is fairly straightforward). In our analysis, we assume that each job is composed of distinct nonoverlapping computational fragments or *phases*. Each phase is either a *computation phase* or an *object-access phase*. Shared objects are not accessed during a computation phase. An object-access phase consists of exactly one retry loop. We assume that tasks are indexed such that, if a job of task T_i can preempt a job of task T_j , then $i < j$ (such an indexing is possible under both RM and EDF scheduling). The following is a list of symbols that will be used in deriving our scheduling conditions.

- N - The number of tasks in the system. We use i, j , and l as task indices; each is universally quantified over $\{1, \dots, N\}$.
- Q - The length of the scheduling quantum.
- p_i - The period of task T_i .
- w_i - The number of phases in a job of task T_i . The phases are numbered from 1 to w_i . We use u and v to denote phases.
- x_i - The number of object-access phases in a job of task T_i .
- c_i^v - The worst-case computational cost of the v^{th} phase of task T_i , where $1 \leq v \leq w_i$, assuming no contention for the processor or shared objects. We denote total cost over all phases by $c_i = \sum_{v=1}^{w_i} c_i^v$.
- r_i^v - The cost of a retry if the v^{th} phase of task T_i is interfered with. For computation phases, $r_i^v = 0$. For object-access phases, we usually have $r_i^v < c_i^v$, because retries are performed sequentially. We let $r_i = \max_{i,v}(r_i^v)$.
- $m_i^v(j, t)$ - The worst-case number of interferences in T_i ’s v^{th} phase due to T_j in an interval of length t .

- f_i^v - An upper bound on the number of interferences of the retry loop in the v^{th} phase of T_i during a single execution of that phase.

A simple bound on interference costs. The simplest way to account for object interference costs is to simply inflate each task T_i 's computation time to account for such costs. This can be done by solving the following recurrence.

$$c'_i = c_i + \min[x_i, (\lceil \frac{c'_i}{Q} \rceil - 1)] \cdot r_i \quad (1)$$

c'_i is obtained here by inflating c_i by r_i for each quantum boundary that is crossed, up to a maximum of x_i such boundaries (since T_i accesses at most x_i objects in total). If task T_i accesses objects with widely varying retry costs, then the above recurrence may be too pessimistic. Let $r_{i,1}$ be the maximum retry cost of any of T_i 's object-access phases, let $r_{i,2}$ be the next-highest cost, and so on. Also, let $v_i = \min[x_i, (\lceil c'_i/Q \rceil - 1)]$. Then, we can more accurately inflate c_i by solving the following recurrence.

$$c'_i = c_i + \sum_{k=1}^{v_i} r_{i,k} \quad (2)$$

Once such c'_i values have been calculated, they can be used within scheduling conditions that apply to independent tasks. A condition for the RM scheme is given in the following theorem.

Theorem 1: *In an RM-scheduled quantum-based uniprocessor system, a set of tasks with objects implemented using the proposed retry algorithms is schedulable if the following holds for every task T_i .*

$$(\exists t : 0 < t \leq p_i :: \min(Q, \max_{j>i}(c'_j)) + \sum_{j=1}^i \lceil \frac{t}{p_j} \rceil c'_j \leq t) \quad \square$$

In the above expression, $\min(Q, \max_{j>i}(c'_j))$ is a blocking term that arises due to the use of quantum-based scheduling [16].² The next theorem gives a scheduling condition for the EDF scheme.

Theorem 2: *In an EDF-scheduled quantum-based uniprocessor system, a set of tasks with objects implemented using the proposed retry algorithms is schedulable if the following holds.*

$$\sum_{i=1}^N \frac{c'_i}{p_i} \leq 1 \wedge (\forall i : 1 \leq i \leq N :: (\forall t : p_1 < t < p_i :: \min(Q, c'_i) + \sum_{j=1}^{i-1} \lceil \frac{t-1}{p_j} \rceil c'_j \leq t)) \quad \square$$

The above condition is obtained by adapting the condition given by Jeffay et al. in [14] for nonpreemptive EDF scheduling. Note that this condition reduces to that of Jeffay et al. when $Q = \infty$ and to that for preemptive EDF scheduling [18] when $Q = 0$.

²In [16], it is assumed that timer interrupts are spaced apart by a constant amount of time. If a task completes execution between these interrupts, then the processor is allocated to the next ready task, if such a task exist. This newly-selected task will execute for a length of time that is less than a quantum before possibly being preempted. In our work, we assume that whenever the processor is allocated to a task, that task executes for an entire quantum (or until it terminates) before possibly being preempted. Nonetheless, the blocking calculations due to quantum-based scheduling are the same in both models.

Bounding interference costs using linear programming. Anderson and Ramamurthy showed that when lock-free objects are used in a uniprocessor system, object interference costs due to preemptions can be more accurately bounded using linear programming [3]. Given the Preemption Axiom, we show that it is possible to obtain bounds that are tighter than those of Anderson and Ramamurthy.

Our linear programming conditions make use of a bit of additional notation. If a job of T_j interferes with the v^{th} phase of a job of T_i , then an additional demand is placed on the processor, because another execution of the retry-loop iteration in T_i 's v^{th} phase is required. We denote this additional demand by $s_i^v(j)$. Formally, $s_i^v(j)$ is defined as follows.

Definition 2.1: Let T_i and T_j be two distinct tasks, where T_i has at least v phases. Let z_j denote the set of objects modified by T_j , and a_i^v denote the set of objects accessed in the v^{th} phase of T_i . Then,

$$s_i^v(j) = \begin{cases} r_i^v & \text{if } j < i \wedge a_i^v \cap z_j \neq \emptyset \\ 0 & \text{otherwise.} \end{cases} \quad \square$$

Give the above definition of $s_i^v(j)$, we can state an *exact* expression for the worst-case interference cost in tasks T_1 through T_i in any interval of length t .

Definition 2.2: The total cost of interferences in jobs of tasks T_1 through T_i in any interval of length t , denoted $E_i(t)$, is defined as follows: $E_i(t) \equiv \sum_{j=1}^i \sum_{v=1}^{w_j} \sum_{l=1}^{j-1} m_j^v(l, t) s_j^v(l)$. □

The term $m_j^v(l, t)$ in the above expression denotes the worst-case number of interferences caused in T_j 's v^{th} phase by jobs of T_l in an interval of length t . The term $s_j^v(l)$ represents the amount of additional demand required if T_l interferes once with T_j 's v^{th} phase. The expression within the leftmost summation denotes the total cost of interferences in a task T_j over all phases of all jobs of T_j in an interval of length t .

Expression $E_i(t)$ accurately reflects the worst-case additional demand placed on the processor in an interval \mathcal{I} of length t due to interferences in tasks T_1 through T_i . Of course, to evaluate this expression, we first must determine values for the $m_j^v(l, t)$ terms. Unfortunately, in order to do so, we potentially have to examine an exponential number of possible task interleavings in the interval \mathcal{I} . Instead of exactly computing $E_i(t)$, our approach is to obtain a bound on $E_i(t)$ that is as tight as possible. We do this by viewing $E_i(t)$ as an expression to be maximized. The $m_j^v(l, t)$ terms are the “variables” in this expression. These variables are subject to certain constraints. We obtain a bound for $E_i(t)$ by using linear programming to determine a maximum value of $E_i(t)$ subject to these constraints. We now explain how appropriate constraints on the $m_j^v(l, t)$ variables are obtained. In this explanation, we focus on the RM scheme. Defining similar constraints for the EDF scheme is fairly straightforward.

We impose six sets of constraints on the $m_i^v(j, t)$ variables.

Constraint Set 1: $(\forall i, j : j < i :: \sum_{v=1}^{w_i} m_i^v(j, t) \leq \left\lceil \frac{t+1}{p_j} \right\rceil)$. □

Constraint Set 2: $(\forall i :: \sum_{j=1}^i \sum_{v=1}^{w_j} \sum_{l=1}^{j-1} m_j^v(l, t) \leq \sum_{j=1}^{i-1} \left\lceil \frac{t+1}{p_j} \right\rceil)$. □

Constraint Set 3: $(\forall i, v :: \sum_{j=1}^{i-1} m_i^v(j, t) \leq \left\lceil \frac{t+1}{p_i} \right\rceil f_i^v)$. □

Constraint Set 4: $(\forall i, v :: f_i^v \leq 1)$. □

Constraint Set 5: $(\forall i :: \sum_{j=1}^{i-1} \sum_{v=1}^{w_j} m_i^v(j, t) \leq \left(\left\lceil \frac{c'_i}{Q} \right\rceil - 1 \right) \cdot \left\lceil \frac{t+1}{p_i} \right\rceil)$. □

Constraint Set 6: $(\forall i :: \sum_{j=1}^{i-1} \sum_{v=1}^{w_j} m_i^v(j, t) \leq x_i \cdot \left\lceil \frac{t+1}{p_i} \right\rceil)$. □

There first three constraint sets were given previously by Anderson and Ramamurthy [3]. The first set of constraints follows because the number of interferences in jobs of T_i due to T_j in an interval \mathcal{I} of length t is bounded by the maximum number of jobs of T_j that can be released in \mathcal{I} . The second set of constraints follows from a result presented in [5], which states that the total number of interferences in all jobs of tasks T_1 through T_i in an interval \mathcal{I} of length t is bounded by the maximum number of jobs of tasks T_1 through T_{i-1} released in \mathcal{I} . In the third set of constraints, the term f_i^v is an upper bound on the number of interferences of the retry loop in the v^{th} phase of T_i during a single execution of that phase. The reasoning behind this set of constraints is as follows. If at most f_i^v interferences can occur in the v^{th} phase of a job of T_i , and if there are n jobs of T_i released in an interval \mathcal{I} , then at most $n f_i^v$ interferences can occur in the v^{th} phase of T_i in \mathcal{I} . In Anderson and Ramamurthy's paper, the f_i^v terms are calculated by solving an additional set of linear programming problems. In our case, they can be bounded as shown in the fourth set of constraints.³ This is because, by the Preemption Axiom, each object access can be interfered with at most once. The fifth and six set of constraints arise for precisely the same reasons as given when recurrence (1) was explained. The c'_i term in the fifth constraint set can be calculated by solving recurrence (1) or (2).

We are now in a position to state scheduling conditions for the RM and EDF schemes. Recall that $E_i(t)$ is the actual worst-case cost of interferences in jobs of tasks T_1 through T_i in any interval of length t . We let $E'_i(t)$ denote a bound on $E_i(t)$ that is determined using linear programming as described above. A scheduling condition for the RM scheme is as follows.

Theorem 3: *In an RM-scheduled quantum-based uniprocessor system, a set of tasks with objects implemented using the proposed retry algorithms is schedulable if the following holds for every task T_i .*

$$(\exists t : 0 < t \leq p_i :: \min(Q, \max_{j>i}(c'_j)) + \sum_{j=1}^i \left\lceil \frac{t}{p_j} \right\rceil c_j + E'_i(t-1) \leq t) \quad \square$$

This condition is obtained by modifying one proved in [3] by including a blocking factor for the scheduling quantum. For EDF scheduling, we have the following.

Theorem 4: *In an EDF-scheduled quantum-based uniprocessor system, a set of tasks with objects implemented using the proposed retry algorithms is schedulable if the following holds.*

$$(\forall t :: \sum_{j=1}^N \left\lceil \frac{t}{p_j} \right\rceil c_j + E'_N(t-1) \leq t) \quad \square$$

³It is actually possible to eliminate Constraint Set 4, because the linear programming solver will always maximize each f_i^v term to be 1. Furthermore, when substituting 1 for f_i^v in Constraint Set 3, the resulting set of constraints implies those given in Constraint Set 6, so these constraints can be removed as well. We did not minimize the constraint sets in this way because we felt that this would make them more difficult to understand, especially when comparing them against those in [3].

This condition was also proved in [3]. Since t is checked beginning at time 0, a blocking factor is not required. As stated, the expression in Theorem 4 cannot be verified because the value of t is unbounded. However, there is an implicit bound on t . In particular, we only need to consider values less than or equal to the least common multiple of the task periods. (If an upper bound on the utilization available for the tasks is known, then we can restrict t to a much smaller range [10].)

Note that, in a quantum-based system, no object access by a task that is guaranteed to complete within the first quantum allocated to a job of that task can be interfered with. Thus, such an access can be performed using a less-costly code fragment that is purely sequential. All of the scheduling conditions presented in this subsection can be improved by accounting for this fact.

Experimental Comparison. In order to compare the retry-cost estimates produced by the linear programming methods proposed in this paper and in [3], we conducted a series of simulation experiments involving randomly-generated task sets scheduled under the RM scheme. Each task set in these experiments was defined to consist of ten tasks that access up to ten shared objects. 120 task sets were generated in total, and for each task set, a retry cost was computed for each task using the two methods being compared. The methodology we used in generating task sets is as follows. First, we defined access costs for each of the ten shared objects. Three objects were defined to have access times of 7-8 time units, five to have access times of 57-96 time units, and two to have access times of 134-180 time units. These values were chosen based upon the object-access times reported by Ramamurthy [21]. Each task was assigned a computation cost of between one and three quanta, with a quantum being 1000 time units. The number of quanta required by a task was selected at random, with 40% of the generated tasks taking one quantum, 40% taking two, and 20% taking three. Each quantum in a task’s computation was defined to include two object calls. The object to call was selected from the set of ten predetermined objects at random. Task periods were initially selected at random with a range of 6,000 to 50,000 time units. The periods were then scaled up until the task set was deemed to be schedulable by applying a non-linear-programming-based scheduling condition for tasks using lock-free objects reported in [5]. This condition provides a less accurate schedulability check than either of the two methods being compared. As a result, it was known before submitting a task set to either method that it was indeed schedulable.

The results of these experiments are depicted in Figure 5. This figure shows the average retry cost of each task over all generated task sets as computed by each method. As before, tasks are indexed in order of increasing periods. Thus, T_1 has highest priority in all experiments, and as a result, its retry cost is estimated to be zero under both methods. Retry-cost estimates increase as the priority-level decreases. It can be seen in Figure 5 that both methods yield similar retry costs for lower-priority tasks. However, the method of this paper yields retry-cost estimates for higher-priority tasks that are about 10% to 20% lower than those produced by the method of [3]. In addition to determining retry-cost estimates, we also kept track of how long each schedulability check took to complete. On average, the schedulability check proposed in this paper took 11.7 seconds per task set, while the one proposed in [3] took 235 seconds. This is because of the complicated procedure invoked to compute

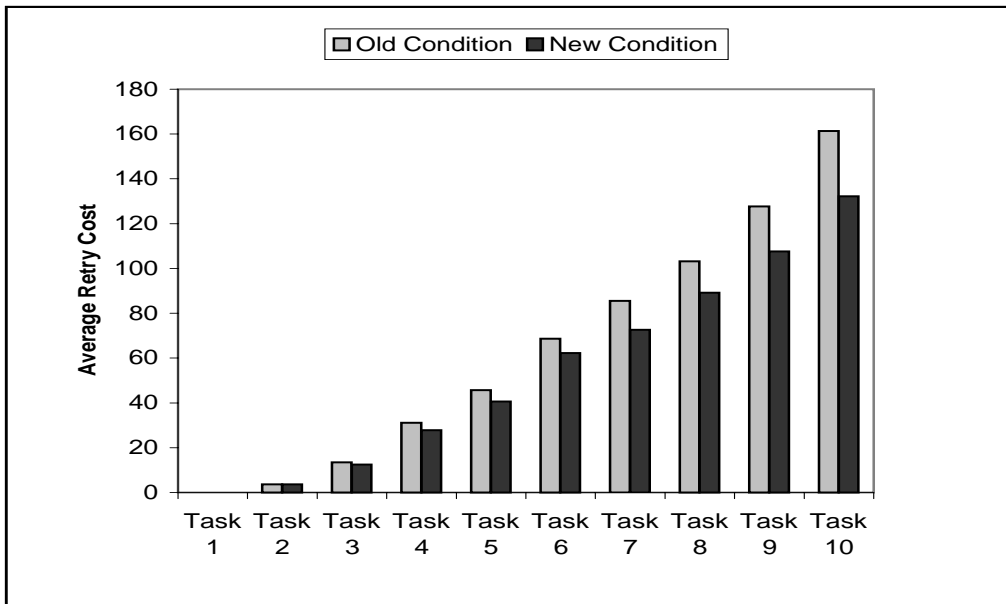


Figure 5: Comparison of linear programming scheduling conditions. Each task’s average estimated retry cost is shown.

f_i^v values in the method of [3]. Our method renders this procedure unnecessary by exploiting characteristics of quantum-based systems.

Proportional-share scheduling. In the PS scheduling literature, the term “client” is used to refer to a schedulable entity. In a PS system, clients may join and leave the system arbitrarily. Under PS scheduling, each client is assigned a *share* of the processor, which represents the fraction of processing time that that client should receive. Quanta are allocated in a manner that ensures that the amount of processor time each client receives is commensurate with its share.

In PS systems, the primary measure of performance is the *lag* between the time a client should have received in an ideal system with a quantum approaching zero, and the time it actually receives in a real system. Stoica et al. showed that optimal lag bounds can be achieved by using *earliest-eligible-virtual-deadline-first* (EEVDF) scheduling [24]. Due to space limitations, give here only a very brief overview of the EEVDF scheme — the interested reader is referred to [24] for details. The EEVDF algorithm makes scheduling decisions in the virtual-time domain, where virtual times are defined by considering an ideal system. Informally, the ideal PS system executes client k for w_k time units during each virtual-time unit, where w_k is its weight. The EEVDF algorithm associates a deadline in the virtual time domain with each client request. A new quantum is always allocated to the client that has the eligible request with the earliest virtual deadline.

Stoica et al. derived lag bounds for the EEVDF algorithm for both *steady systems* and *pseudo-steady systems*. In a steady system, the lag of any client joining or leaving the system is zero. In a pseudo-steady system, the lag of any client joining the system is zero, but the lag of any client leaving the system can be positive. In this paper, we consider only steady systems. Stoica et al. established the following lag bounds for steady systems.

Theorem 5: *Let R be the size of the current request issued by client k in a steady EEVDF-scheduled system. Then, the lag of client k at any time t while its request is pending is bounded by $-R < lag_k(t) < \max(Q, R)$. \square*

Thus, the deviation in the processor time a client receives in EEVDF scheduling is bounded by the size of scheduling quantum and the size of the client’s request. Theorem 5 implies there are both system and application tradeoffs between accuracy and system overhead: a shorter request or quantum results in better allocation accuracy, but higher scheduling overhead. When our object-sharing algorithms are used, the lag bound becomes as follows.

Theorem 6: *Let R be the size of current request issued by client k in a steady EEVDF-scheduled system. Further, assume that client k accesses at most n shared objects, each with cost bounded by s . Then, the lag of the client k at any time while its request is pending is bounded by $-R < lag < \max(Q, R + \min(n, \lceil \frac{R}{Q} \rceil - 1) \cdot s)$. \square*

Intuitively, an additional source of lag error is introduced as a result of object sharing. This error term is upper bounded by $\min(n, \lceil \frac{R}{Q} \rceil - 1) \cdot s$. In particular, client k can be preempted at most once during any object access, and there can be at most $\min(n, \lceil \frac{R}{Q} \rceil - 1)$ such preemptions. This condition is pessimistic because it assumes all object accesses to be of the same cost. It can be refined by considering the actual costs of the $\min(n, \lceil \frac{R}{Q} \rceil - 1)$ most expensive object accesses made by client k . Observe that, for the special case when $R < Q$, the bounds on lag are the same as given by Theorem 5. Moreover, an application can always choose to make $R < Q$ by breaking its request into a sequence of smaller requests, in which case each object call fits within a quantum. However, as mentioned above, this comes at the cost of increased scheduling overhead.

To ensure the real-timeliness of clients, the completion times of client requests must be bounded. Stoica et al. established the following bound on completion times in steady systems.

Theorem 7: *Let d be the deadline of the current request issued by client k in a steady EEVDF-scheduled system, and let f be the actual time when this request is fulfilled. Then, the request of the client k is fulfilled no later than time $d + Q$, i.e., $f \leq d + Q$. \square*

The “lateness” of a client is unaffected by object sharing if the size of its request is less than the size of the scheduling quantum, i.e., if $R \leq Q$. Thus, for this special case, there is no penalty to be paid for object sharing. For the case where $R > Q$, retry costs inflate the request time to $R + (\min(n, \lceil \frac{R}{Q} \rceil - 1) \cdot s)$. The client’s deadline is postponed correspondingly; in particular, d becomes $d + (\min(n, \lceil \frac{R}{Q} \rceil - 1) \cdot s) \cdot k_t$, where k_t is a constant that relates the passage of virtual time to real time.

Alternatives to our approach include using non-uniform quanta, so that object accesses are nonpreemptive [9], and using lock-based implementations, with ceiling- or inheritance-like schemes [23] to bound blocking times.

In this paper, we have strictly limited attention to systems with a uniform quantum. We hope to investigate systems with non-uniform quanta in future work. In PS systems, a ceiling-like scheme seems problematic, due to the fact that clients may join and leave the system arbitrarily. This complicates the job of maintaining ceiling bookkeeping information regarding which tasks access which objects that is embedded within the kernel. An inheritance-like scheme would not require such bookkeeping information, and thus may be easier to implement in a PS system. A lag bound for this case is given by $-R < lag < max(Q, R + n \cdot s)$ for a client that accesses n objects with a worst-case cost of s per object. This is because a blocking term may be experienced for each object access. In comparing these bounds to those stated in Theorem 6, it can be seen that the object-sharing algorithms we propose should give rise to a smaller lag error if it is the case that most object calls fit within a quantum. Similar object-sharing overhead terms apply to deadline calculations.

3 Multiprocessor Systems

With the recent advent of multiprocessor workstations, the problem of implementing real-time applications on multiprocessors is of growing importance. In this section, we describe a new approach to implementing shared objects in quantum-based multiprocessor systems. This approach is based on a retry mechanism that is designed in such a way that scheduling analysis can be performed on each processor using the uniprocessor scheduling conditions considered in the previous section. In Section 3.1, we describe this retry mechanism in detail. In Section 3.2, we present results from experiments conducted to evaluate our approach.

3.1 Implementing Objects

In a multiprocessor system, a retry mechanism by itself is not sufficient, because a task on one processor may be repeatedly interfered with due to object invocations performed by tasks on other processors. Our approach is to use a retry mechanism in conjunction with a preemptable queue lock. A *queue lock* is a spin lock in which waiting tasks form a queue [19]. Queue locks are useful in real-time systems because waiting times can be bounded. With a preemptable queue lock, a task waiting for or holding a lock can be preempted without impeding the progress of other tasks waiting for the lock. Given such a locking mechanism, any preempted operation can be safely retried. As before, we can appeal to the Preemption Axiom to bound retries, because retries are caused only by preemptions, not by interferences across processors. The Preemption Axiom is still reasonable to assume if we focus on systems with a small to moderate number of processors (the cost an operation depends on the spin queue length, which in turn depends on the number of processors in the system). We believe that it is unlikely that a real-time application would be implemented on a large multiprocessor, and even if it were, it is probably unlikely that one object would be shared across a large number of processors.

Queue locks come in two flavors: array-based locks, which use an array of spin locations [7, 12], and list-based locks, in which spinning tasks form a linked list [19]. List-based queue locks have the advantage of requiring only constant space overhead per task per lock. In addition, list-based queue locks exist in which all spins are

local if applied on multiprocessors either with coherent caches or distributed shared memory [19]. In contrast, with existing array-based locks, spins are local only if applied in a system with coherent caches.

All work known to us on preemptable queue locks involves list-based locks [25, 26]. This is probably due to the advantages listed in the previous paragraph that (nonpreemptable) list-based locks have over array-based ones. However, correctly maintaining a linked list of spinning tasks in the face of preemptions is very tricky. Wisniewski et al. handle such problems by exploiting a rather non-standard kernel interface that has the ability to “warn” tasks before they are preempted so that they can take appropriate action in time [26]. In the absence of such a kernel interface, list maintenance becomes quite hard, leading to complicated algorithms. For example, a list-based preemptable queue lock proposed by Takada and Sakamura at last year’s RTSS requires a total of 63 executable statements [25]. Our preemptable queue lock is an array-based lock and is quite simple, consisting of only 17 lines of code. In addition, all that we require the kernel to do is to set a shared variable whenever a task is preempted indicating that that task is no longer running. As with other array-based locks, our algorithm has linear space overhead per lock and requires coherent caches in order for spins to be local. However, most modern workstation-class multiprocessors have coherent caches. Also, in many applications, most objects are shared only by a relatively small number of tasks, so having linear space per lock shouldn’t be a severe problem. In any event, these disadvantages seem to be far outweighed by the fact that our algorithm is so simple.

Our algorithm is shown in Figure 6. For clarity, the lock being implemented has been left implicit. In an actual implementation, the shared variables *Tail*, *State*, and *Pred* would be associated with a particular lock and a pointer to that lock would be passed to the *acquire_lock* and *release_lock* procedures.

The *State* array consists of $2N$ “slots”, which are used as spin locations. A task T_i alternates between using slots i and $i + N$. T_i appends itself onto the end of the spin queue by performing a *fetch_and_store* operation on the *Tail* variable (line 5). It then spins until either it is preempted, its predecessor in the spin queue is preempted, or its predecessor releases the lock (line 9). In a system with coherent caches, this spin is local. If T_i stops spinning because its predecessor is preempted, then T_i takes its predecessor’s predecessor as its new predecessor (lines 12-13). If T_i is preempted before acquiring the lock, then (when it resumes execution) it stops spinning and re-executes the algorithm using its other spin location (line 2). Note that the Preemption Axiom ensures that T_i will not be preempted when it re-executes the algorithm. In addition, by the time T_i acquires the lock and then releases it to another task, no task is waiting on either of its two spin locations, i.e., they can be safely reused when T_i performs future lock accesses. Without the Preemption Axiom, correctly “pruning” a preempted task from the spin queue would be much more complicated. (For multiprocessors, the Preemption Axiom can be relaxed to state that a task can be preempted at most once across two consecutive attempts to complete the *same* object call. If our lock algorithm is used by tasks on P processors, then a task that is preempted may have to wait for $P - 1$ tasks on other processors to complete their object calls when it resumes execution. Thus, the Preemption Axiom is tantamount to requiring that the quantum is long enough to contain $P + 1$ consecutive object calls in total on the P processors across which the object is shared.)

We have depicted the algorithm assuming that each task performs its object access as a critical section with

```

shared variable
  Tail: 0..2N - 1 initially 0;
  State: array[0..2N - 1] of {WAITING, DONE, PREEMPTED} initially DONE;
  Pred: array[0..N - 1] of 0..2N - 1

private variable /* local to task  $T_p$  */
  pred: 0..2N - 1;
  slot: {p, p + N} initially p /* assumed to retain its value across procedure invocations */

procedure acquire_lock()
1: while true do /* can only loop at most twice */
2:   slot := (slot + N) mod 2N;
3:   State[slot] := WAITING;
4:   disable interrupts;
5:   pred := fetch_and_store(&Tail, slot); /* join end of spin queue */
6:   Pred[slot mod N] := pred;
7:   enable interrupts;
8:   while State[slot]  $\neq$  PREEMPTED do
9:     while State[slot] = WAITING  $\wedge$  State[pred] = WAITING do /* spin */ od;
    /*
    * after the spin, State[slot] = PREEMPTED or State[pred] = PREEMPTED
    * or State[pred] = DONE
    */
10:    if State[slot]  $\neq$  PREEMPTED then
11:      if State[pred] = PREEMPTED then
12:        pred := Pred[pred mod N]; /* predecessor is preempted - get new predecessor */
13:        Pred[slot mod N] := pred;
14:      else /* State[pred] = DONE */
15:        disable interrupts;
16:        if State[slot] = WAITING then return /* lock acquired */ else enable interrupts fi
17:      fi
    od
  od

procedure release_lock()
16: State[slot] := DONE;
17: enable interrupts

```

Figure 6: Preemptable spin-lock algorithm for quantum-based multiprocessors. In this figure, task indices are assumed to range over $\{0, \dots, N - 1\}$.

interrupts turned off (see lines 14 and 17). Instead, object accesses could be performed using lock-free code, in which case the entire implementation would be preemptable. It can be seen in Figure 6 that the code fragment at lines 5-6 is required to be executed without preemption. This ensures that the predecessor of a preempted task can always be determined. As an alternative to disabling interrupts, if a preemption occurs between lines 5 and 6, then the kernel could roll the preempted task forward one statement when saving its state. This alternative would be necessary in systems in which tasks do not have the ability to disable interrupts.

When a task T_i is preempted while waiting for the lock, the kernel must establish $State[slot] = PREEMPTED$. It is not necessary for the kernel to scan state information per lock to do this. The appropriate variable to update can be determined by having a single shared pointer $Stateptr[i]$ for each task T_i that is used across

all locks. Prior to assigning “ $State[slot] := \text{WAITING}$ ” in line 3, T_i would first update $Stateptr[i]$ to point to $State[slot]$. By reading $Stateptr[i]$, the kernel would know which state variable to update upon a preemption. (If locks can be nested, then multiple $Stateptr$ variables would be required per task.)

Few real-time object-sharing schemes for multiprocessors have been proposed that are efficient enough to have been actually implemented. In contrast, the scheme proposed here would be easy to apply and should lead to good performance. As far as scheduling analysis is concerned, our preemptable queue lock is designed in such a way that any of the uniprocessor scheduling conditions considered in the Section 2 could be used. Our approach also has the advantage that the kernel can be completely oblivious to the fact that tasks share objects, with the lone exception of assigning state variables when preemptions occur. The multiprocessor priority-ceiling protocol (MPCP) is perhaps the best known approach to implementing shared objects in real-time multiprocessors [20]. When using the MPCP, tasks are susceptible to very large block factors. In practice, we believe that our approach would lead to much better schedulability than the MPCP. Actually verifying this belief would involve implementing the MPCP, which to the best of our knowledge, no one has ever done.

3.2 Experimental Comparison

We have conducted performance experiments to compare our preemptable queue lock algorithm to a preemptable queue lock presented last year by Takada and Sakamura [25]. Their lock is designated as the “SPEPP/MCS algorithm” in their paper, so we will use that term here (SPEPP stands for “spinning processor executes for preempted processors”; MCS denotes that this lock is derived from one published previously by Mellor-Crummey and Scott [19]). The SPEPP/MCS algorithm was the fastest in the face of preemptions of several lock algorithms tested by Takada and Sakamura. Our experiments were conducted using the Proteus parallel architecture simulator [11]. Using a simulator made it easy to provide the kernel interface needed by each algorithm. The simulator was configured to simulate a bus-based shared-memory multiprocessor, with an equal number of processors and memory modules. The simulated system follows a bus-based snoopy protocol with write-invalidation for cache coherence. Tasks are assigned to processors and are not allowed to migrate. On each processor, tasks are scheduled for execution using a quantum-based round-robin scheduling policy. The scheduling quantum in our simulation was taken to be 10 milliseconds.

Figure 7 presents the results of our experiments. In this figure, the average time is shown for a task to acquire the lock, execute its critical section, and release the lock. These curves were obtained with a multiprogramming level of five tasks per processor, with each task performing 50 lock accesses. The execution cost of the critical section was fixed at 600 microseconds. Each task was configured to perform a noncritical section between lock accesses, the cost of which was randomly chosen between 0 and 600 microseconds. The simulations we conducted indicate that only the number of processors in the system affects relative performance; simulations for different numbers of lock accesses and multiprogramming levels resulted in similar graphs. The curves in Figure 7 indicate that the time taken to acquire the lock in our algorithm is up to 25% less than that for the SPEPP/MCS algorithm (the time taken to acquire the lock is obtained by subtracting the critical section

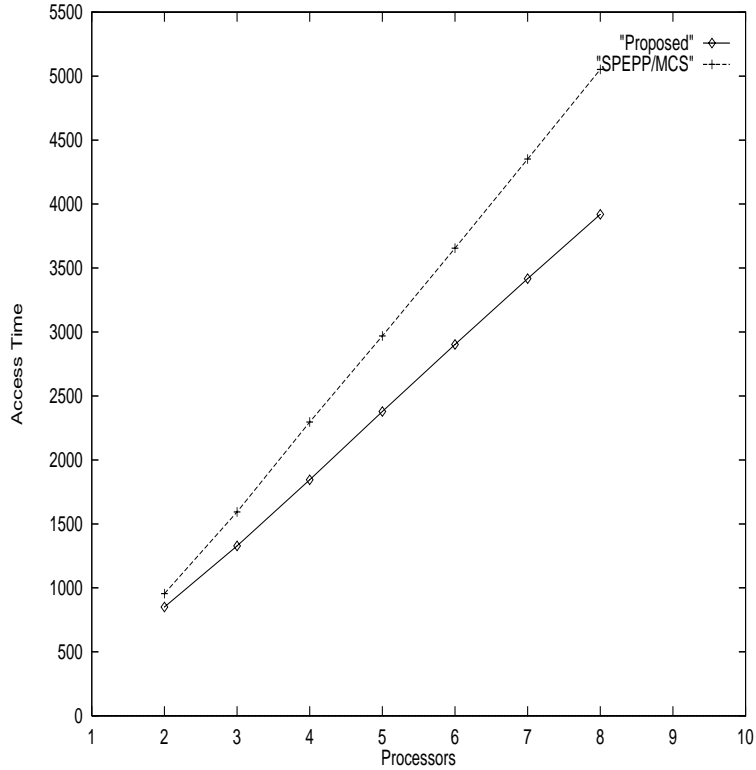


Figure 7: Experimental comparison of preemptable spin-lock algorithms. Curves show average access times. Times are in microseconds.

execution time from the values in Figure 7). The performance of our algorithm is such that, for two processors, the access cost is only a little more than one critical section execution (a cost that must be paid), and for every additional processor, the average access time increases by approximately the cost of one additional critical section. We also instrumented the code to measure the time taken to acquire the lock in the best case. For each algorithm, the time taken by a task to acquire the lock is minimized when that task is at the head of the spin queue. The best-case time for acquiring the lock was 100 microseconds for our algorithm, and 200 microseconds for the SPEPP/MCS algorithm.

In real-time systems, worst-case execution times are also of importance. Unfortunately, we were unable to obtain worst-case times because of limitations imposed by Proteus simulator. However, we can informally argue that the worst-case performance of our algorithm is marginally better than that of the SPEPP/MCS algorithm. With our algorithm applied in a P -processor system, the worst case arises when a task waiting for the lock has $P - 1$ tasks ahead of it in the queue, and just before that task reaches the head of the queue it gets preempted. When this task is next scheduled for execution, it is guaranteed to acquire the lock, but it might have to again wait for $P - 1$ other tasks to execute their critical sections. Thus, in the worst case, a task might have to wait for $2P - 2$ critical section executions of other tasks. In other words, worst-case performance is linear in the number of *processors* across which the algorithm is being executed.

In the SPEPP/MCS algorithm, the time spent by a task waiting for the lock is proportional to the number of tasks ahead of it in the queue. Thus, in the worst case, a task’s waiting time is proportional to $(N - 1) \cdot T$, where N is the number of tasks and T is the time to execute one critical section. In other words, worst-case performance is linear in the number of *tasks* that may access the lock. In [25], Takada and Sakamura suggest a variant of the SPEPP/MCS algorithm in which there is a single node for all tasks on one processor, resulting in $\Theta(P)$ worst-case performance for P processors, like our algorithm. However, they do not describe this variant of their algorithm in any detail, so we did not know how to implement it for our tests. Given the fact that their original algorithm is quite complex (63 lines of code compared to 17 for our algorithm, and many more calls to synchronization primitives than in our algorithm), we suspect that the constant hidden in this $\Theta(P)$ term might be rather large.

4 Concluding Remarks

We have presented a new approach to implementing shared objects in quantum-based real-time uniprocessor and multiprocessor systems. The essence of this approach is to exploit common characteristics of such systems. In the proposed object implementations, object calls are performed using an optimistic retry mechanism coupled with the assumption that each task can be preempted at most once across two consecutive object calls. We have presented experimental evidence that shows that such implementations should entail low overhead in practice.

In a recent related paper, Anderson, Jain, and Ott presented a number of new results on the theoretical foundations of wait-free synchronization in quantum-based systems [1]. It was shown in that paper that the ability to achieve wait-free synchronization in quantum-based systems is a function of both the “power” of available synchronization primitives and the size of the scheduling quantum. In addition, an asymptotically tight characterization of the conditions under which wait-free synchronization is possible was given. Intuitively, synchronization primitives allow processes on different processors to coordinate, and the scheduling quantum allows processes on the same processor to coordinate. We hope the results of [1] and this paper will spark further research on synchronization problems arising in quantum-based systems.

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