

# Automatic Generation of Test-cases of Increasing Complexity for Autonomous Vehicles at Intersections

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# Have we tested enough yet?

**Waymo's autonomous vehicles have clocked 20 million miles on public roads**

**Waymo's driverless cars were involved in 18 accidents over 20 months**

Autonomous vehicles would have to be driven hundreds of millions of miles and sometimes hundreds of billions of miles to demonstrate their reliability in terms of fatalities and injuries.

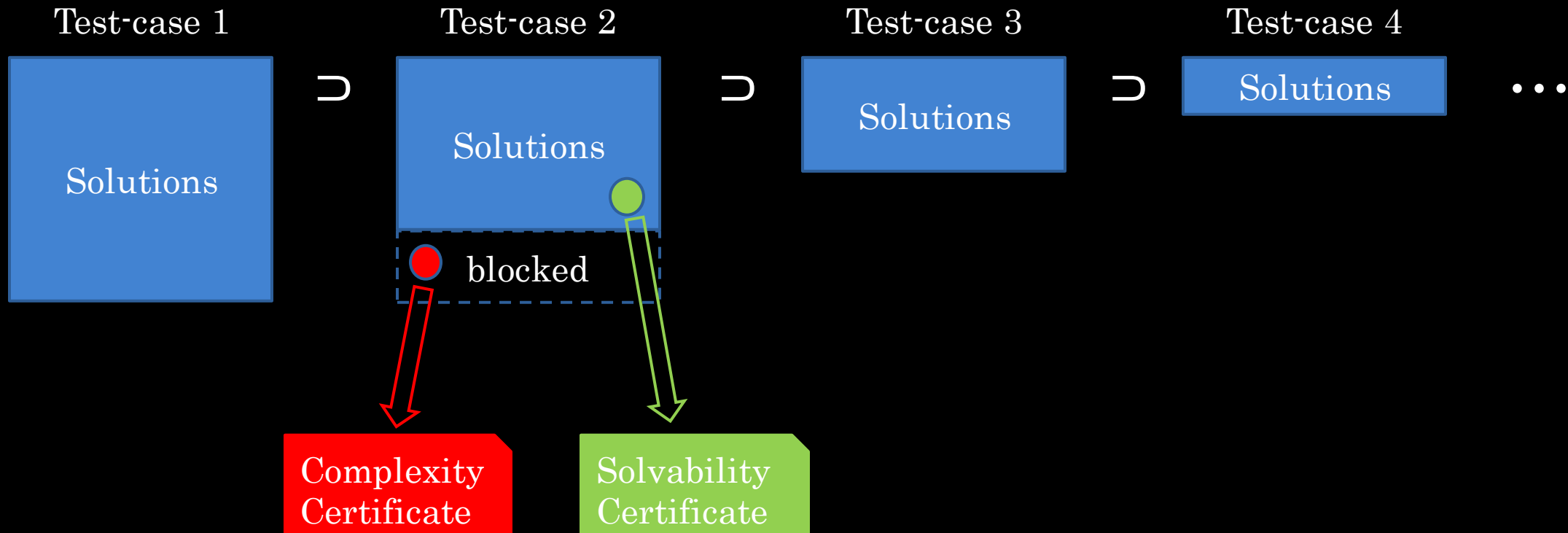
**Tesla cars register one crash for every 4.31 million miles driven with Autopilot**



# Test-case complexity

- Shrink the set of solutions incrementally

$\supset$  : proper superset





# Contributions

## 1. Formalized Test-case Complexity

- More right-of-way constraints → more-complex

## 2. Generate test-cases

- Traffic rules → concrete trajectories

## 3. Generate certificates

- Complexity
- Solvability



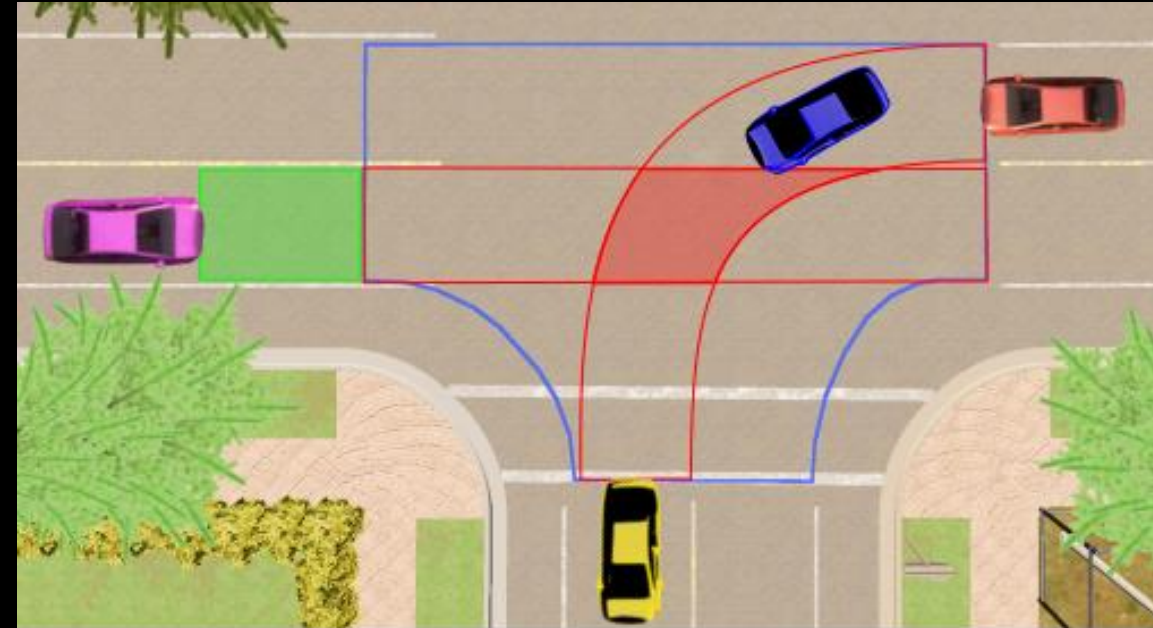
# Outline

- Test-case scenarios
  - Predicate-level abstraction of a scenario
  - Traffic rules as PASS/FAIL criteria
- Generation algorithm
  1. Ordering of events using ASP
  2. Concretize timing of events and speed profiles using SMT
  3. If collisions, try next ASP solution
- Results



# Predicate abstraction of a scenario

- Regions
  - Lanes
  - Lane sections
- Events
  - Entering
  - Exiting
  - Velocity reaching a threshold
- Temporal relations
  - Earlier
  - Same time



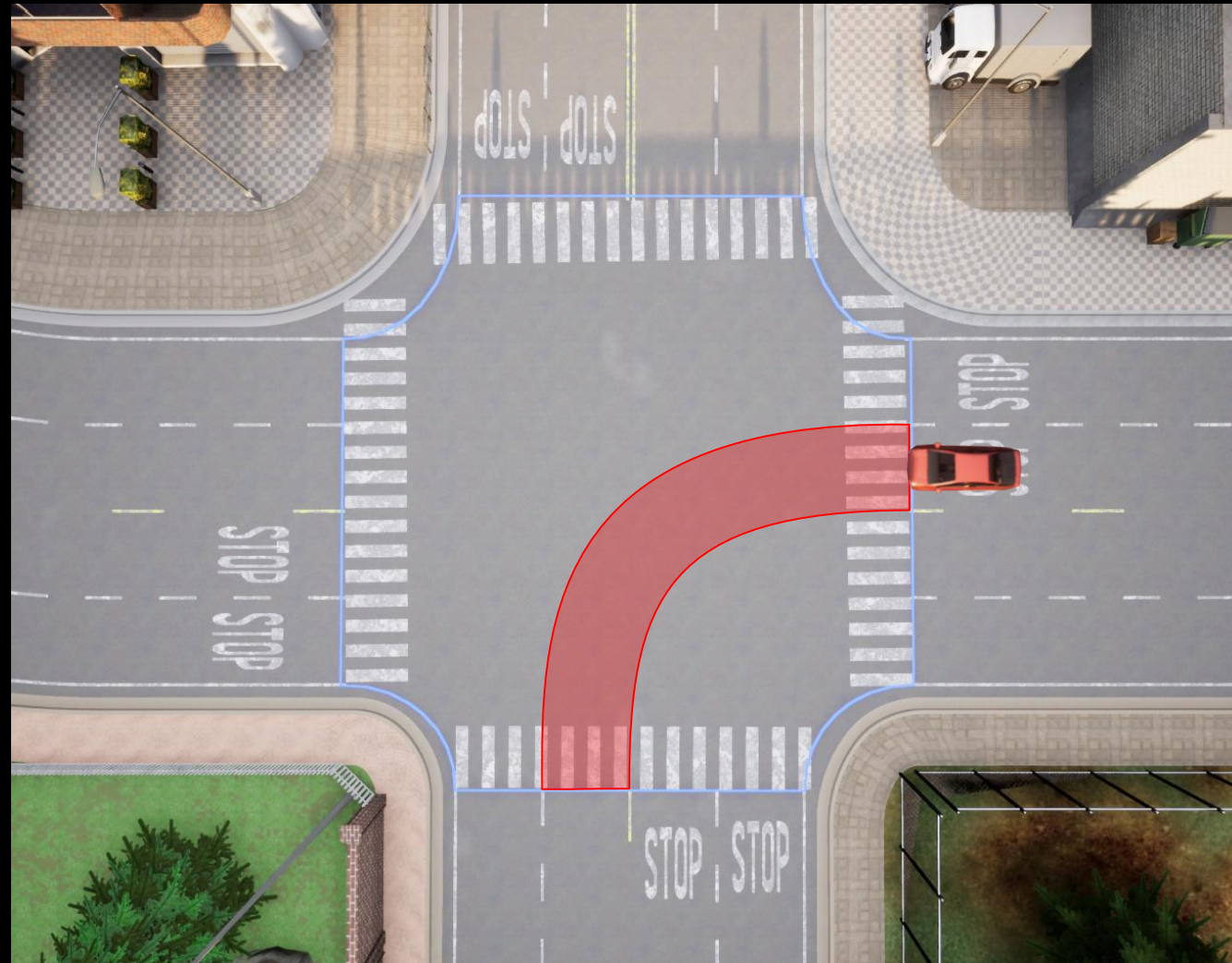


# Event: arrival at intersection





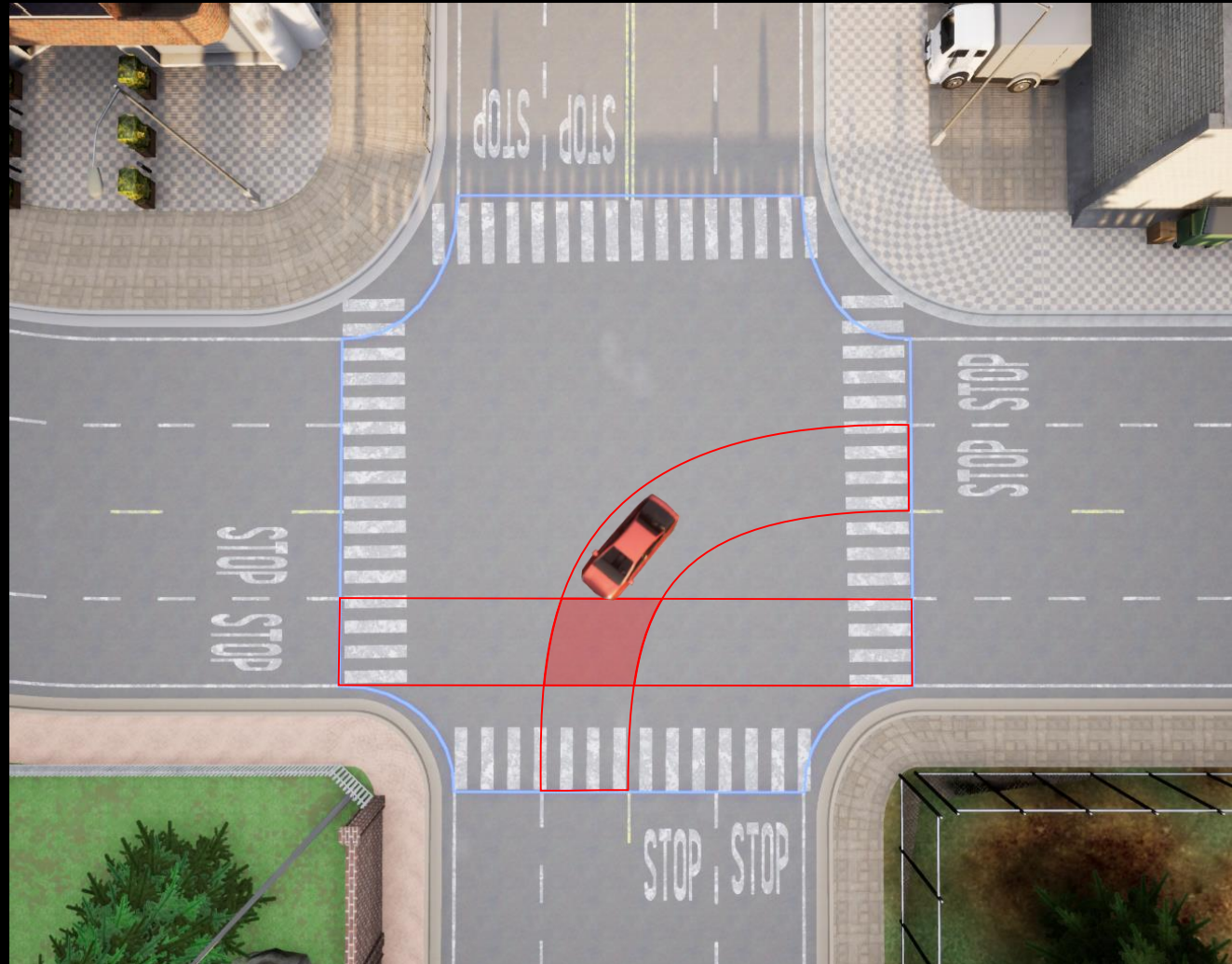
# Event: entering a lane





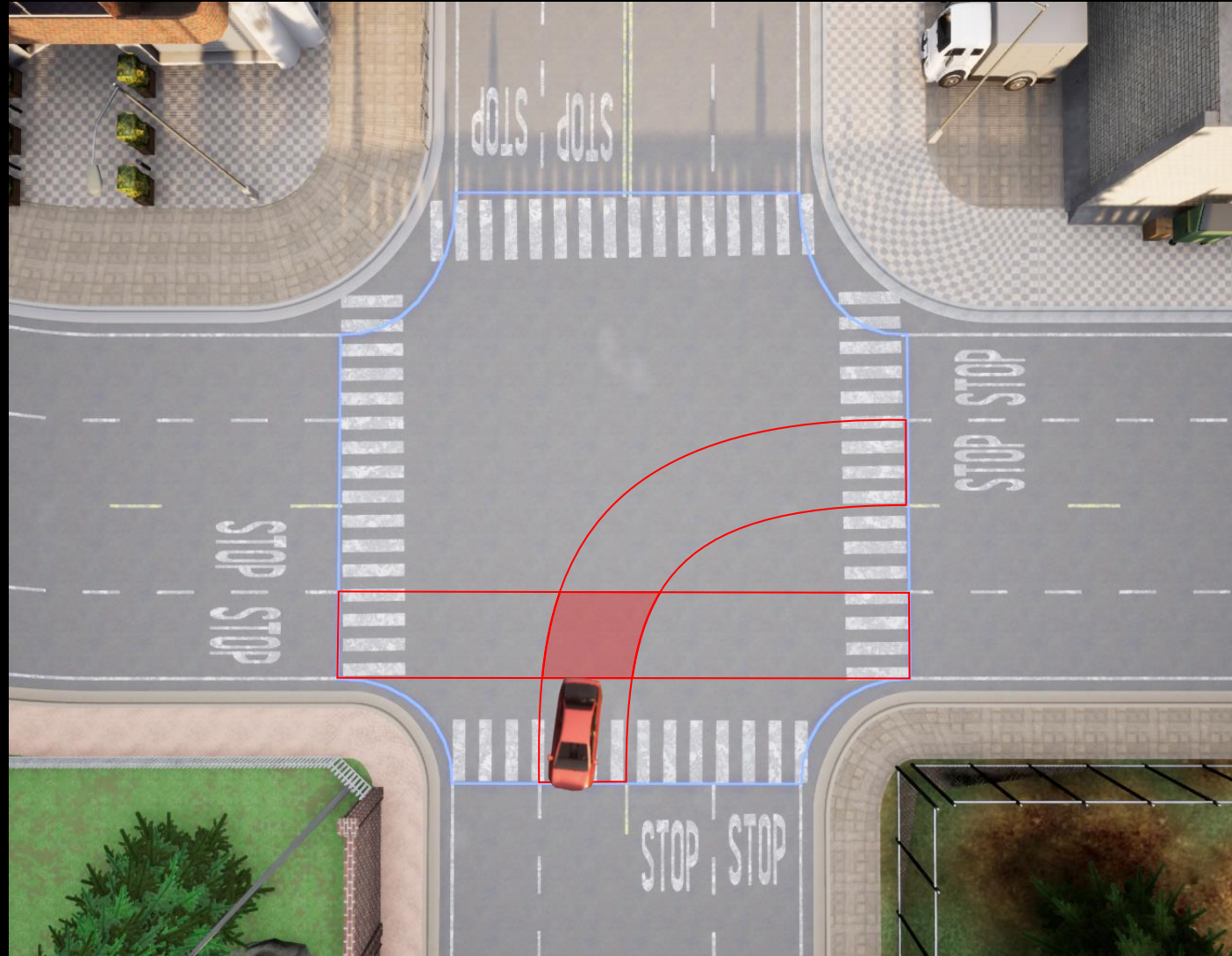


# Event: entering a shared section



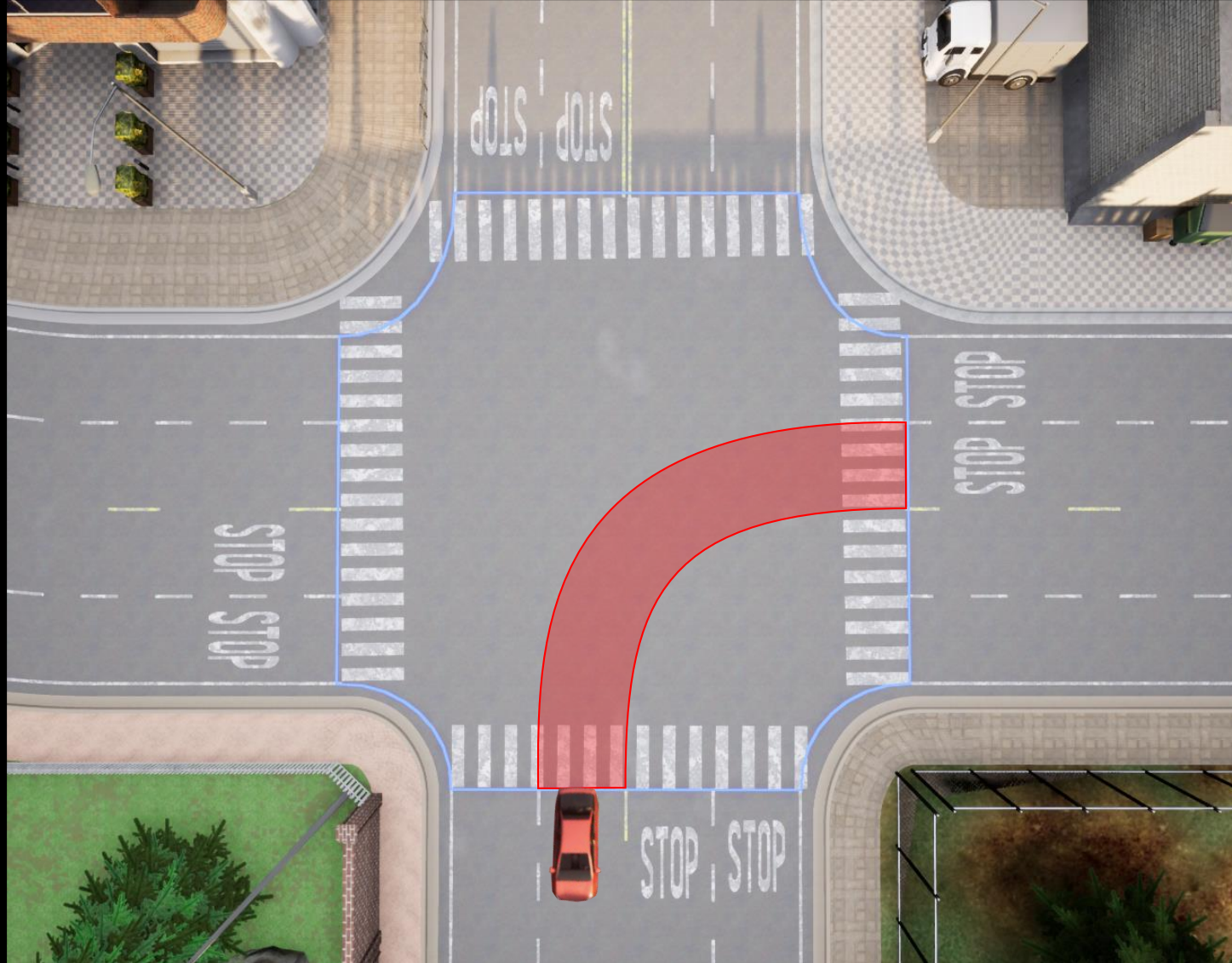


# Event: exiting a shared section





# Events: exiting a lane



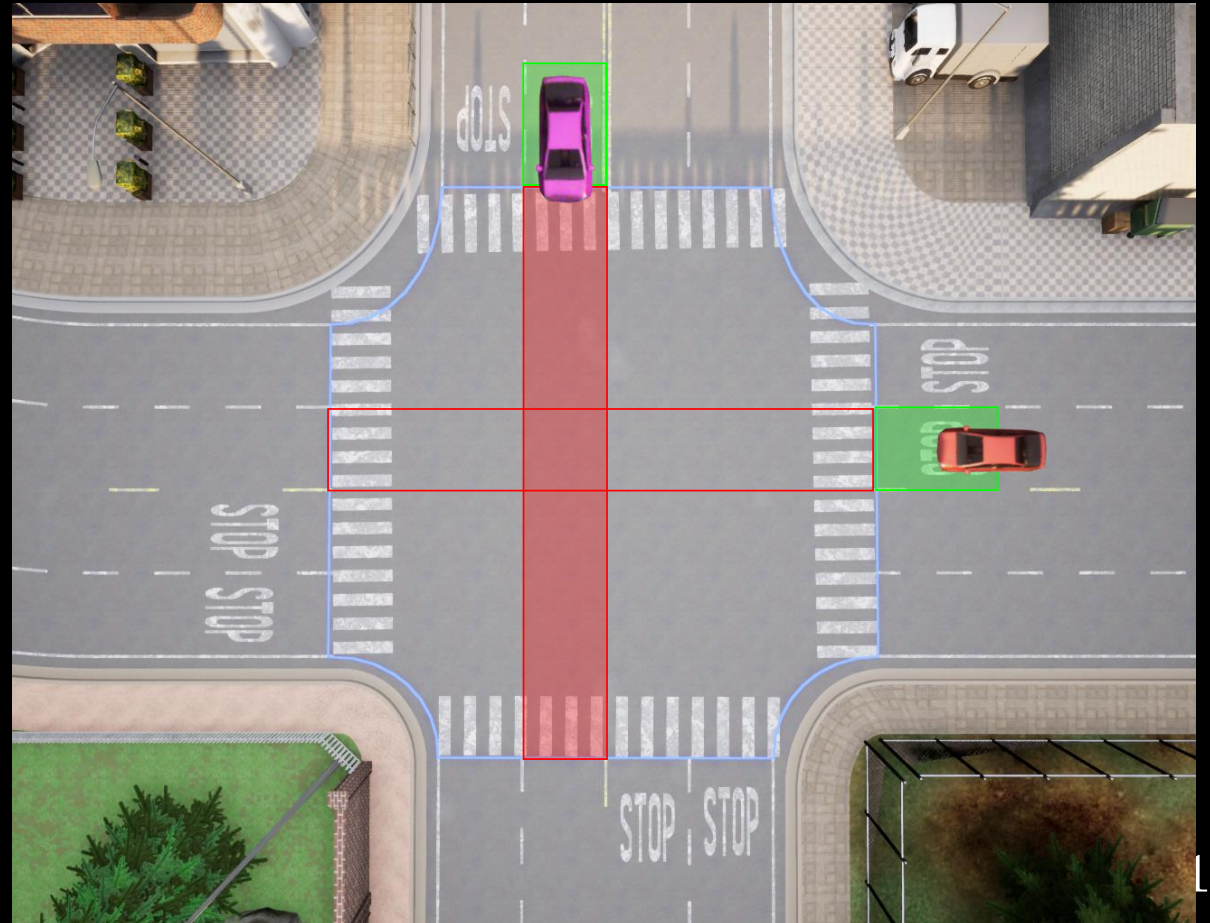


# Relative order of events

Pink arrives first.



Pink enters first.





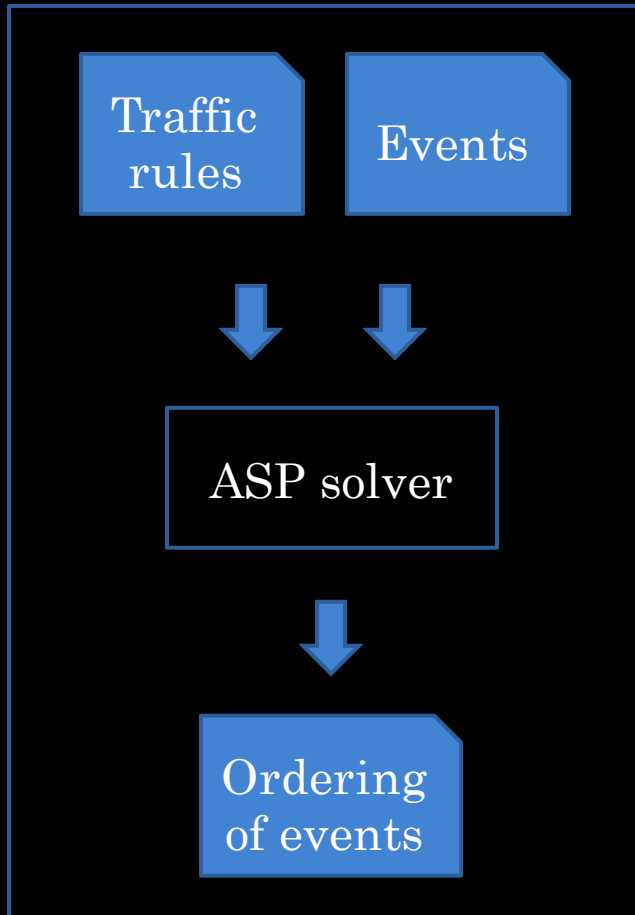
# Traffic rules and events' order

- *"whoever **arrives first**, should **enter first**."*
- *First-Order-Logic formulation:*

```
violatesRightOfForRule(V1, V2, fcfs) :-  
  arrivedAtTime(V1, Ta1),  
  arrivedAtTime(V2, Ta2),  
  lessThan(Ta1, Ta2),  
  enteredAtTime(V1, Te1),  
  enteredAtTime(V2, Te2),  
  lessThan(Te2, Te1).
```



# Order events using ASP



```
violatesRightOf(V1, V2) :-  
  arrivedAtTime(V1, Ta1),  
  arrivedAtTime(V2, Ta2),  
  lessThan(Ta1, Ta2),  
  enteredAtTime(V1, Te1),  
  enteredAtTime(V2, Te2),  
  lessThan(Te2, Te1).
```

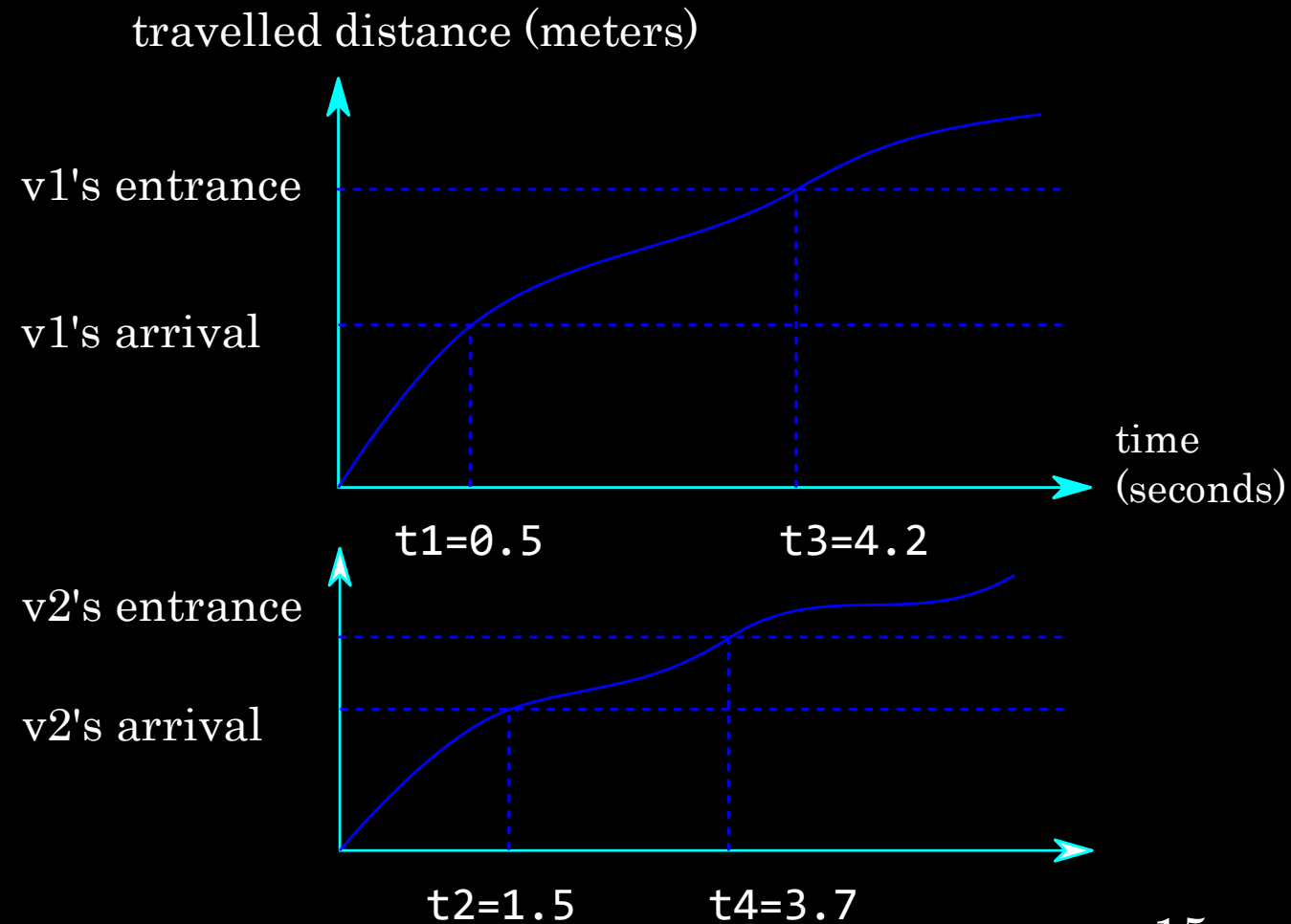
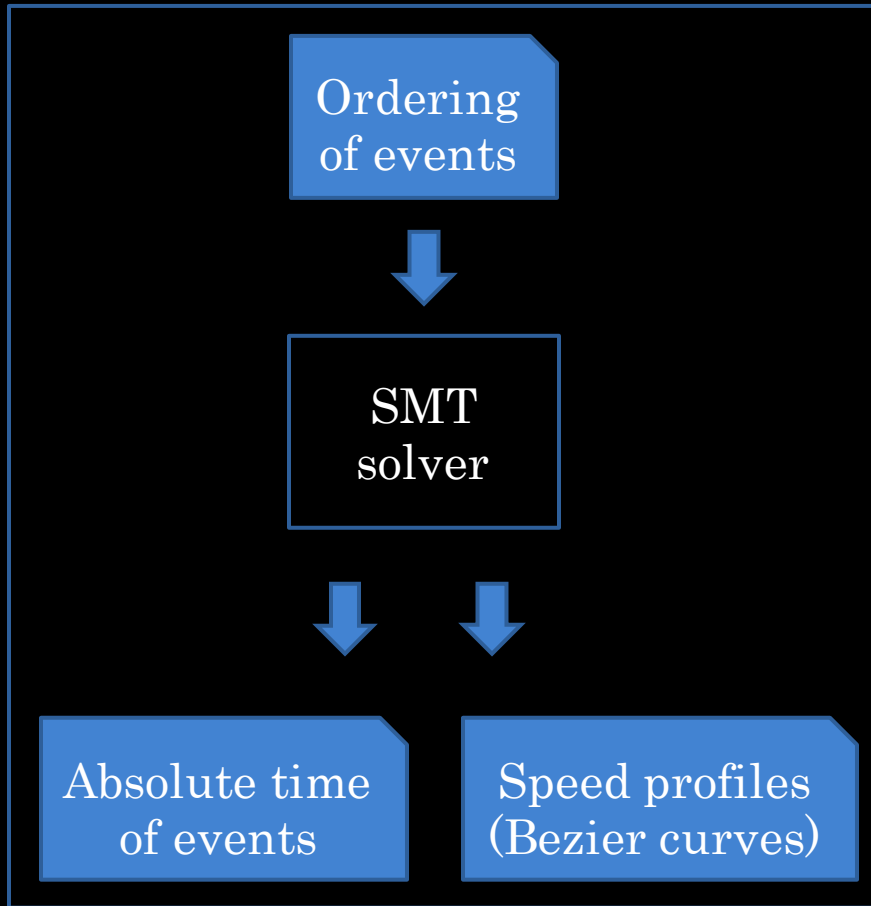
```
arrivedAtTime(v1, t1).  
arrivedAtTime(v2, t2).  
enteredAtTime(v1, t3).  
enteredAtTime(v2, t4).
```



```
lessThan(t1, t2).  
lessThan(t4, t3).
```

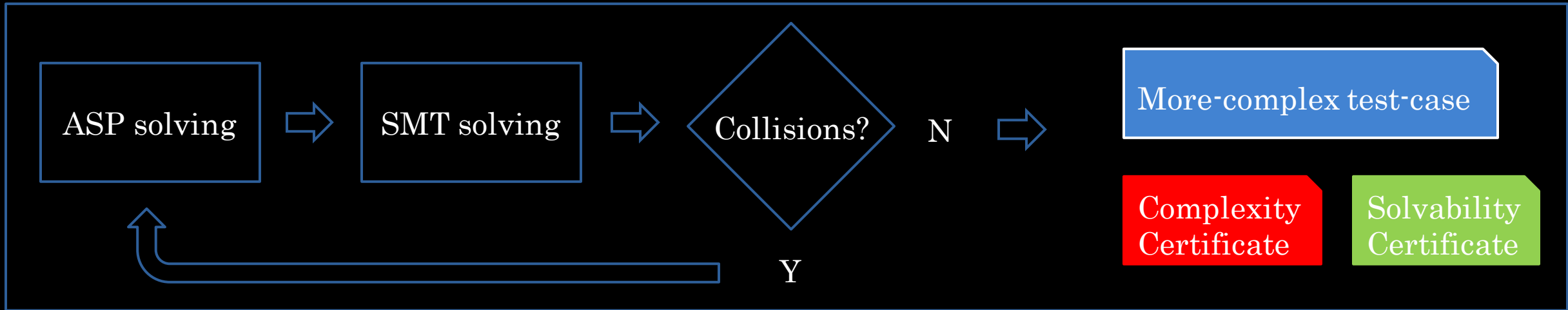


# Absolute timing of events using SMT





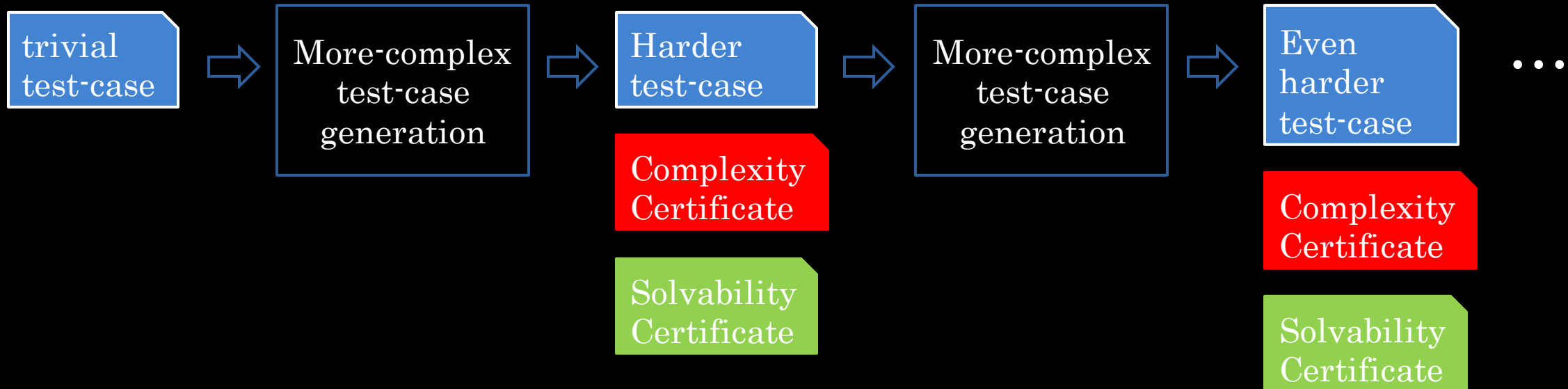
# ASP + SMT + collisions







# Sequence of increasingly more complex test-cases





# Results

- Generate test-cases
- Test autopilot
- Test autopilot + RSS
- Show certificates



# Autopilot **passes** Test-case 1





# Autopilot **fails** Test-case 2 !





# Autopilot+RSS passes Test-case 2 !





# Autopilot+RSS fails Test-case 3 !



# Test-case 2 certificates



- **Complexity Certificate:**
  - yields to Test-case 1 non-egos
  - violates a Test-case 2 non-ego
- **Solvability Certificate:**
  - yields to Test-case 1&2 non-egos





# Future work

1. Generating reactive scenarios:
  - a non-ego behavior is a function of ego
2. Numerical approximation of complexity
  - Finitization of trajectory space  
e.g. motion primitives and lattices
3. Better collision-checking (or enforcing)







# Extra slides



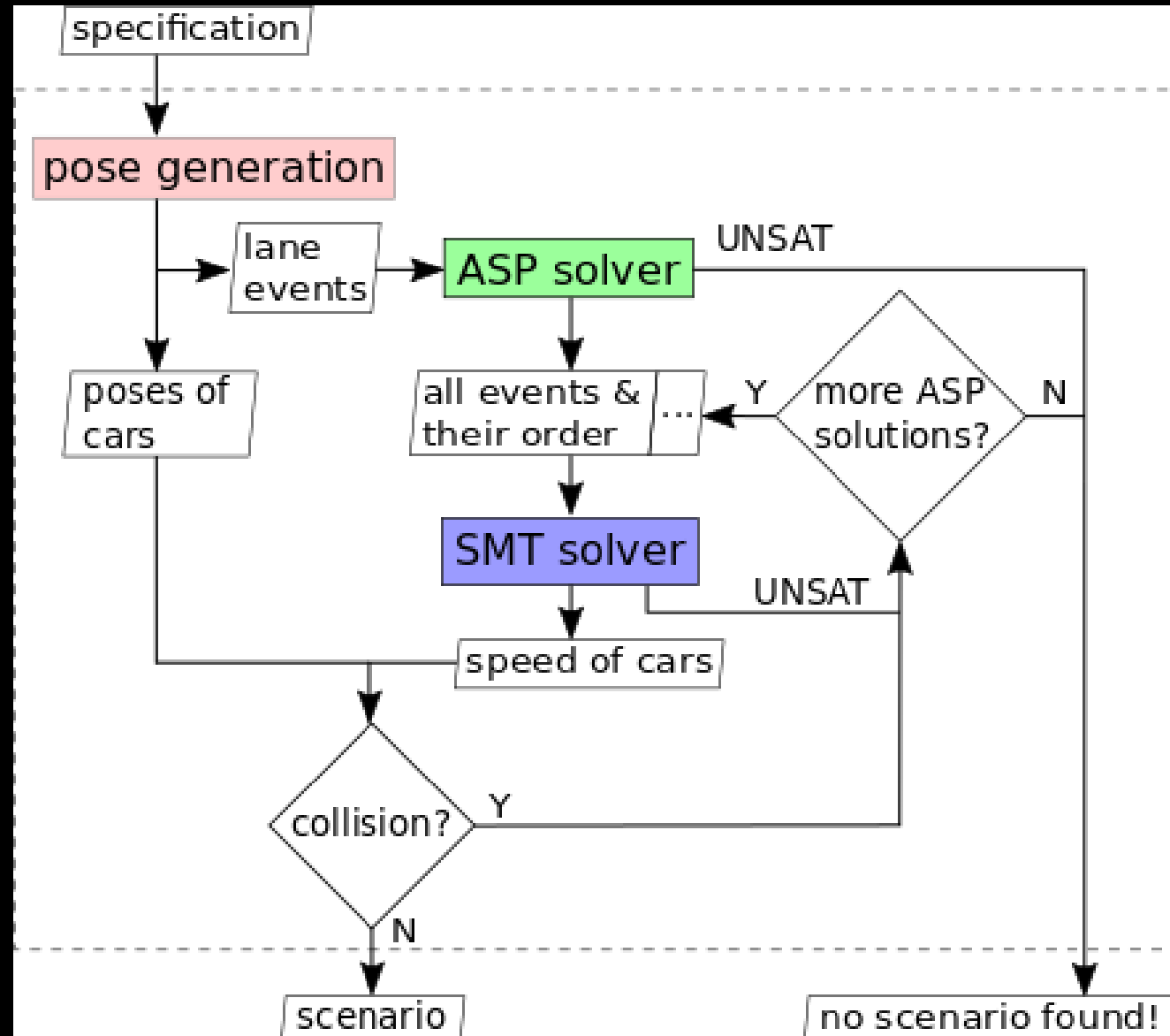
# Complexity of SMT constraints

- Linear constraints
  - Temporal order of events
  - Bounds on instantaneous speed at an event
    - Slope between control points
- Quadratic constraints
  - Continuity of speed
    - left slope = right slope
  - Bounds on acceleration



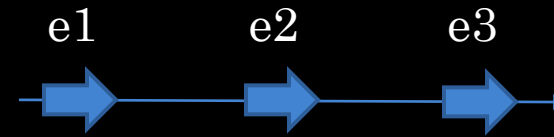
Autopilot+RSS passes Test-case 1

# Scenario Generation algorithm

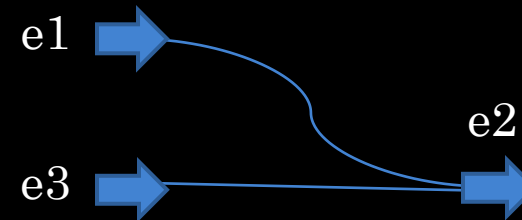




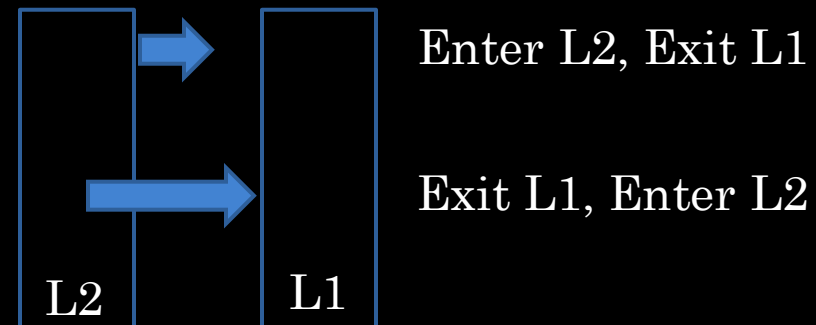
- No teleportation!



- Nonholonomic steering



- Size of vehicles





# Traffic rules and order of events

- Whoever arrives first, should enter first.
- If A and B arrive simultaneously and A is on the right of B, then A should enter first.
- ...



# Automatic test-case generation

## 1. Goal:

- Combinatorial coverage of sequence of events,  
VS probabilistic coverage (random sampling)

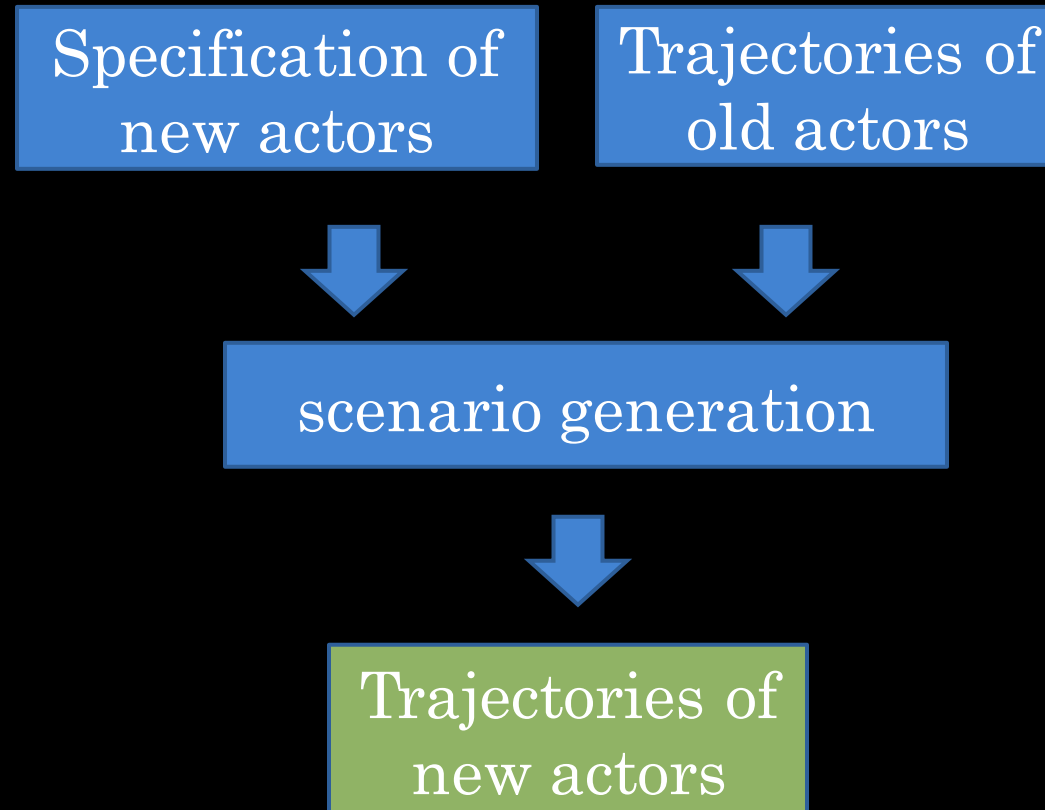
## 2. Constraints:

- Kinematics (nonholonomic steering, smooth velocities, ...)
- Collisions (vehicles cannot pass through each other)



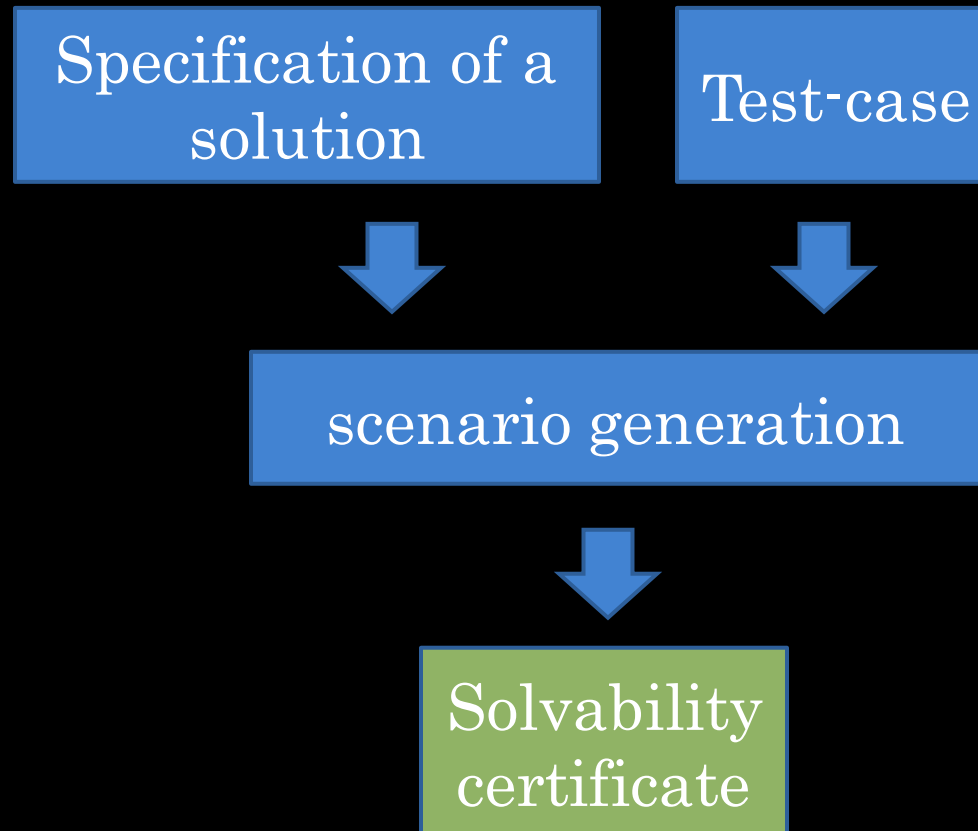


# Adding new actors to a scenario



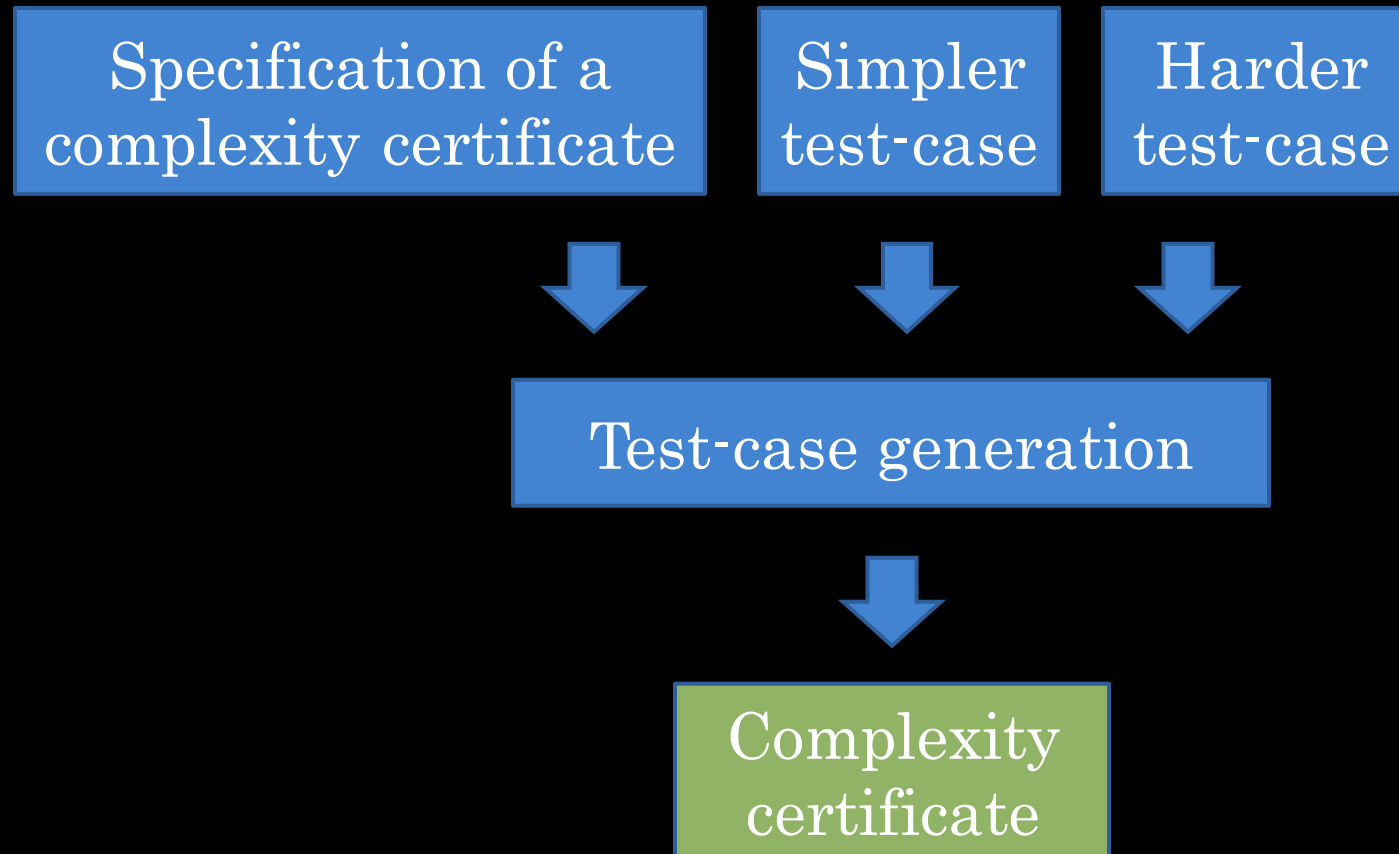


# Synthesizing solvability certificate

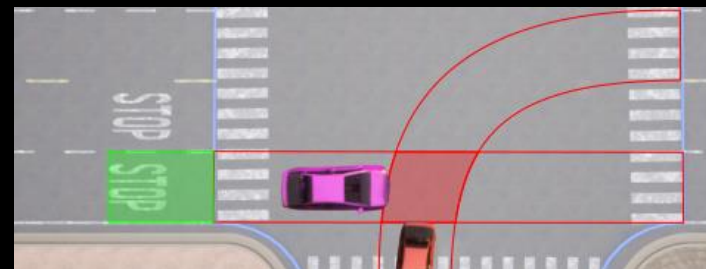
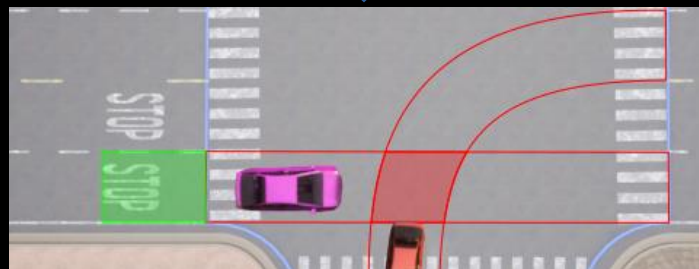
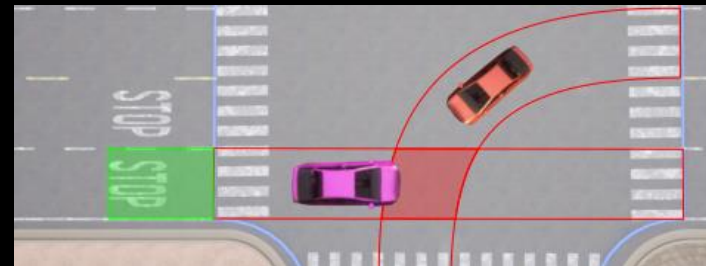
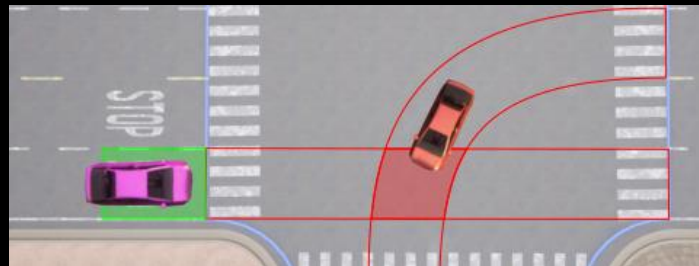
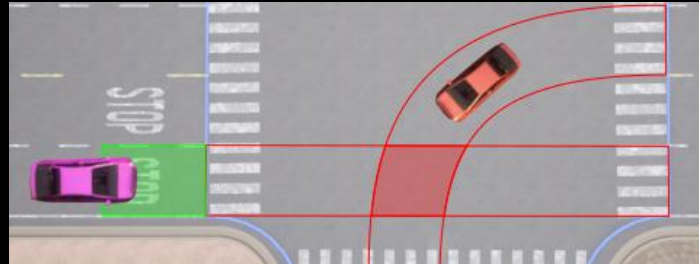




# Synthesizing complexity certificate



# Event ordering examples





# Test-case complexity

- Increases probability of failure
  - e.g. difficulty levels of video games
- Fair & efficient comparison of AVs
  - How many levels each AV passes?
- Interpretability
  - Event-level specification
  - Trajectory-level certificate (a blocked solution)



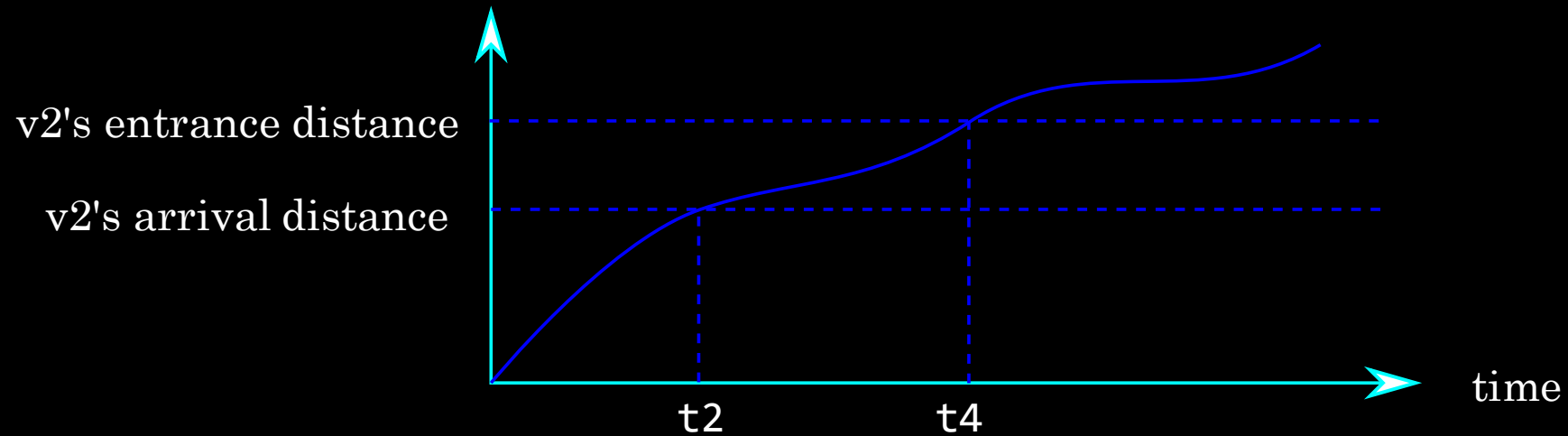
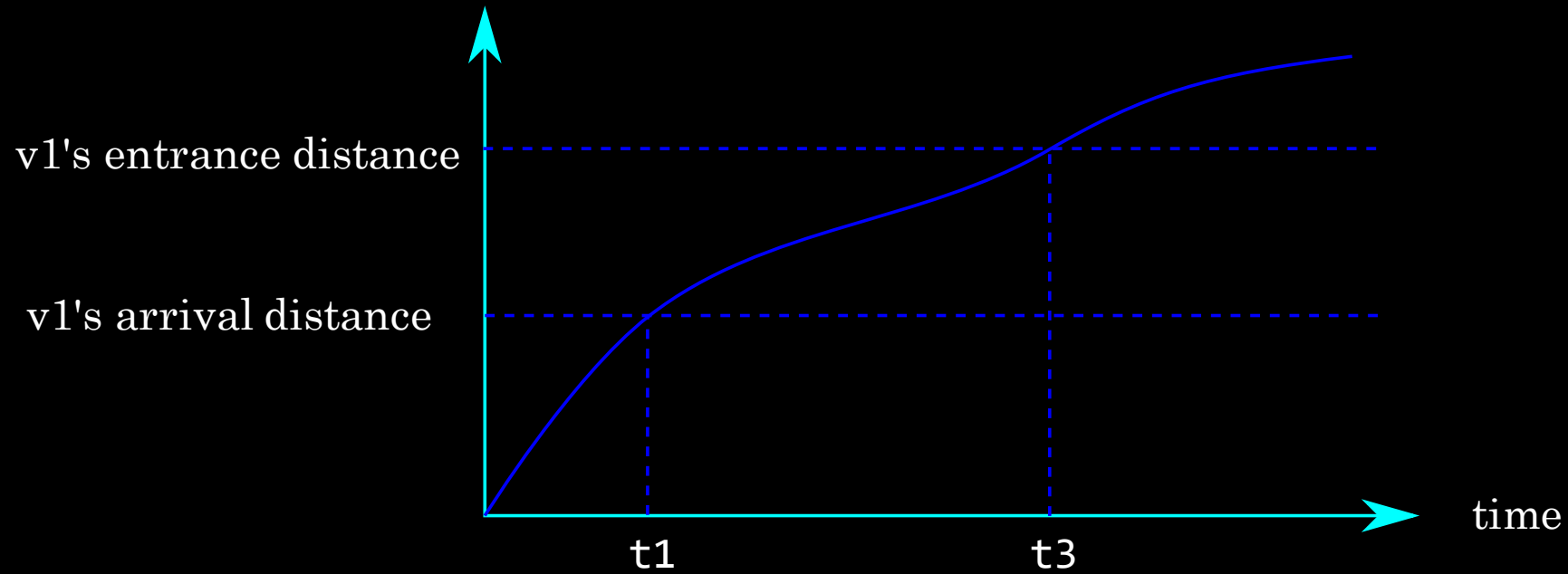
# Test-case generation: events



```
arrivedAtTime(v1, t1).  
arrivedAtTime(v2, t2).  
:- violatedRightOf(v2, v1).
```

```
lessThan(t1, t2).  
enteredAtTime(v1, t3).  
enteredAtTime(v2, t4).  
lessThan(t4, t3).
```

# Test-case generation: velocities





# Scenario-based testing

- System-level vs. Component-level
- External vs. internal behavior
  - traffic rules vs. energy consumption
- Blackbox
- Simulation-based





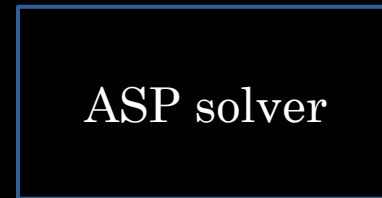
# Forcing increase in complexity

Given an old test-case, generate a more-complex new test-case

Event-level specification of  
scenario

+

Specification of a  
complexity evidence



Lane events and  
their temporal order

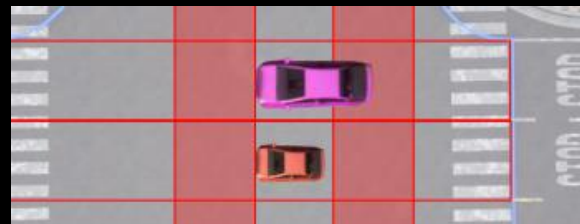


Complexity  
Certificate

Solvability  
Certificate

Complexity  
Certificate

Solvability  
Certificate



L2 L1

Enter L2, Exit L1

Exit L1, Enter L2