# Distillation Codes and DOS Resistant Multicast

Prepared for CS 624 – Fabian Monrose Johns Hopkins University

Ryan Gardner

## **Multicast Overview**



## **Multicast Overview**

- Multicast enabled routers
- 224.0.0.0 239.255.255.255 (class D)
- IGMP (Internet Group Management Protocol)
- Subscribe to groups and unsubscribe

# Applications

- Interactive applications
  - Teleconferencing
  - Video conferencing
- Information broadcasts
  - News
  - Stocks
- Updates
  - Software
  - Viruses

# Challenges

- Authenticity
- Malicious users
- Tolerate packet loss
- Minimal delay
- (DoS attacks)

# Outline

- Three naive solutions
- Brief summary of related work
- Efficient Multicast Stream Authentication using Erasure Codes
- Distillation codes
- Conclusion

## Naive Solution 1 Symmetric Authentication

#### Review of MAC



## Naive Solution 1 Symmetric Authentication



# Naive Solution 1 Symmetric Authentication

- Pros
  - Fast
  - Low space overhead
  - Virtually no delay
  - Simple
- Cons
  - Any member of the group can "authenticate packets"

## Naive Solution 2 Sign Every Packet

#### **Review of Signature**



- DSA
- IBE short signatures

# Naive Solution 2 Sign Every Packet



# Naive Solution 2 Sign Every Packet

- Pros
  - Guarantees authenticity
  - Perfect loss tolerance
  - Almost no delay
- Cons
  - Computationally expensive for sender and receiver
  - High bandwidth overhead

## Naive Solution 3 Basic Signature Amortization



## Naive Solution 3 Basic Signature Amortization

- Pros
  - Unforgeable
  - Low computational cost
  - Low bandwidth overhead
- Cons
  - No packet loss tolerance
  - Delay at receiver

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## **Related Work**

- "Asymmetric MACs"
  - TESLA [12,13]
  - Biba "signature" [11]
- Signature amortization...

## Signature Amortization

- Signature generations are expensive
- Boneh, Durfee, and Franklin showed can't use MACs entirely... [2]
- Break single signature into multiple packets
- Fundamental issues
  - Packet loss
  - Maliciously inserted packets (DoS)
- Some work done
  - Accumulators [16]
  - Erasure Codes [9,10]

## How to Sign Digital Streams [4] CRYPTO '97

- Objectives
  - Stream signing (not necessarily multicast)
  - Authenticity
  - Non-repudiation (even for partial streams)
  - Inexpensive
  - Low delay
- General approach
  - Authentication chain bootstrapped with signature

## How to Sign Digital Streams



## How to Sign Digital Streams

#### Pros

- Simple
- Low computation (single signature)
- Low overhead
- Authenticity
- Non-repudiation (even for partial streams)
- Low delay (if packets are sent at high frequency)
- Cons
  - No loss tolerance

# Digital Signatures for Flows and Multicasts [16] *IEEE/ACM Transactions on Networking* 1999

- Objectives
  - Authenticity
  - "High" signing and verification rates
  - Loss tolerant
  - Non-repudiation
  - Inexpensive
  - Low delay
- General approach
  - Create a common signature for blocks of packets
  - Self authenticating packets

#### **Digital Signatures for Flows and Multicasts**

#### Star Chaining





# Digital Signatures for Flows and Multicasts Star Chaining



#### **Digital Signatures for Flows and Multicasts**

#### • Pros

- Authenticity
- "High" signing and verification rates
- Perfect loss tolerance
- Non-repudiation
- Cons
  - Small sender delay
  - Extremely high bandwidth overhead

## Summary of Related Work

- Still significant deficiencies
  - No loss tolerance
  - Extremely high bandwidth overhead
  - Vulnerable to DoS attacks
    - Computational
    - Memory exhaustion

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   using Erasure Codes
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# Efficient Multicast Stream Authentication using Erasure Codes [10]

ACM Transactions on Information and Systems Security 2003

- Objectives
  - Ensure authenticity (non-repudiation)
  - Robustness to packet loss
  - Minimal overhead & delay
  - Robust against en route packet modification or insertion of small number of bogus packets
- General approach
  - Amortize a signature over several packets using erasure codes

# **Erasure Codes**

Sender

Take *m* objects (the original data) and creates
 *n* "erasure encoded objects"

- Receiver
  - Needs any *m* of the *n* objects sent, and can reconstruct "erasure decode" the original data
- Space optimal

### Information Dispersal Algorithm (IDA) [14]

- Basics
  - Create an *n* row matrix A such that any *m* of the *n* rows are linearly independent
  - Multiply that by our data
  - On receipt of m chunks, grab the corresponding m rows of A, A'
  - Multiply received data by A'-1
- Kevin will cover...
- Pretty light computationally
  - One matrix multiplication at each end (matrix inversion at receiver)
  - $O(n^2)$  encode
  - $O(m^2)$  decode

# Signature Amortization using IDA - Description

Break a stream up into blocks

$$P_{1,1}$$
 $P_{1,2}$ 
 $P_{1,m}$ 
 $P_{2,1}$ 
 $P_{2,2}$ 
 $P_{2,m}$ 
 $P_{3,1}$ 
 $P_{3,2}$ 
 $P_{3,m}$ 
 $P_{3,m}$ 

#### For each block



 $F = h(P_1) || h(P_2) || \dots || h(P_n)$ 

#### Erasure encode F using IDA





#### Form each packet



#### Reconstruction




# Delays

- Sender
  - Must append information to *n* packets before sending
- Receiver
  - Must receive *m* packets to authenticate and use
  - (Frequently, all *m* packets should arrive approximately at the same time)
- Consequences
  - Approximate additional delay of the time span of each block
  - For minimal delay, we need smaller block size

# **Practical Costs - Computation**

#### **Computational costs per block**

Operations possible per second

	Sender	Receiver	Pentium 2.4 GHz
Erasure encodes	1	0	2,755
Erasure decodes	0	1	3,700
RSA-1024 signature generations	1	0	25
RSA-1024 signature verifications	0	1	1,170

We can send approximately one block every 40 ms.

# Acceptable Delay

The International Telecommunications Union – Telecommunications Standardization Sector states the following maximum end to end transmission times that they consider "allowable" with echo control. (Recommendation G.114) [5]

Delay	Acceptability.
0 - 150 ms	acceptable to most user application.
150 - 400 ms	acceptable when the impact on quality is aware of.
400 ms	unacceptable

### Practical Costs - Bandwidth

#### Given:

n/m = 1.5

using RSA-1024

20 byte SHA-1 hash

blocks of 64 packets (unencoded) of size 1024 bytes (65536 bytes total)

Bandwidth overhead = 2112 bytes per block 3.2%

Conclusion: Costs are extremely reasonable in the simple case.

### **Authentication Probability**

- Burst losses are an important part of their analysis
- 2 models
  - -2 state Markov chain model (2-MC)
  - "Biased coin toss"

# 2 State Markov Chain Model (2-MC)





# Internet Traffic Loss

"probe" packets sent from University of Massachusetts, Amherst [17] number of destinations in multicast is unknown...

time given in eastern daylight time

date	time	type	destination	duration	sending interval	loss %
Nov '97	09:52	unicast	SICS, Sweeden	8 hrs	80 ms	2.7%
Nov '97	09:53	multicast	SICS, Sweeden	8 hrs	80 ms	11.0%
Dec '97	13:41	unicast	Seattle	2.5 hrs	20 ms	1.7%
Dec '97	13:39	multicast	Seattle	2.5 hrs	20 ms	3.8%

# Internet Traffic Loss

Distribution of packet loss bursts for the Seattle unicast data



### **Authentication Probability Results**

### Authentication probability $\rightarrow \Phi(k)$ as $n \rightarrow \infty$



### Authentication Probability vs. Block Size



### Problem – DoS on SAIDA

A single bogus packet will prevent the authentication of an entire block.

### Problem – DoS on SAIDA



# Possible Solution – Error Correcting Codes (ECCs)

- Similar to erasure codes
  - Encode *m* objects to *n* (*n*>*m*)
  - Receiver decodes back to original message
- Allow for a certain number of errors
- More expensive
  - Computation
  - Size
- Common example: Reed-Solomon [15]
  - Plots a polynomial of degree *m-1* in a field
  - Over-plots the polynomial with redundant points (sends them)
  - Can interpolate through a number of bad points

### Addition of Error Correcting Codes

### For each block



 $\Omega = (h(c_1 ||\sigma_1)|| h(c_2 ||\sigma_2)|| \dots ||h(c_n ||\sigma_n))$ 



### Append to each packet P<sub>i</sub> c<sub>i</sub> σ<sub>i</sub> ω<sub>i</sub>



 $\Omega = (h(c_1||\sigma_1)|| h(c_2||\sigma_2)|| \dots ||h(c_n||\sigma_n))$ 

For each candidate packet:  $P_{j} c_{j} \sigma_{j}'$ verify  $\Omega_{j} = h(c_{j}'||\sigma_{j}')$ 

### DoS on SAIDA

### Claim –

The addition of error correcting codes can prevent the attack where an adversary injects a "small" number of bogus packets into the stream.

## DoS on SAIDA with Error Correcting Codes



# SAIDA Summary

#### Pros

- Ensures use of legitimate packets only
- Computationally feasible
- Low bandwidth overhead
- Good verification probability in burst loss model
- Withstand attacks when a small number of garbage packets are injected

#### Cons

Delay at the sender and receiver

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Distillation Codes and Applications to DoS Resistant Multicast Authentication [6] NDSS 2004

- Objectives
  - Introduce and address a new adversarial model
    - Robustness against pollution attacks (adversary injects many invalid symbols)
  - "Loss model independent"

### **Pollution Attack on SAIDA**

### Claim –

If an adversary injects sufficiently many packets (a number equal to that of the legitimate sender) into a multicast stream, she will launch a complete denial of service attack on the receivers.

### **Pollution Attack on SAIDA**



### **Strawman Solutions**

- Decode all possibilities (using erasure code scheme)
  - $-\binom{t}{m}$  possibilities (exponential)
- Digitally sign every symbol
  - Very expensive (computational, bandwidth)
  - Computational DoS attacks

## **Distillation Codes**

- GOAL: Solve pollution attack vulnerability with "distillation codes"
- General approach
  - Break the packets into groups where all the good packets are exclusively in the same group
  - Compute at most one signature per group
  - Only compute signatures for groups that are sufficiently large
  - This will force a maximum number of signature verifications of only one per X packets received.

### **General Idea**

### Partition the symbols



### Partitioning the Symbols

- Want one partition to contain *exactly* all the valid symbols (*distillation property*)
  - If it is valid, we want it in the right partition
  - Don't want anyone to be able to create a symbol that could be placed in the same partition as another symbol they simply saw
- Challenges
  - Need secure set membership computed at the receiver's end

### **One Way Accumulators**

One way accumulator Assume set S of symbols  $\{s_1, \dots, s_n\}$ 

Accumulate(S)  $\rightarrow$  a (accumulator) Witness(s,S)  $\rightarrow$  w Verify(s,w,a)  $\rightarrow$  b (true,false) Recover(s,w)  $\rightarrow$  a

### **One Way Accumulators**

Must be hard to forge an element of the set

Must be hard to find s', w' where s'  $\notin$  S and Recover(s',w') = Accumulate(S)

### **One Way Accumulator Examples**

- Merkle hash trees [7]
- Benalod and de Mare *quasi*commutative one way accumulators
  [1]
- Camenisch and Lysyanskaya dynamic accumulators [3]

### Claim: Given a One Way Accumulator, We Can Partition Symbols

Assume D is our set of valid symbols.

Accumulate(D)  $\rightarrow$  a Witness(s,D)  $\rightarrow$  w Verify(s,w,a)  $\rightarrow$  b Recover(s,w)  $\rightarrow$  a

Can't find s' ∉ D, and w' where Recover(s',w') = Accumulate(D)



### Claim: Given a One Way Accumulator, We Can Partition Symbols

- The definition of Recover(s,w) ensures that all "good" symbols will end up in the same partition.
- The *unforgeability property* of the accumulator ensures that a "bad" symbol cannot be placed in the same partition as the good ones.
- Therefore, with a one way accumulator, we obtain the *distillation property* (by placing each symbol in the partition indexed by its accumulator).

### Merkle Hash Trees – Our One Way Accumulator



### Merkle Hash Trees – Our One Way Accumulator

# Merkle hash trees are a valid one way accumulator.

### Finding a Solution to Pollution Attacks...

Putting it all together...
#### **Distillation Code – Definition**

An (n,t) distillation code encodes a message D into a set of *n* symbols  $\{s_1, s_2, \dots, s_n\}$  and transmits them over a polluted erasure channel ensuring:

Authenticity. It will never give an invalid reconstruction.

**Correctness**. If given set of symbols T contains at least *n*-*t* (*m*) valid symbols of D, then an execution of the decoder on T will output a valid reconstruction.

# **Distillation Codes - Encoding**

#### Sign the message D



# **Distillation Codes - Decoding**

Partition the received symbols (packets)

Remove witness information

Throw away partitions with less than *m* (say 2)



#### Distillation Codes – Decoding (cont') For each remaining **S**'<sub>3</sub> s'<sub>4</sub> s'<sub>1</sub> **S**<sup>'</sup><sub>2</sub> s'<sub>m</sub> partition: Erasure decode the m symbols d'<sub>3</sub> $d'_4$ d'<sub>1</sub> $d_2'$ d'<sub>m</sub> . . . sig<sub>K\_priv</sub>(D') D' Verify whether D' has a valid valid signature sig? yes no Use it Discard

## **Distillation Codes**

Our construction now satisfies the authenticity and correctness properties. (It is a valid *distillation code*.)

Authenticity. The last step of the decoding is a signature verification. We assume a false signature cannot be generated. (Note that the signature also gives us non-repudiation here.)

**Correctness**. We know our partitioning scheme satisfies the distillation property. Therefore, there is one partition that contains *exactly* the valid symbols. Since we verify each partition, we will verify this one.

#### **Resistance to Pollution Attacks**

Claim –

A receiver using distillation codes will compute at most one signature for every *m* packets, she receives.

#### **Distillation Codes – Attack Example**



#### **Distillation Codes – Attack Example**



#### **Distillation Codes – Attack Example**



## Attack Resilience Snapshot

- They claimed attack factor of 10 with 4 Mbs stream required at most 13% CPU in the worst case.
- Assuming a maximum packet delay of 2 seconds, that same stream requires at most 11.87 MB of memory.

# **Distillation Codes Summary**

#### • Pros

- Robust against pollution attacks (with an attack factor of no more than 10)
- Ensures authenticity (with non-repudiation)
- Robust to packet loss
- Small overhead
- Cons
  - (Loss model dependent)
  - Delay at both the sender and receiver
  - Still vulnerable to attacks with more packets

# Conclusion

- Information assurance through multicast is challenging
- Can be done at various costs
- Still no perfect solution
- They fit applications well
- Many tools out there that can be useful in various situations

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