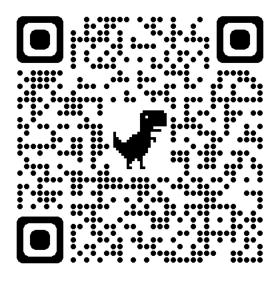
Lecture 5: Image Processing

COMP 590/776: Computer Vision

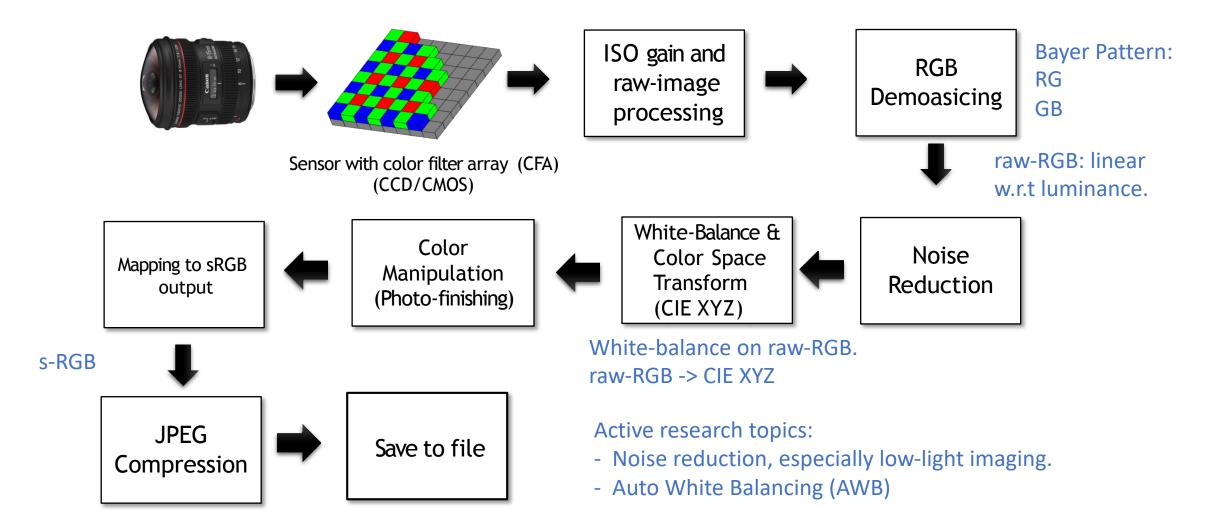
Instructor: Soumyadip (Roni) Sengupta

TA: Mykhailo (Misha) Shvets



Course Website: Scan Me!

Recap: A typical color imaging pipeline

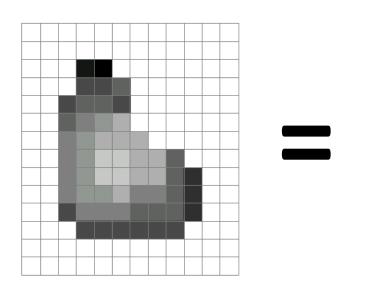


So far: How cameras capture images of the world?

Next: How to we extract useful information and edit images? a.k.a Image Processing (often a whole course of its own)

What is an image?

A grid (matrix) of intensity values

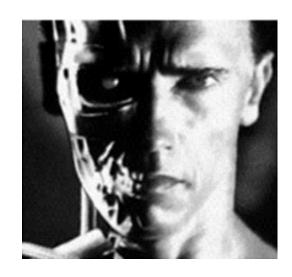


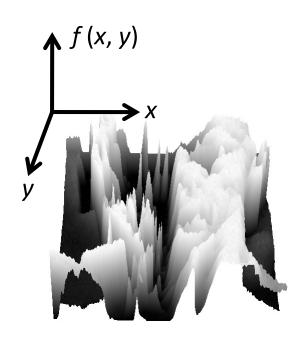
255	255	255	255	255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255	255	255	255	255
255	255	255	20	0	255	255	255	255	255	255	255
255	255	255	75	75	75	255	255	255	255	255	255
255	255	75	95	95	75	255	255	255	255	255	255
255	255	96	127	145	175	255	255	255	255	255	255
255	255	127	145	175	175	175	255	255	255	255	255
255	255	127	145	200	200	175	175	95	255	255	255
255	255	127	145	200	200	175	175	95	47	255	255
255	255	127	145	145	175	127	127	95	47	255	255
255	255	74	127	127	127	95	95	95	47	255	255
255	255	255	74	74	74	74	74	74	255	255	255
255	255	255	255	255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255	255	255	255	255

(common to use one byte per value: 0 = black, 255 = white)

What is an image?

- Can think of a (grayscale) image as a **function** f from R² to R:
 - f(x,y) gives the **intensity** at position (x,y)





• A digital image is a discrete (sampled, quantized) version of this function

This lecture: Image Transformations & Filtering

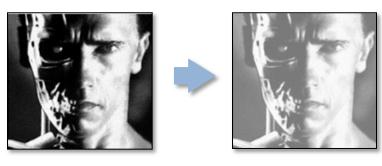
- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

This lecture: Image Transformations & Filtering

- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

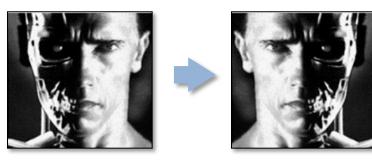
Examples of Point Processing

• As with any function, we can apply operators to an image



$$g(x,y) = f(x,y) + 20$$

brightness



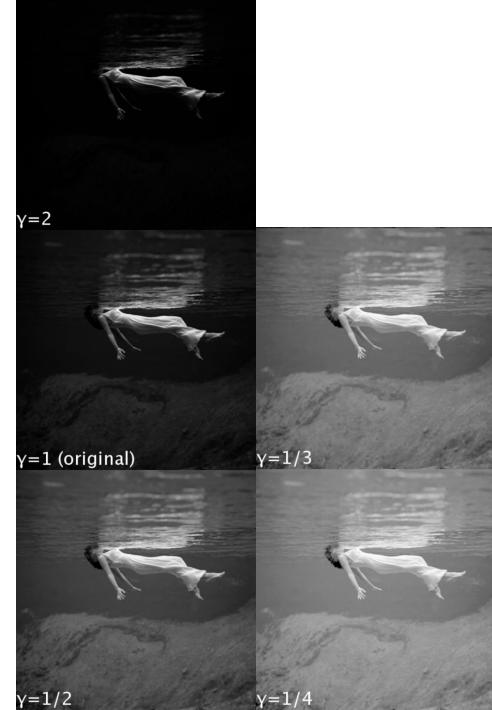
$$g(x,y) = f(-x,y)$$

Horizontal flip

Gamma Correction $V_{\mathrm{out}} = AV_{\mathrm{in}}^{\gamma}$,

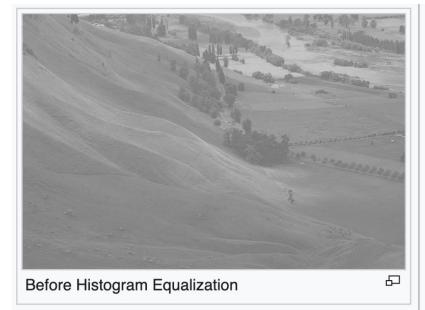
Seen in last class

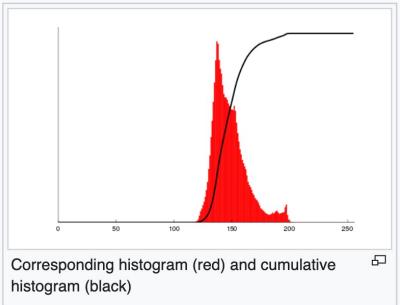
- Most images we work with are in sRGB space, i.e., already tone-mapped.
- Many Vision algorithms expects the image to be in linear space.
- sRGB -> Linear space conversion requires explicit knowledge of camera processing pipeline. Requires knowledge of tone-production curve.
- In absence of it it is very common to use $\gamma = 2.2$.
- Note: This is not accurate, just a cheap approximation that works for most Vision tasks.

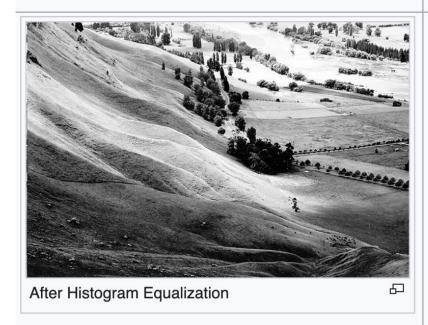


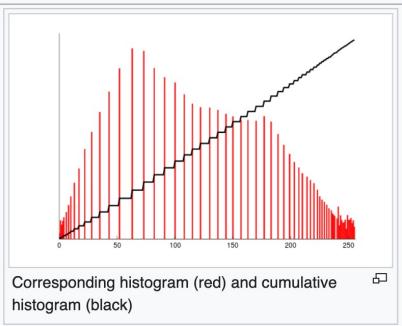
credits: wiki

Histogram Equalization

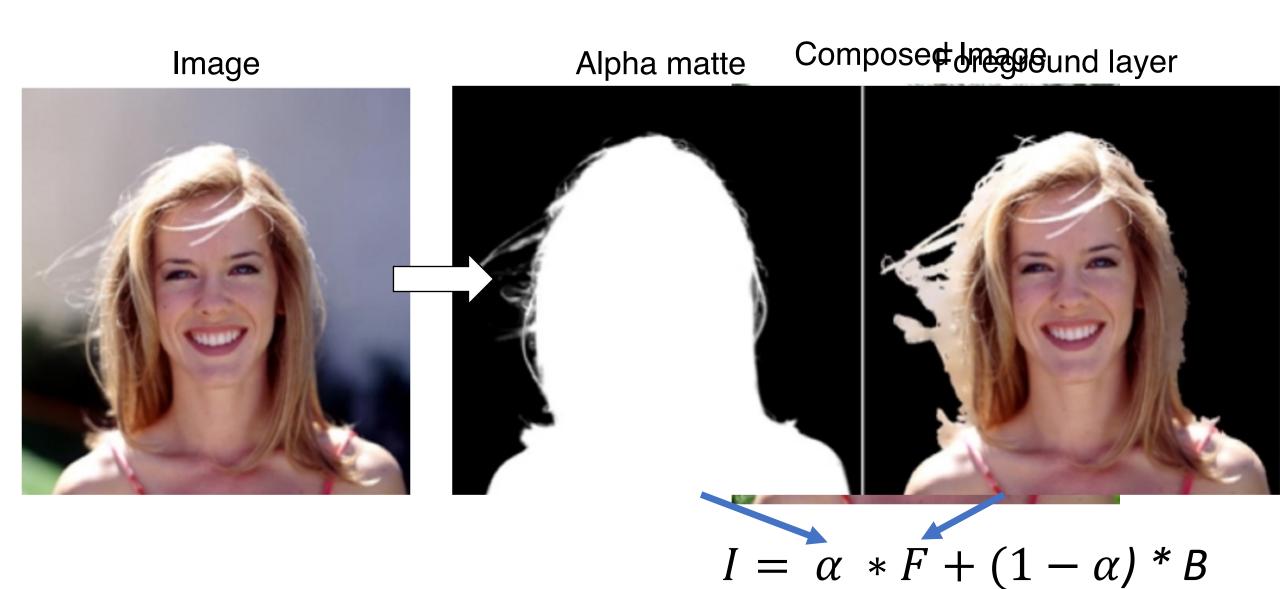








Alpha Matting



This lecture: Image Transformations & Filtering

- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

Filters

- Filtering
 - Form a new image whose pixel values are a combination of the original pixel values.
- Why?
 - To get useful information from images
 - E.g., extract edges or contours (to understand shape)
 - To enhance the image
 - E.g., to remove noise
 - E.g., to sharpen and "enhance image" a la CSI
 - A key operator in Convolutional Neural Networks

Canonical Image Processing problems

- Image Restoration
 - denoising
 - deblurring
- Image Compression
 - JPEG, HEIF, MPEG, ...
- Computing Field Properties
 - optical flow
 - disparity
- Locating Structural Features
 - corners
 - edges

Question: Noise reduction

• Given a camera and a still scene, how can you reduce noise?



Take lots of images and average them!

Image filtering

 Modify the pixels in an image based on some function of a local neighborhood of each pixel

10	5	3
4	5	1
1	1	7

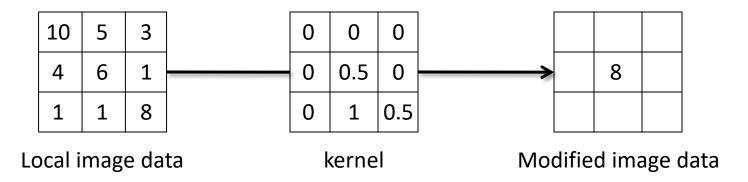




Modified image data

Linear filtering

- One simple version of filtering: linear filtering (cross-correlation, convolution)
 - Replace each pixel by a linear combination (a weighted sum) of its neighbors
- The prescription for the linear combination is called the "kernel" (or "mask", "filter")



Source: L. Zhang

Cross-correlation

Let F be the image, H be the kernel (of size $2k+1 \times 2k+1$), and be the output image G

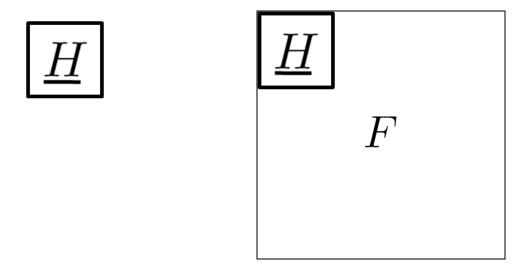
$$G[i,j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u,v]F[i+u,j+v]$$

This is called a **cross-correlation** operation:

$$G = H \otimes F$$

 Can think of as a "dot product" between local neighborhood and kernel for each pixel

Cross-Correlation



Convolution

 Same as cross-correlation, except that the kernel is "flipped" (horizontally and vertically)

$$G[i,j] = \sum_{u=-k}^{k} \sum_{v=-k}^{k} H[u,v]F[i-u,j-v]$$

$$G[i,j] = \sum_{u=-k}^{\kappa} \sum_{v=-k}^{\kappa} H[u,v] F[i+u,j+v] \quad \text{Cross-correlation}$$

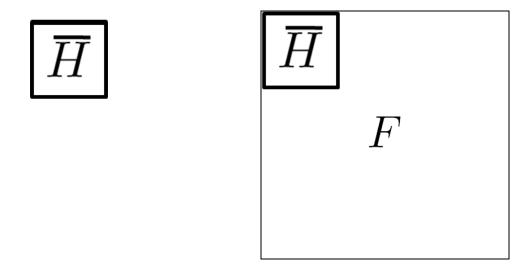
Convolution is commutative and associative

Convolution is nice!

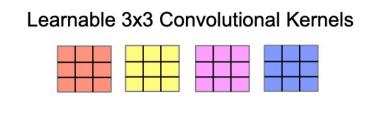
• Notation: $b = c \star a$

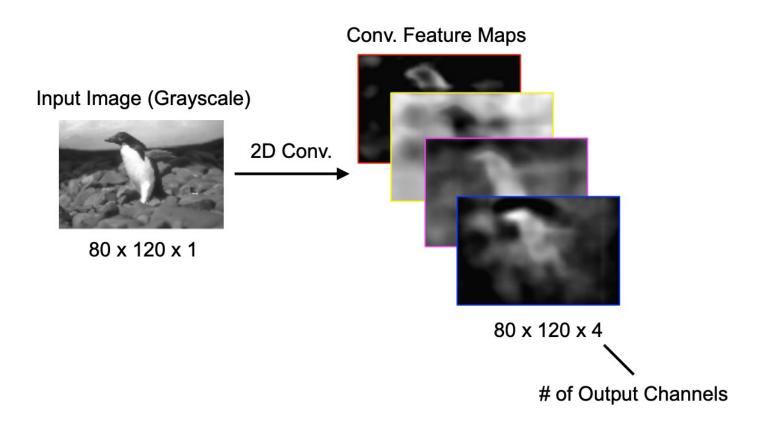
- Convolution is a multiplication-like operation
 - commutative $a \star b = b \star a$
 - associative $a \star (b \star c) = (a \star b) \star c$
 - distributes over addition $a \star (b+c) = a \star b + a \star c$
 - scalars factor out $\alpha a \star b = a \star \alpha b = \alpha (a \star b)$
 - identity: unit impulse e = [..., 0, 0, 1, 0, 0, ...] $a \star e = a$
- Usefulness of associativity
 - often apply several filters one after another: $(((a * b_1) * b_2) * b_3)$
 - this is equivalent to applying one filter: a * $(b_1 * b_2 * b_3)$

Convolution

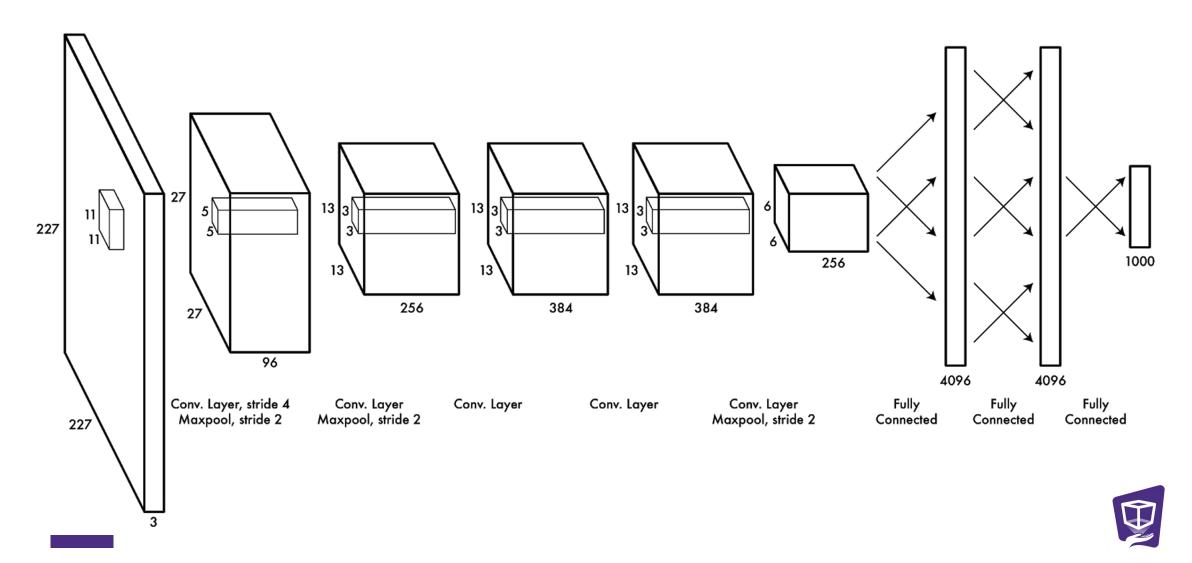


Convolutional Networks

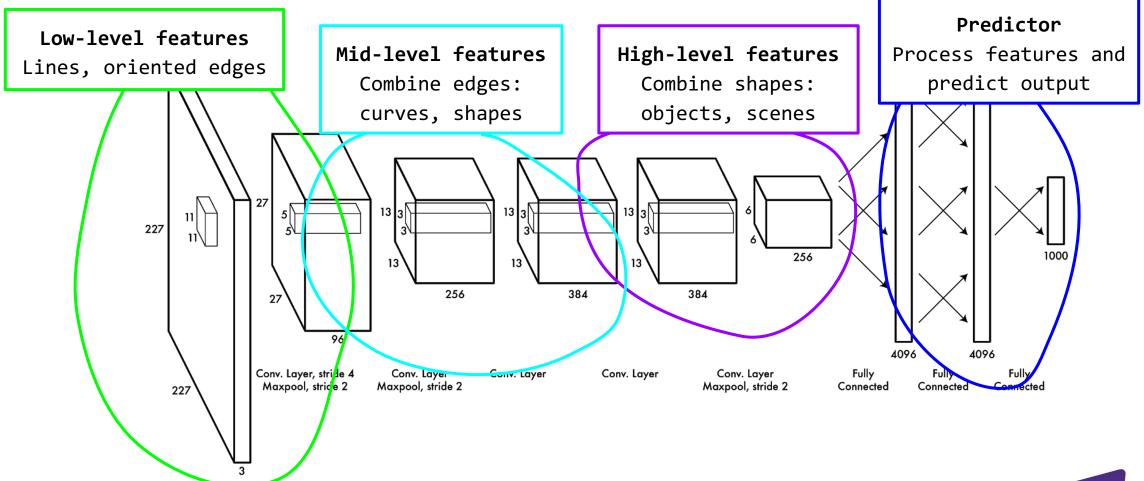




AlexNet: An Early Example

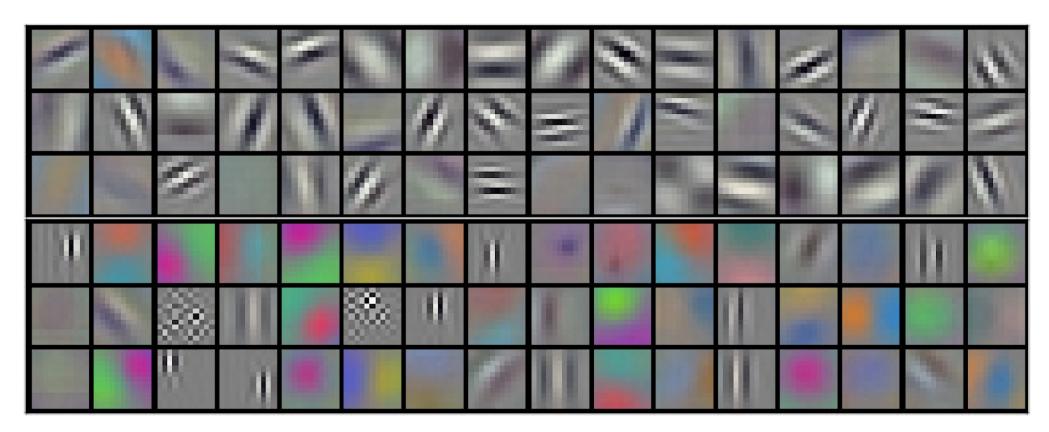


Where Models Learn Features of an Image





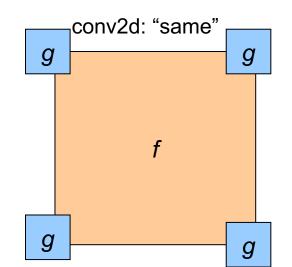
What are Models Actually Looking For?

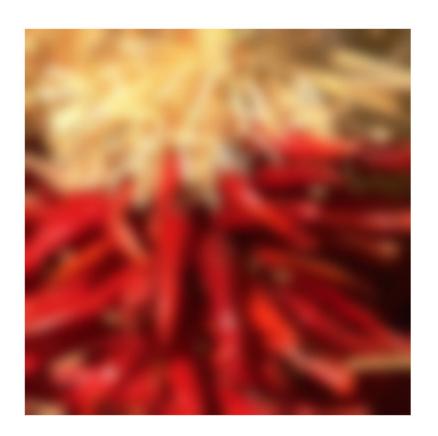




Conv/Filtering: Practical matters

- What about near the edge?
 - the filter window falls off the edge of the image
 - need to extrapolate
 - methods:
 - clip filter (black)
 - wrap around (circular)
 - copy edge
 - reflect across edge





Padding & Stride in CNN

CLASS torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, dilation=1, groups=1, bias=True, padding_mode='zeros', device=None, dtype=None) [SOURCE]

Applies a 2D convolution over an input signal composed of several input planes.

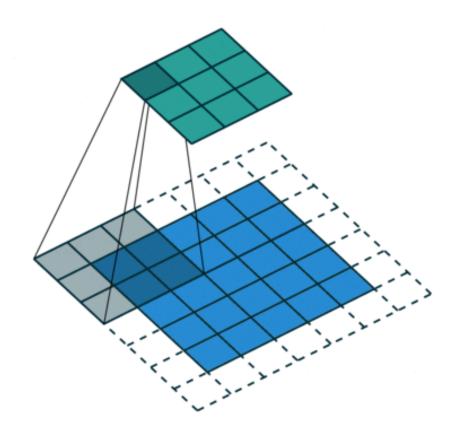
In the simplest case, the output value of the layer with input size $(N, C_{\rm in}, H, W)$ and output $(N, C_{\rm out}, H_{\rm out}, W_{\rm out})$ can be precisely described as:

$$\operatorname{out}(N_i, C_{\operatorname{out}_j}) = \operatorname{bias}(C_{\operatorname{out}_j}) + \sum_{k=0}^{C_{\operatorname{in}}-1} \operatorname{weight}(C_{\operatorname{out}_j}, k) \star \operatorname{input}(N_i, k)$$

where \star is the valid 2D cross-correlation operator, N is a batch size, C denotes a number of channels, H is a height of input planes in pixels, and W is width in pixels.

$$H_{out} = \left\lfloor rac{H_{in} + 2 imes \mathrm{padding}[0] - \mathrm{dilation}[0] imes (\mathrm{kernel_size}[0] - 1) - 1}{\mathrm{stride}[0]} + 1
ight
floor$$

$$W_{out} = \left\lfloor rac{W_{in} + 2 imes \mathrm{padding}[1] - \mathrm{dilation}[1] imes (\mathrm{kernel_size}[1] - 1) - 1}{\mathrm{stride}[1]} + 1
ight
floor$$



padding=1, stride=2

Linear filters: examples





0	0	0
0	1	0
0	0	0

Original

Linear filters: examples

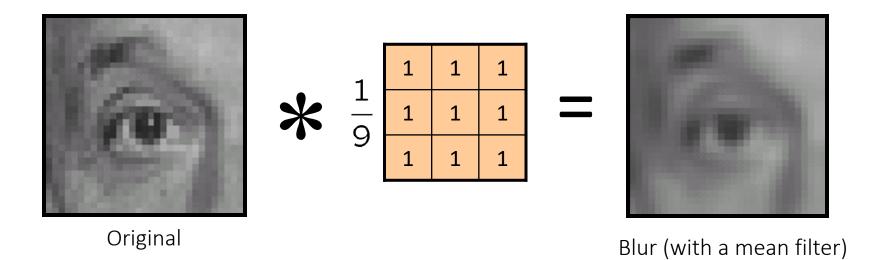




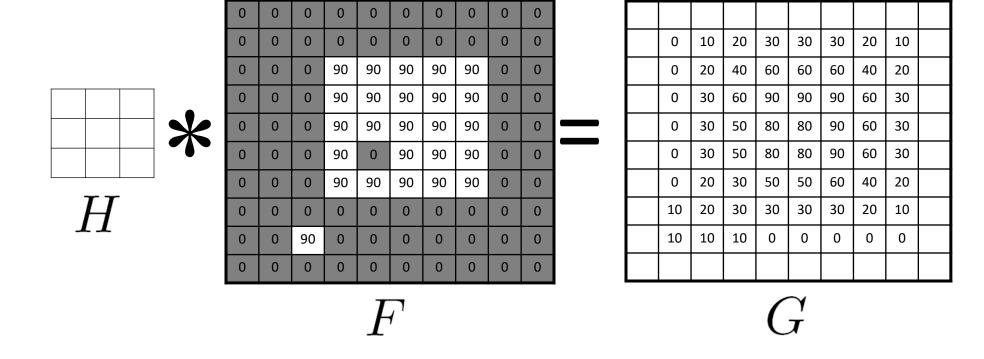
0	0	0
1	0	0
0	0	0

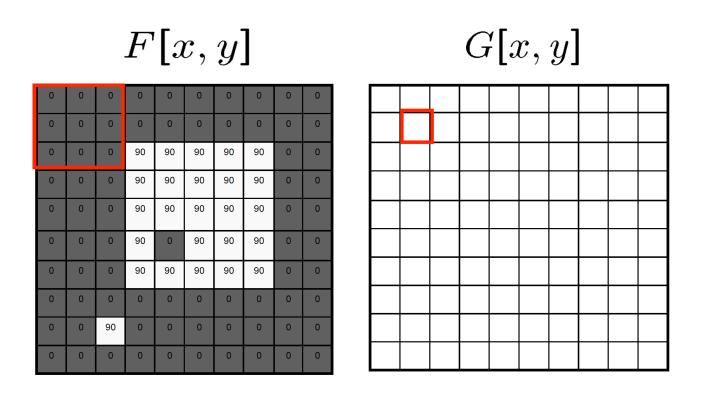
Original

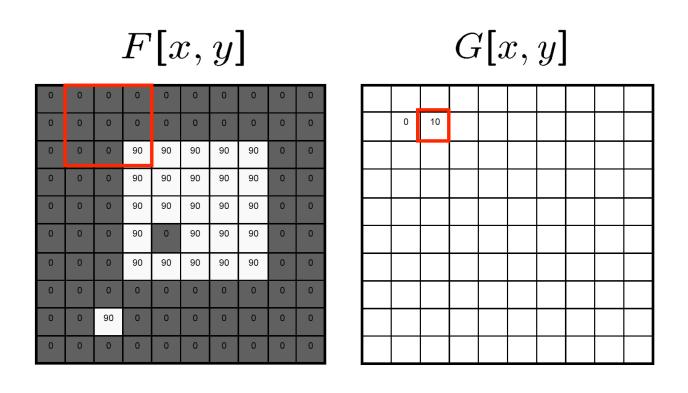
Linear filters: examples

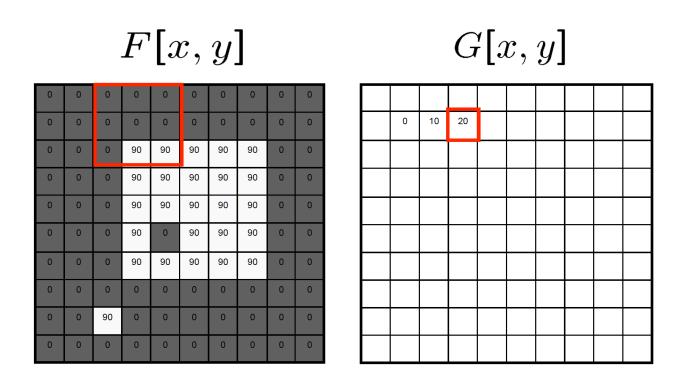


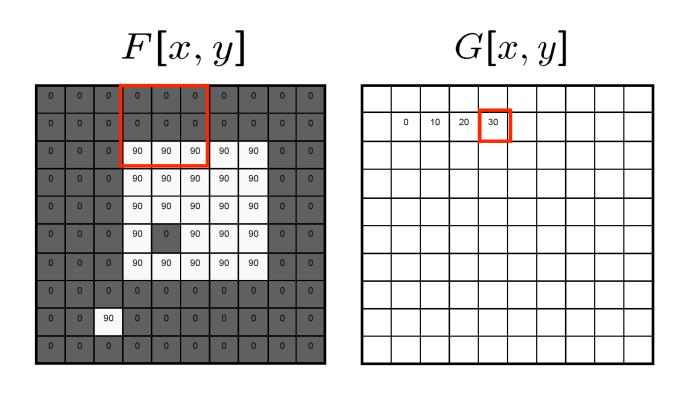
Mean filtering

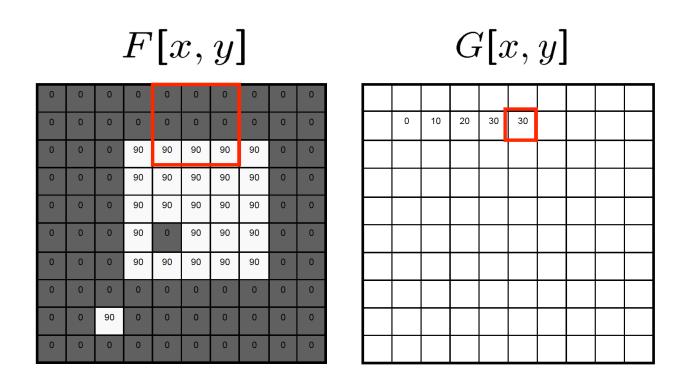




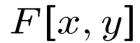


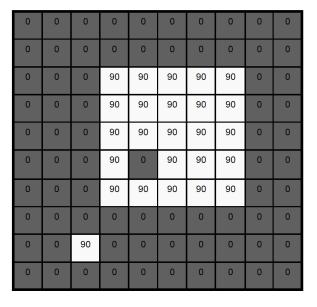






Mean filtering/Moving average

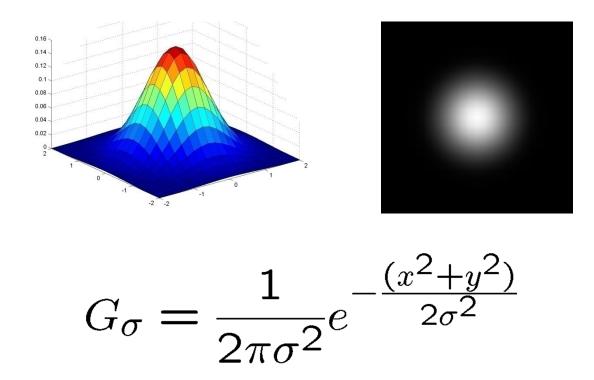




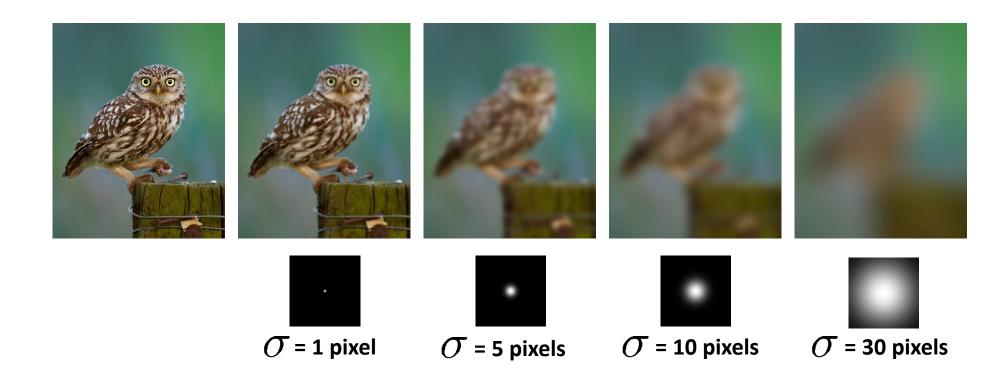
G[x,y]

0	10	20	30	30	30	20	10	
0	20	40	60	60	60	40	20	
0	30	60	90	90	90	60	30	
0	30	50	80	80	90	60	30	
0	30	50	80	80	90	60	30	
0	20	30	50	50	60	40	20	
10	20	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	

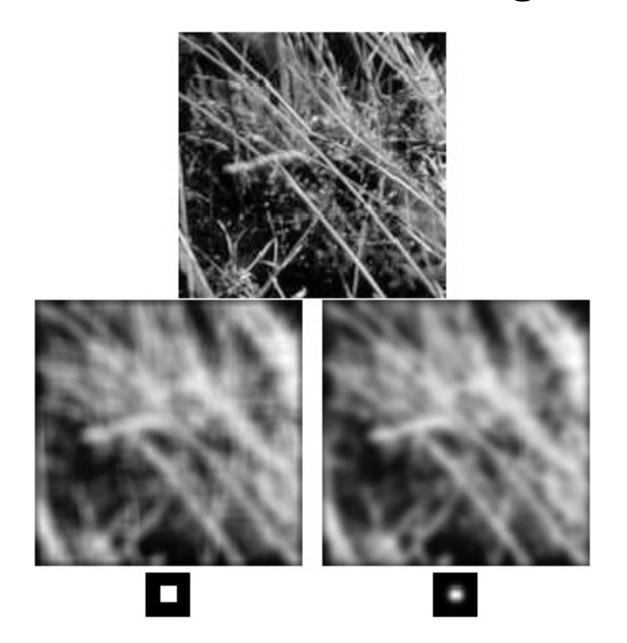
Gaussian kernel



Gaussian filters



Mean vs. Gaussian filtering



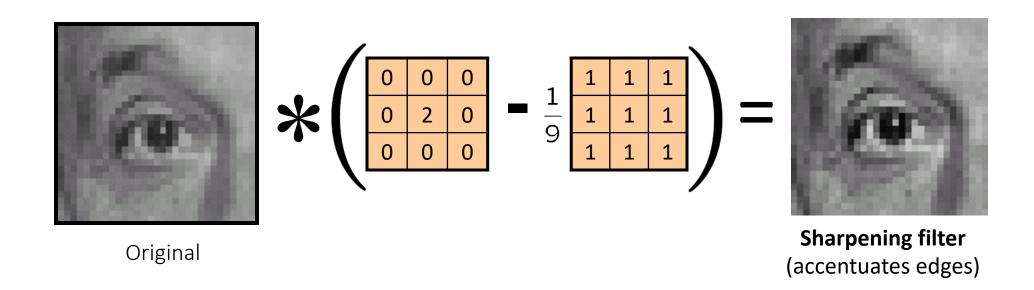
Gaussian filter

- Removes "high-frequency" components from the image (low-pass filter)
- Convolution with self is another Gaussian

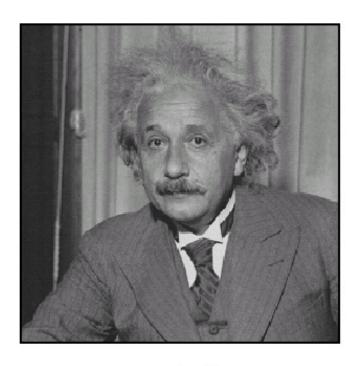


• Convolving twice with Gaussian kernel of width σ = Convolving once with kernel of width $\sigma\sqrt{2}$

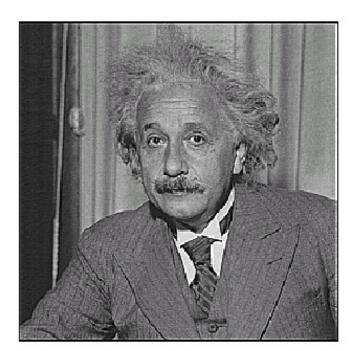
Linear filters: examples



Sharpening



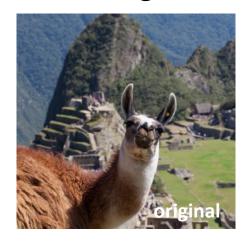




after

Sharpening

What does blurring take away?



Let's add it back:



detail

(This "detail extraction" operation is also called a *high-pass filter*)



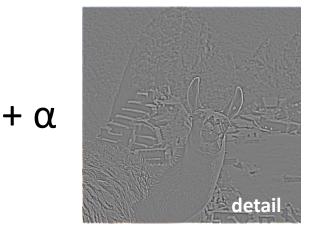
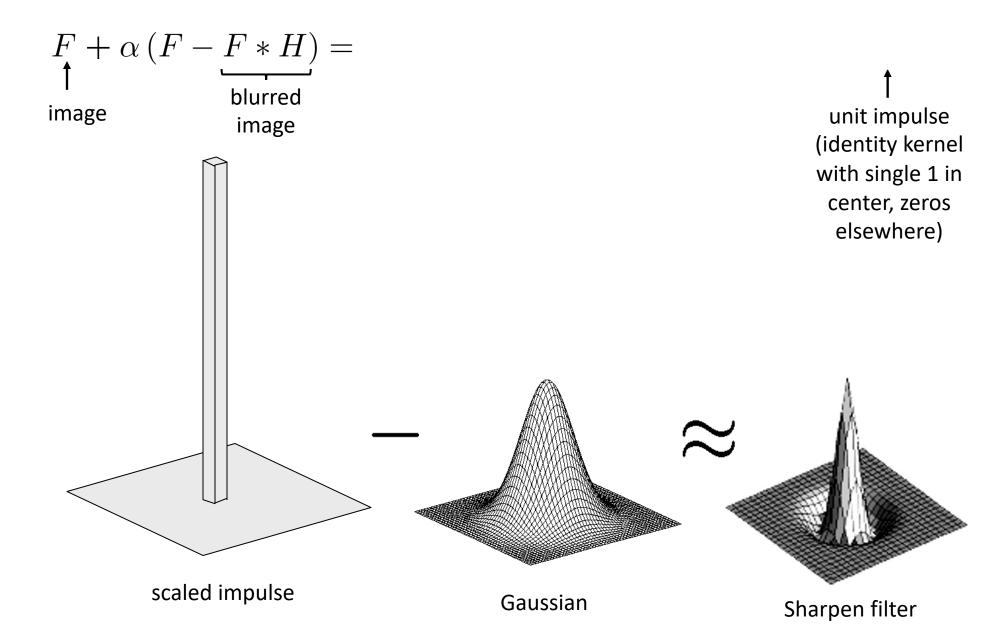


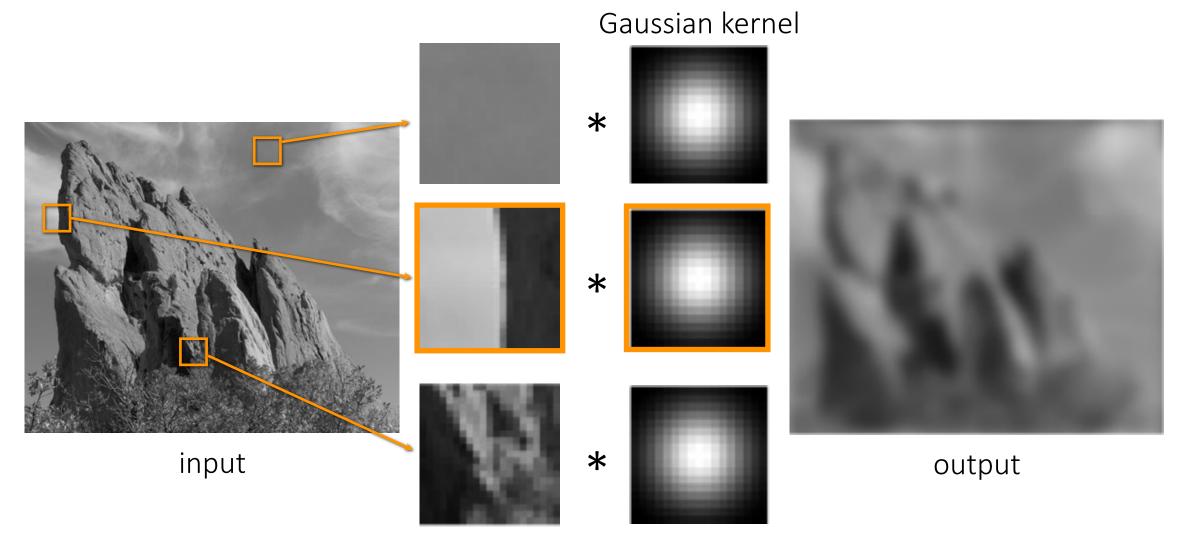


Photo credit: https://www.flickr.com/photos/geezaweezer/16089096376/

Sharpen filter



The problem with Gaussian filtering



Blur kernel averages across edges

The bilateral filtering solution

bilateral filter kernel * * * input output

Do not blur if there is an edge! How does it do that?

Gaussian filtering

$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

Bilateral filtering

$$h[m,n] = \frac{1}{W_{mn}} \sum_{k,l} g[k,l] r_{mn}[k,l] f[m+k,n+l]$$

Gaussian filtering

Bilateral filtering

$$h[m,n] = \sum_{k,l} m{g[k,l]} f[m+k,n+l]$$
 Spatial weighting: favor nearby pixels $h[m,n] = rac{1}{W_{mn}} \sum_{k,l} m{g[k,l]} r_{mn}[k,l] f[m+k,n+l]$

Gaussian filtering

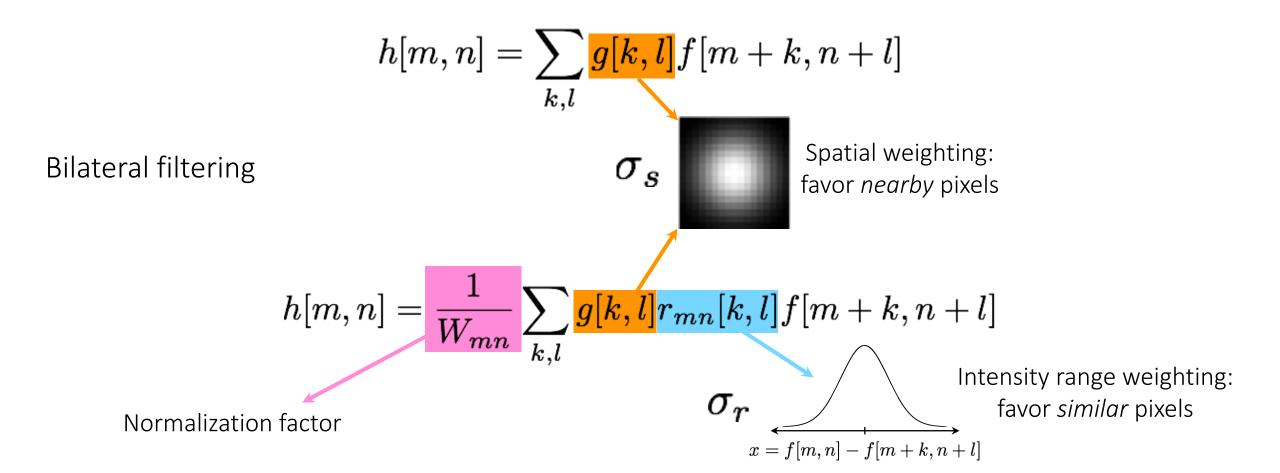
Bilateral filtering

$$h[m,n] = \sum_{k,l} {m g[k,l]} f[m+k,n+l]$$
 Spatial weighting: favor nearby pixels

Intensity range weighting: favor similar pixels

x = f[m, n] - f[m + k, n + l]

Gaussian filtering



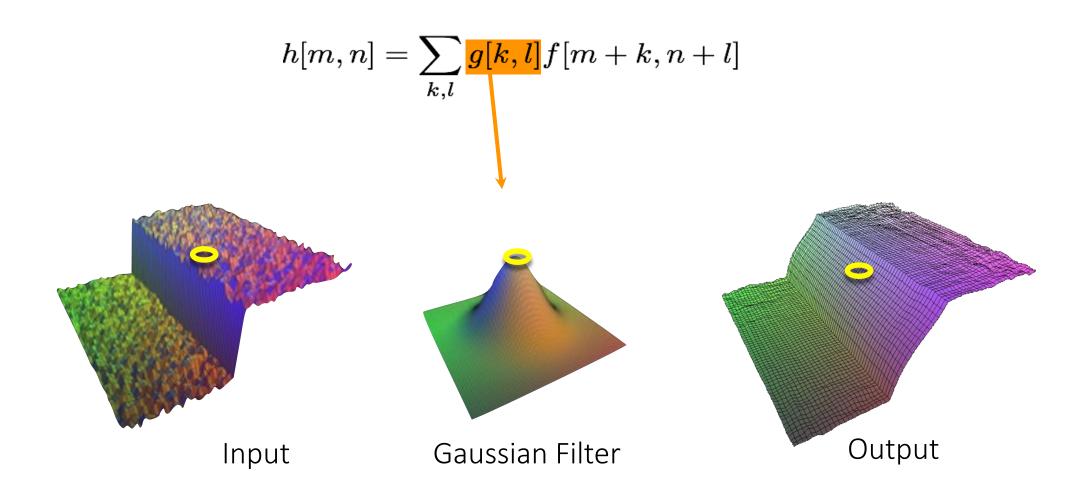
Gaussian filtering

Smooths everything nearby (even edges)
Only depends on *spatial* distance

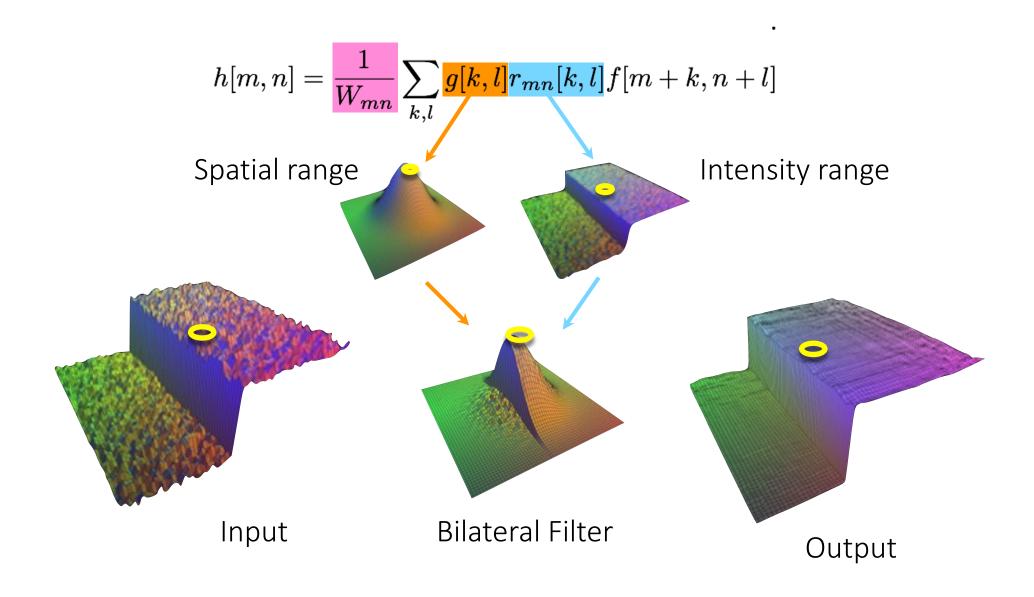
Bilateral filtering

Smooths 'close' pixels in space and intensity Depends on *spatial* and *intensity* distance

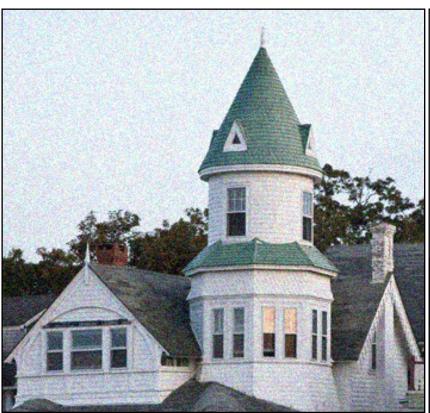
Gaussian filtering visualization



Bilateral filtering visualization



Denoising







noisy input

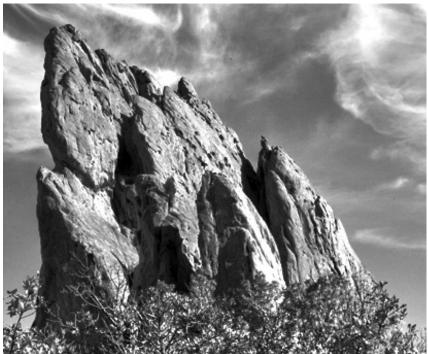
bilateral filtering

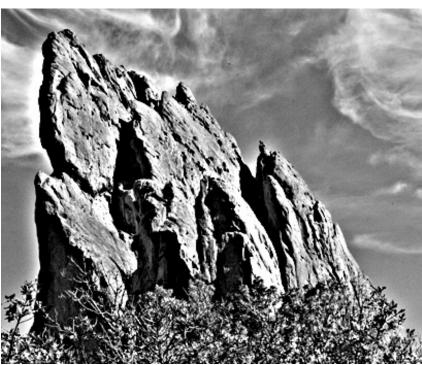
median filtering

Contrast enhancement

How would you use Gaussian or bilateral filtering for sharpening?







input

sharpening based on bilateral filtering

sharpening based on Gaussian filtering

Photo retouching





Photo retouching





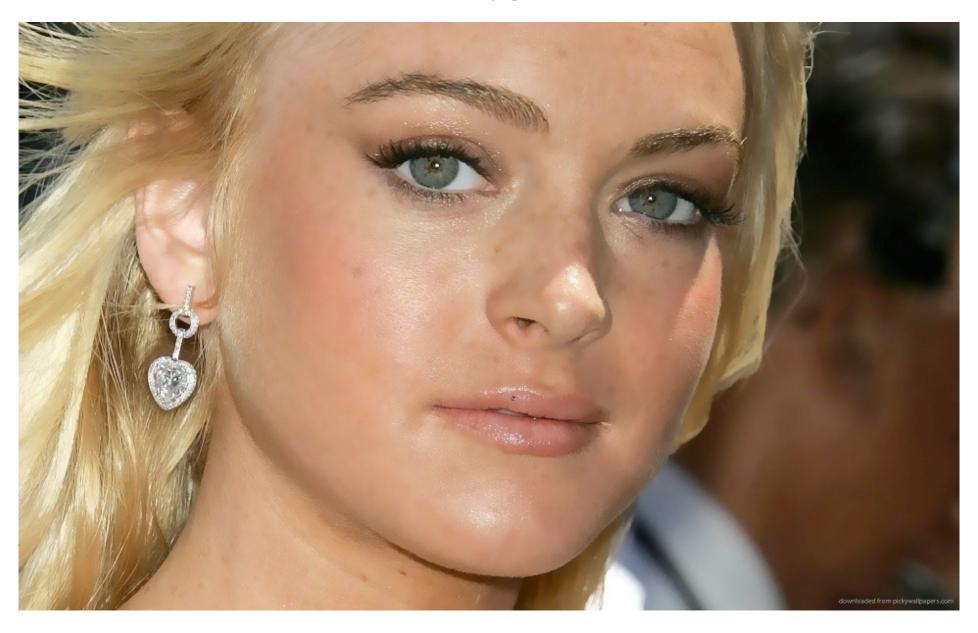
original

digital pore removal (aka bilateral filtering)

Before



After



Close-up comparison



original

digital pore removal (aka bilateral filtering)

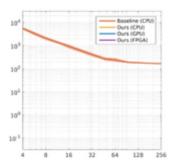
Cartoonization





input cartoon rendition

Actively used in various research problems



A Hardware-Friendly Bilateral Solver for Real-Time Virtual Reality Video
Amrita Mazumdar, Armin Alaghi, Jonathan T. Barron, David Gallup, Luis Ceze, Mark Oskin,
Steven M. Seitz
High-Performance Graphics (HPG), 2017
project page

A reformulation of the bilateral solver can be implemented efficiently on GPUs and FPGAs.



Deep Bilateral Learning for Real-Time Image Enhancement Michaël Gharbi, Jiawen Chen, Jonathan T. Barron, Samuel W. Hasinoff, Frédo Durand SIGGRAPH, 2017 project page / video / bibtex / press

By training a deep network in bilateral space we can learn a model for high-resolution and real-time image enhancement.



The Fast Bilateral Solver

Jonathan T. Barron, Ben Poole

ECCV, 2016 (Oral Presentation, Best Paper Honorable Mention)

arXiv / bibtex / video (they messed up my slides, use →) / keynote (or PDF) / code / depth super-res results / reviews

Our solver smooths things better than other filters and faster than other optimization algorithms, and you can backprop through it.

This lecture: Image Transformations & Filtering

- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

Image half-sizing

This image is too big to fit on the screen. How can we reduce it?

How to generate a half-sized version?

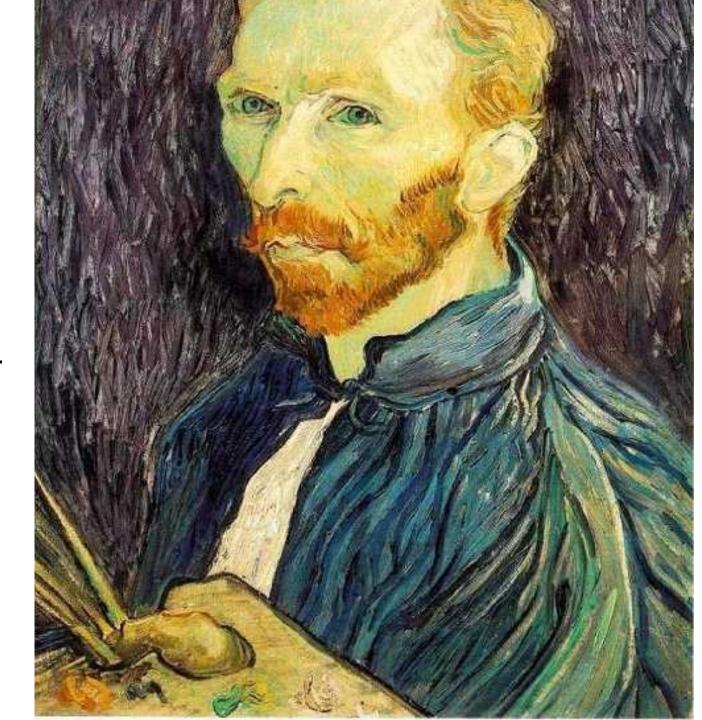
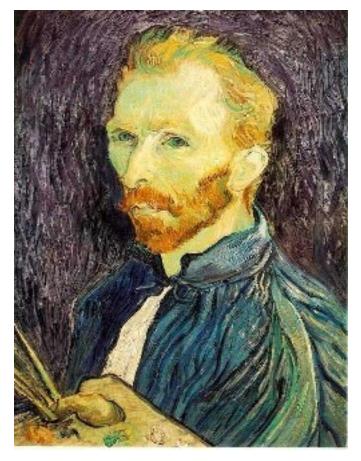


Image sub-sampling



Throw away every other row and column to create a 1/2 size image - called *image sub-sampling*





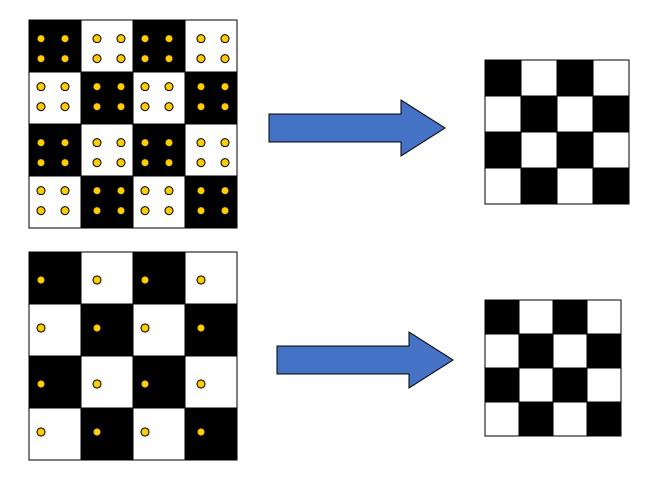
1/4

Image sub-sampling



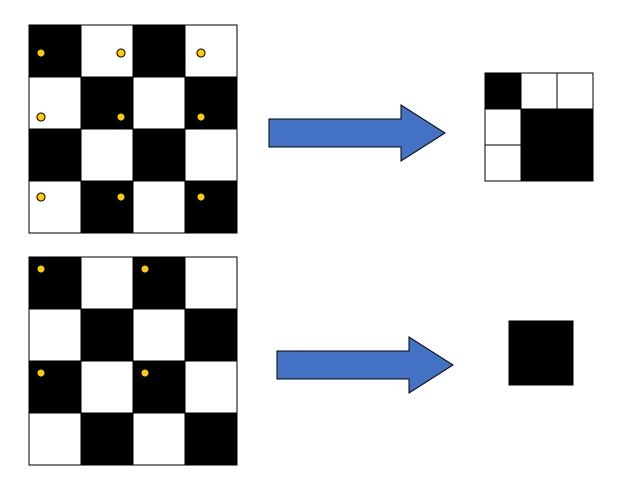
Aliasing! What do we do?

Sampling an image



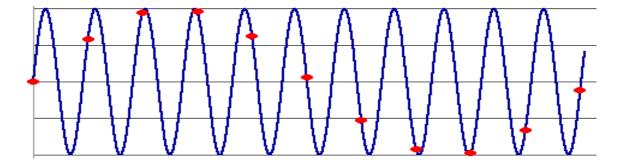
Examples of GOOD sampling

Undersampling



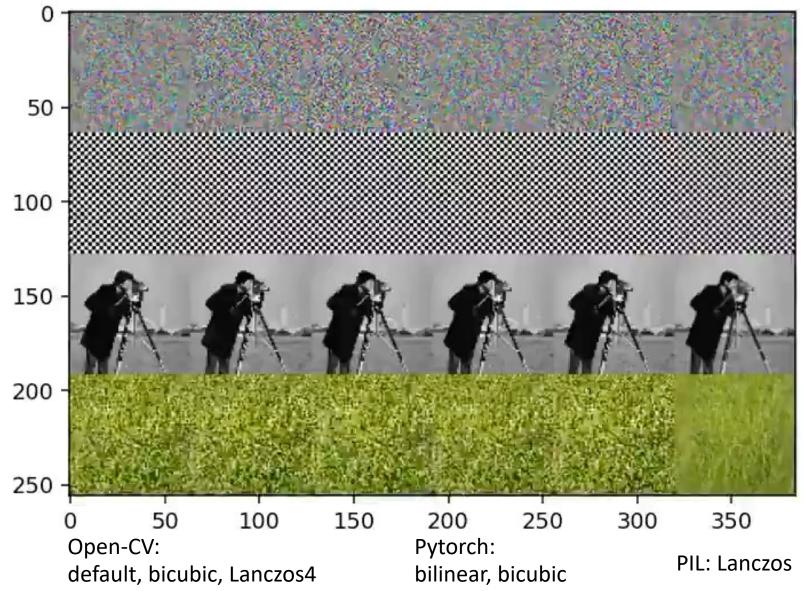
Examples of BAD sampling -> Aliasing

Aliasing



- Occurs when your sampling rate is not high enough to capture the amount of detail in your image
- Can give you the wrong signal/image—an alias
- To do sampling right, need to understand the structure of your signal/image
- Enter Monsieur Fourier...
 - "But what is the Fourier Transform? A visual introduction." (We will learn it next class!) https://www.youtube.com/watch?v=spUNpyF58BY
- To avoid aliasing:
 - sampling rate ≥ 2 * max frequency in the image
 - said another way: ≥ two samples per cycle
 - This minimum sampling rate is called the Nyquist rate

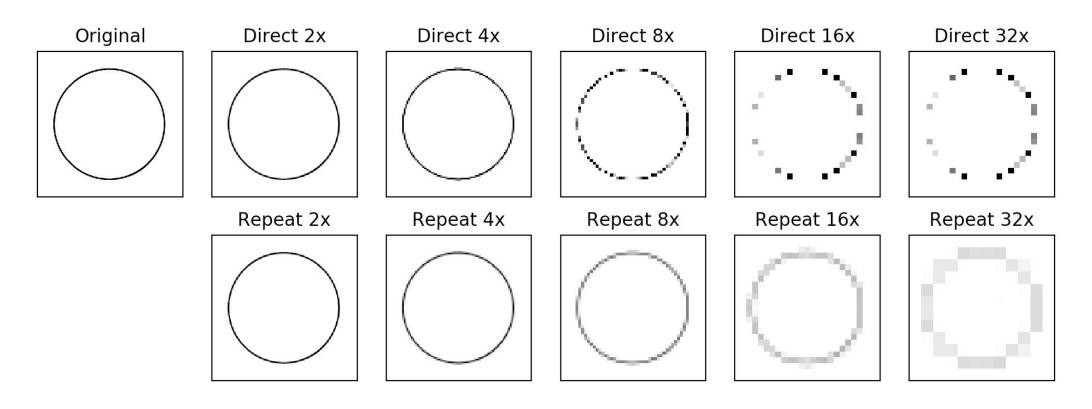
A real problem!



Credit: @jaakkolehtinen

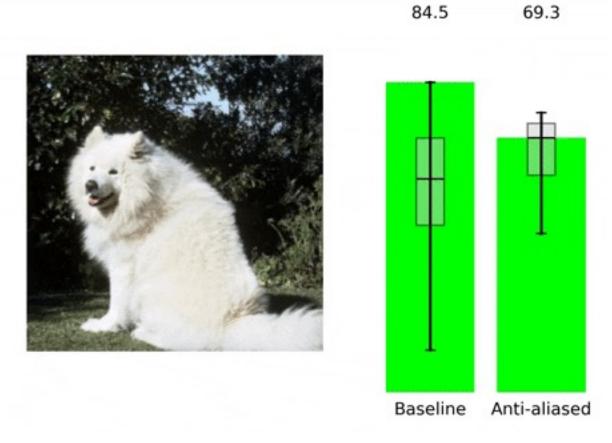
A real problem!

Bilinear downsampling with F.interpolate() in PyTorch



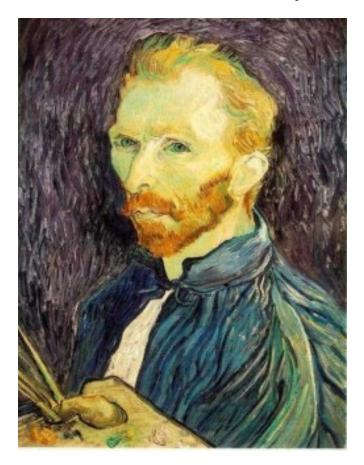
Credits: Richard Zhang

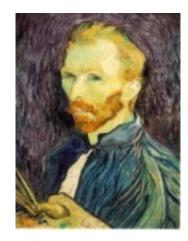
problems in NN too



Anti-aliasing in CNNs

Gaussian (lowpass) pre-filtering







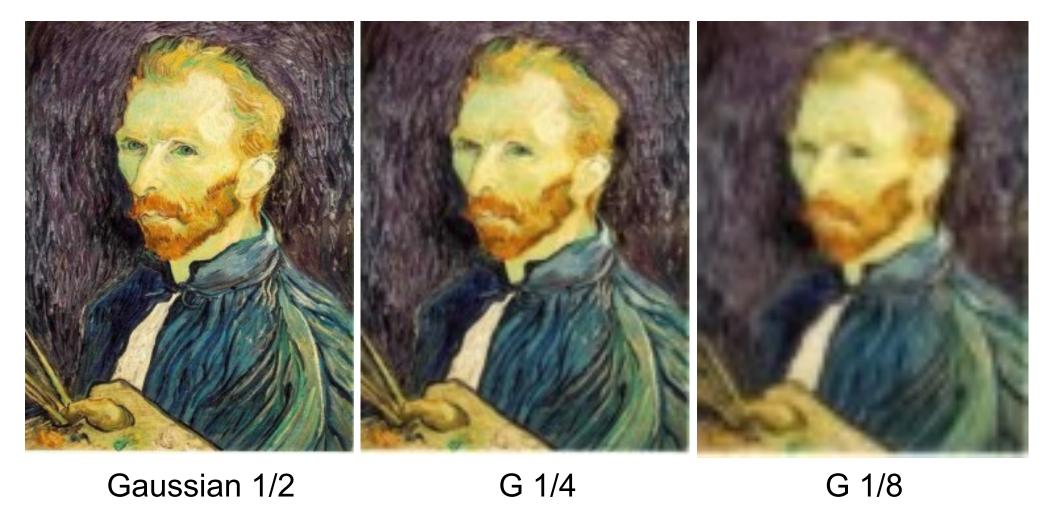
G 1/4

Gaussian 1/2

Solution: filter the image, then subsample

Filter size should double for each ½ size reduction.

Subsampling with Gaussian pre-filtering

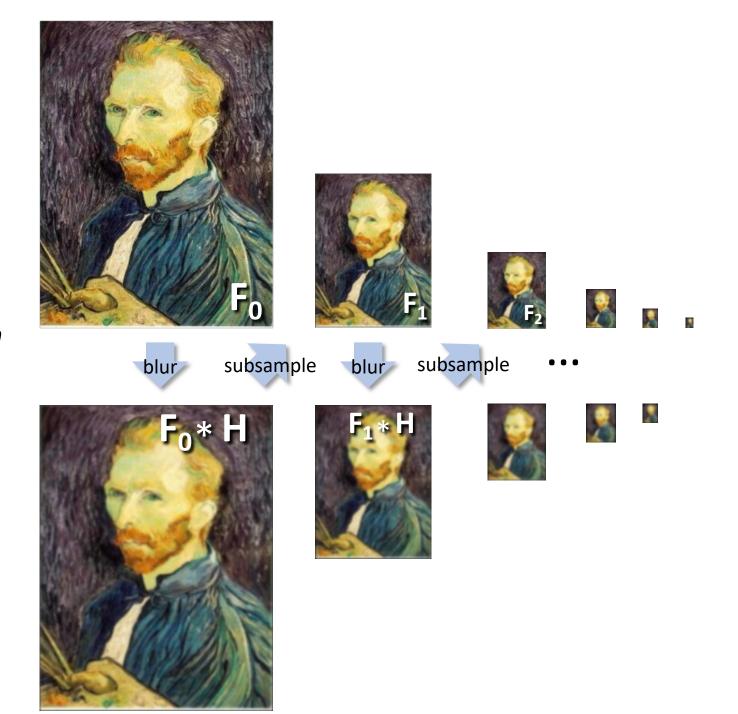


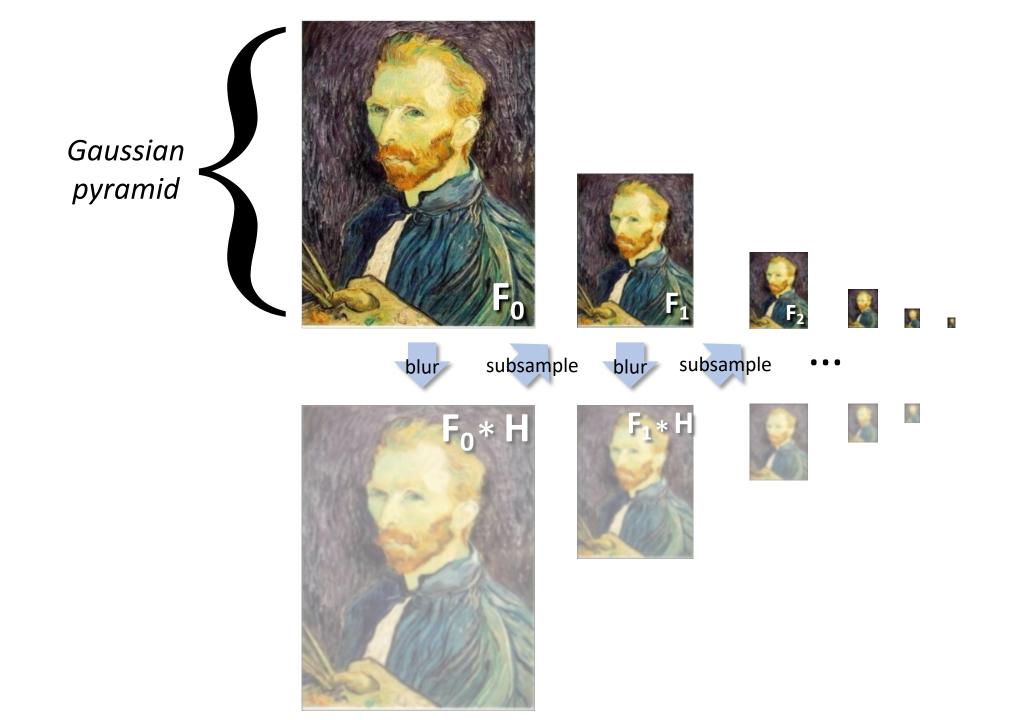
Compare with...

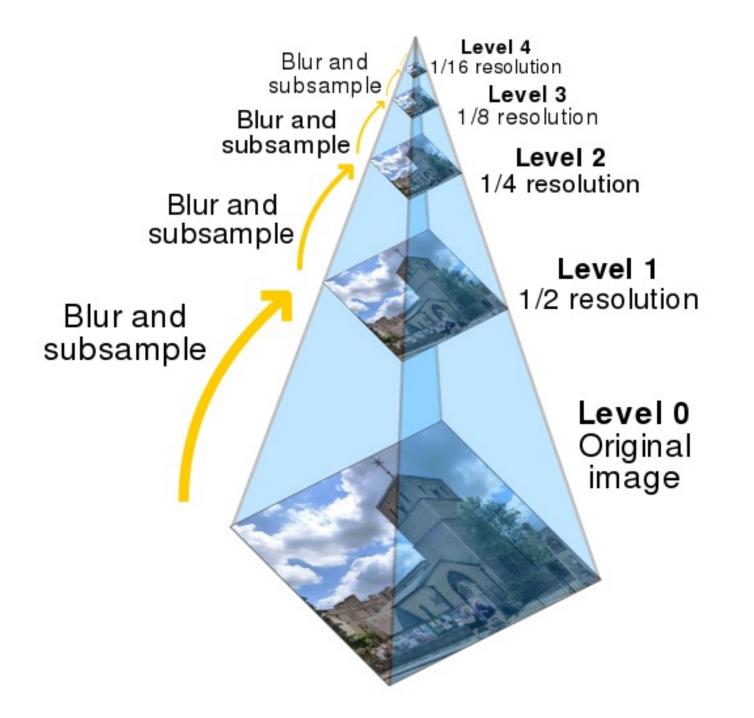


Gaussian prefiltering

• Solution: filter the image, then subsample







Similar to Gaussian Pyramids, there are Laplacian Pyramids.

What do Laplace filters do?

We will learn about Laplacian pyramids and how it is used for blending and compositing images in Lecture 10.

We will use something similar to stitching and blending images to form a panorama in our HWs!

What are they good for?

- Improve Search
 - Search over translations
 - Classic coarse-to-fine strategy
 - Search over scale
 - Template matching
 - E.g. find a face at different scales

Upsampling

• This image is too small for this screen:



- How can we make it 10 times as big?
- Simplest approach:
 repeat each row
 and column 10 times
- ("Nearest neighbor interpolation")



Image interpolation

Original image: 🔊 x 10





Nearest-neighbor interpolation

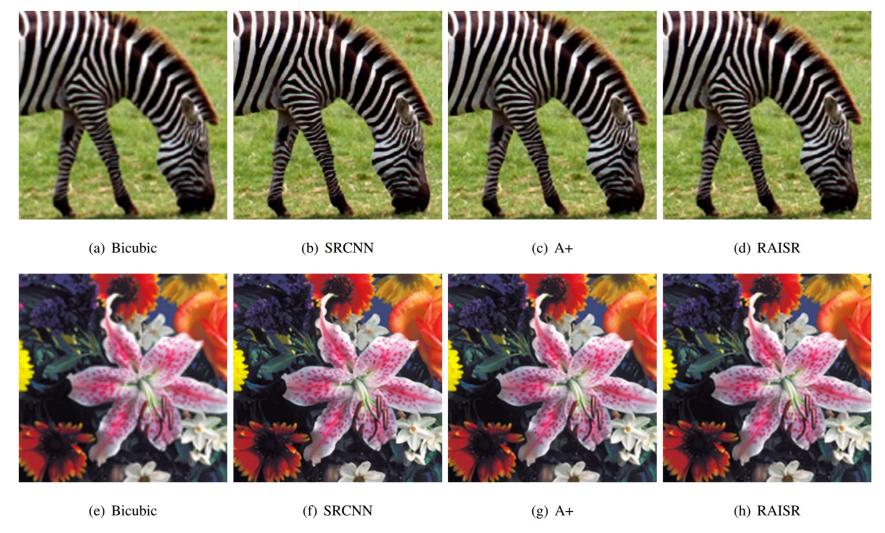


Bilinear interpolation



Bicubic interpolation

Modern methods



From Romano, et al: RAISR: Rapid and Accurate Image Super Resolution, https://arxiv.org/abs/1606.01299

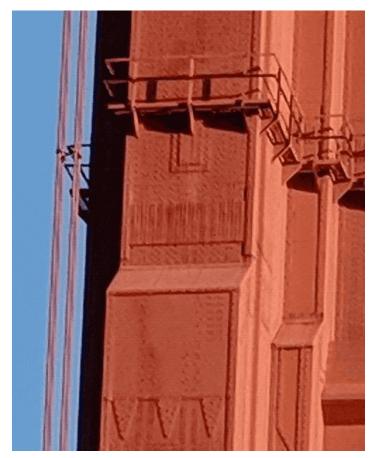
Super-resolution with multiple images

- Can do better upsampling if you have multiple images of the scene taken with small (subpixel) shifts
- Some cellphone cameras (like the Google Pixel line) capture a burst of photos
- Can we use that burst for upsampling?

Google Pixel 3 Super Res Zoom



Effect of hand tremor as seen in a cropped burst of photos, after global alignment



Example photo with and without super res zoom (smart burst align and merge)

https://ai.googleblog.com/2018/10/see-better-and-further-with-super-res.html

This lecture: Image Transformations & Filtering

- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

Partial derivatives with convolution

Image is function f(x,y)

$$\frac{\partial f(x,y)}{\partial x} = \lim_{\epsilon \to 0} \frac{f(x+\epsilon,y) - f(x,y)}{\epsilon}$$

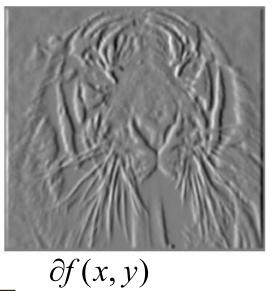
$$\frac{\partial f(x,y)}{\partial x} \approx \frac{f(x+1,y) - f(x,y)}{1}$$

Another one:

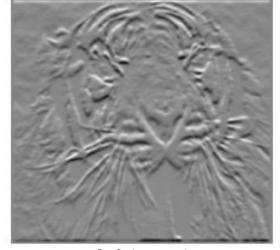
$$\frac{\partial f(x,y)}{\partial x} \approx \frac{f(x+1,y) - f(x-1,y)}{2}$$

Image Gradient





 ∂x



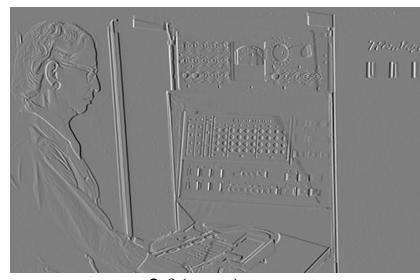
$$\frac{\partial f(x,y)}{\partial y}$$

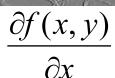
$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

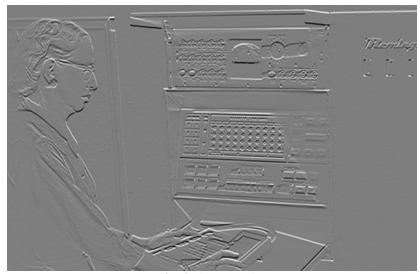


Partial Derivatives









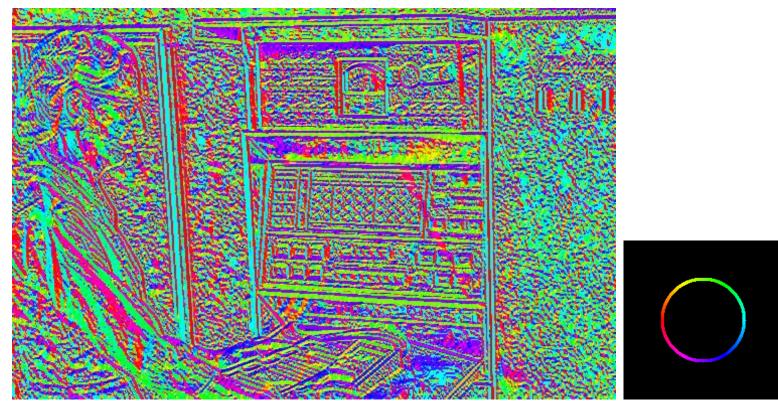
Gradient magnitude

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$



Gradient Orientation

$$\theta = \tan^{-1}\left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x}\right)$$



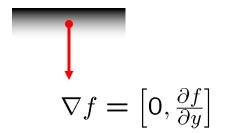
all the gradients

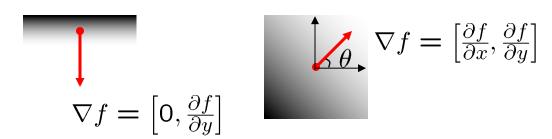
Source: D. Fouhey

Image gradient

• The gradient of an image:

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$





The gradient points in the direction of most rapid increase in intensity

How does this direction relate to the direction of the edge?

The *edge strength* is given by the gradient magnitude

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

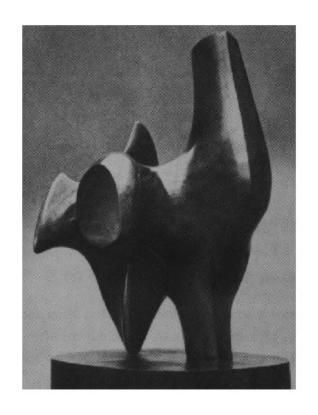
The gradient direction is given by $\theta = \tan^{-1}\left(\frac{\partial f}{\partial u}/\frac{\partial f}{\partial x}\right)$

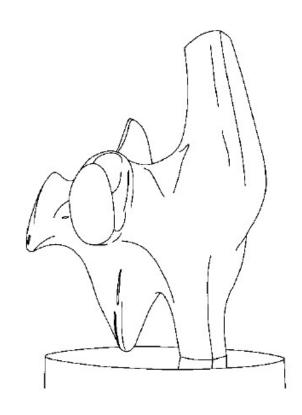
Source: Steve Seitz

This lecture: Image Transformations & Filtering

- Point Processing
- Linear Filtering
- Sampling & Aliasing
- Image Derivatives
- Edge Detection

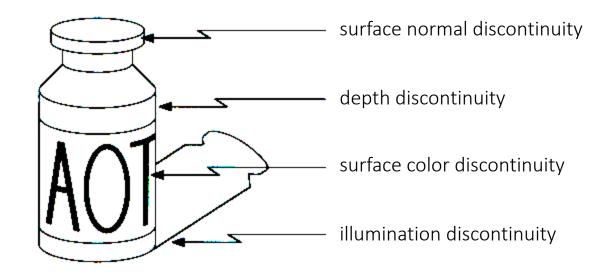
Edge detection





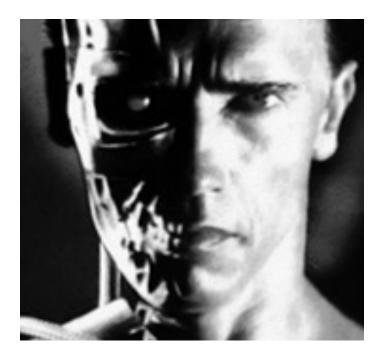
- Convert a 2D image into a set of curves
 - Extracts salient features of the scene
 - More compact than pixels

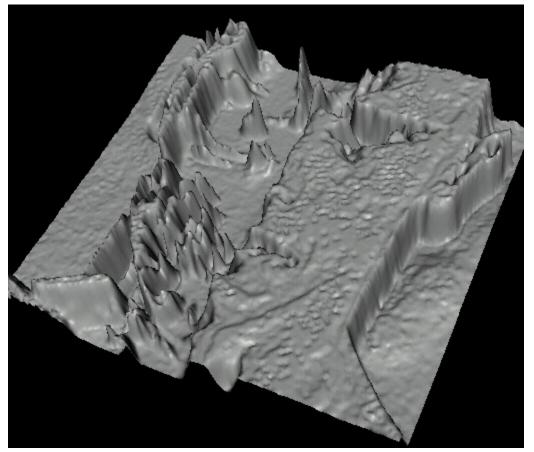
Origin of edges



• Edges are caused by a variety of factors

Images as functions...





• Edges look like steep cliffs

Characterizing edges

• An edge is a place of rapid change in the image intensity function

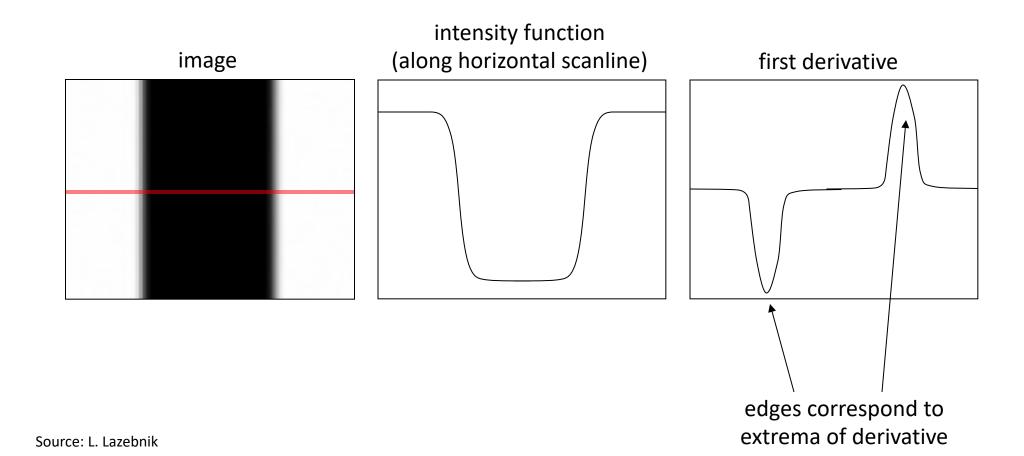
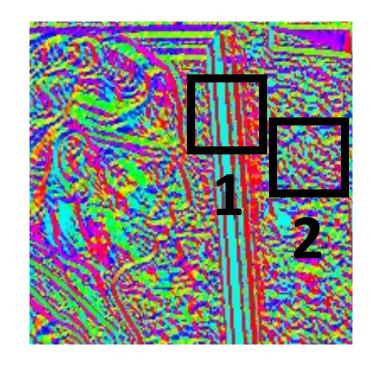


Image Gradient & Edges

$$\theta = \tan^{-1}\left(\frac{\partial f}{\partial y}/\frac{\partial f}{\partial x}\right)$$
 Direction of image gradients

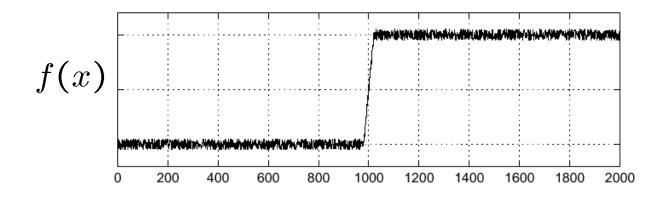
Why is there structure at 1 and not at 2?

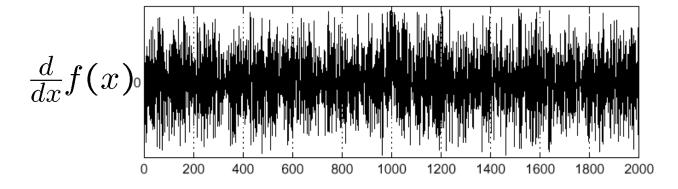




Effects of noise

- Consider a single row or column of the image
 - Plotting intensity as a function of position gives a signal

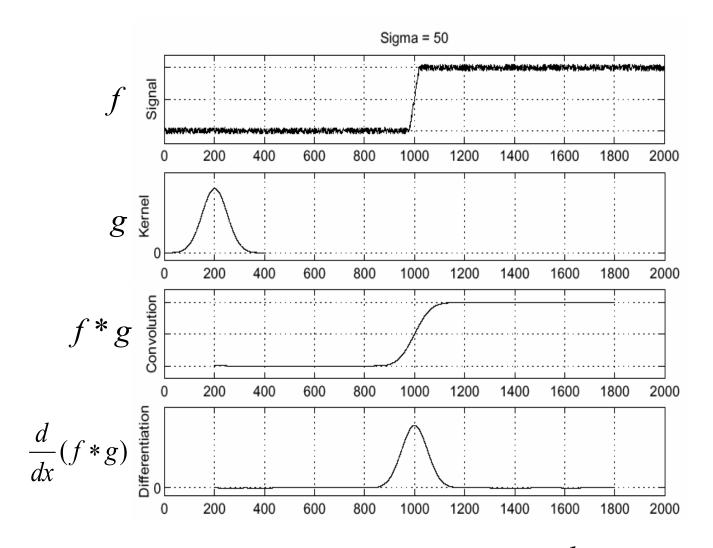




Where is the edge?

Source: S. Seitz

Solution: smooth first



• To find edges, look for peaks in $\frac{d}{dx}(f*g)$

Source: S. Seitz

Noise in 2D

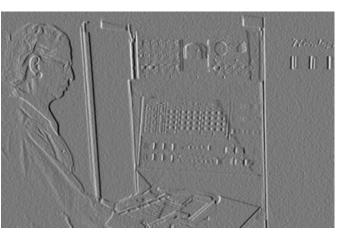
Noisy Input Ix via [-1,0,1] Zoom

Source: D. Fouhey

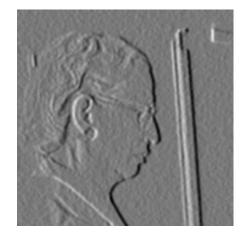
Noise + Smoothing

Smoothed Input

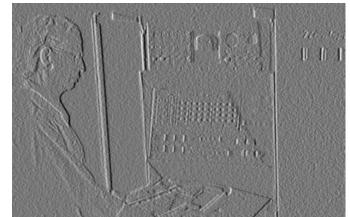
Ix via [-1,01]



Zoom



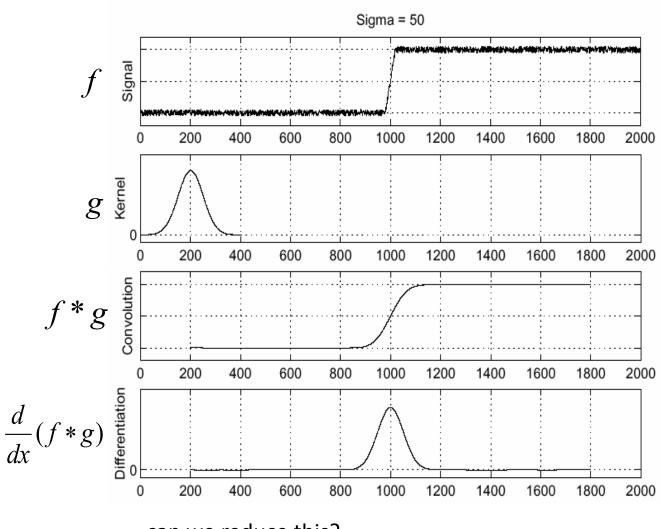






Source: D. Fouhey

How many convolutions here?

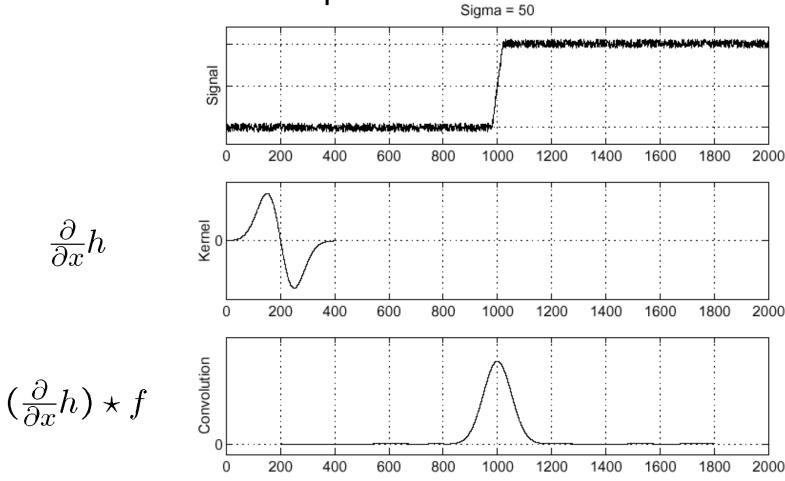


can we reduce this?

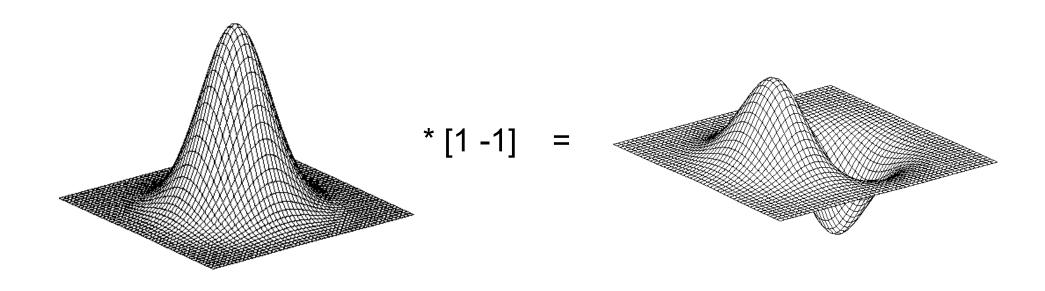
Derivative theorem of convolution

$$\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$$

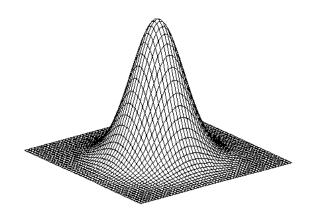
• This saves us one operation:



Derivative of Gaussian filter

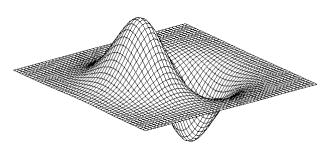


2D edge detection filters



Gaussian

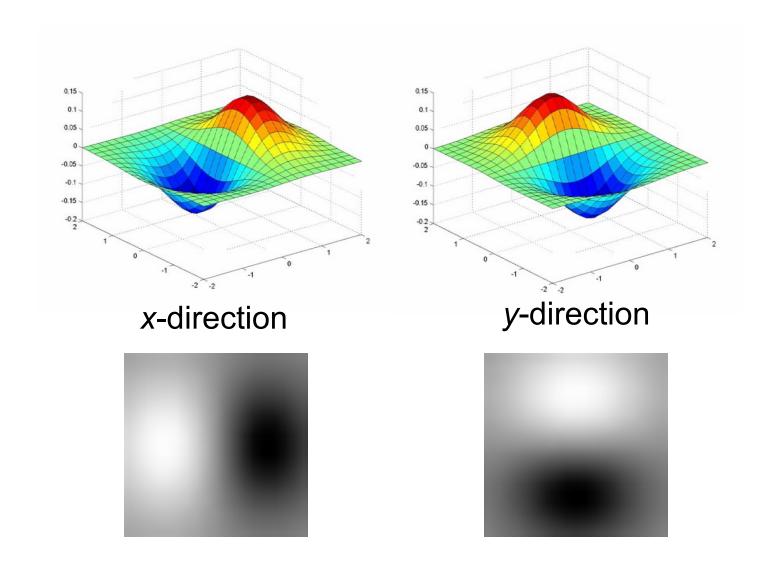
$$h_{\sigma}(u,v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian (x)

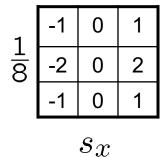
$$\frac{\partial}{\partial x}h_{\sigma}(u,v)$$

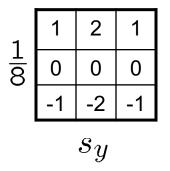
Derivative of Gaussian filter



The Sobel operator

Common approximation of derivative of Gaussian





- The standard definition of the Sobel operator omits the 1/8 term
 - doesn't make a difference for edge detection
 - the 1/8 term is needed to get the right gradient magnitude

Sobel operator: example











Source: Wikipedia

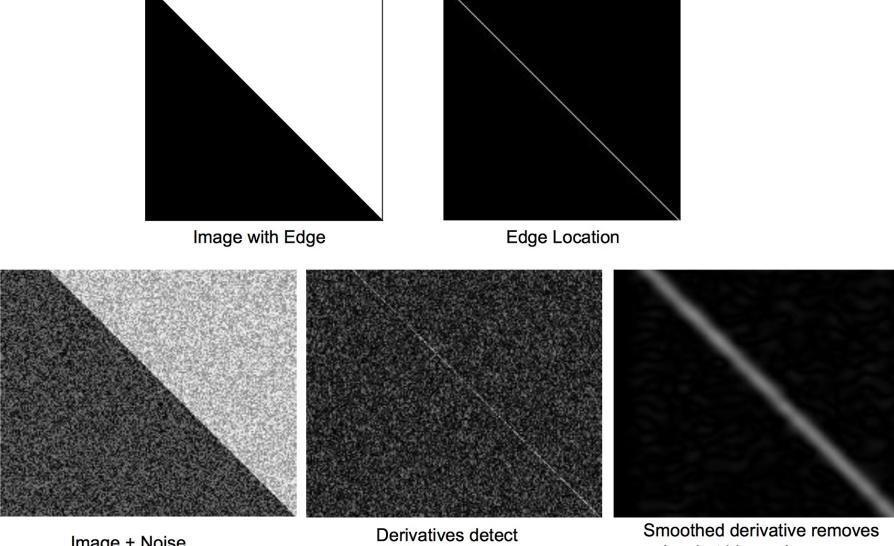


Image + Noise

edge and noise

noise, but blurs edge

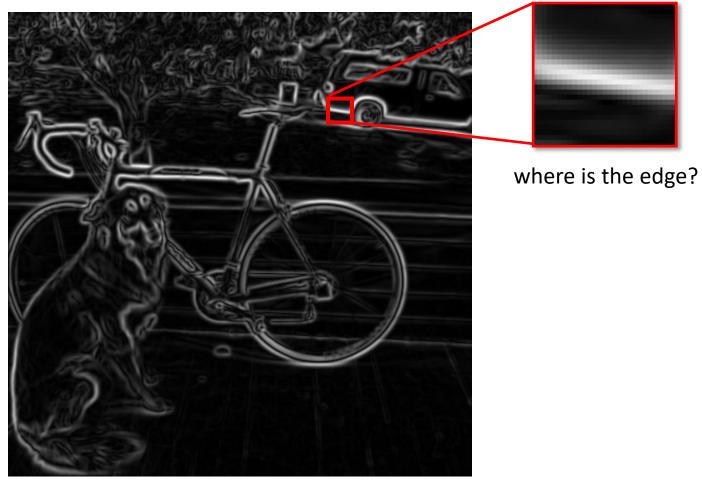
Example



original image

Demo: http://bigwww.epfl.ch/demo/ip/demos/edgeDetector/

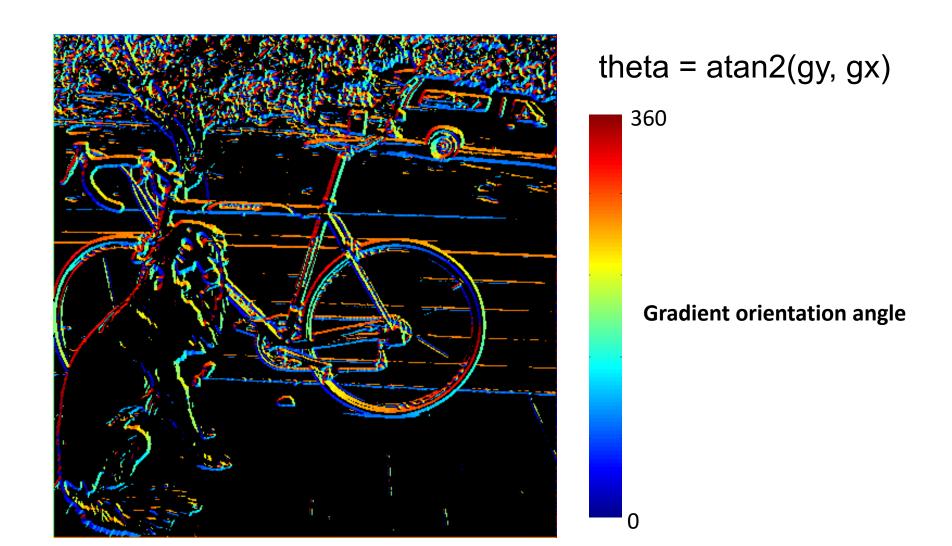
Finding edges



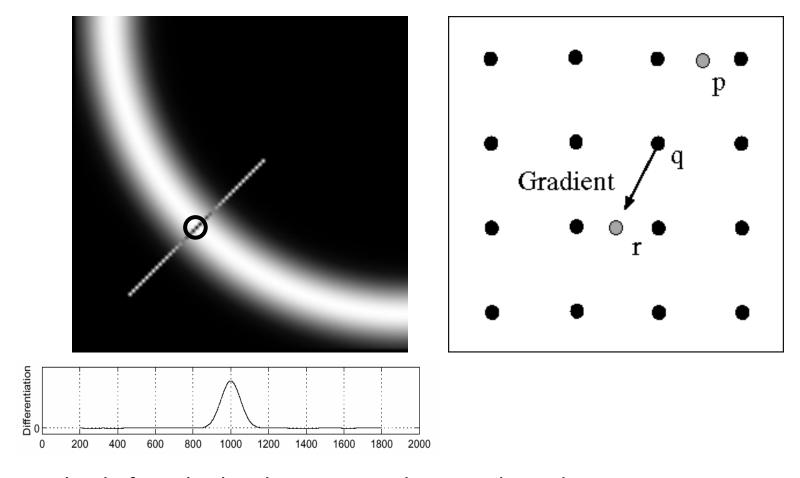
smoothed gradient magnitude

Get Orientation at Each Pixel

• Get orientation (below, threshold at minimum gradient magnitude)



Non-maximum supression



- Check if pixel is local maximum along gradient direction
 - requires interpolating pixels p and r

Before Non-max Suppression

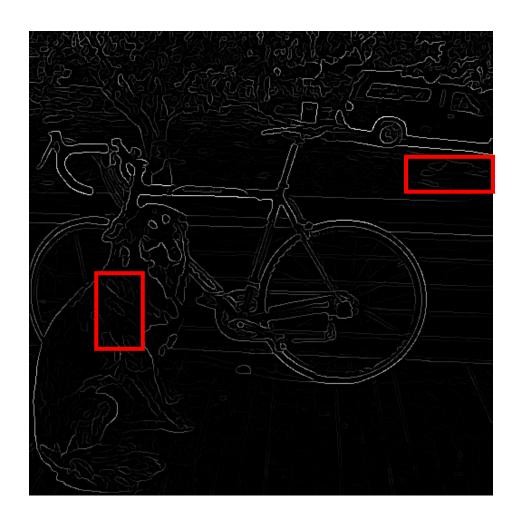


After Non-max Suppression



Still noise exists!





Thresholding edges

- Still some noise
- Only want strong edges
- 2 thresholds, 3 cases
 - R > T: strong edge
 - R < T but R > t: weak edge
 - R < t: no edge

- Strong edges are edges!
- Weak edges are edges iff they connect to strong
 - Look in some neighborhood (usually 8 closest)





Canny edge detector



- 1. Filter image with derivative of Gaussian
- 2. Find magnitude and orientation of gradient



3. Non-maximum suppression



- 4. Linking and thresholding (hysteresis):
 - Define two thresholds: low and high
 - Use the high threshold to start edge curves and the low threshold to continue them

Canny edge detector

- Our first computer vision pipeline!
- Still a widely used edge detector in computer vision

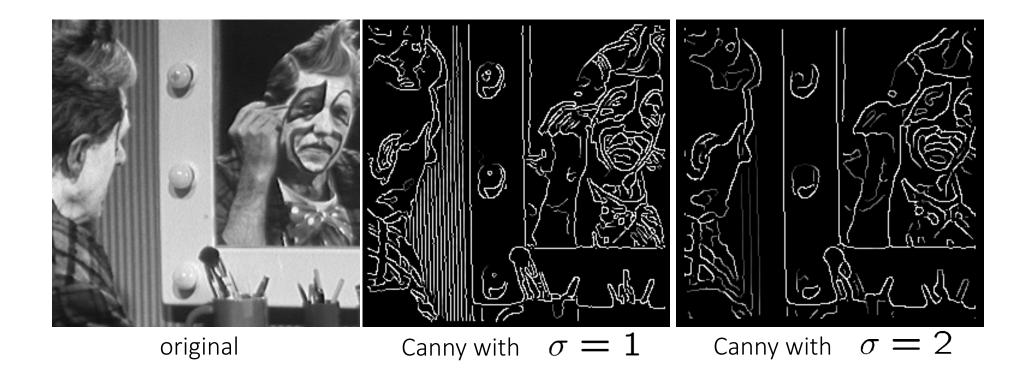
J. Canny, <u>A Computational Approach To Edge Detection</u>, IEEE Trans. Pattern Analysis and Machine Intelligence, 8:679-714, 1986.

Depends on several parameters:

high threshold low threshold

 σ : width of the Gaussian blur

Canny edge detector



- ullet The choice of $\,\sigma\,$ depends on desired behavior
 - large σ detects "large-scale" edges
 - small σ detects fine edges

Slide Credits

- <u>CS5670, Introduction to Computer Vision</u>, Cornell Tech, by Noah Snavely.
- <u>CS 194-26/294-26</u>: Intro to Computer Vision and Computational Photography, UC Berkeley, by Alyosha Efros.
- CS 15-463, 663, 862, CMU, by Computational Photography, Ioannis Gkioulekas.

Suggested Reading

- Szeliski, Chapter 3.1, 3.2, 3.3, 3.5 (3.4 will be covered in next lecture)
- Forsyth & Ponce, Chapter 4, Chapter 5.1, 5.2, 5.3