Secure and Efficient Metering

Moni Naor and Benny Pinkas Eurocrypt '98

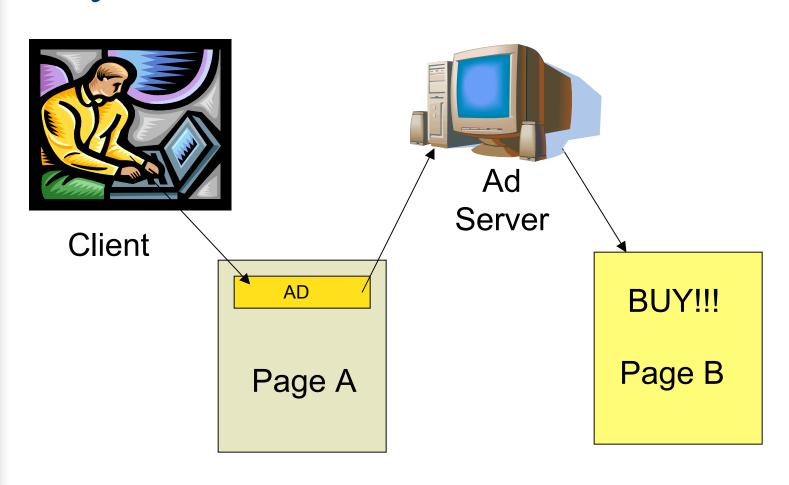
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- Secure and Efficient Metering

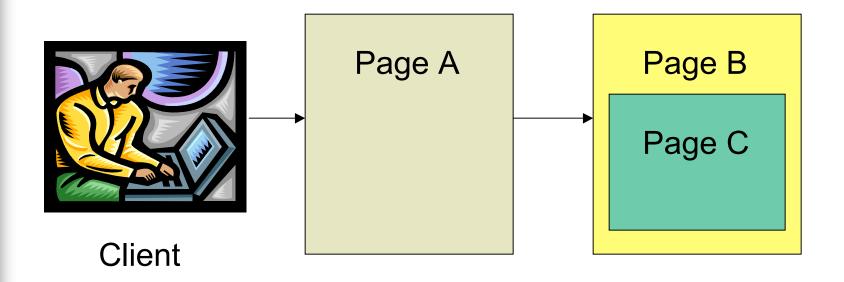
Motivation

- Advertising
 - Webpage popularity
 - Cost
- Measure server & client interaction
- Royalties payment

Pay-Per-Click Scheme



Hit Inflation



- Alternatives
 - Pay-per-sale
 - Pay-per-lead

SAWM: A Tool for Secure and Authenticated Web Metering

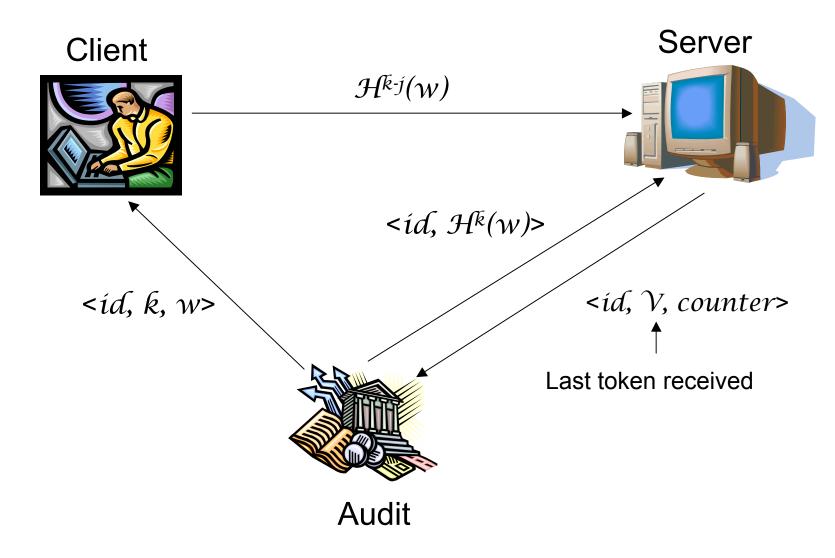
Blundo and Cimato

Proceedings of the 14th International Conference on Software engineering and knowledge engineering 2002

SAWM: A Tool for Secure and Authenticated Web Metering

- Hash chaining
- Three participants
 - Audit Agency
 - Client
 - Server
- Parameters
 - Random seed w
 - Hash function ${\mathcal H}$
 - Client identifier id
 - Number of applications k

SAWM Protocol



Shortcomings

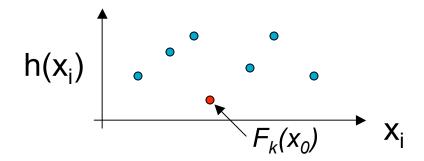
- Requires client & audit agency interaction
- Client and server can collude
- Corrupt servers can share client tokens
- Fake servers can collect tokens

Auditable Metering with Lightweight Security

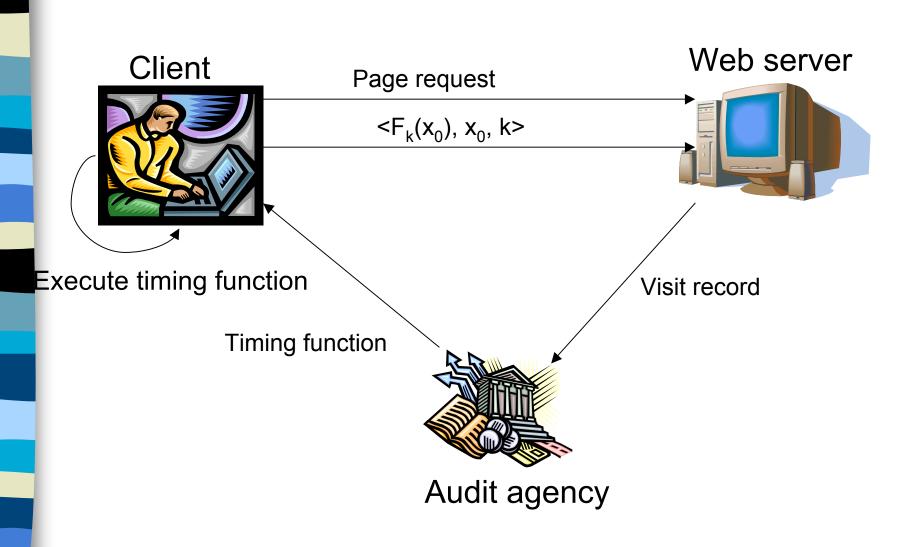
Franklin and Malkhi Financial Crypto 1997

Auditable Metering with Lightweight Security

- Hash function h
- Timing function F
 - Apply hash function iteratively k times to x_0 such that $x_{j+1} = h(x_j)$
 - $-F_k(x_0) = min\{x_i\}$, where $0 \le j \le k$



Auditable Metering with Lightweight Security



Lightweight Security Auditing

Method 1

- Determine low probability visit records $\langle F_k(x_0), x_0, k \rangle$
- Verify these values

Method 2

- $-y=F_k(x_0)$
- Estimator function $\mu(y)$ that estimates k'
- Check if estimator function approximates timing function

Lightweight Security Shortcomings

- Client can cheat server
- Client can collude with server
- Does not take into account different processing power of clients
- Costly verification
- Security based on statistical probabilities

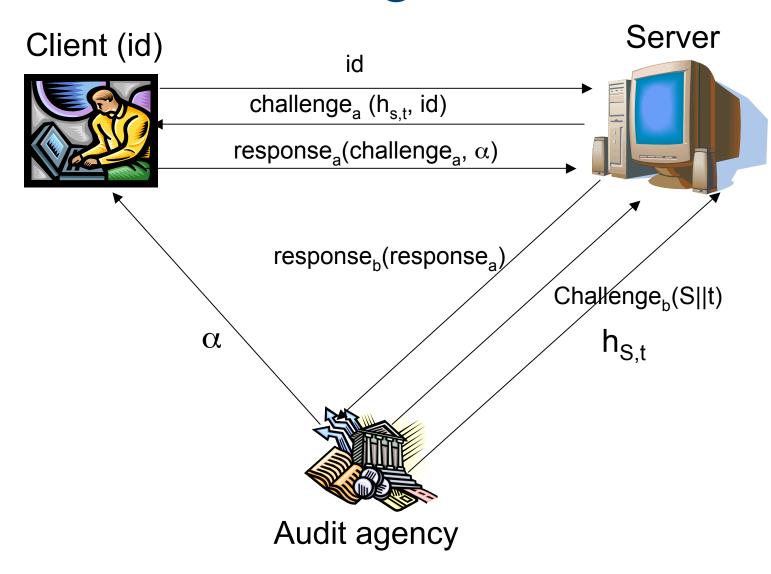
Secure and Efficient Metering

Naor and Pinkas EuroCrypt '98

Secure and Efficient Metering

- Uses variant of Shamir secret sharing scheme
- Cryptographically secure scheme
- Requirements
 - Security
 - Efficiency
 - Accuracy
 - Privacy
 - Turnover

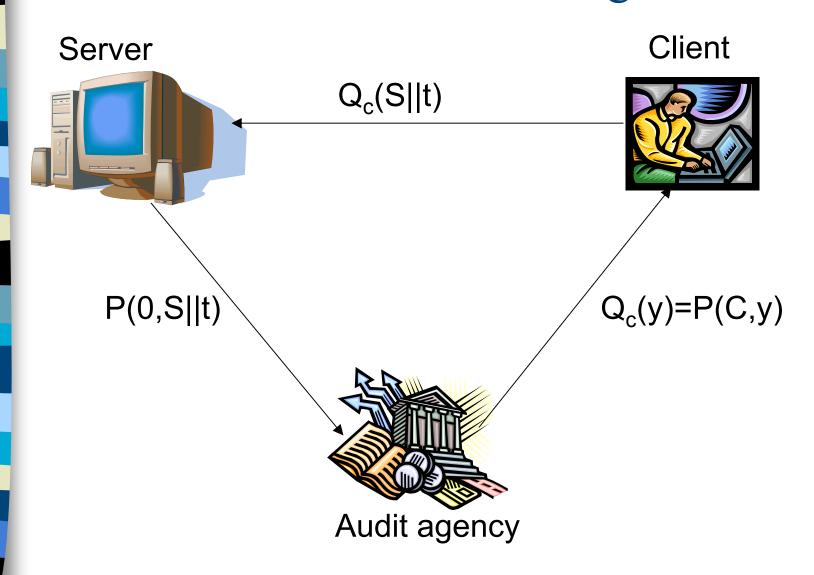
General Metering Scheme



Secure & Efficient Metering Parameters

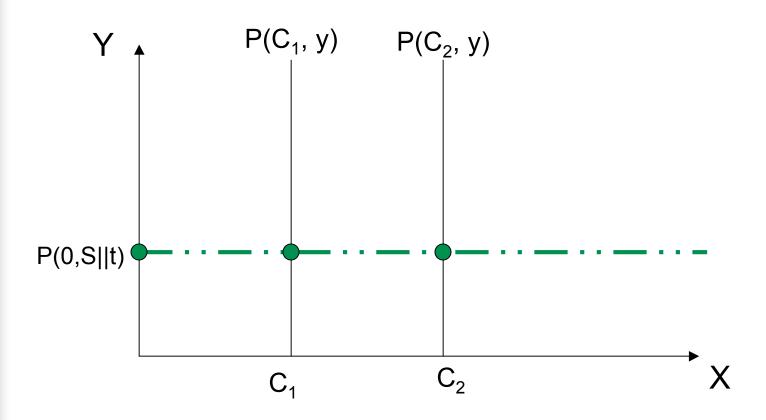
- Bivariate polynomial: P(x,y)
 - Degree k-1 in x
 - Degree d-1 in y
 - Finite field Z_p
 - Selected by audit agency
- Client value: C
- Server value: S
- Time frame: t

Secure and Efficient Metering Scheme



Calculating P(0, S||t)

Use Lagrange interpolation

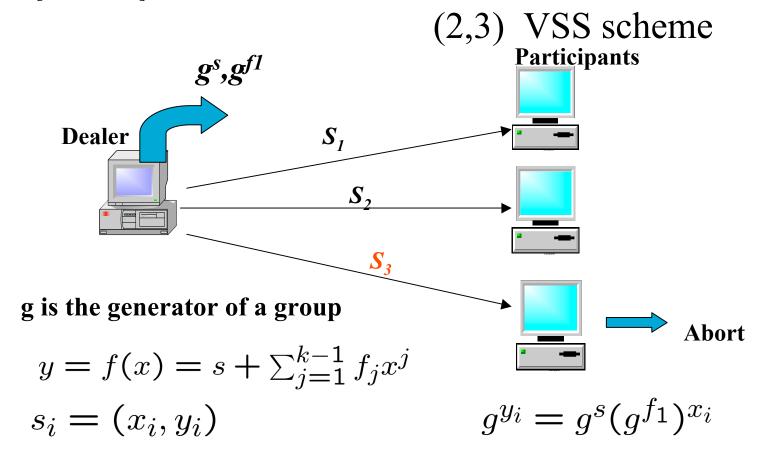


Security Analysis

- Without k visits, server has 1/p chances of finding P(0, S||t)
- Corrupt clients can collude with servers
- Corrupt servers can donate client information from previous time frames
- Polynomial P replaced every d times frames

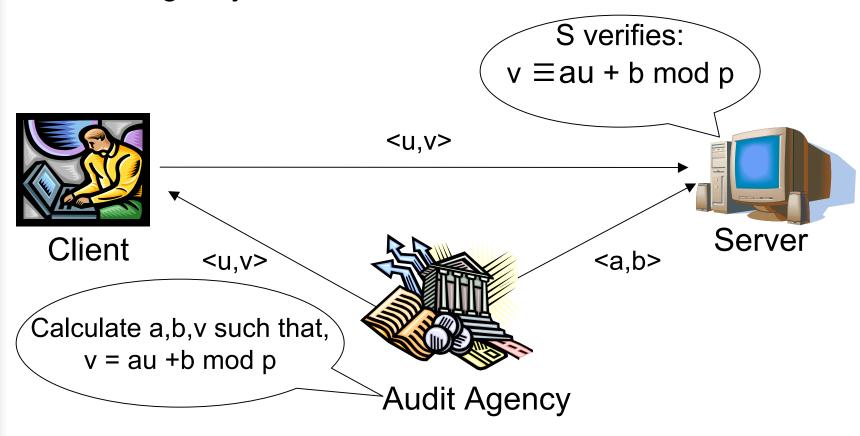
- Corrupt clients can give the server wrong values
- Even with wrong values, a server should still be able to prove it had k visits
- Non-interactive verifiable secret sharing

Verifiable Secret Sharing for Shamir's scheme [Feldman87]



Robustness: Alternate Method

Audit agency wants the client to tell the server u.



- P(x,y): degree k-1 in x, degree d-1 in y
- A(x,y): degree a in x and b in y
- \blacksquare B(y): degree b in y
- Audit Agency calculates:

$$V(x,y) = A(x,y) \cdot P(x,y) + B(y)$$

Client

Verifies: V = AP+B

Server



P(C, S||t), V(C, S||t)

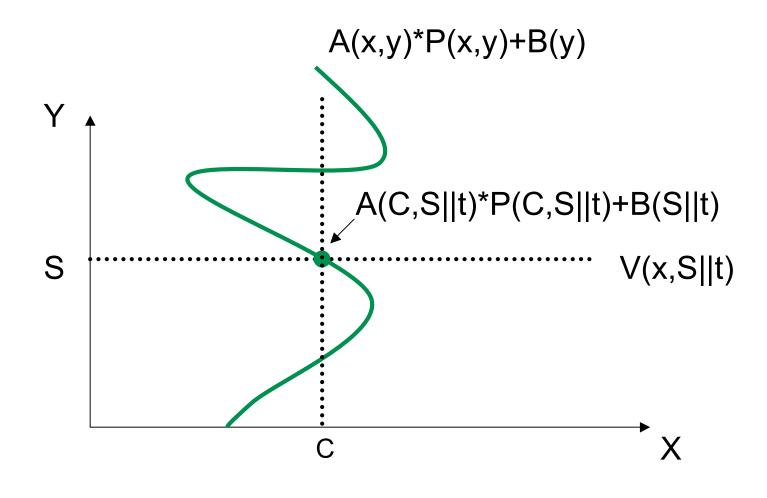
P(C,y), V(C,y)

 $A(x,S||t_i), B(S||t_i)$

Calculates:

V = AP + B

Audit Agency



- Audit agency must compute V, A and B
- Server must store A and B for all time frames t
- Server must compute A and B for each client that visits
- Server must check V=AP+B
- Client must evaluate V for each server and time frame
- Additional communication overhead

Increasing Efficiency

Divide k into n classes

```
n = k/k'
```

- **n** random polynomials: $P_1(x,y) \dots P_n(x,y)$
- Map clients randomly to {1,...,n}
- Client gets respective polynomial P_i(x,y)
- Client sends class along with P_i(C, S||t)
- Server only needs k' clients from a class to interpolate

Increasing Efficiency

Coupon Collector problem

Given a set of possible outcomes, what is the expected number of events before the entire set of possible outcomes occurs

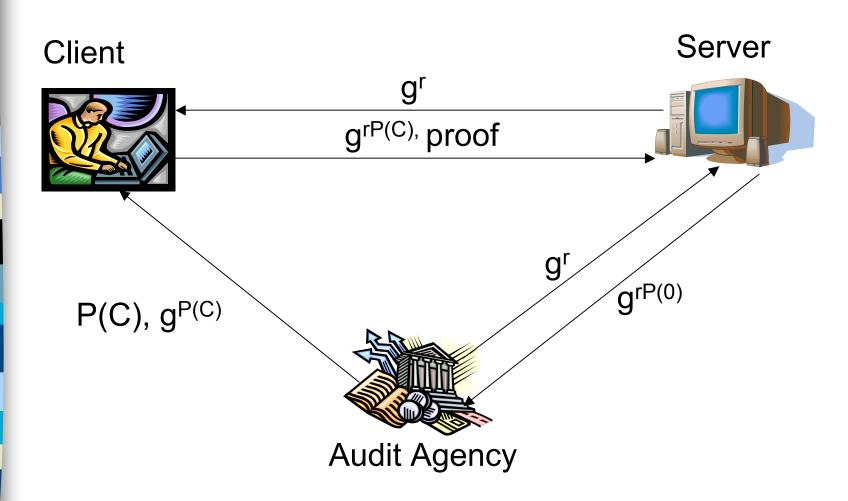
Coupon Collector Example

- 3 toys: A,B,C
- Probability of obtaining any toy is 1/3
- Expected time to collect all 3
 - = E[waiting time for 1st toy] +E[waiting time for 2nd toy] +E[waiting time for 3rd toy]
 - = 3/3 + 3/2 + 3/1
 - = 5.5 tries

Increased Efficiency

- Audit agency must produce multiple polynomials
- Audit agency must map clients to polynomials and store the mapping
- Server must store the client's class as well as P_i(C, S||t)
- Client must store it's class with the polynomial P
- Probabilistic scheme rather than deterministic

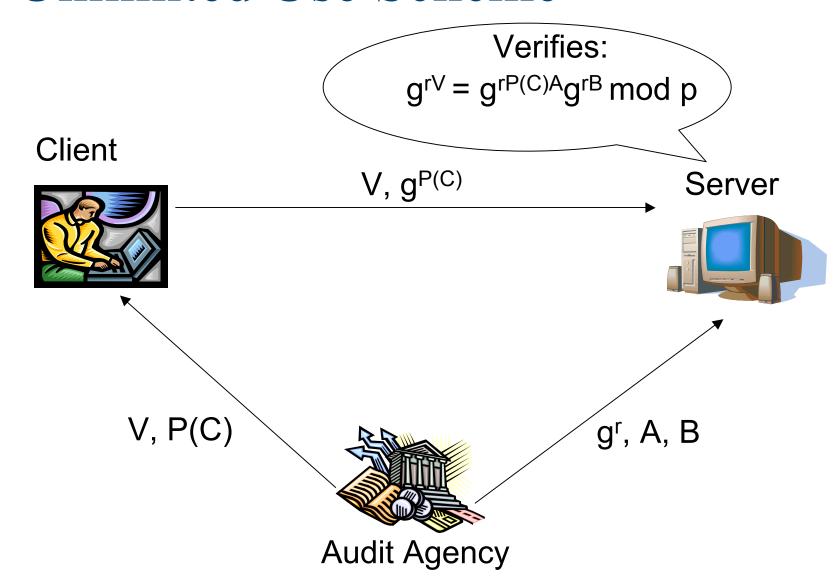
- Basic scheme requires replacing P after d time frames
- Unlimited use scheme parameters
 - generator g
 - random value r



- Decisional Diffie-Hellman
 - Given g^a , g^b , y, compute if $y == g^{ab}$
- Computational Diffie-Hellman
 - Given g, g^a , g^b , compute g^{ab}
 - In this case, the server has g, g^r and $g^{rP(Ci)}$, where 0 < i < k
 - If it can calculate $g^{rP(0)}$ it can break CDH

- Client proof construction
 - Same as robustness scheme
 - Audit agency calculates V(x,y), A(x,y) and B(y) such that when x = C and y = S, $g^{rV} = g^{rP(C)A}g^{B} \mod p$

Unlimited Use Scheme



Unlimited Use Scheme

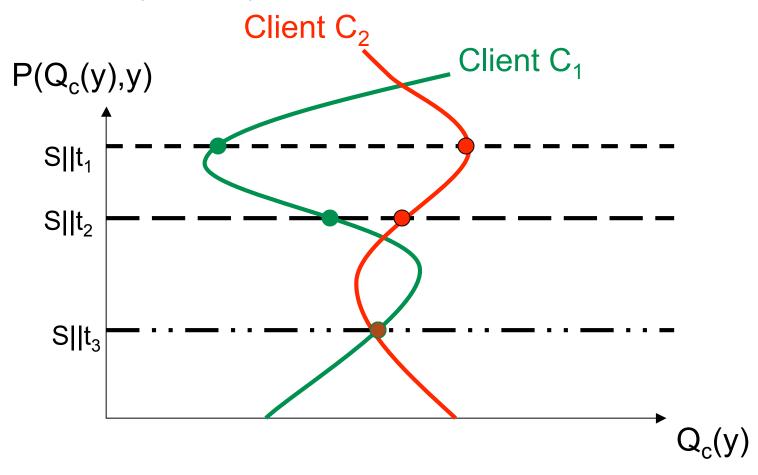
- Exponentiation of polynomials is computationally expensive
- Each time frame a new r is used and gr must be calculated
- Additional communication overhead between audit agency and server
- Server must verify $g^{rV} = g^{rP(C)A}g^{rB} \mod p$

Anonymity

Preserves client privacy over multiple time periods

- Instead of P(C,y), have $P(Q_c(y),y)$
 - $-Q_c(y)$: random polynomial of degree u
 - where y = S||t|
 - $-Q_c(y)$ changes for each time period

Anonymity



Anonymity

- Audit agency must now generate $Q_c(y)$
- \blacksquare Clients must store $Q_c(y)$
- Clients must calculate $Q_c(y)$ for each visit
- Corrupt audit agencies can cooperate with servers to track client activity

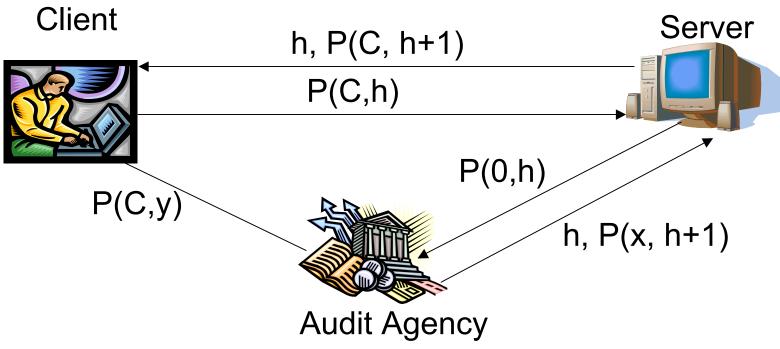
Variants

Variants: Metering Period

- Servers have varying amounts of traffic
- Replace timeframe t with challenge h
- Allows for variable metering periods
- Server now sends h to client when a page is requested

Variants: Metering Period

- Servers now send h
- Servers may try to send false *h* values



Variants: Client Turnover

- Advertising agencies may want to determine client loyalty
- Aids in developing payment schemes
- Detects corrupt servers

Variants: Client Turnover

Audit agency sends server challenge t with domain c*k and hash function h with range c*k

After receiving c^*k new clients, server should find $g^{riP(C)}$ such that $h(g^{riP(C)}) = t$

Variants: Adaptability

- Servers with less traffic may never see k clients for a given time frame
- Decrease k to allow more fine grained measurements
- If server receives k'<k, ask for k-k'</p>
 polynomial values to complete interpolation
- Server sets k'

Open Problems

- Efficient schemes limited usage times
- Unlimited use schemes inefficient
- Value for k must be preset
 - Cannot tolerate the number of clients changing
 - Even under adaptability scheme, k is still preset

Questions