Lecture 2: Introduction to Computer Graphics

Representing geometry, cameras, reflectance, lighting, and rendering images

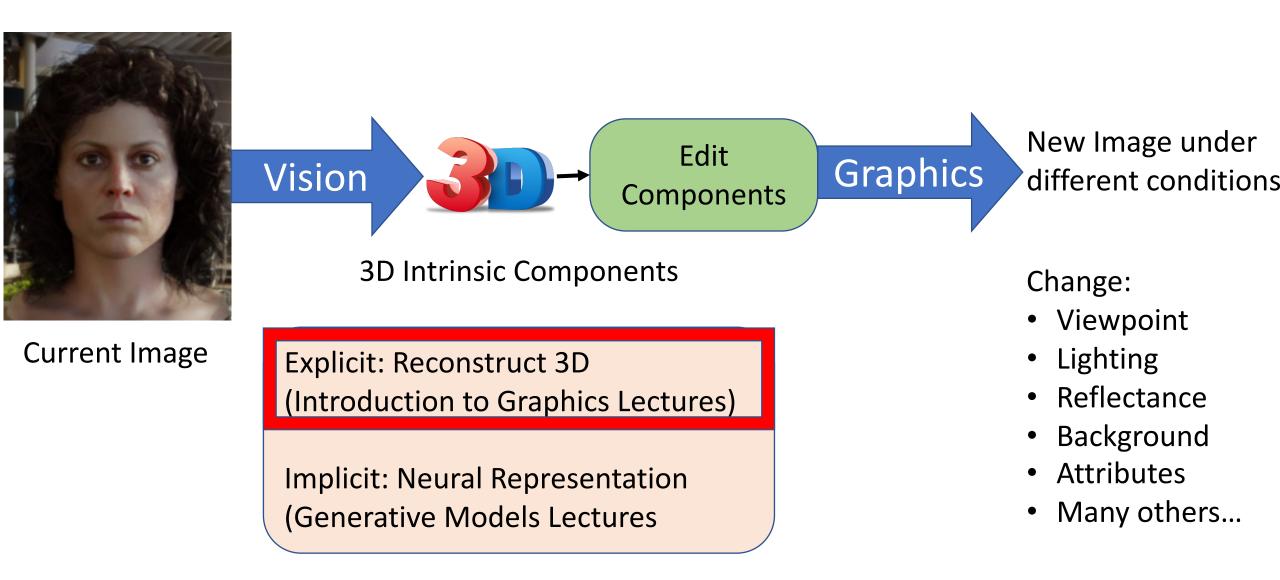
Respond at **PollEv.com/ronisen** Text **RONISEN** to **22333** once to join, then text your message

Feel free to share your questions...

Few reminders

- 590: Assignment 1 is out, due date next Thursday Aug 25!
- 790: Starting planning your project proposal and forming your group. If you want to work on your own project, send an email, explain why, and have my written approval.
- 590/790: Please indicate your paper presentation preference by filling out the google form (See course website, under presentation).
- Change in grading plans:
 - Paper presentation: only 790
 - Paper review: only 590
 - 590: 5 assignments instead of 4, but significantly easier, 4 assignment can be done on google colab.

How does Computer Vision & Graphics work together?



Agenda

- How do we define geometry/shape of an object?
- How do we define a camera model? 3D object to 2D image
- How do we define material property? glossy, metallic

Slide Credits

- UC Berkeley CS 184/284a Spring 2021 (Ren Ng, Angjoo Kanazawa)
- CMU 16-385 Computer Vision Spring 2017 (Kris Kitani)
- Many amazing research papers!

Agenda

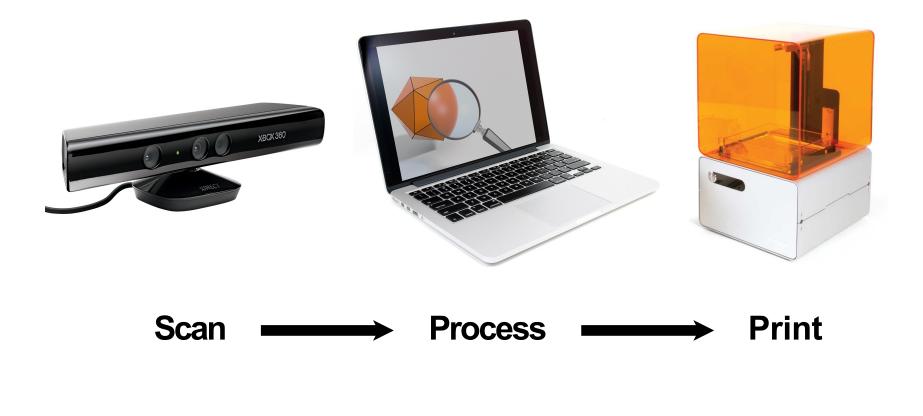
- How do we define geometry/shape of an object?
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Digital Geometry Processing





Geometry Processing Pipeline



How do we represent geometry?

Geometry: How do we represent shape of an object?

2.5D representation:1) Depth & Normal map

Explicit representation:

- 2) Mesh
- 3) Voxels
- 4) Point Cloud

Implicit representation:

5) Surface Representation (SDF)

Geometry: How do we represent shape of an object?

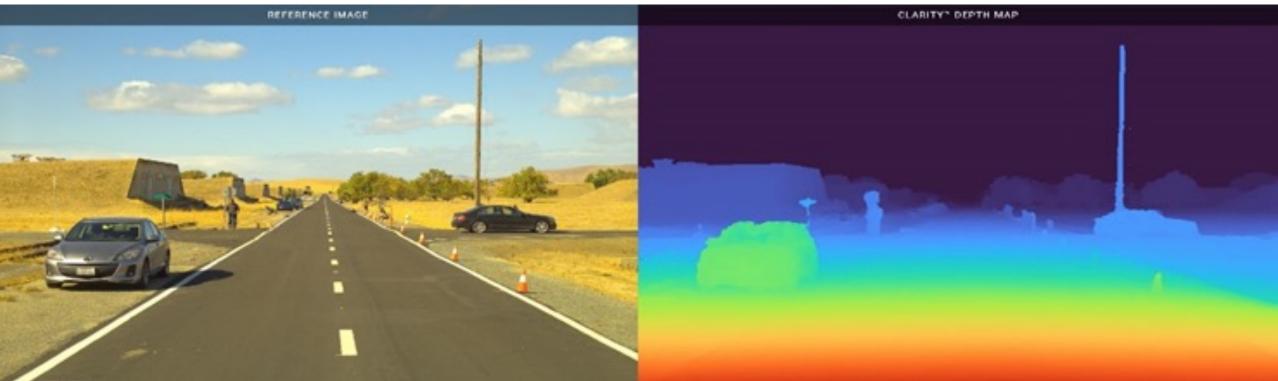
2.5D representation:1) Depth & Normal map

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Depth Map

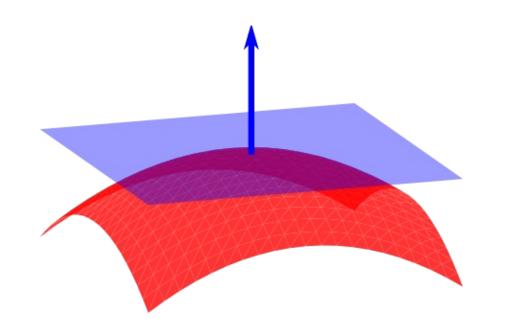


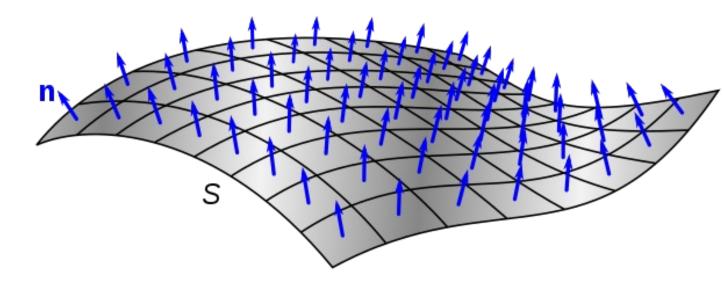
Depth Map D(u,v): Distance of any pixel (u,v) from the camera (usually image plane)

Red-> nearer; blue-> further

For an image HxWx3, a depth map is HxWx1 (scalar value for every pixel)

Surface Normal



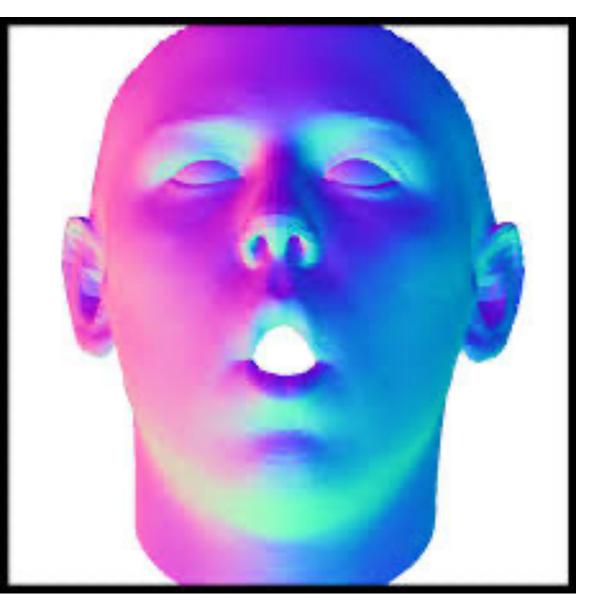


Surface Normal (in blue) of a point P is a vector perpendicular to the tanget plane at P.

Surface normal (in blue) of a surface

Surface normal indicate orientation of the surface.

Normal Map



Normal Map N(u,v): [Nx,Ny,Nz] is a unit vector indicating the orientation of the surface.

Pink-> towards left; blue-> towards right

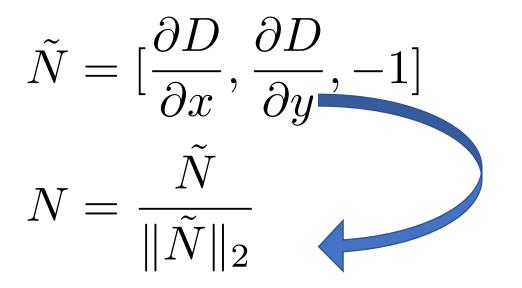
For an image HxWx3, a normal map is HxWx3.

What is a unit vector?

- L2 norm (magnitude) of the vector is 1.
- $-Nx^{2} + Ny^{2} + Nz^{2} = 1$

Credits: ibug imperial college london

Relationship between Depth & Normal Map



Normalizing to unit vector.

- Differentiation of depth map leads to normal map
- Integration of normal map leads to depth map

Further reading: Normal Integration: A Survey

Geometry: How do we represent shape of an object?

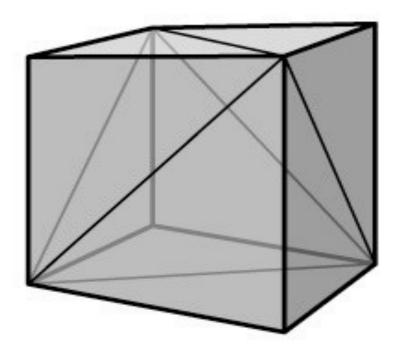
2.5D representation: 1) Depth & Normal map

Explicit representation: 2) Mesh 3) Voxels 4) Point Cloud

Implicit representation:

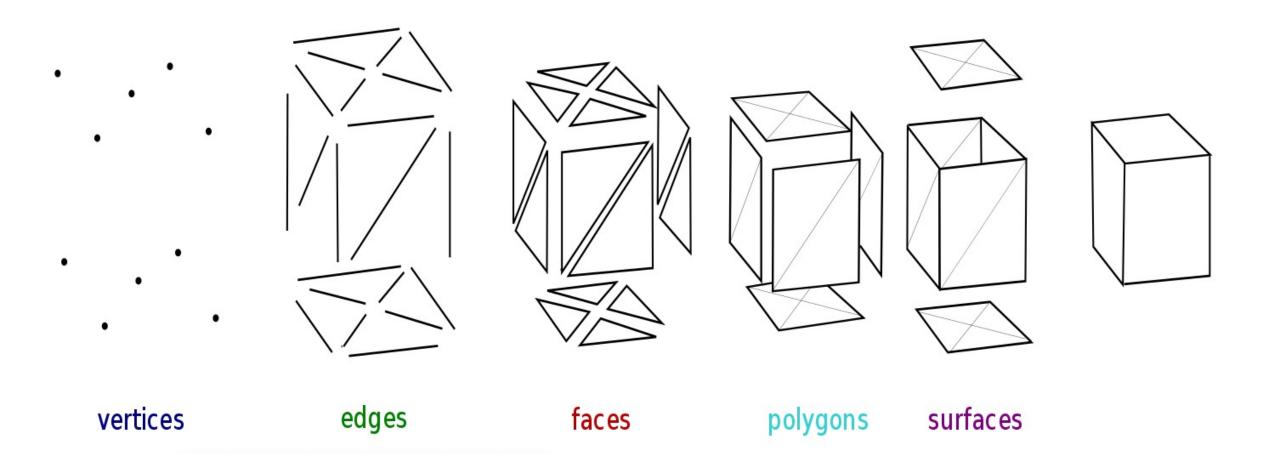
5) Surface Representation (SDF)

A Small Triangle Mesh



8 vertices, 12 triangles

Mesh



How do you represent a mesh file?

Wavefront .obj file

A list of vertices defined by their 3D x,y,z coordinates

v =0.23876920554499864 1.3103797270601687 0.13001260700009193 v =0.27582915374543276 1.2582563331865875 0.12364597630502337 v =0.2674888336016338 1.3474373225751202 0.15912747459742976 v =0.3128662756980407 1.222713216834852 0.14623565543301947

A list of faces that defines which vertices will combine to produce a triangle on the mesh

Note: This is the most naïve way of defining a mesh. You can add vertex normal, vertex texture, separate material model, and many other things with the .obj format.

MeshLab: a great software to load and visualize a mesh in 3D!

Show demo of using MeshLab to view an object in 3D

Texture Mapping: How do you add color/texture on a mesh?



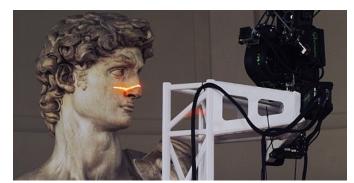
- Texture map is a 2D image
- Texture mapping takes the RGB color of each pixel (u,v) from the texture map and colors a vertex V (x,y,z) of the mesh.
- Color of each faces (triangles of the mesh) are often interpolated between the 3 vertex colors
- Note: Many variation of the above algorithm exist.

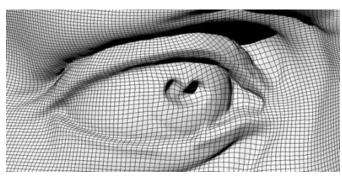
Few important/cool research works on meshes

A Large Triangle Mesh

David

Digital Michelangelo Project 28,184,526 vertices 56,230,343 triangles

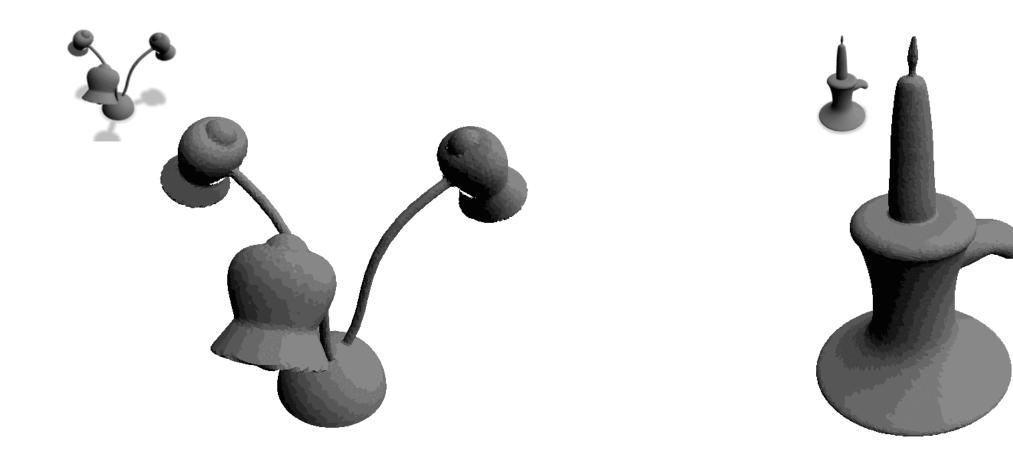






Marc Levoy at Stanford (https://accademia.stanford.edu/mich/)

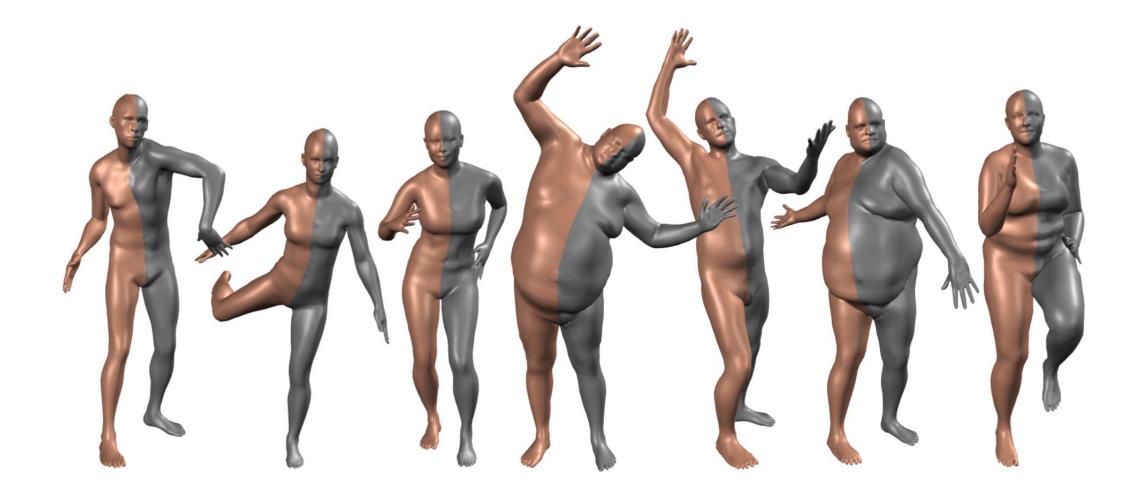
Text2Mesh, CVPR'22



A Brick Lamp

Colorful Crochet Candle

SMPL model, MPI



Geometry: How do we represent shape of an object?

2.5D representation: 1) Depth & Normal map

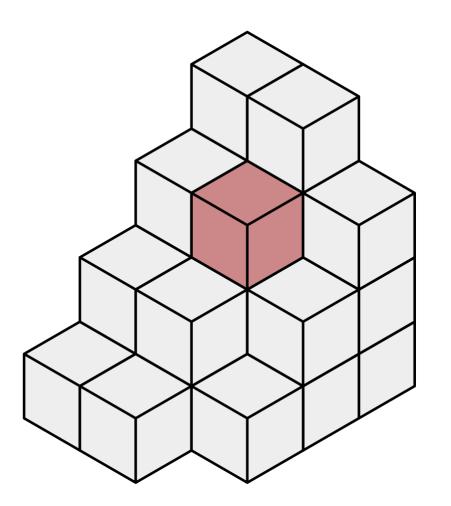
Explicit representation:

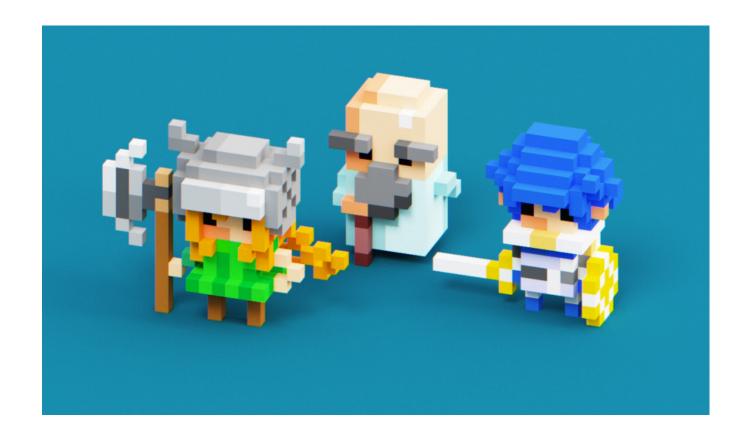
2) Mesh 3) Voxels 4) Point Cloud

Implicit representation:

5) Surface Representation (SDF) – implicit

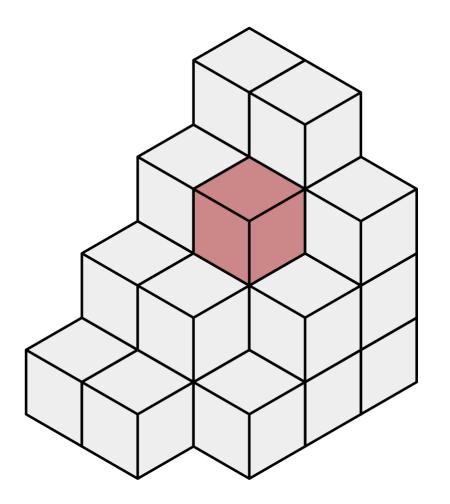
Voxel Representation

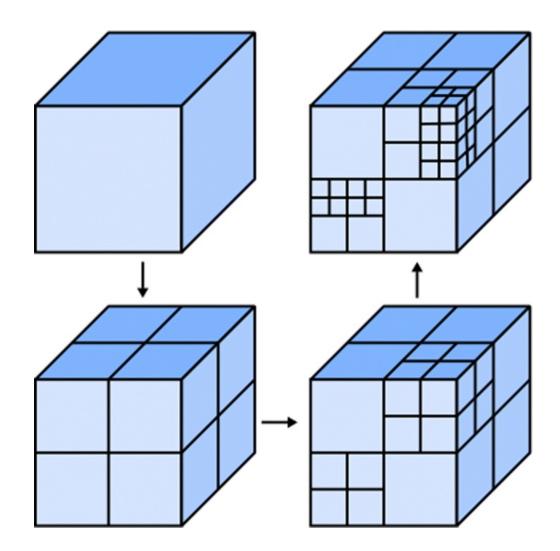




It's like playing with Lego!

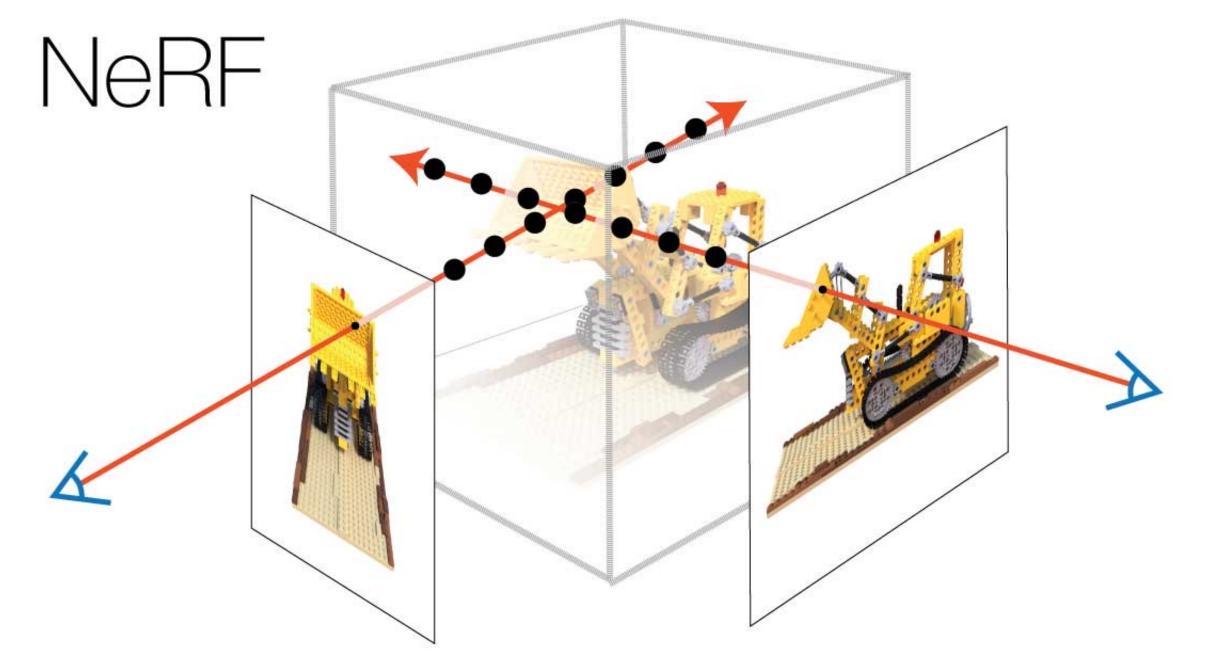
Voxel Representation





Voxel with octree

Few important/cool research works on voxels.



We will learn a lot about voxels in 2nd half of the class when we discuss NeRF.

Geometry: How do we represent shape of an object?

2.5D representation: 1) Depth & Normal map

Explicit representation:

2) Mesh 3) Voxels 4) Point Cloud

Implicit representation:

5) Surface Representation (SDF) – implicit

LiDAR and many other range sensors produces point cloud.

A REAL PROPERTY AND A REAL

Point Clouds



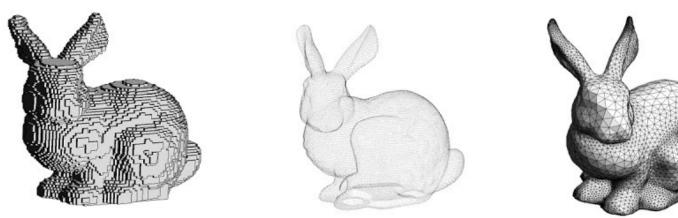
Sparse model of central Rome using 21K photos produced by COLMAP's SfM pipeline.



Dense models of several landmarks produced by COLMAP's MVS pipeline.

Started at UNC!! – Jan Michael Frahm's group

3D Representations (Explicit)



	Voxel	Point cloud	Polygon mesh
Memory efficiency	Poor	Not good	Good
Textures	Not good	No	Yes
For neural networks	Easy	Not easy	Not easy

We adopt polygon mesh for its high potential

Images are from

http://cse.iitkgp.ac.in/~pb/research/3dpoly/3dpoly.html

http://waldyrious.net/learning-holography/pb-cgh-formulas.xhtm

http://www.cs.mun.ca/~omeruvia/philosophy/images/BunnyWire.gif

Geometry: How do we represent shape of an object?

2.5D representation:1) Depth & Normal map

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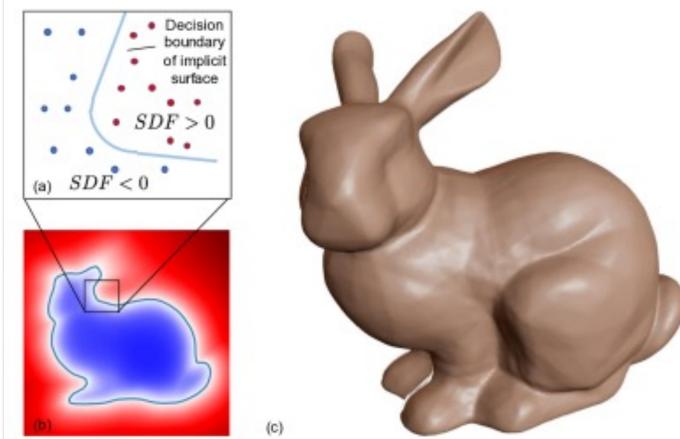
Implicit representation:

5) Surface Representation (SDF)

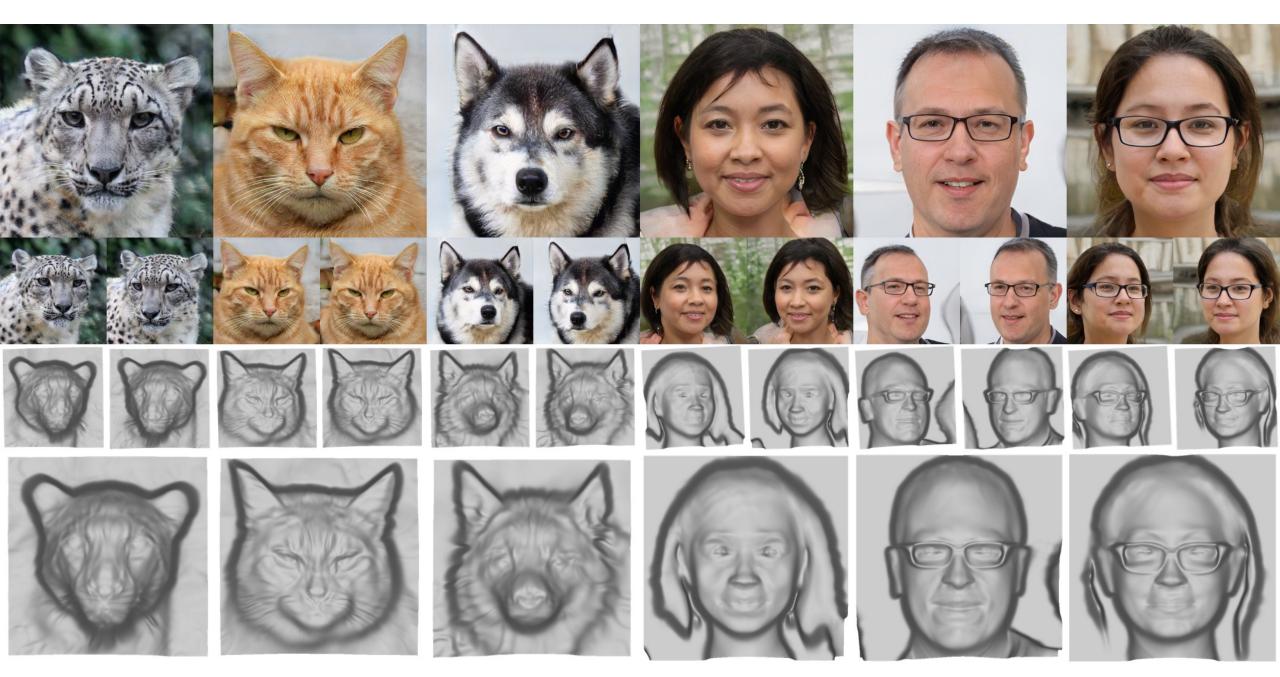
Surface Representation: Signed Distance Function (SDF) - implicit representation via level set

SDF(X) = 0, when X is on the surface. SDF(X) > 0, when X is outside the surface SDF(X) < 0, when X is inside the surface</pre>

Note: SDF is an implicit representation! Suitable for neural networks but hard to import inside existing graphics software.



Deep SDF: Use a neural network (co-ordinate based MLP) to represent the SDF function.



StyleSDF, Or-El et. al



Neural RGB-D Scene Reconstruction, Azinovic et. al.

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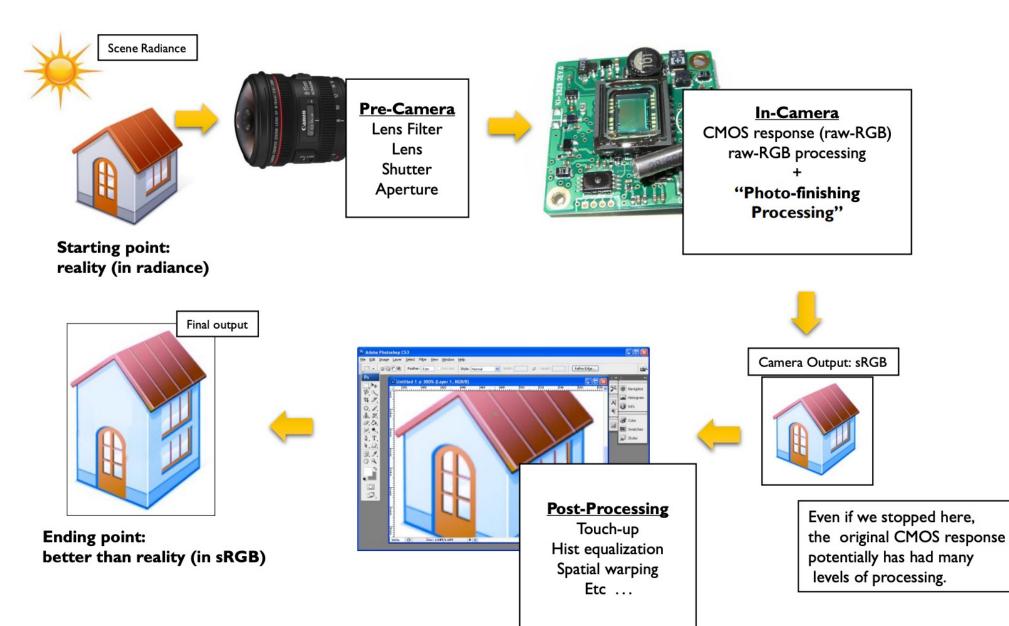
Feel free to share your questions...

Agenda

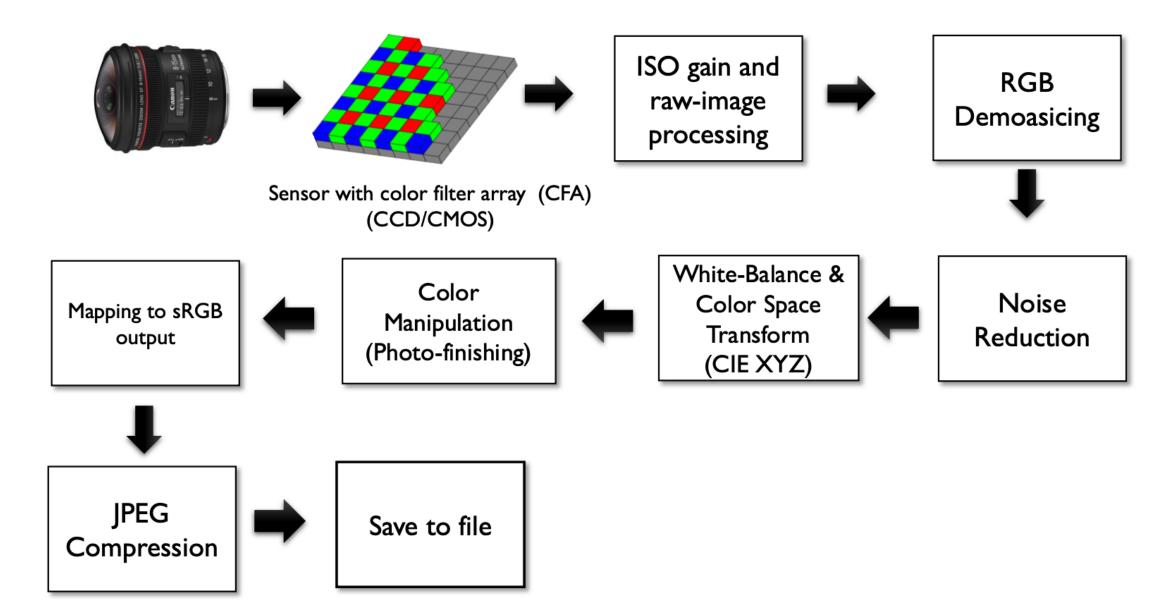
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- How do we define material property? glossy, metallic

Further reading: Understanding Color and the In-Camera Image Processing Pipeline for Computer Vision

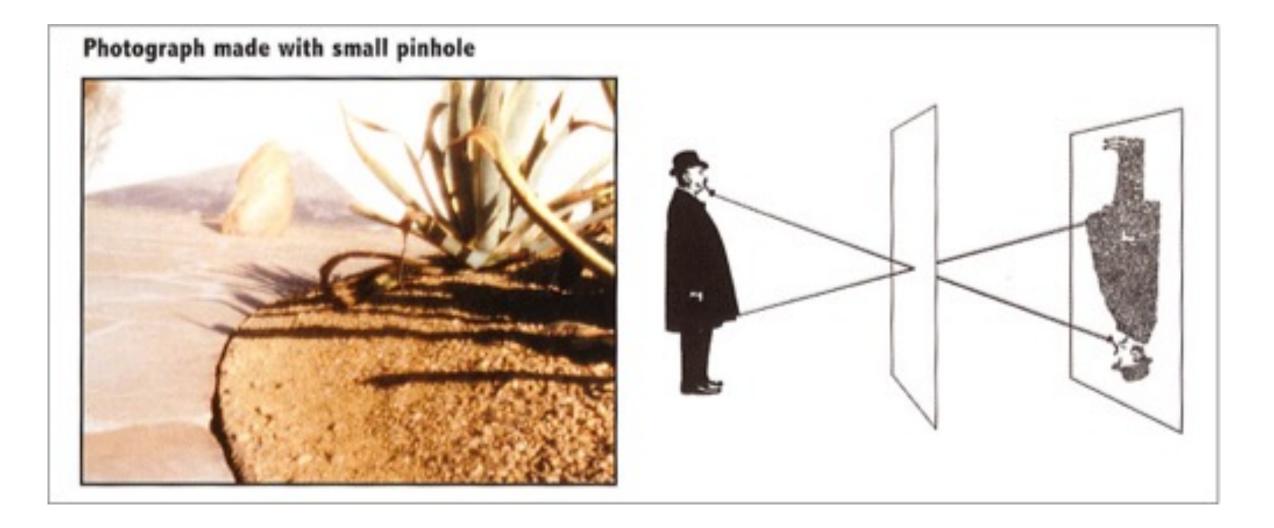
Modern photography pipeline



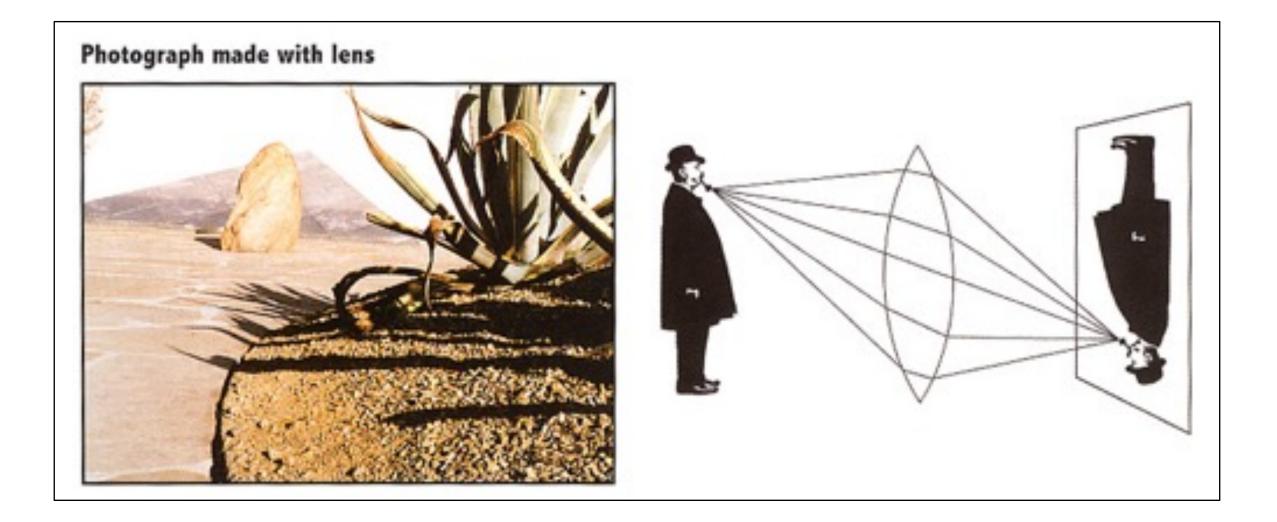
A typical color imaging pipeline



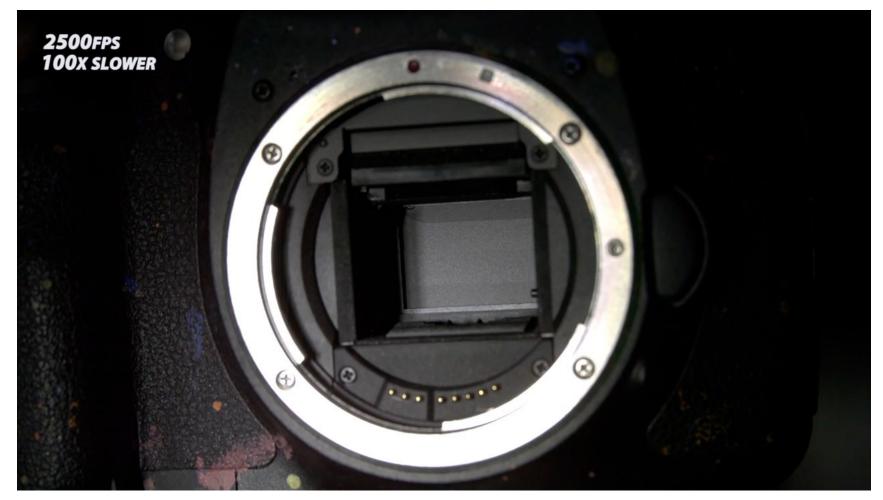
Pinholes & Lenses Form Image on Sensor



Pinholes & Lenses Form Image on Sensor



Shutter Exposes Sensor For Precise Duration



The Slow Mo Guys, https://youtu.be/CmjeCchGRQo

Sensor Accumulates Irradiance During Exposure

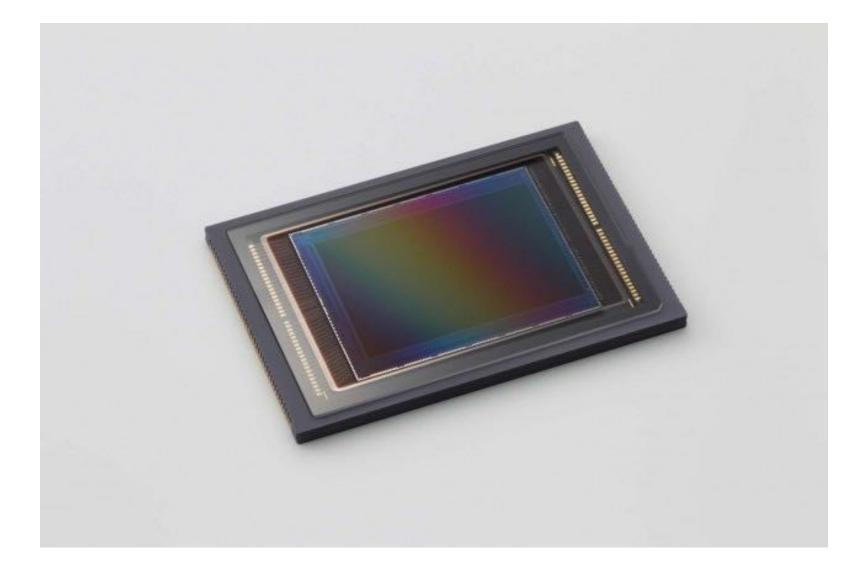
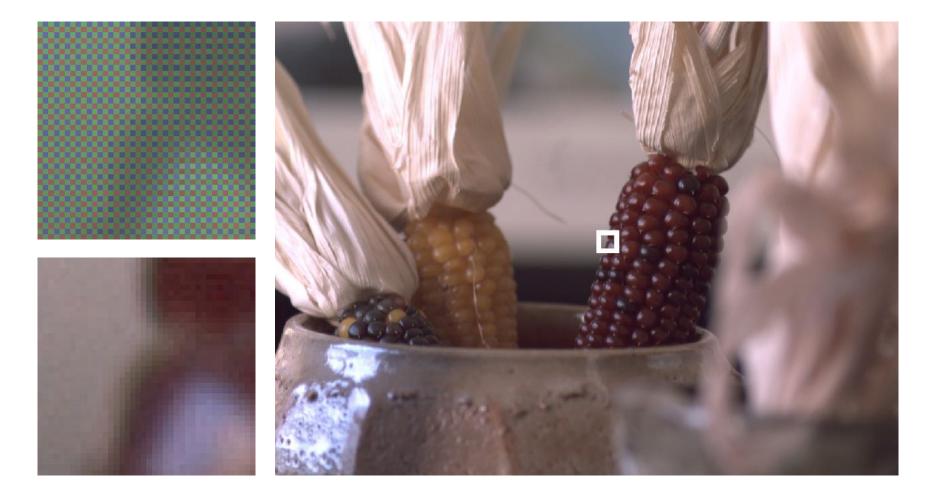
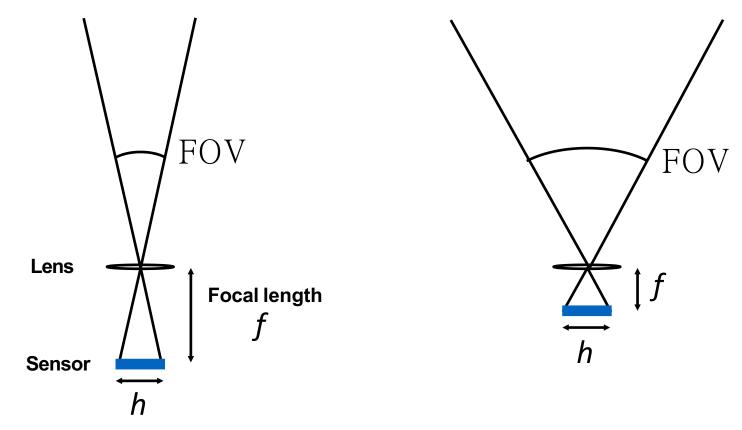


Image Processing: From Sensor Values to Image



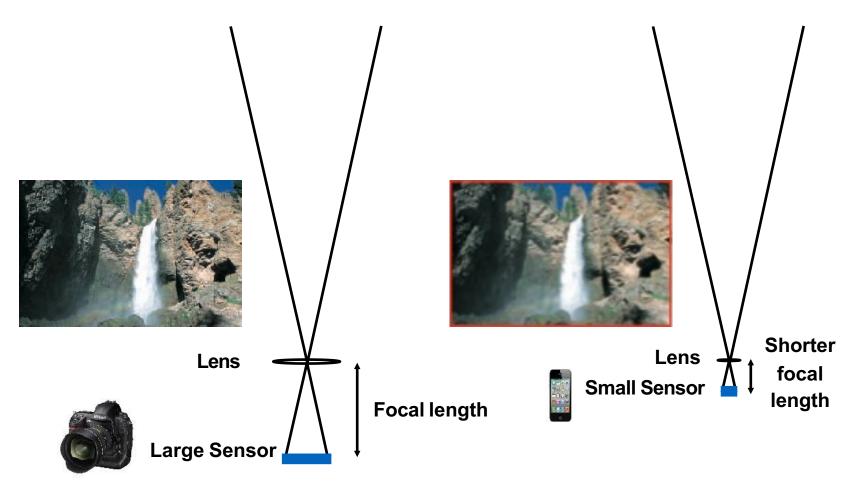
Optics of Image Formation: Field of View

Effect of Focal Length on FOV



For a fixed sensor size, decreasing the focal length increases the field of view. FOV = 2 arctan $\frac{h}{2f}$

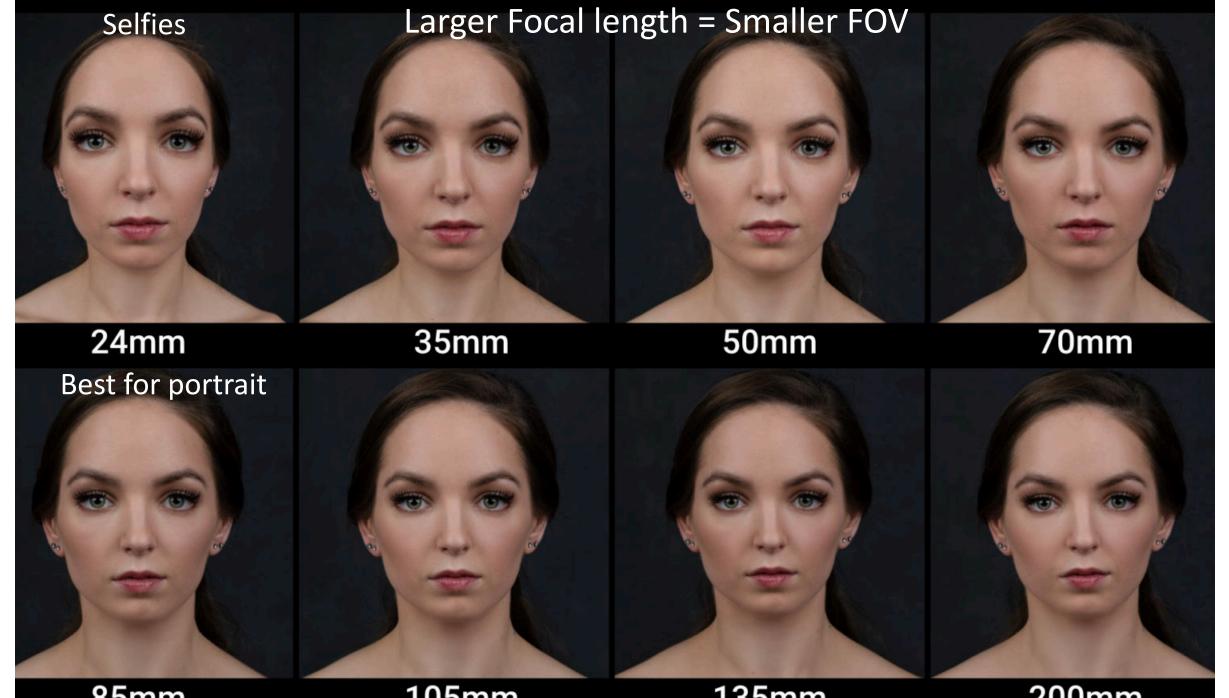
Maintain FOV on Smaller Sensor?



To maintain FOV, decrease focal length of lens in proportion to width/height of sensor

Larger Focal length = Smaller FOV





85mm

105mm

135mm

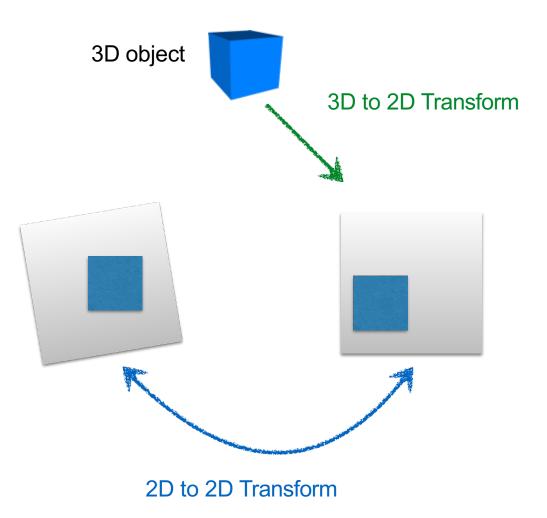
200mm

A camera is a mapping between

the **3D world**

and

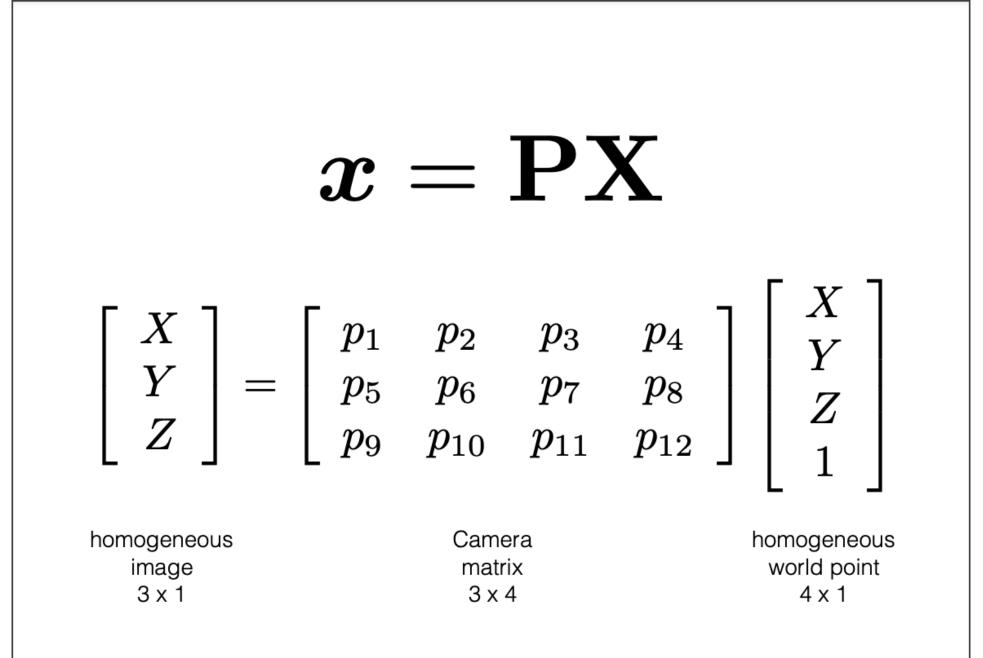
a 2D image



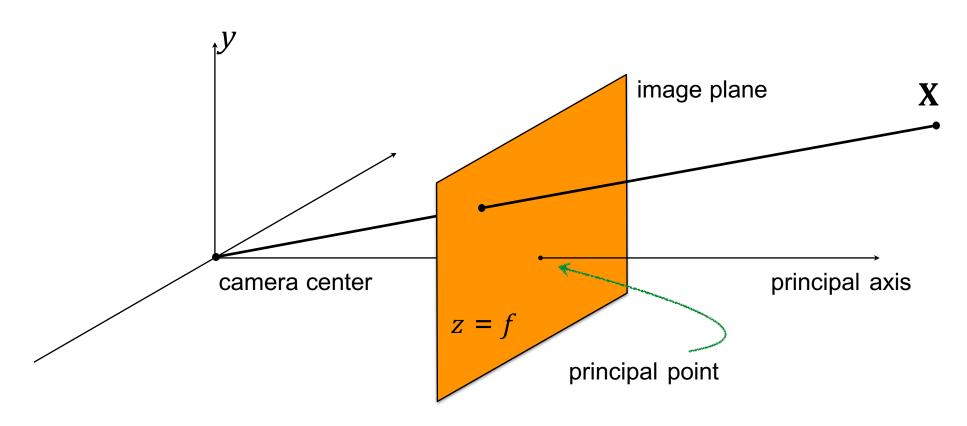
A camera is a mapping between the 3D world and a 2D image

$\mathbf{x} = \mathbf{P}\mathbf{X}$

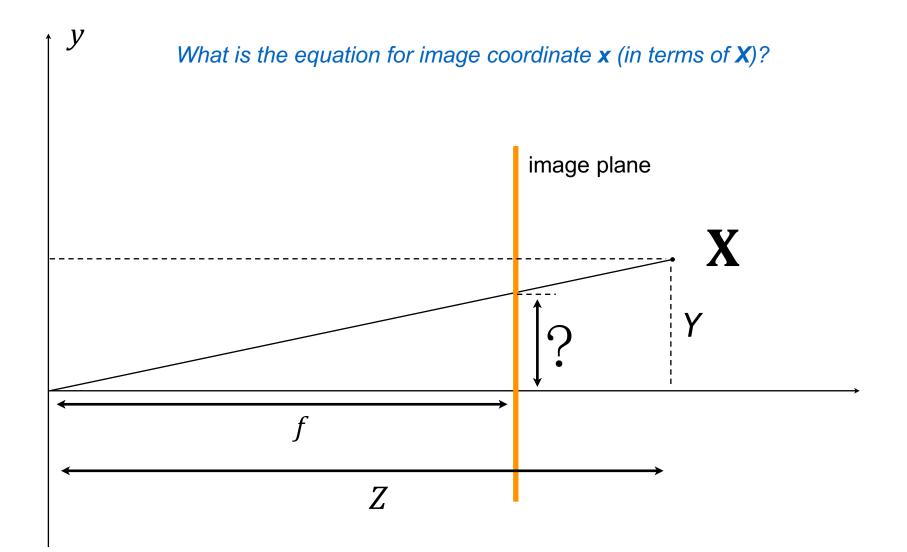
2D imagecamera3D worldpointmatrixpoint

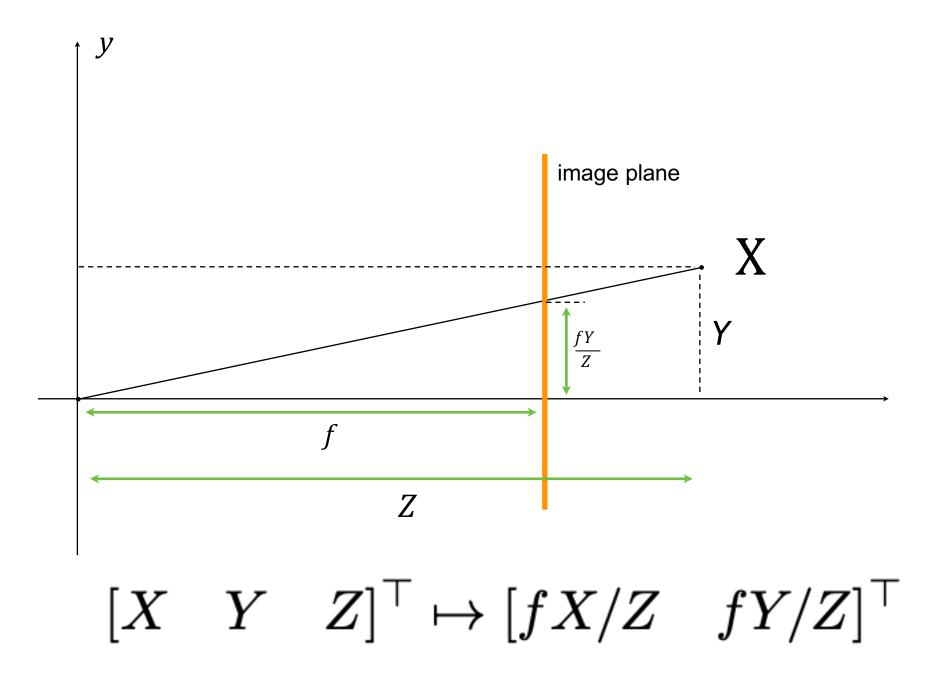


The pinhole camera

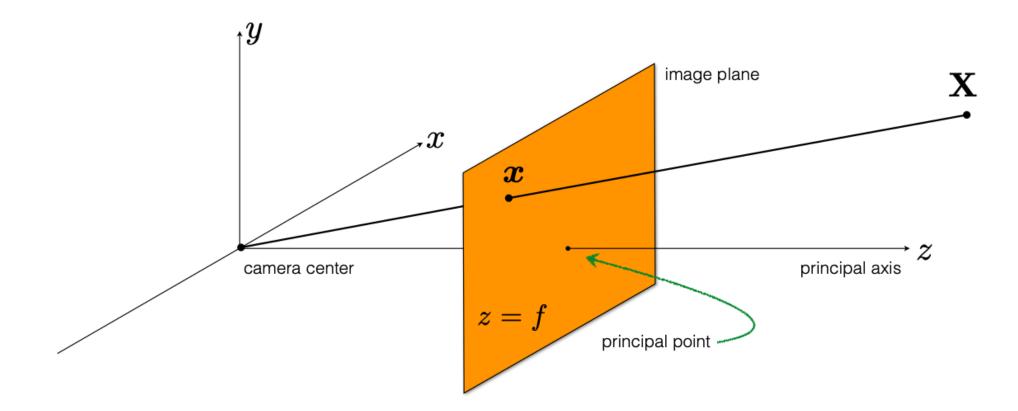


What is the equation for image coordinate **x** (in terms of **X**)?





Pinhole camera geometry



What is the camera matrix **P** for a pinhole camera model?

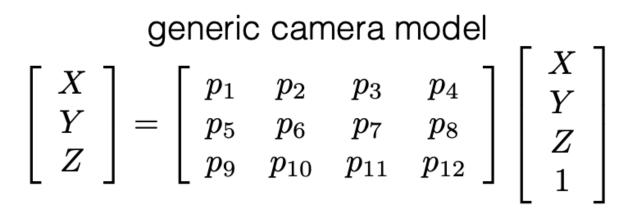
 $\boldsymbol{x} = \mathbf{P}\mathbf{X}$

Relationship from similar triangles... $[X \quad Y \quad Z]^\top \mapsto [fX/Z \quad fY/Z]^\top$

generic camera model
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

What does the pinhole camera model look like?

Relationship from similar triangles... $[X \quad Y \quad Z]^\top \mapsto [fX/Z \quad fY/Z]^\top$



What does the pinhole camera model look like?

$$\mathbf{P} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$$\mathbf{P} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

Camera origin and image origin might be different

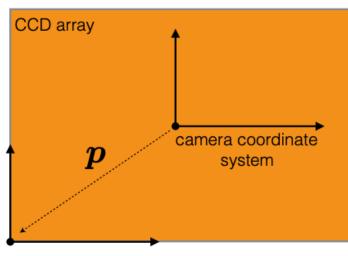


image coordinate system

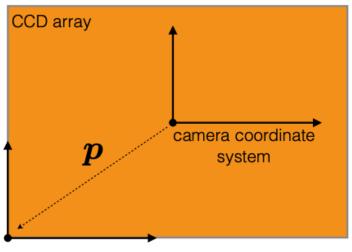
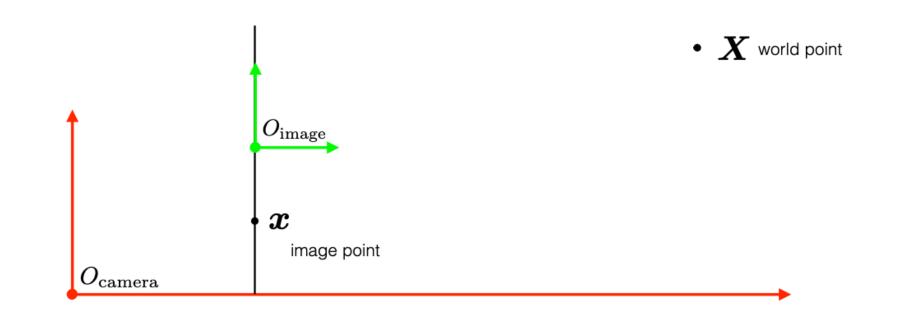


image coordinate system

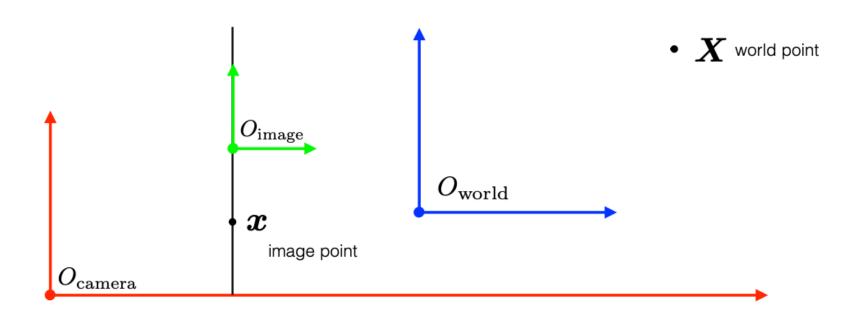
$$\mathbf{P} = \left[\begin{array}{rrrr} f & 0 & p_x & 0 \\ 0 & f & p_y & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]$$

Accounts for different origins

In general, the camera and image sensor have **different** coordinate systems



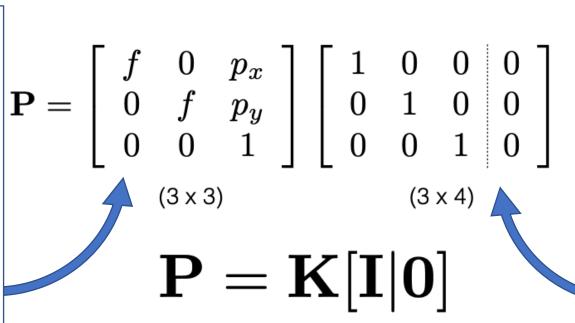
In general, there are **three different** coordinate systems...



so you need the know the transformations between them

Can be decomposed into two matrices,

- Relationship between image & camera coord.
 Systems.
- Camera Calibration matrix
- Camera Extrinsic
- Can be obtained from image meta data.



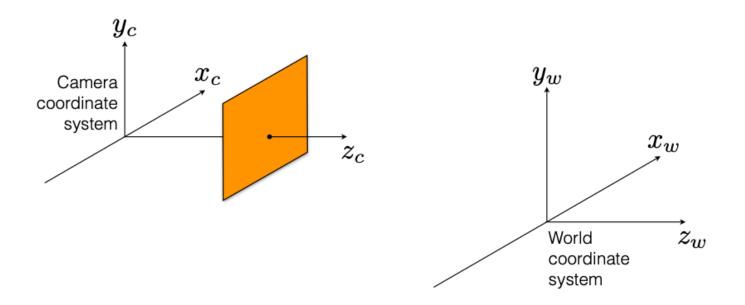
$$\mathbf{K}=\left[egin{array}{ccc} f&0&p_x\0&f&p_y\0&0&1 \end{array}
ight]$$

- Relationship between world & camera coord. Systems.
- Camera Intrinsic
- Often known as 'Camera Pose Estimation/ Camera Localization problem'.

calibration matrix

Assumes that the **camera** and **world** share the same coordinate system $\mathbf{P} = \begin{bmatrix} f & 0 & p_x \\ 0 & f & p_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \leftarrow$

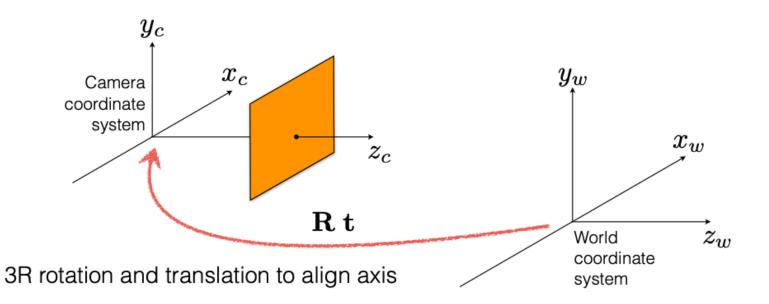
> What if they are different? How do we align them?

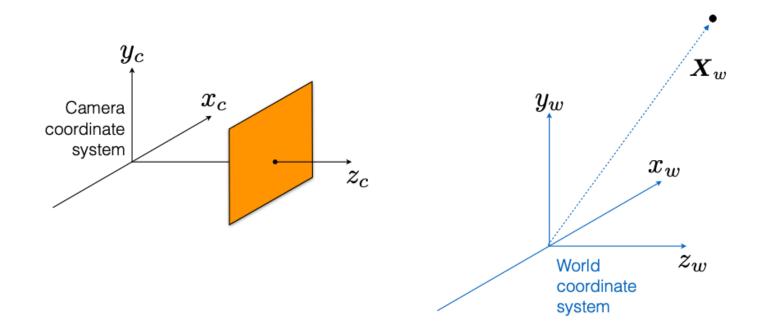


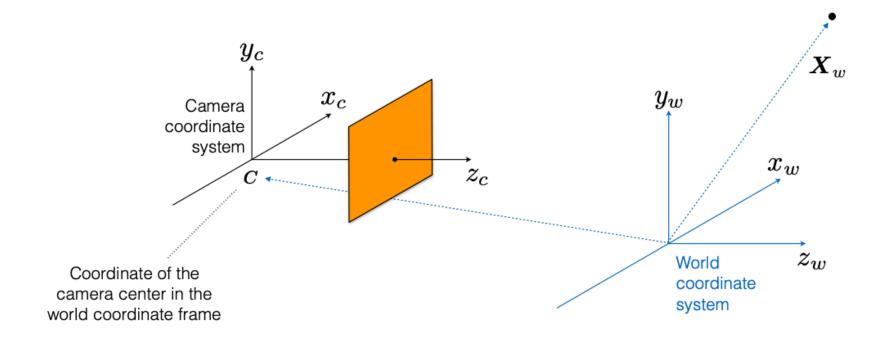
Assumes that the camera and world share the same coordinate system

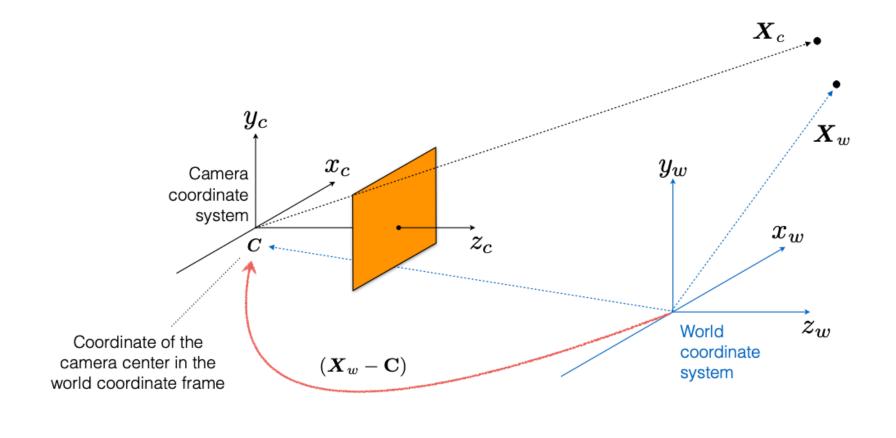
$$\mathbf{P} = \begin{bmatrix} f & 0 & p_x \\ 0 & f & p_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \boldsymbol{\leftarrow}$$

What if they are different? How do we align them?



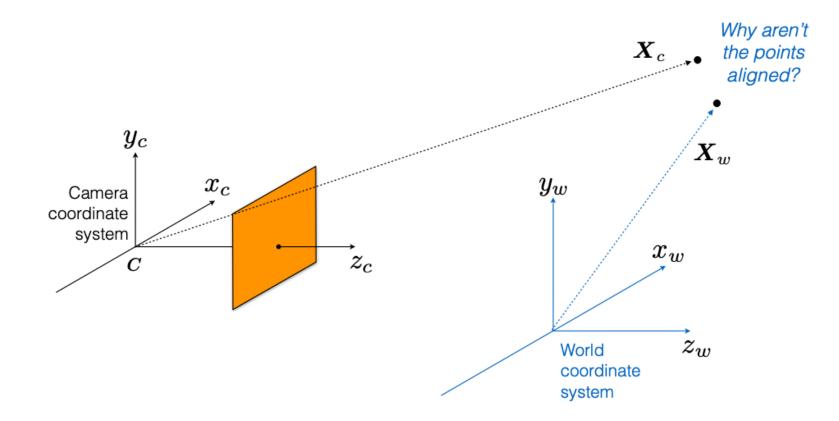






 $({oldsymbol X}_w-{f C})$

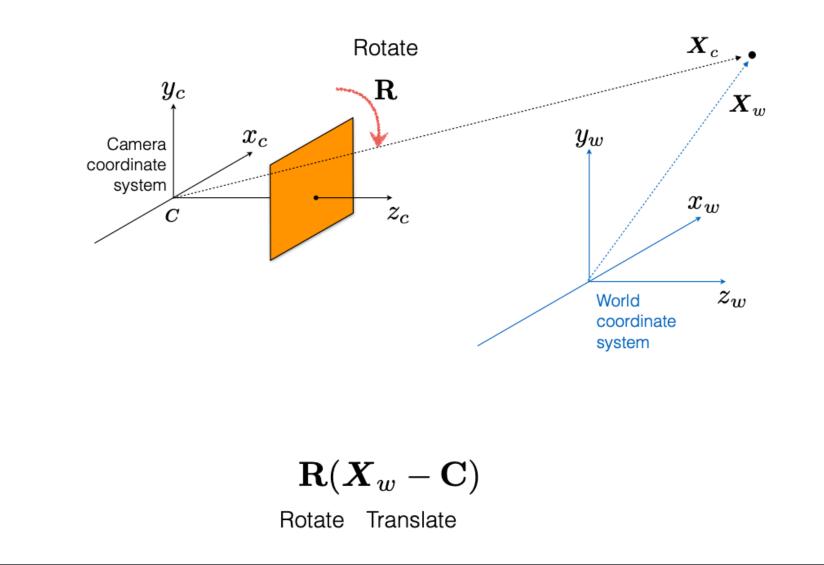
Translate



 $(X_w - \mathbf{C})$

Translate

What happens to points after alignment?



In inhomogeneous coordinates:

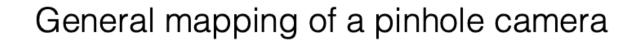
$$\boldsymbol{X}_c = \mathbf{R}(\boldsymbol{X}_w - \mathbf{C})$$

Optionally in homogeneous coordinates:

$$\left[egin{array}{c} X_c \ Y_c \ Z_c \ 1 \end{array}
ight] = \left[egin{array}{c} \mathbf{R} & -\mathbf{R}\mathbf{C} \ \mathbf{0} & 1 \end{array}
ight] \left[egin{array}{c} X_w \ Y_w \ Z_w \ 1 \end{array}
ight]$$

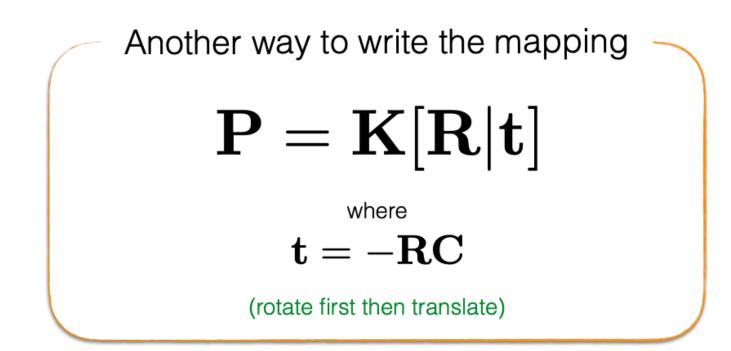
General mapping of a pinhole camera

$$\mathbf{P} = \mathbf{K}\mathbf{R}[\mathbf{I}| - \mathbf{C}]$$



$\mathbf{P} = \mathbf{K}\mathbf{R}[\mathbf{I}| - \mathbf{C}]$

(translate first then rotate)



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- How do we define geometry/shape of an object?
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What is Material in Computer Graphics?



3D coffee mug model

Rendered

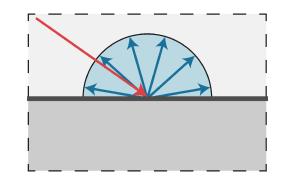
Rendered

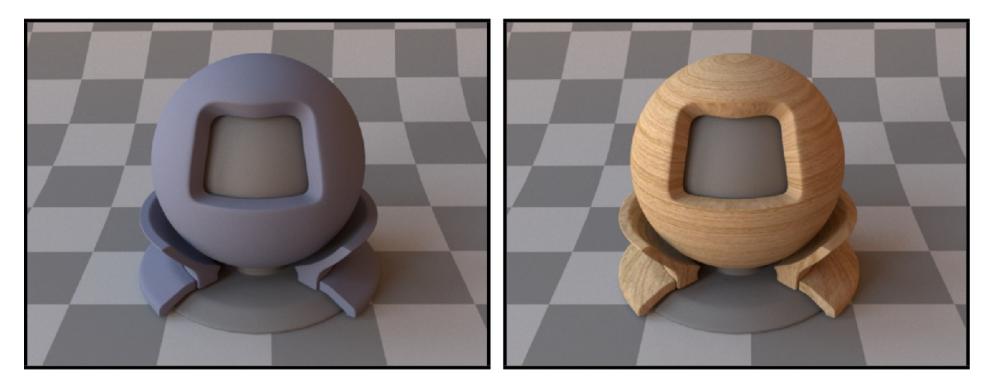
[From TurboSquid, created by artist 3dror]

Material == BRDF

Further reading: <u>https://en.wikipedia.org/wiki/Bidirectional_reflectance_distribution_function</u>

Diffuse / Lambertian Material (BRDF)





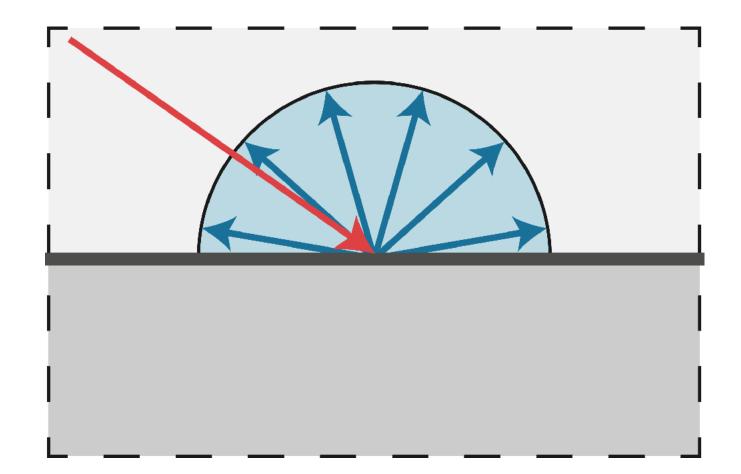
Uniform colored diffuse BRDF

Textured diffuse BRDF

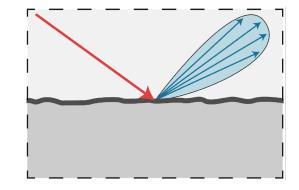
CS184/284A

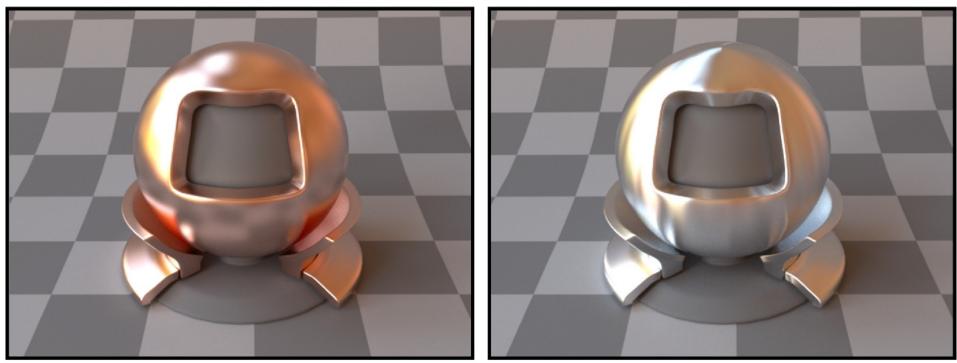
[Mitsuba renderer, Wenzel Jakob, 2010]

Diffuse/ Lambertian



Glossy material (BRDF)

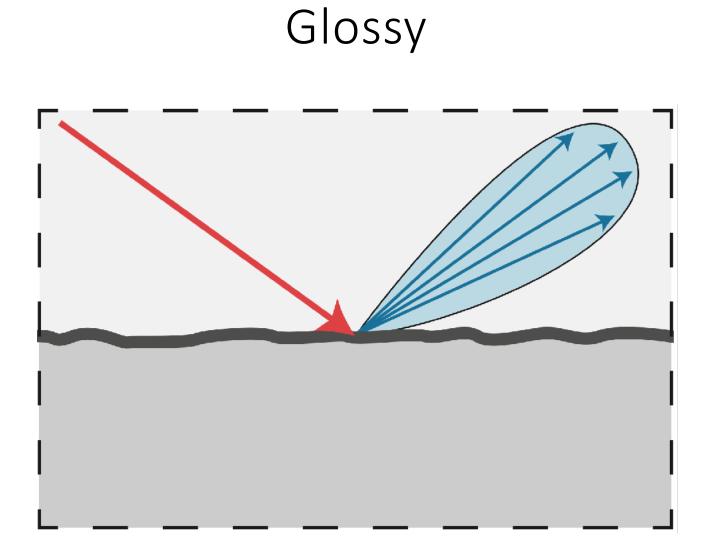




Copper

Aluminum

[Mitsuba renderer, Wenzel Jakob, 2010]



Refraction

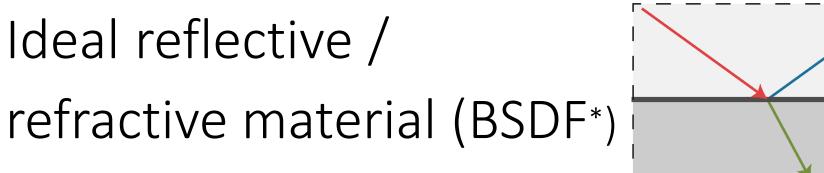
In addition to reflecting off surface, light may be transmitted through surface.

Light refracts when it enters a new medium.

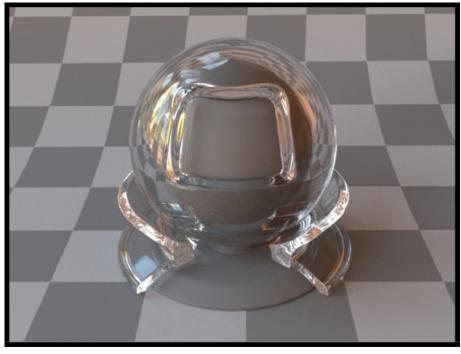


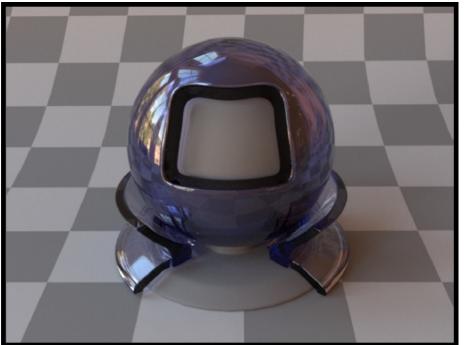






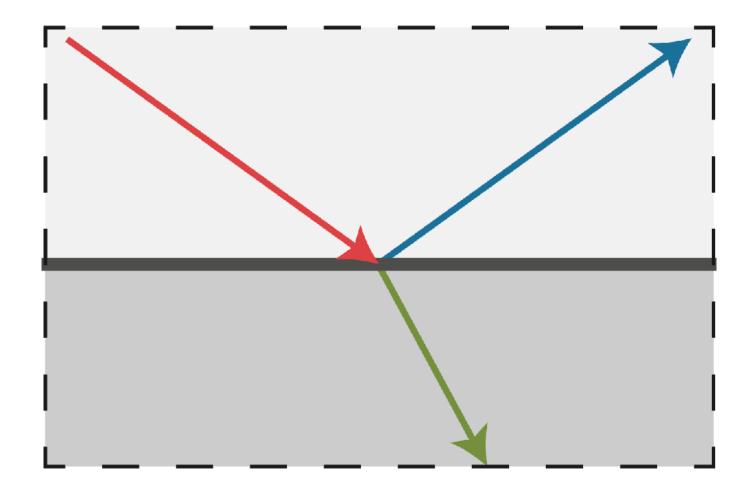
[Mitsuba renderer, Wenzel Jakob, 2010]





Air <-> plastic interface

Air <-> glass interface (with absorption)



Bi-directional Radiance Distribution Function (BRDF)

Light is reciprocative

ω

ω

E=Irradiance.

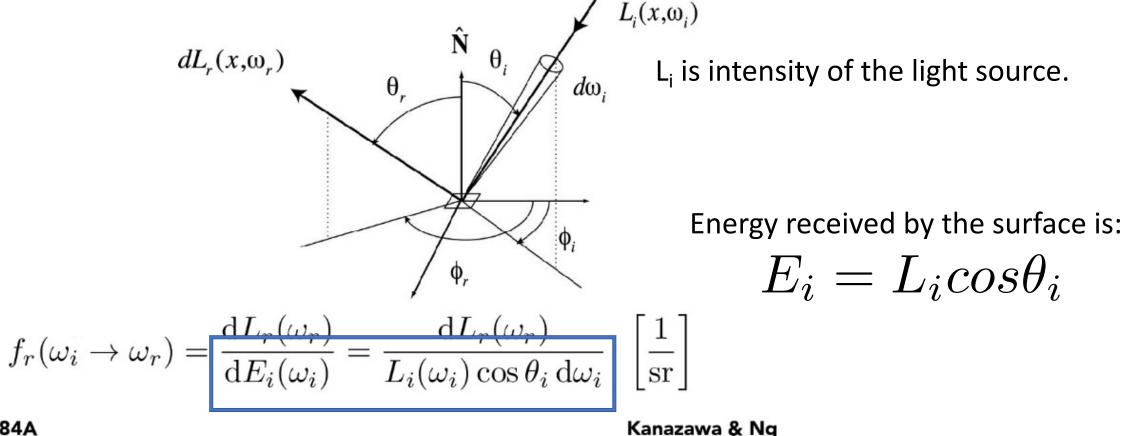
energy per unit area received on the surface in the incoming lighting direction.

L=Radiance

energy per unit area exiting the surface. in the outgoing lighting direction.

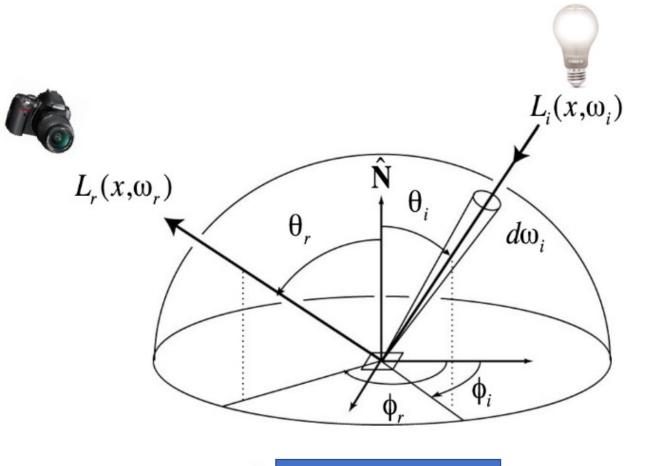
BRDF

Definition: The bidirectional reflectance distribution function (BRDF) represents how much light is reflected into each outgoing direction ω_r from each incoming direction



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The Reflection Equation

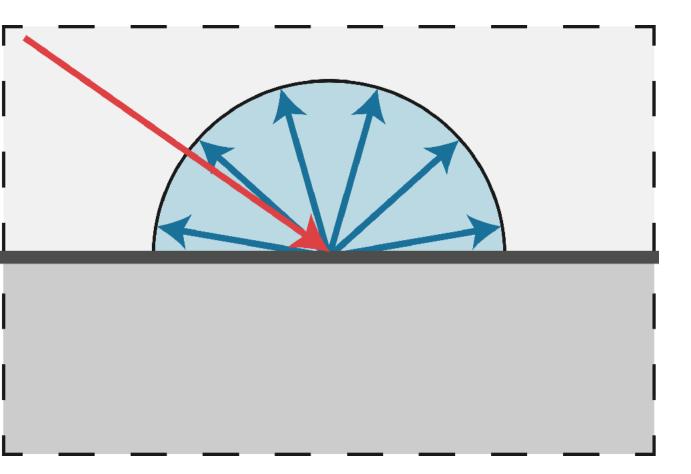


BRDF at a point p on the surface is a 4D function of 4 angles related to incoming and outgoing lighting direction.

$$L_r(\mathbf{p}, \omega_r) = \int_{H^2} f_r(\mathbf{p}, \omega_i \to \omega_r) L_i(\mathbf{p}, \omega_i) \cos \theta_i \, \mathrm{d}\omega_i$$

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Diffuse/ Lambertian



$$f(p, w_i \to w_r) = a(p)$$

a(p) is termed as Albedo.

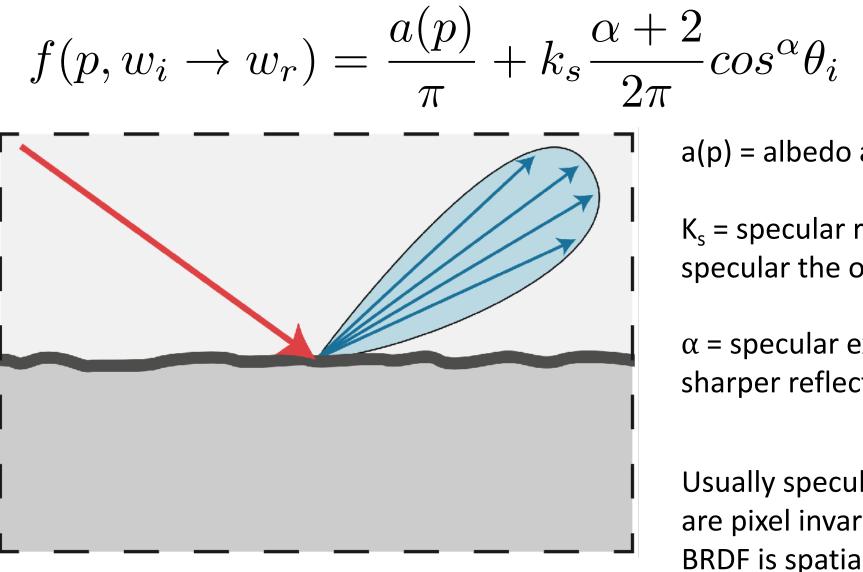
Albedo for a HxWx3 RGB image is HxWx3

Given a point light source L_i, image intensity at pixel p can be then written as:

$$I(p) = A(p)\langle Li, N(p) \rangle = A(p)L_i cos\theta_i$$

Note: θ is the angle between surface normal N(p) and incident lighting direction L_i.

Glossy/Specular (Phong Reflectance Model)

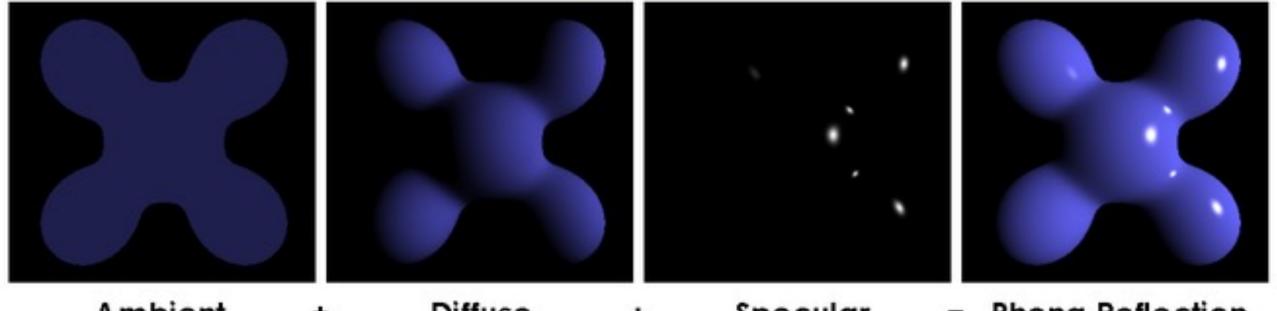


a(p) = albedo at pixel p.

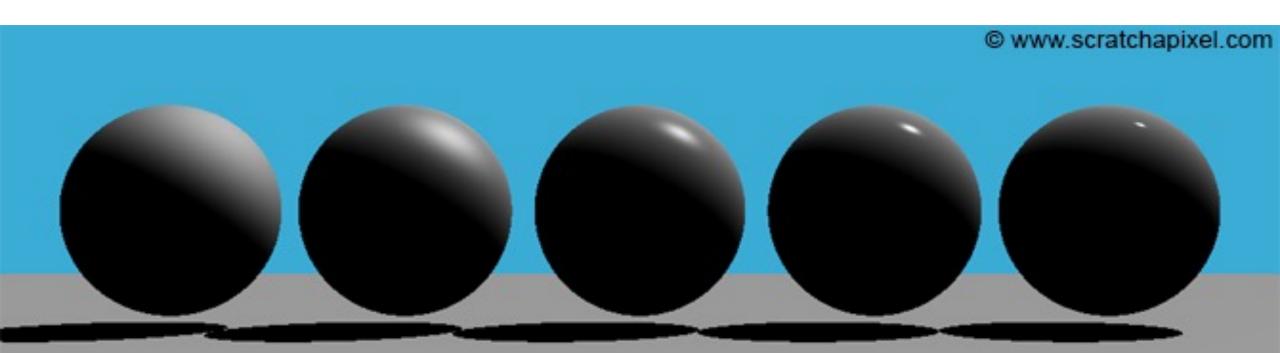
K_s = specular reflectivity, controls how specular the object is.

 α = specular exponent, higher value indicates sharper reflections.

Usually specular reflectivity and exponent are pixel invariant, i.e. we assume that the BRDF is spatially in-variant!



Ambient + Diffuse + Specular = Phong Reflection



n=2 n=10 n=50 n=250 n=1250 Ks=0.04 Ks=0.08 Ks=0.1 Ks=0.15 Ks=0.2

K_s = specular reflectivity, controls how specular the object is.

 α (written as n in the picture)= specular exponent, higher value indicates sharper reflections.

Microfacet Material Model

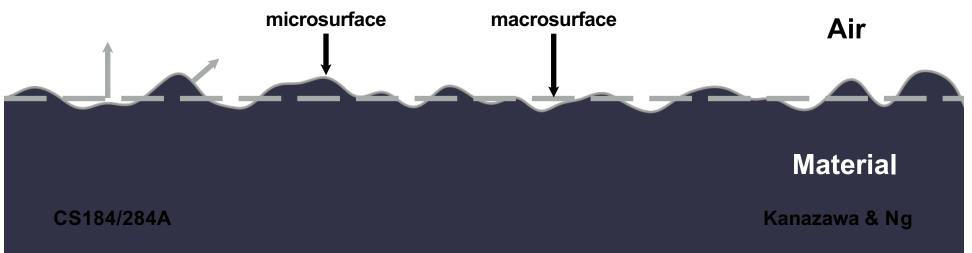
Microfacet Theory

Rough surface

- Macroscale: flat & rough
- Microscale: bumpy & specular

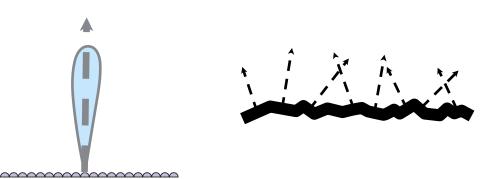
Individual elements of surface act like mirrors

- Known as "microfacets"
- Each microfacet has its own normal vector (photometric normal)



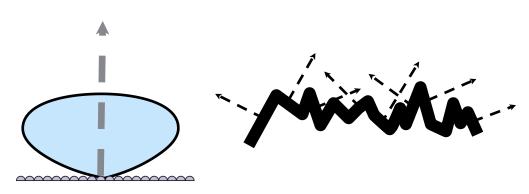
Microfacet BRDF

- Key: the distribution of microfacets' normals
 - Concentrated <==> glossy



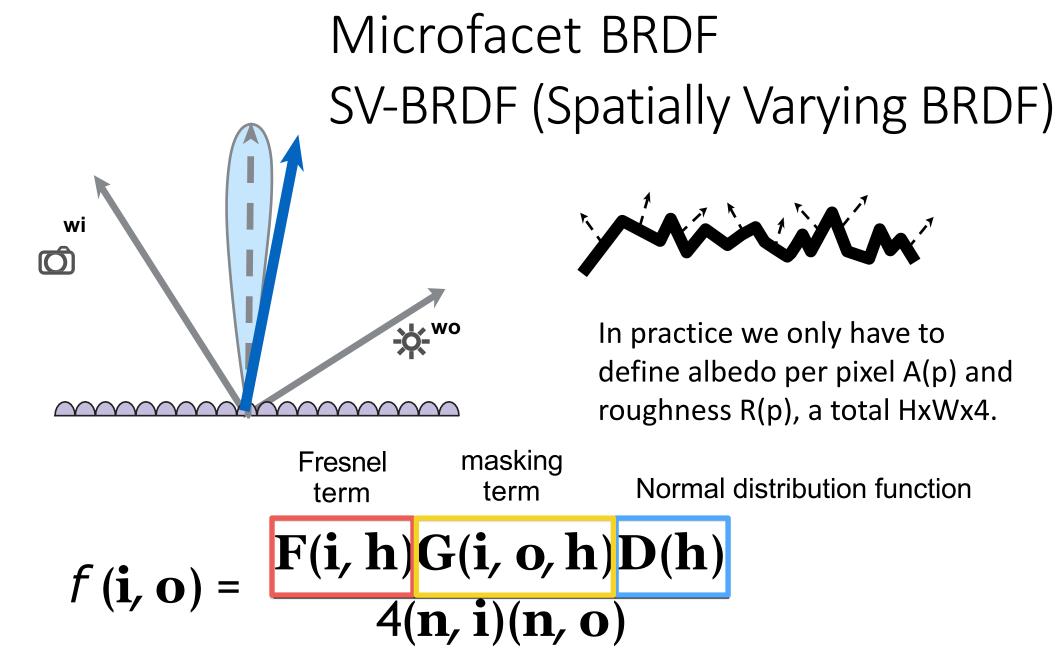


Spread out <==> diffuse









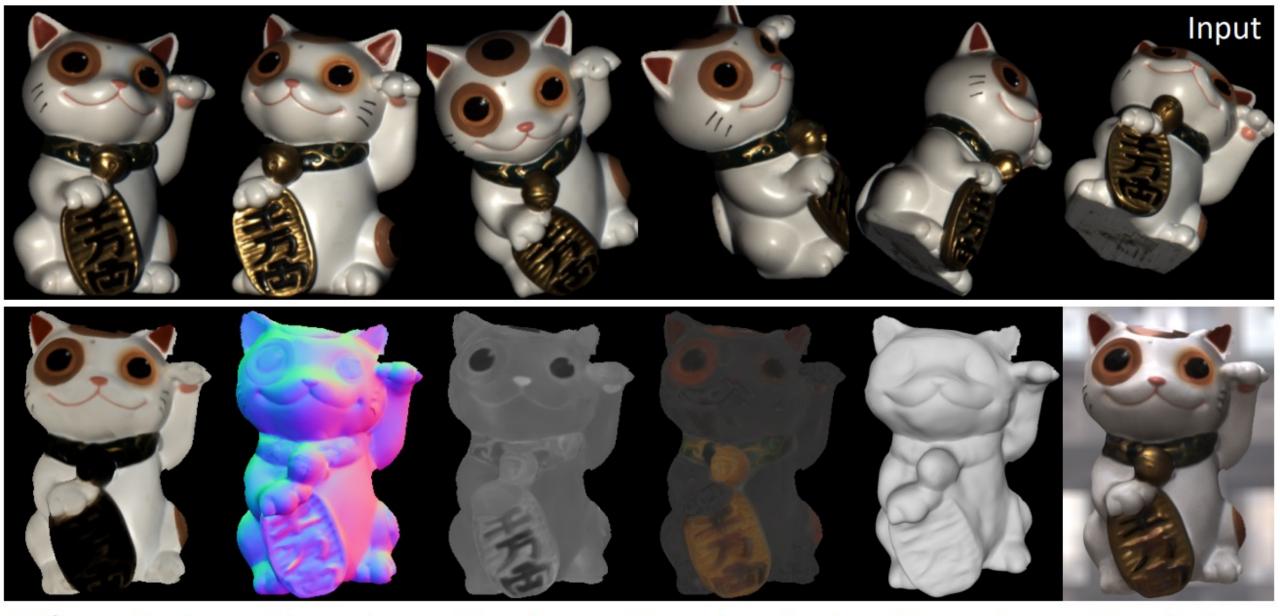
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Microfacet BRDF: Examples



[Autodesk Fusion 360]





Diffuse albedo Normal Roughness Specular albedo Geometry Rendering

Deep 3D Capture: Geometry and Reflectance from Sparse Multi-View Images, Bi et. al.

Isotropic vs Anisotropic Reflection

- So far, Point light + Metal = Round / Elliptical highlight
- What can we see inside many metal elevators?



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Inside an elevator

Isotropic vs Anisotropic Reflection





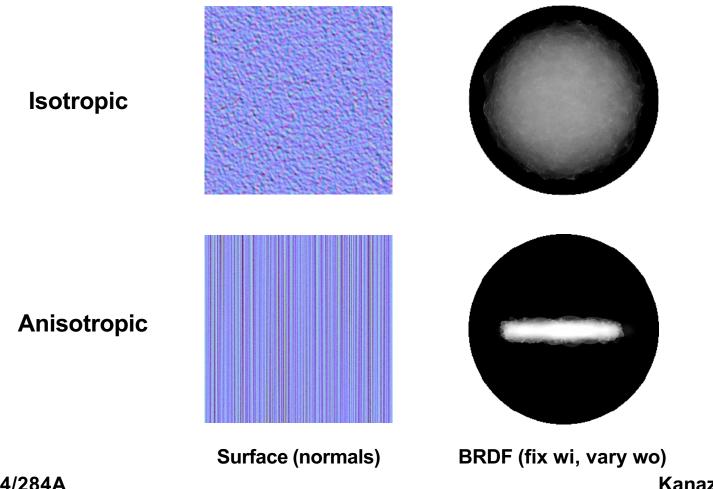
Isotropic

Anisotropic

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Isotropic / Anisotropic Materials (BRDFs)

• Key: directionality of underlying surface

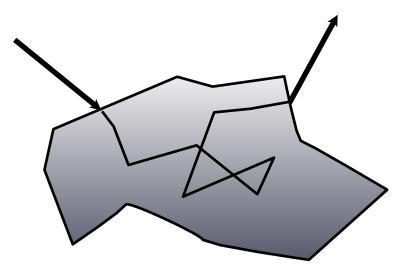


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Subsurface Scattering

Visual characteristics of many surfaces caused by light exiting at different points than it enters

• Violates a fundamental assumption of the BRDF



• Different from transparent



[Jensen et al 2001]



[Donner et al 2008]

BRDF vs BSSRDF (models sub-surface scattering)



BRDF

BSSRDF

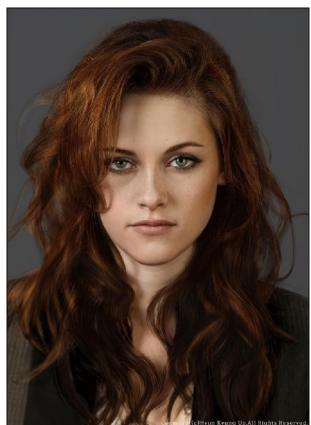
[Jensen et al. 2001]

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BSSRDF: Application



[Artist: Teruyuki and Yuka]





[Artist: Dan Roarty]

[Artist: Hyun Kyung]

https://cgelves.com/10-most-realistic-human-3d-models-that-will-wow-you/



Respond at **PollEv.com/ronisen** Text **RONISEN** to **22333** once to join, then text your message

Feel free to share your questions...

To be continued ...

Anti Racist Computer Graphics - by Theodore Kim, Yale Univ.

Computer Graphics has a race problem!

Listen to this 1hour presentation by Prof. Kim: <u>https://www.youtube.com/watch?v=ROuE8xYLpX8</u>



BRDF



"Skin" = Subsurface Scattering

Figure 11: A face rendered using the BRDF model (top) and the BSSRDF model (bottom). We used our measured values for skin (skin1) and the same lighting conditions in both images (the BRDF

"Skin" = White Skin

Jensen, Marschner, Levoy and Hanrahan, A Practical Model for Subsurface Light Transport, Proceedings of SIGGRAPH (2001).

Jensen, Marschner, Levoy and Hanrahan, A Practical Model for Subsurface Light Transport, Proceedings of SIGGRAPH (2001). Stam, An Illumination Model for a Skin Layer Bounded by Rough Surfaces, Rendering Techniques (2001). Jensen and Buhler, A Rapid Hierarchical Rendering Technique for Translucent Materials, ACM Transactions on Graphics (2002). Xie, Olano, Karis, Narkowicz, Real-time Subsurface Scattering with Single Pass Variance-guided Adaptive Importance Sampling, Proceedings of the ACM on Computer Graphics and Interactive Techniques (2020). D'Eon, Luebke, Enderton, Efficient Rendering of Human Skin, Rendering Techniques (2007).



Jimenez, Zsolnai, Jarabo, Freude, Auzinger, We, von der Pahlen, Wimmer, Gutierrez, Separable Subsurface Scattering, Computer Graphics Forum (2015). d'Eon, Irving, A Quantized-Diffusion Model for Rendering Translucent Materials, ACM Transactions on Graphics (2011). Frederickx, Dutre, A Forward Scattering Dipole Model from a Functional Integral Approximation, ACM Transactions on Graphics (2017). Donner and Jensen, Light Diffusion in Multi-Layered Translucent Materials, ACM Transactions on Graphics (2005). Jimenez, Scully, Barbosa, Donner, Alvarez, Vieira, Matts, Orvalho, Gutierrez, Weyrich, A Practical Appearance Model for Dynamic Facial Color, ACM Transactions on Graphics (2010). Habel, Christensen, Jarosz, Photon Beam Diffusion: A Hybrid Monte Carlo Method for Subsurface Scattering, Eurographics Symposium on Rendering (2013).

- Whiter skin has more subsurface scattering, leading to more smoothing effect.
- Darker skin has more specular reflection and less subsurface scattering.





"MetaHuman Creator Documentation." Unreal Engine. Accessed August 4, 2021. https://docs.metahuman.unrealengine.com/. Clockers, (1995).



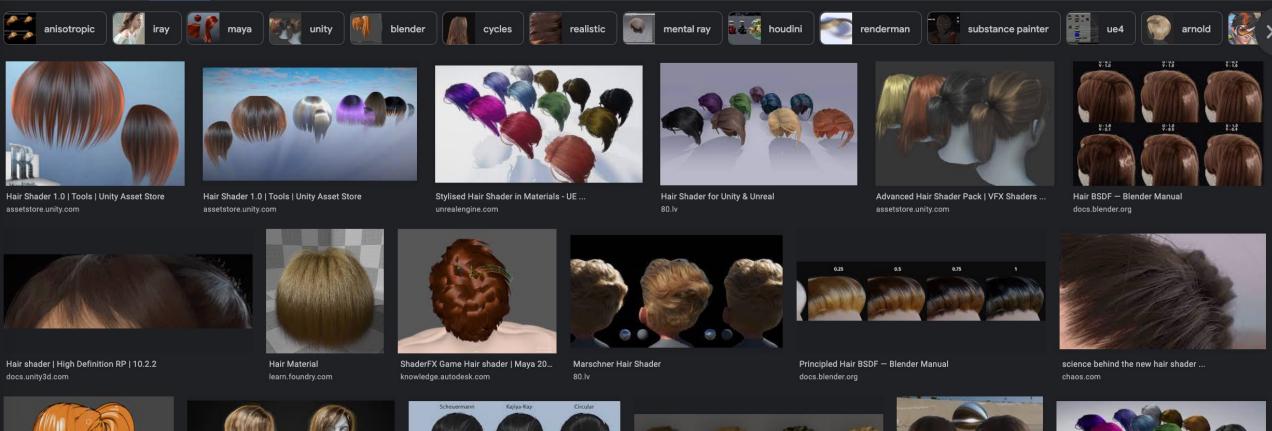


Black Panther, (2018).

"MetaHuman Creator Documentation." Unreal Engine. Accessed August 4, 2021. https://docs.metahuman.unrealengine.com/.

Other racial bias in Computer Graphics?

• Hair = 'Straight hair'





ArtStation - Blender Anime Hair Shader artstation.com · In stock



cgcookie.com



hair, Shader pack .. pinterest.com



Confluence Mobile - Arnold Renderer docs.arnoldrenderer.com



I put out a major update to Hair wit... twitter.com



Stylised Hair Shader in Materials - UE ... unrealengine.com

Camera color tone bias





So what do we do now?

- Incentivize creating good dataset and benchmarks that is diverse and inclusive of all race, ethnicity, genders, disability status etc.
- Discourage working on research problems that are going to potentially cause harm to marginalized community, e.g. detecting sexual orientation from images.
- If working on specific subpopulation, make sure to clarify that in the paper, e.g. write 'whiter skin tone' instead of 'human skin tone'.